

Global Positioning System
Measurements on the Island of Hawaii
from 1987 to 1990

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By John J. Dvorak, Arnold T. Okamura, Michael Lisowski, William H. Prescott, *and*
Jerry L. Svarc

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ABSTRACT

The Global Positioning System (GPS) is a satellite-based system that can be used to determine relative ground positions to a few centimeters or less over distances of tens to hundreds of kilometers. The system was used in Hawaii to measure the pattern of ground displacement associated with (1) the slow withdrawal of magma from the summit reservoir of Kilauea and (2) a magnitude 6.1 earthquake beneath the south flank of Kilauea on June 26, 1989.

GPS surveys were conducted on the island of Hawaii in April 1987, August 1988, August 1989, and August 1990. Approximately 40 ground stations were occupied during each survey. TI4100 radio receivers, which simultaneously receive a P-code and radio signals on two frequencies from four different satellites, were used during all surveys. P-code is an encrypted time code from a satellite that allows unambiguous determination of satellite positions and empirical corrections for drift of each receiver-clock. Receipt of two radio frequencies allows a correction for propagation delays caused by the ionosphere.

We used satellite positions computed from orbits provided by the U.S. Naval Surface Weapons Center (NSWC). For our purpose, these positions were nearly the same as those computed from tracking data obtained from the worldwide system of GPS receivers operated by the National Geodetic Survey (NGS); the difference in relative ground positions on the island of Hawaii varied by a centimeter or less when we used orbits provided by NSWC or computed our own orbits from NGS tracking data. A similar comparison for the 548-km-long line between the GPS-tracking station on Kauai (KOKEE PARK) and our reference station at the Hilo airport (LYMAN2) showed the difference was 128 mm or less (0.23 part per million).

All measurements were processed using the Bernese software package. The internal consistency of each survey was estimated from the daily variation in computed station positions when the same baselines were measured on more than

one day. These daily variations were about five times the standard errors computed using the Bernese package. The least consistent surveys were conducted in August 1988 and August 1989, when radio signals from a key satellite were unavailable. In these cases, daily observing sessions lasted less than 4.4 hours, and four satellites could be tracked simultaneously for only 20 minutes. During surveys in April 1987 and August 1990, when daily observing sessions lasted up to 6.3 hours, the repeatability of station positions was 20 mm for horizontal components and 49 mm for vertical components. These values are as much as a factor of two larger than values reported for surveys of similar baseline lengths conducted in California. The lower repeatability of our surveys may be the result of our shorter observing sessions and of the location of our surveys outside the dense network of GPS-tracking stations on North America that were used to compute satellite orbits.

Our GPS measurements show that the summit area of Kilauea subsided at least 0.2 m between April 1987 and August 1990. The subsidence, which was indicated also by repeated leveling surveys, was probably related to continued eruption of the volcano. During the four years spanned by our surveys, Kilauea erupted about 0.3 km³ of lava; 10 percent of the erupted volume can be accounted for by net subsidence of the summit area. We suggest that the other 90 percent was supplied by a deeper source that had no significant influence on ground displacement measured by GPS or other geodetic techniques.

The largest ground displacement recorded by GPS were associated with a magnitude 6.1 earthquake beneath the south flank of Kilauea on June 26, 1989. Horizontal displacements at sites located over the aftershock zone showed seaward displacement of the south flank of as much as 0.3 m. Subsidence of as much as 0.25 m occurred near the eastern edge of the aftershock zone.

INTRODUCTION

The attempt to provide accurate predictions of volcanic eruptions has benefited from the measurement of ground

displacement that results when magma moves up toward the ground surface. Though standard land-surveying techniques, such as leveling, triangulation and trilateration, have been used to record this displacement, these techniques require at least several days to complete and are restricted in the choice of survey sites. These limitations are partially overcome by a satellite-surveying technique that makes use of the Global Positioning System (GPS).

GPS uses a set of satellites and mobile ground-based receivers to determine ground positions. Though this system is still being developed, measurements made during the last few years show that relative three-dimensional positions on a centimeter-scale can be determined across baselines that range from tens to hundreds of kilometers. The speed, accuracy, and versatility of GPS make it an especially attractive as a tool to study active volcanoes.

We began using GPS in April 1987 on the active volcanoes in Hawaii, in particular on Kilauea volcano (fig. 1), one of the most active and thoroughly studied volcanoes in the world. The existence of extensive and frequently measured geodetic networks on Kilauea allows a comparison to be made of the amount of ground displacement measured by GPS and by other techniques.

HISTORY OF GROUND MOVEMENTS ON THE ISLAND OF HAWAII

Thomas A. Jaggar, Jr., one of the pioneers of the study of active volcanoes, began daily tilt measurements in the summit area of Kilauea in 1913. After two decades of measurements, Jaggar concluded that magma accumulated slowly in a shallow reservoir beneath the summit area (Jaggar and Finch, 1929). The accumulation was interrupted when an eruption occurred along one of two radial rift zones, and magma drained rapidly from the summit reservoir. Ground displacement caused by several dozen cycles of slow filling, each ending by a rapid withdrawal of magma and usually a rift-zone eruption, has now been recorded using a wide variety of techniques.

Beginning in the 1960s, these same techniques were extended to other areas of the island of Hawaii to search for other possible components of ground displacement. These efforts were quickly rewarded when measurements showed seaward displacement of the south flank of Kilauea, the portion of Kilauea that lies south of the two rift zones. The displacement was related to formation of new eruptive fissures (Swanson and others, 1976) and to a magnitude 7.2 earthquake beneath the south flank (Lipman and others, 1985). Measurements at adjacent Mauna Loa volcano showed gradual uplift, then rapid subsidence of the summit area associated with the 1984 eruption (Decker and others, 1983; Lockwood and others, 1987). Other measurements on Kilauea revealed a secondary magma reservoir along the east rift zone (Jackson and others, 1975), a migration of uplift

centers in the summit area (Fiske and Kinoshita, 1969), the size of dikes that fed the 1971 and 1983 eruptive fissures (Dvorak and others, 1984; Dvorak, 1990), and the growth rate of the 1983 eruptive fissure (Okamura and others, 1988).

The rate and pattern of ground displacement of Kilauea have been used, along with studies of seismicity, gas emission, and petrology of erupted material, to propose a model

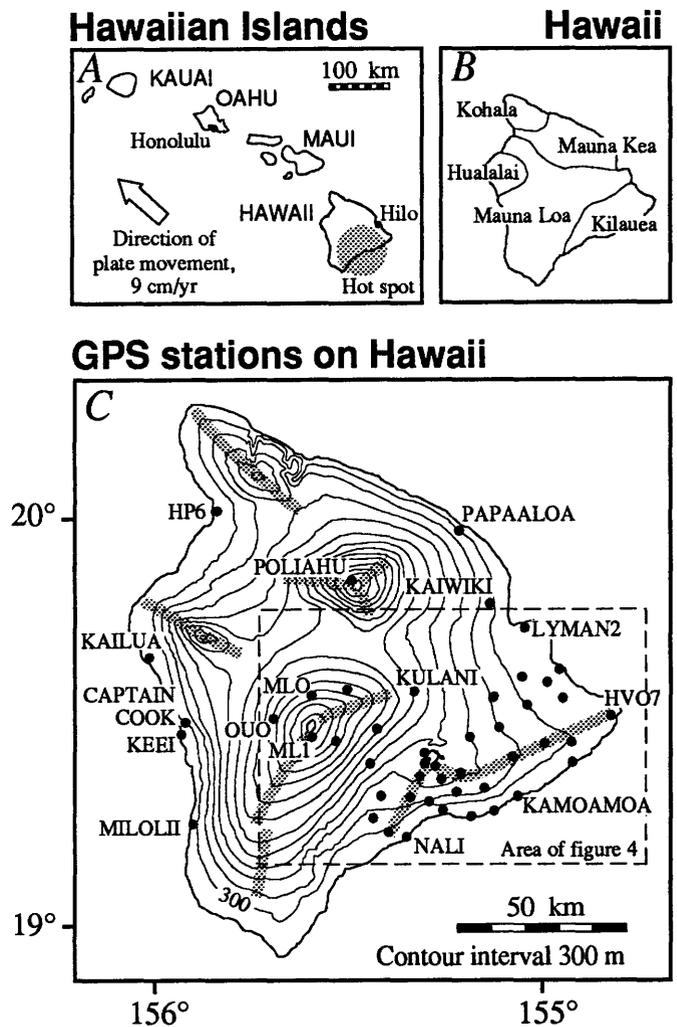


Figure 1. The island of Hawaii lies at southeast end of the Hawaiian island chain, over an anomaly in the mantle termed a hot spot (A). The hot spot supplies magma to the active volcanoes, where it is erupted either in one of the summit areas or along one of the long rift zones radial to each summit area, indicated in map C as broad shaded lines. Hawaii is composed of five volcanoes (B): Kohala is considered extinct; Mauna Kea and Hualalai last erupted 4,000 and 200 years ago, respectively; Mauna Loa last erupted in 1984; and Kilauea has been erupting since 1983. Most GPS stations, indicated as solid circles in map C, are located on Kilauea. Stations have also been located around the summit area and upper slopes of Mauna Loa and along the southwest coast of the island, the Kealakekua fault system. An enlargement of the area enclosed by the dashed rectangle in C is shown in figure 4.

for the way Kilauea works (Eaton and Murata, 1960; Wright and Fiske, 1971; Decker, 1987; Dvorak and others, 1992; Tilling and Dvorak, 1993). As magma rises from the mantle into the summit reservoir located a few kilometers beneath the summit area, the surface of the volcano rises and distends. Magma accumulation is usually gradual, causing tens to hundreds of millimeters of ground displacement in the summit area over a period of several months to a year. When magma moves laterally from the summit reservoir along a conduit beneath a rift zone, the summit area subsides rapidly, dropping several hundred millimeters within a few hours. A dike that feeds an eruption begins to grow upward from a depth of a few kilometers either from magma stored in the summit reservoir or stored beneath a rift zone. By the time the dike has breached the surface and an eruption ensues, the dike may be a few kilometers high, several kilometers long, and a meter or more wide. A dike widens the rift zone and compresses the adjacent portion of the flank. Repeated injection of magma as dikes and compression of the flank cannot continue indefinitely. Eventually, the compression is relieved as a large earthquake, and the south flank of Kilauea suddenly moves seaward (Swanson and others, 1976).

LIMITATIONS OF CONVENTIONAL LAND-SURVEYING TECHNIQUES

The three strategies used at Kilauea to measure ground displacement are designed to record changes in (1) elevation, using a standard leveling technique, (2) horizontal strain by making trilateration measurements, or (3) ground inclination, called tilt.

The releveling of benchmarks to determine elevation changes is the best way to reveal a detailed pattern of vertical ground displacement if stations are closely spaced. Furthermore, vertical displacement of less than a part per million can be measured by using very simple equipment and field procedures (Dzurisin, 1992); a second-order leveling survey, which is usually achieved at Kilauea, has an accuracy of 10 mm over a distance of 25 km. Major limitations are that the distance between stations must be easy to traverse, which usually requires the existence of a drivable road, and that a survey requires a few weeks to complete. These two limitations have restricted the use of leveling surveys to only a few volcanoes. One happens to be Kilauea, because the summit area is accessible by paved roads.

The second strategy makes use of electronic-distance-measuring (EDM) instruments to measure changes in distance between pairs of benchmarks. Most EDM instruments now use a laser, which, depending on how the correction for atmospheric refraction is made, can be used to measure a horizontal distance to an accuracy of a few millimeters to a few centimeters over distances of 50 km or less. In order for these measurements to be made rapidly and over a broad area at Kilauea—rapid measurements are important because

the surface of the volcano can move in several quick events in a month or less—temperature measurements of the atmosphere are made only at the two benchmarks, not over the entire path of the laser beam. Field tests show that endpoint temperature measurements limit the refraction correction to an accuracy of 3 or 4 parts per million (Decker and others, 1966), and so the distance between benchmarks separated by 10 km must change by more than 30 to 40 mm to be detected. Another disadvantage of trilateration measurements is that stations must be intervisible; thus, it is difficult to locate stations in rugged and steep terrain or in heavily forested areas, which are common around many volcanoes. To a degree, these limitations also apply to Kilauea. Few trilateration measurements have been made across the forested areas on the north flank and along portions of the east rift zone, and because of steep terrain, few measurements link activity along the rift zones and displacement of the south flank.

Though many different techniques have been developed to measure changes in ground tilt, all techniques have the problem of being able to record ground displacement over a short baseline. The difficulty is reduced where tilt changes are determined by measuring elevation changes between benchmarks separated by a few tens of meters. This technique, often called the “dry-tilt” method, has been used to record tilt changes as small as a few microradians (Yamashita, 1992). Because many volcanoes have steep slopes, this technique has had limited use. A further limitation of the dry-tilt method is that benchmarks must be very stable: A vertical change of 0.1 mm over a baseline of 30 m indicates a tilt change of 3 microradians.

In summary, the severest limitation of conventional land-surveying techniques is the choice of sites. Potential GPS stations, however, can be located almost anywhere, as long as a clear view of the sky is visible 20° above the horizon and the station is not near metal structures, such as buildings and wire fences. Furthermore, GPS measurements can be made in more severe weather conditions than conventional techniques, and the radio receivers can operate unattended for days to months.

BRIEF DESCRIPTION OF THE GLOBAL POSITIONING SYSTEM

The GPS was designed by the U.S. Department of Defense as a satellite-based navigational system for real-time military applications. Military users can use GPS to determine absolute positions to within a few meters. Because radio signals from the satellites are encrypted and altered intentionally, civilian users are limited to an accuracy of absolute positions of 100 m; however, radio signals received by two ground receivers operating in a differential mode can be combined to determine relative positions at

the centimeter-level over distances of tens to hundreds of kilometers. It is in the high-precision, differential mode that GPS becomes a tool to measure surface displacement of geophysical interest.

Radio signals are transmitted from a constellation of satellites in 20,000-km-high orbits, giving an orbital period of 12 hours, and inclined 60° to the equator (fig. 2). Each satellite transmits on two L-band frequencies (L1 on 1575.42 MHz and L2 on 1227.60 MHz), which correspond to wavelengths of 0.19 m for L1 and 0.24 m for L2. Meter-level positioning is obtained by military users by receiving a special ranging code transmitted by each satellite, which enables the user to determine the distance to three or more satellites whose orbital positions are already known. Because errors are still present in satellite and receiver clocks, the range estimates are called pseudoranges, to distinguish them from the actual range distances between the satellites and a ground receiver.

In the differential mode, in which each pair of ground receivers observes simultaneously four or more satellites (fig. 3), we use pseudorange measurements to compute empirical corrections of drift of the receiver clocks. A high precision in positioning is obtained because of the submeter wavelength of the L-band signals and the use of carrier-phase measurements on the radio signals. By using phase measurements, the resulting distance between each satellite and receiver pair is ambiguous by an integer number of wavelengths. Because a large number of phase measurements is made, the phase ambiguities can be resolved, if we keep track of the number of cycles that occur between phase measurements. The use of two radio frequencies is needed to correct for the time delay as the radio signals pass through the ionosphere. Also there is a need to recompute satellite positions from observations taken from widely spaced sites when our surveys were conducted, because the satellite positions broadcast by the satellites at the time of the survey are

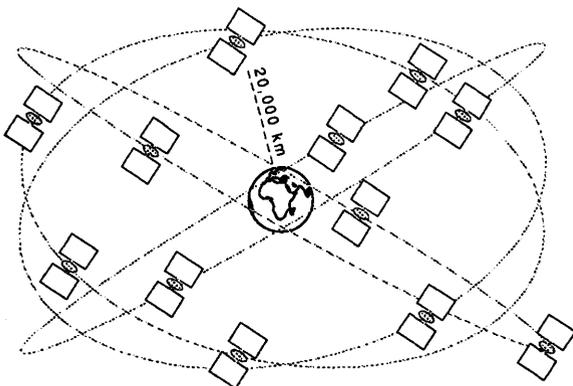


Figure 2. GPS consists of a network of NAVSTAR satellites in 20,000-km-high orbits. At this height, each satellite has an orbital period of about 12 hours. The future operation of 21 satellites will give 24-hour coverage over most areas of the world.

extrapolations and may be further reduced in accuracy by the Department of Defense by a procedure known as selective availability. Additional details of how phase measurements are used to determine ground positions, as well as a more complete description of GPS, are given in Wells and others (1986) and Dixon (1991).

DESCRIPTION OF SURVEYS

Four GPS surveys were conducted on the island of Hawaii between April 1987 and August 1990 using dual radio-frequency TI4100 receivers. Forty-seven sites were occupied (figs. 1 and 4), of which many were occupied for only one day during each survey.

GOALS OF THESE SURVEYS

Frequent volcanic and seismic activity at Kilauea has made this volcano a proving ground for new techniques designed to measure magmatic activity in the upper crust. We had the following goals for using GPS in Hawaii.

- *Evaluate GPS as a technique to measure slow crustal displacement in the mid-Pacific.*—Many GPS surveys have been conducted on large continental land masses, often at latitudes of the continental U.S. or higher, such as Alaska (Beutler and others, 1987) and California and the Rocky Mountain States (Davis and others, 1989). The island of Hawaii is a different environment because it is located at low latitudes and is surrounded by ocean. High humidity may limit the accuracy of GPS in Hawaii and elsewhere in the subtropics and tropics.

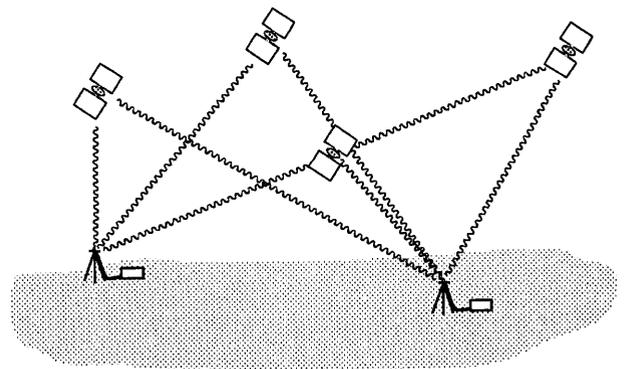


Figure 3. Though GPS was originally designed to determine absolute positions at meter level, station locations can be determined to centimeter level by making relative measurements between pairs of ground-based receivers. Each receiver records signals from the same subset of NAVSTAR satellites. Generally, four or more satellites must be observed simultaneously to determine three-dimensional position of each receiver and to make an empirical correction of drift of each receiver clock.

• *Compare measurements made using GPS and conventional land-surveying techniques.*—Several decades of measurements of ground displacement have been made in many dynamic regions of the world, especially along fault systems and volcanic chains. Before GPS can take the role as the primary means to make these measurements, simultaneous measurements must be made using both GPS and established techniques to understand the peculiarities of old and new techniques and to test that the same rates of ground displacement are measured by both techniques.

• *Carry out the initial Hawaiian surveys in the summit area and along the south flank of Kilauea, where the largest ground displacement is expected.*—For more than three decades, intensive land surveys of Kilauea have identified several major components of ground displacement. We concentrated our initial effort in the summit area and along the south flank because these areas have had the largest amount and highest rates of ground displacement and are easily accessible. Thus, they are the most likely places for us to measure displacement.

• *Extend later surveys to areas where conventional land-surveying techniques are difficult to conduct (the summit*

area and upper slopes of Mauna Loa and along the Kealakekua fault system).—Topography has limited, or prevented, the use of conventional techniques in two areas of special interest: the summit area and upper slopes of Mauna Loa and along the Kealakekua fault system on the southwest coast of the island. While Mauna Loa does not erupt as frequently as Kilauea, eruptions of Mauna Loa are usually more voluminous, by a factor of 10 (Macdonald and others, 1983), which suggests a larger magma reservoir associated with Mauna Loa. The remoteness of Mauna Loa makes it difficult to repeat leveling or trilateration measurements. Much is known about how Kilauea works, but infrequent eruptions of Mauna Loa have left a gap in a general understanding about Hawaiian volcanoes. The Kealakekua fault system offers an analogue to the Hilina fault system along the south flank of Kilauea, where two magnitude >6.0 earthquakes have occurred since 1975. During the last 40 years, three damaging earthquakes, all believed to be greater than magnitude 6.0, occurred along the Kealakekua fault system. Furthermore, the earthquake risk has increased greatly along the west coast of Hawaii because of a rapid urban growth.

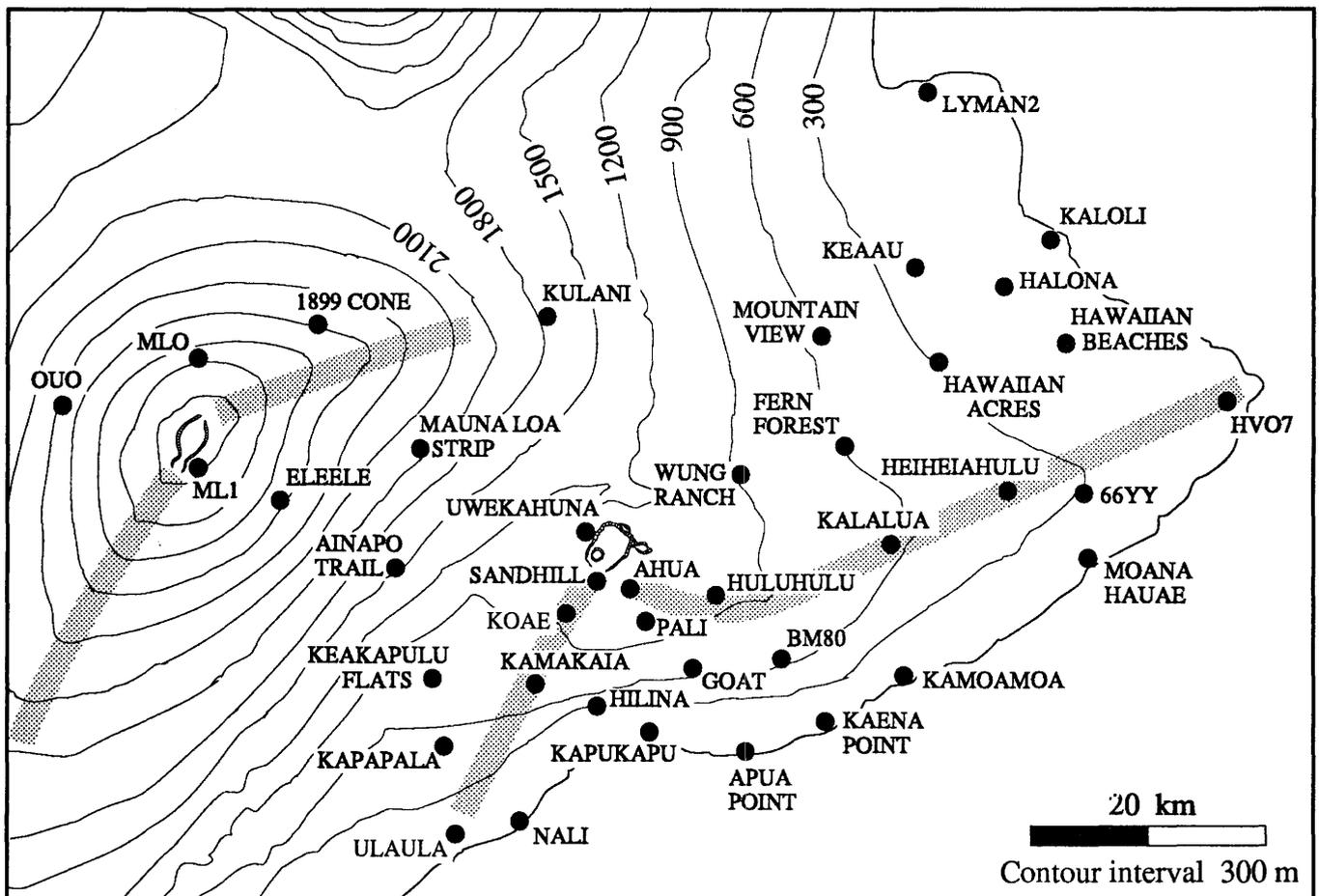


Figure 4. Most GPS stations are located on Kilauea, the most active Hawaiian volcano. Kilauea has been erupting along the east rift zone near KALALUA since 1983. The broad shaded lines are rift zones of Kilauea and the adjacent volcano Mauna Loa.

SURVEY DATES AND STATIONS

A summary of the four GPS surveys is given in table 1. Each survey lasted 3 to 6 weeks. Because a complete set of satellites was not yet in operation at the time we conducted our surveys, our observing sessions were restricted to a duration of 6 hours or less and to time of day, which depended on the time of year of each survey. The first three surveys used only so-called "Block I" satellites. The last survey used Block I satellites as well as three "Block II" satellites, which have more precise clocks than Block I but may be subjected to "selective availability," meaning broadcast ephemerides, clock epochs, and clock frequencies may be altered.

The stations occupied by each survey and survey dates are shown in figure 5. Station names and coordinates will be presented later in the section "Survey Results."

Each receiver recorded data on magnetic cassette tape: a pseudorange and a phase measurement were recorded every 30 seconds for both L1- and L2-radio signals. At the end of an observing session, data were transferred from a tape onto two different Macintosh computer diskettes. At the end of a survey, one set of diskettes and data sheets, which recorded station name and antenna height and listed when satellites were observed, was sent to Menlo Park.

When available, tracking data from the Cooperative International GPS Network (CIGNET) was obtained from the National Geodetic Survey (Chin, 1992), as well as data in 1987 from a GPS receiver operated by the University of Texas at Austin (D. Carroll, oral commun., 1989)

DATA ANALYSIS

Except for the choice of satellite orbits, our procedure to process data followed that outlined by Davis and

others (1989), using the Bernese software package developed by Beutler and others (1987).

PROCEDURE

The first step in processing was to make an empirical correction for drift of each receiver clock. The correction used pseudorange measurements to compute an initial time offset and a fifth-degree polynomial for each receiver on each day. This correction probably introduces no more than a 1-mm bias in station positions because we used double-difference values of our phase measurements (Beutler and others, 1987). (No pseudorange measurements from satellite 8 were used because the quartz clock on this satellite was too inaccurate to be used to compute receiver-clock corrections. Some Block I satellites use the more accurate rubidium clocks; the other Block I and all Block II satellites use the highly accurate cesium clocks.)

For each observing session, single-difference values of phase measurements were computed for pairs of stations. Whenever possible, we used the station LYMAN2, located at the Hilo airport, as one station to compute single-difference values so that we would have common baselines year after year. For those days during the 1987 and 1988 surveys when LYMAN2 was not occupied, another reference station was chosen. The use of stations other than LYMAN2 is indicated in the lists of station coordinates.

Double-difference values of phase measurements were computed and used to identify integer cycle slips and bad points. Orbits computed from parameters provided by NSWG were used in the identification. First, the differences of L1-phase measurements were examined, then L2. When no more cycle slips or bad points could be detected either automatically by the program or visually by the operator, double differences were computed for L3, a linear combination of L1 and L2, and examined for integer cycle slips.

Table 1. Summary of GPS surveys in Hawaii.

Survey dates	Type of receivers	Number of stations occupied	Duration of observing session (hours)	Satellites observed
Mar. 31 to Apr. 29, 1987	TI4100	37	5.1	3, 6, 9, 11, 12, 13
Aug. 12 to Sept. 2, 1988	TI4100	35	6.0*	3, 6, 9*, 11, 12, 13
Aug. 8 to Aug 25, 1989	TI4100	44	4.8†	3, 6, 9†, 11, 12, 13
July 31 to Aug. 17, 1990	TI4100	35	6.3	3, 6, 9, 12, 16, 18, 20

*Satellite 9 was not usable from Aug. 17 to Aug. 30, 1988. During these dates, observing sessions were reduced to 4.2 hours.

†Satellite 9 was not usable from Aug. 17 to Aug. 22, 1989. During these dates, observing sessions were reduced to 4.4 hours.

The next step was to compute station positions and possibly new satellite orbits if tracking data from CIGNET (Cooperative International GPS Network) were included. In these computations, we used the constant parameters listed in table 2, as well as measurements of the Earth's orientation and theoretical predictions of solid Earth tides. To minimize multipath error, we required elevation angles of satellites to be 20° or higher (Dixon, 1991).

Once satellite orbits were selected, computation of a station position relative to the fixed position of LYMAN2 was a two-step process. The first step attempted to compute integer phase-cycle ambiguities from wide-lane values of the phase measurements, the so-called L5 phase values. Resolution of the phase ambiguity improves the horizontal position of a station, but has a slight effect on the vertical position (Dixon and others, 1991). Generally,

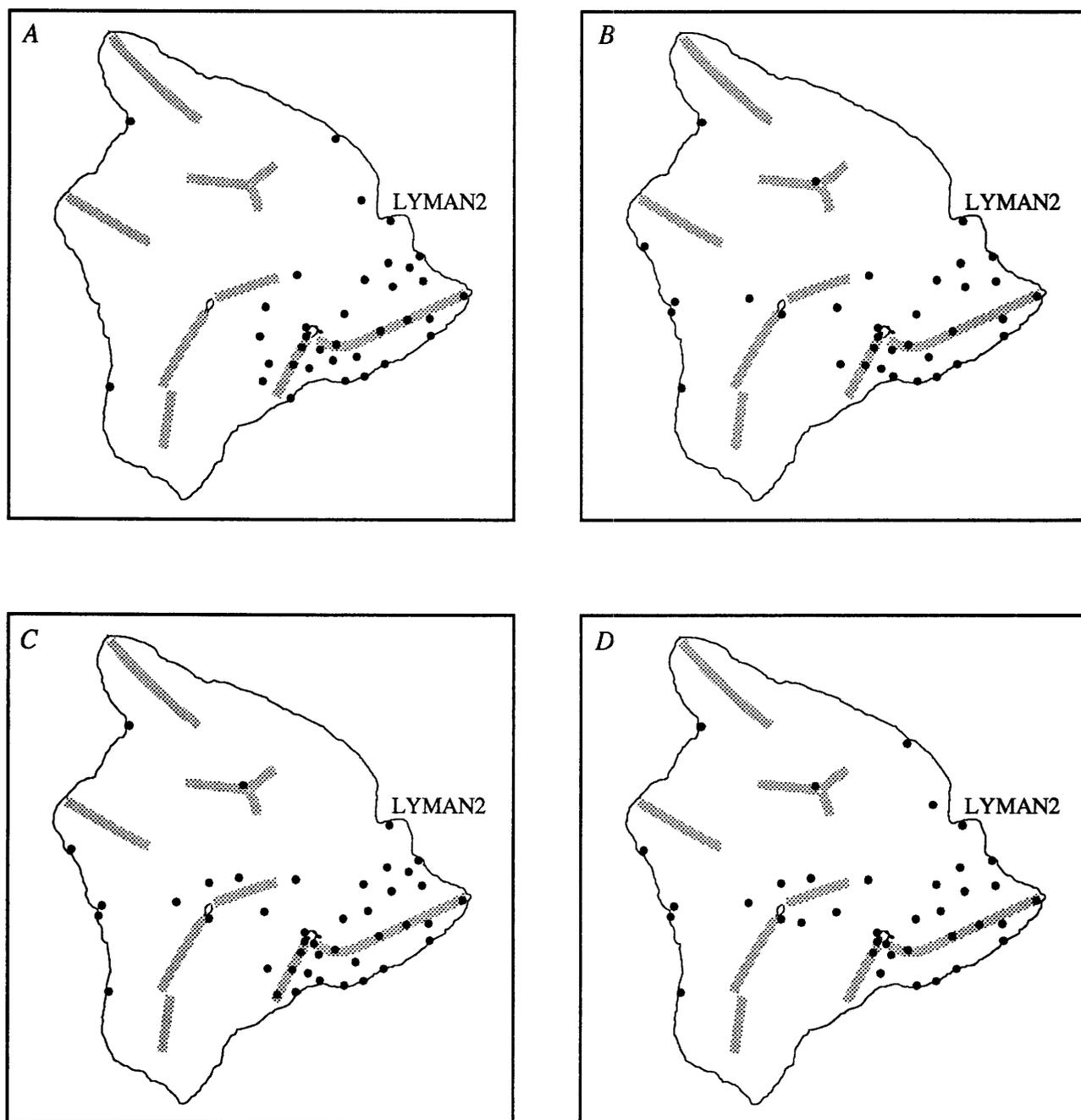


Figure 5. Stations occupied during each of the four annual GPS surveys. Rift zones indicated by shaded lines radial to the summit areas of each volcano. Stations names are shown in figures 1 and 4. WGS-84 station coordinates are listed in table 7. A, March 30 to April 29, 1987; B, August 12 to September 3, 1988; C, August 8 to 25, 1989; D, July 31 to August 17, 1990.

Table 2. Values of constant parameters.

Constant	Value		
Physical constants:			
Velocity of light-----	299792458 m/s		
(Gravity constant) × (Earth's mass)-----	$0.39860044 \times 10^{15} \text{ m}^3/\text{s}^2$		
(Gravity constant) × (Sun's mass)-----	$1.3271250 \times 10^{20} \text{ m}^3/\text{s}^2$		
(Gravity constant) × (Moon's mass)-----	$9027890 \times 10^{12} \text{ m}^3/\text{s}^2$		
Reference ellipsoid:			
Equatorial radius of Earth-----	6378137 m		
Flattening of Earth-----	1/298.257222		
Angular velocity of Earth-----	$7292115.1467 \times 10^{-11} \text{ radians/s}$		
Eccentricity of TI4100 antenna:			
L1-phase center-----	0.227 m above the base of the preamp		
L2-phase center-----	0.212		
Satellite antenna offsets:			
Block I satellites 3, 6, 9, 12, and 13-----	X = 0.21 m	Y = 0.00 m	Z = 0.854 m
Block II satellites 16, 18, 19 and 20-----	X = 0.2794 m	Y = 0.00 m	Z = 1.0229 m

we had good success in computing ambiguities, because most of our baselines were less 100 km.

The second step was to calculate the L1- and L2-ambiguities using the values from the L5 solution, then to compute final station positions by incorporating a model for the troposphere. The ionospheric delay was eliminated by a linear combination of the L1- and L2-phase measurements and the L1- and L2-carrier frequencies (Wells and others, 1986). Radio waves are nondispersive in the troposphere, so the tropospheric delay was determined by computing a single-parameter, zenith-delay model and by using an azimuthal-independent mapping function to compute the delay of any elevation angle (Davis and others, 1989). The following values at the height of the reference ellipsoid were used to compute the tropospheric delay: temperature=18°C, pressure=1013.5 millibars, and 50 percent humidity. This is the so-called "dry" correction, which assumes the troposphere is in hydrostatic equilibrium. A significant nonhydrostatic component may be caused by variations in content of water vapor, especially at the low subtropical latitudes of Hawaii. This problem is amplified on the island of Hawaii because a wide range of climatic conditions exists both laterally across the island (wet-windward versus dry-leeward sides) and over the 4-km elevation change between sea level and the summit areas of Mauna Loa and Mauna Kea. A correction for a nonhydrostatic component, the so-called "wet" correction, can be made if simultaneous measurements are made of water-vapor content during a GPS survey (Ware and others, 1986); however, water-vapor measurements are expensive and were not made in Hawaii. The result is probably a larger uncertainty of station positions for surveys conducted in the subtropics and tropics (Dixon and others, 1991).

SELECTION OF SATELLITE ORBITS

GPS can be used to determine precise station positions if satellite positions are well known. For example, at a distance of 20,000 km, a satellite position must be known to within a few meters to attain centimeter-level accuracy in ground position across a 100-km baseline. This requires careful evaluation of the quality of orbits, which we evaluated by measuring changes along presumed stable baselines.

SOURCES

We considered three sources of satellite orbits: (1) positions broadcast by the satellites at the time of each survey, (2) orbits provided by the Naval Surface Weapons Center (NSWC) and (3) our own improved orbits using tracking data supplied by National Geodetic Survey from CIGNET.

Both L1- and L2-radio signals are modulated with a data stream that includes an orbital ephemeris of each satellite. Each ephemeris, which is broadcast on the hour, consists of the six osculating elements that uniquely define a position in space. A broadcast ephemeris is a predicted satellite trajectory computed from about one week of data collected from GPS stations operated by the Department of Defense (Wells and others, 1986). A new ephemeris is sent to a satellite at least once a day, though 6-hour updates are sent occasionally. Because these broadcast ephemerides are predicted satellite orbits, they are not adequate to determine precise ground positions, except for short baselines—that is, baselines less than 15 km in length. For this reason, we used broadcast ephemerides only to compute approximate

Table 3. Coordinates of CIGNET stations.

[Values provided by National Geodetic Survey (Chin, 1992, and written communication)]

	X	Y	Z	Receiver
April 1987:				
Austin, Tex.	-743773.949	-5460643.710	3200347.492	TI4100
Kokee Park, Ha.	-5543817.052	-2054588.402	2387854.185	TI4100
Mojave, Calif.	-2356214.416	-4646733.924	3668460.609	TI4100
Westford, Mass.	1492233.223	-4458091.535	4296045.911	TI4100
August 1988:				
Kokee Park, Ha.	-5543818.046	-2054583.269	2387857.553	TI4100
Mojave, Calif.	-2356214.438	-4646733.930	3668460.620	TI4100
Richmond, Fla.	961318.469	-5674057.739	2740565.215	TI4100
Westford, Mass.	1492233.228	-4458091.550	4296045.925	TI4100
August 1989:				
Kokee Park, Ha.	-5543818.046	-2054583.269	2387857.553	TI4100
Mojave, Calif.	-2356215.619	-4646736.395	3668456.424	MiniMac
Richmond, Fla.	961319.516	-5674075.349	2740538.919	MiniMac
Westford, Mass.	1492233.301	-4458088.267	4296047.992	MiniMac

station positions, which we can compare with a final station position computed using other satellite orbits if that station position deviated from our other estimates. In this way, we identified possible problems that occurred in computing our own orbits or in orbits obtained from NSWC.

Precise satellite ephemerides are provided by NSWC several weeks after data has been received at a worldwide network of nine or more tracking stations. We use the NSWC ephemerides to compute satellite positions by straightforward integration, taking into account gravitational attraction of Earth, Sun, and Moon; a tenth-order and -degree model of Earth's gravitational field, called GEM10 (Lerch and others, 1979); solar radiation pressure; and a force on a satellite called the y-bias factor, which presumably is caused by thermal radiation of the satellite or misaligned solar panels (Schultz and others, 1990). The resultant integration, which is performed over an 8- to 56-hour period, depending on the number of successive days a station was occupied, is used to compute a new set of osculating elements and a single parameter for solar radiation pressure and another parameter for the y-bias factor.

As a third source, we computed our own improved orbits using data collected by CIGNET tracking stations. Type of receiver and location and type of antenna often changed during the years of our four surveys (Chin, 1992). As a result, different coordinates and different combinations of CIGNET stations were used during our first three surveys (table 3). (No orbits were computed for the last survey because the receiver at Kokee Park, Kauai, did not track satellites at the same time of day that our 1990 survey was conducted.) Most station coordinates listed in table 3, taken from a list of station coordinates and offsets listed in Chin (1992), are the positions of the L1-phase center expressed in the World Geodetic System 1984 (WGS-84), a terrestrial Earth-centered reference frame tied to the inertial coordinate system of the satellites (Wells and others, 1986). (In

WGS-84, the X-axis passes through the intersection of the Greenwich meridian and the equatorial plane; the Z-axis passes through the average position of Earth's rotational pole for the 1984 epoch; and the Y-axis is orthogonal to the other two axes so that a right-handed coordinate system is formed.) The exceptions were the 1987 coordinates of Austin and Kokee Park. The station coordinate for Austin was provided by M. Chin (written commun., 1989) from measurements made in January 1987. From March 28 to April 12, 1987, the GPS antenna at Kokee Park was at a temporary location at the WVRM monument (M. Chin, written commun., 1989). We have compared all 1987 coordinates obtained from NGS and coordinates in a reference frame called SV5 provided by M. Murray (written commun., 1990). The Y- and Z-coordinates of the NGS and SV5 reference frames are all within 0.2 m. The X-coordinates are biased an average of 0.371 m; after subtraction of this average value, the X-coordinates of all four stations listed in table 3 for 1987 are within 0.034 m for the two reference frames. Baselines computed with broadcast and precise ephemerides show the latter to be more accurate (such as, Remondi and Hofmann-Wellenhof, 1990) because the precise ephemerides were computed from actual tracking of the satellites and, unlike the broadcast ephemerides, were not a prediction of satellite positions. We computed similar three-dimensional positions of baselines using satellite orbits provided by NSWC and orbits computed by ourselves from CIGNET tracking data. As will be shown in the next subsection, these positions were offset 0.3 m from positions computed from broadcast orbits.

EVALUATION

We evaluated satellite orbits three ways: (1) the ability to determine the three-dimensional position of the station

LYMAN2 relative to KOKEE PARK, both by a comparison of annual determinations and during several single-day measurements during the 1987 surveys, (2) the variation in computed station positions using NSWC orbits and our own improved orbits, and (3) daily variations in station positions computed during each survey. A fourth means, which will be presented in the next section, compared annual determinations of station positions across what we expect are stable baselines on the island of Hawaii.

Annual determinations of the position of LYMAN2 are listed in table 4, using either NSWC orbits or our improved orbits and expressed in WGS-84. The values shown in table 4 were the result of multiday calculations. For 1987, the values were the average of two multiday determinations, from April 1 to 4 and from April 5 to 8. For 1988, the values determined from NSWC orbits were from April 13 to 16, from April 19 to 20, from April 24 to 26, and from April 28 to 31; the values determined from our computed orbits using CIGNET data were calculated from April 13 to 16. For 1989, only values determined from NSWC orbits are given, averaged from values determined from April 8 to 11 and from April 23 to 25; the loss of satellite 9 in August 1989 prevented us from computing an improved orbit. No positions for LYMAN2 were deter-

mined for 1990 because the Trimble GPS receiver at KOKEE PARK did not track simultaneously the same satellites we were tracking on the island of Hawaii.

The bottom of table 4 lists a conversion of WGS-84 coordinates to latitude, longitude, and height above a reference ellipsoid. Also given is the baseline distance between LYMAN2 and the 1987 position of KOKEE PARK. The largest variations of the east-west and vertical components are about 0.1 ppm for the 548-km-long line between KOKEE PARK and LYMAN2; the variation of the north-south component is 0.26 ppm. In 1987 and 1988, NSWC-derived positions and our improved-orbit positions are within several centimeters for longitude and height, but unexplainably high for latitude. The annual determinations of the baseline length are shown in figure 6.

For 1987 data, we also computed the position of LYMAN2 from single-day data to check the amount of daily scatter. The results of our single-day analyses are compared with the multiday values in figure 7. Each symbol represents a single-day value of each component relative to the average value determined from multiday inversions using NSWC orbits. For comparison, we also show the average values determined from multiday inversions using our improved orbits and broadcast orbits. As reported by many researchers, such as

Table 4. Position of GPS station LYMAN2.

	X	Y	Z			
April 1987						
NSWC orbits	-5445971.060 m	-2533159.910 m	2138839.199 m			
Calculated orbits	-5445971.143	-2533159.923	2138839.162			
August 1988						
NSWC orbits	-5445971.112	-2533159.895	2138839.127			
Calculated orbits	-5445971.082	-233159.900	2138839.252			
August 1989						
NSWC orbits	-5445971.105	-2533159.915	2138839.110			
Largest variation	0.083 m	0.028 m	0.142 m			
	Latitude	Longitude	Height ¹	Distance ²		
April 1987						
NSWC orbits	19° 43'	21.90783"	-155° 3'	17.26675"	26.030 m	548281.852 m
Calculated orbits	19 43	21.90581	-155 3	17.26755	26.093	548281.866
Difference		0.062 m		0.029 m	0.063 m	0.014 m
August 1988						
NSWC orbits	19° 43'	21.90519"	-155° 3'	17.26798"	26.044 m	548281.863 m
Calculated orbits	19 43	21.90929	-155 3	17.26739	26.063	548281.816
Difference		0.126 m		0.017 m	0.019 m	0.047 m
August 1989						
NSWC orbits	19° 43'	21.90465"	-155° 3'	17.26726"	26.040 m	548281.890 m
Largest variation		0.00318"		0.00123"	0.063 m	0.074 m
		0.143 m		0.036 m		
		0.26 ppm ³		0.07 ppm ³	0.11 ppm ³	0.14 ppm ³

¹Height above reference ellipsoid.

²Distance between LYMAN2 and the 1987 position of KOKEE PARK, Ha.

³Based on the 548-km distance between KOKEE PARK and LYMAN2.

Remondi and Hofmann-Wellenhof (1990), similar station positions are computed using orbits derived from actual tracking data, as opposed to the broadcast orbits, which are predicted satellite positions and which have larger biases. Within the daily scatter shown in figure 6, NSWC and our improved orbits yield the same position for LYMAN2—that is, a position within 0.2 ppm or less.

For 1987 data, we compared station positions on the island of Hawaii determined from NSWC and our improved orbits. In this comparison, we computed improved orbits for only the first two weeks of the survey, from March 31 to April 11, when a GPS station was operated at KOKEE PARK. For these two weeks, 21 comparisons were possible, using baseline lengths that varied from 11 to 108 km (fig. 8). If we include all baselines, the apparent changes in north/south and east/west positions both have root-mean-square values of 5 mm. If we include only baselines shorter than 80 km, the root-mean-square values were 2 and 3 mm for north/south and east/west positions, respectively. (The two baselines longer than 80 km were across the entire island, LYMAN2 to HP6 and LYMAN2 to MILOLII.) The root-mean-square value of vertical positions was 27 mm for all baselines, 12 mm for baselines shorter than 80 km. In summary, for stations on the island of Hawaii, the inversion scheme in the Bernese software using either NSWC orbits or our improved orbits from CIGNET tracking data yields horizontal positions to a centimeter or less and vertical positions to within five centimeters. We could not always compute an improved orbit because the CIGNET tracking stations did not always track the same satellites as we did during our surveys, especially when satellite 9 was unavailable during the 1988 and 1989 surveys. Orbits were always available from NSWC, so NSWC orbits were used to process all four Hawaiian GPS surveys. The remaining results in this report were derived solely by using NSWC orbits.

Because the duration of daily observing sessions varied from 4.2 to 6.3 hours and because we lost satellite 9 midway through the 1988 and 1989 surveys (table 1), we must use an independent means to estimate the accuracy of each survey. This was done by computing root-mean-square values

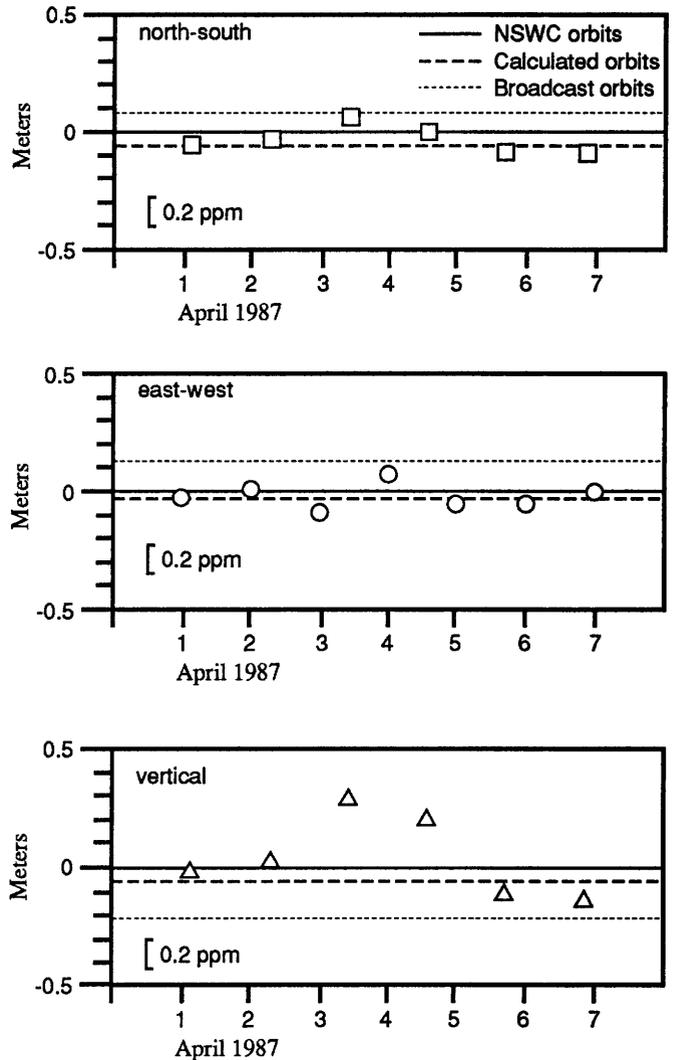
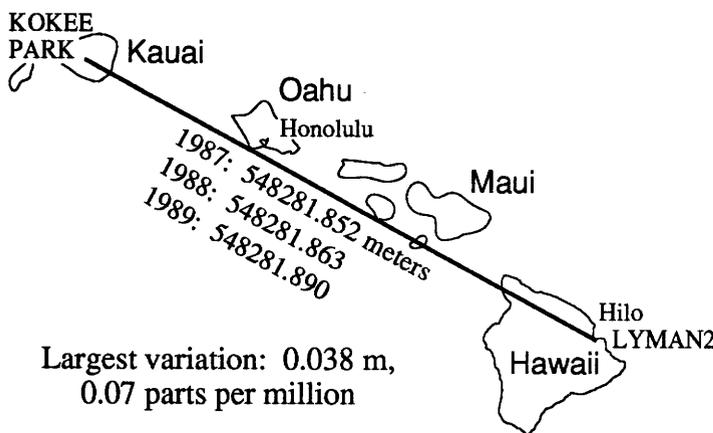


Figure 7. Comparison of daily and multiday determinations of the position of LYMAN2. The three components of position are shown with respect to the average position of LYMAN2 determined from NSWC orbits. Daily determinations are shown as symbols.

Figure 6. Annual measurements of the distance between KOKEE PARK and LYMAN2. Largest variation was 0.038 mm, which, for this 548-km-long line, corresponds to 0.07 parts per million.

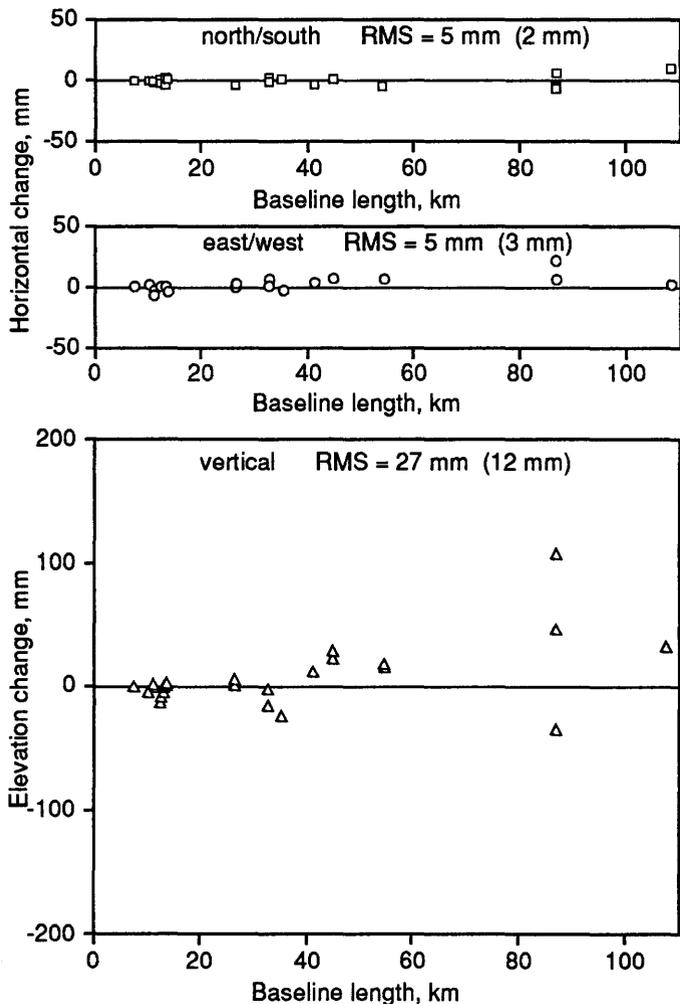


Figure 8. Differences in station positions determined using NSWC orbits and orbits calculated using tracking data from CIGNET. At top of each diagram is the root-mean-square value for all measurements; the numbers in parentheses are root-mean-square values for baselines shorter than 80 km.

for horizontal and vertical components from the daily variation for baselines measured more than once during a survey. For the 1987 survey, repeated measurements were made of 21 baselines. The apparent changes in station positions are shown in figure 9. The north/south and east/west components had root-mean-square values of 8 and 19 mm, respectively. The vertical component was 49 mm. These values are probably too pessimistic because they are based on single observing sessions. Some final station positions, to be given in the next section, are based on multiday analyses, which are more accurate than single-day analyses (for example, see Davis and others, 1989). The repeatability of each survey is listed in table 5, which is based on apparent changes in station positions for baselines repeated during a survey.

The Bernese software computes a standard error for each of the three components of position. Davis and others (1989, p. 13,639) found that these standard errors "were too

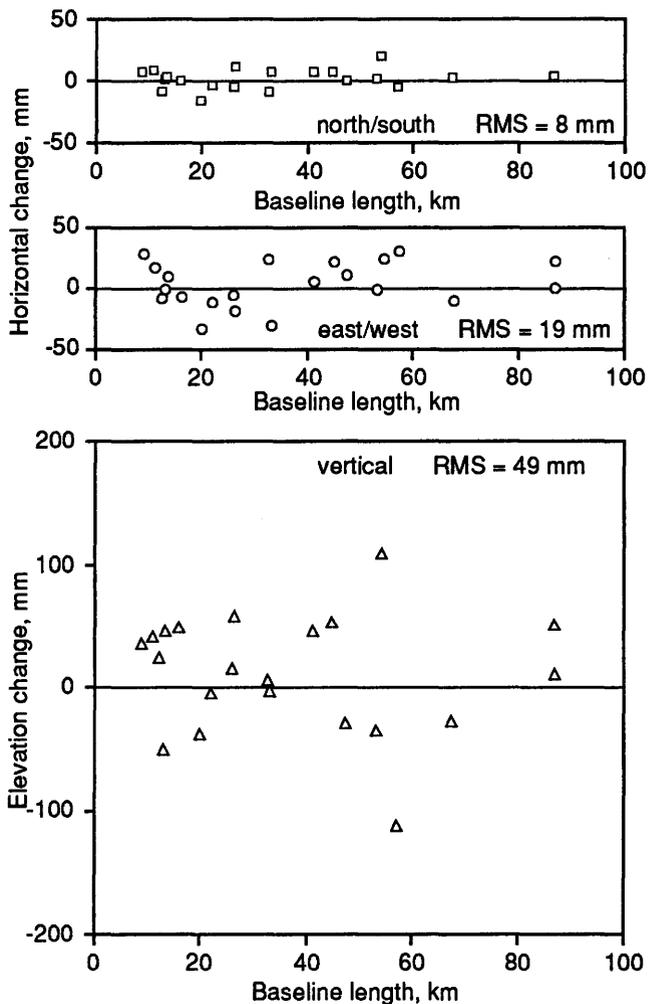


Figure 9. Daily variations in computed station positions using NSWC orbits. The root-mean-square value for each component is given in each diagram.

small by a factor of 3 to 5 to explain long-term variations." We arrived at a similar conclusion when we compared standard errors and daily variations for each survey listed in table 5. To illustrate, for each survey we computed the average standard error of each component and multiplied the result by five. The factor of five increased the standard errors to about the same values determined from our analysis of daily variations (compare tables 5 and 6). Later in this paper, where we report specific uncertainties of a station position, those uncertainties were determined by multiplying the standard error of each component by five.

SURVEY RESULTS

In this section, the position of each station for each annual survey is given in WGS-84 coordinates and in latitude, longitude, and height. Some coordinates are used to

Table 5. Daily variations of each GPS survey.

Survey	Number of Comparisons	north/south	east/west	up/down
April 1987	21	8 mm	19 mm	49 mm
August 1988	4	27	40	66
August 1989	9	20	25	60
August 1990	11	9	20	55

Table 6. Average root-mean-square error of each GPS survey (5x).

Survey	north/south	east/west	up/down
April 1987	9 mm	12 mm	51 mm
August 1988	15	45	55
August 1989	9	21	47
August 1990	9	24	51

compute baseline distances so that comparisons can be made between GPS and trilateration measurements made between several pairs of GPS benchmarks. We also examine the annual remeasurement of several stable baselines on the island of Hawaii so as to have yet another indication of the accuracy of our GPS surveys. A short subsection will report the geoid heights determined across Hawaii by the difference between geometric heights computed from the 1989 GPS survey and orthometric heights measured by a 1989 leveling survey. The remainder of this section reports the GPS results for four areas on Hawaii: the summit area of Kilauea, the south flank of Kilauea, the summit area of Mauna Loa, and the southwest coast of the island along the Kealakekua fault system.

STATION COORDINATES

For each of our four annual surveys, station positions are listed in table 7 in terms of WGS-84 Cartesian coordinates and in table 8 in terms of latitude, longitude, and height

Table 7. WGS-84 Cartesian coordinates.

Station Name	Benchmark	X	Y	Z
April 1987				
LYMAN2	LYMAN NO. 2	-5445971.060	-2533159.910	2138839.199
66YY	66YY RESET	-5451325.398	-2548417.316	2107739.303
AINAPO TRAIL	HVO 87-107	-5476761.807	-2500750.780	2102901.040
APUA POINT	APUA POINT	-5467568.137	-2527222.758	2090533.637
BM80-1 ²	80-1	-5465079.863	-2528993.779	2096703.340
GOAT	(none)	-5467608.099	-2523137.994	2097760.414
HALONA	HALONA	-5446655.633	-2546628.191	2121413.206
HAWAIIAN ACRES	HVO 87-102	-5451577.258	-2539136.530	2118338.297
HAWAIIAN BEACHES	HVO 87-103	-5446938.745	-2548835.776	2118100.255
HEIHEIAHULU	unmarked pipe	-5453582.210	-2544183.916	2107869.200
HILINA PALI	HILINA RESET 1975	-5472049.198	-2516015.185	2094380.298
HP6	HP-6 EL. 124.42	-5468952.383	-2455489.152	2170430.768
HULUHULU ¹	HULUHULU	-5465315.586	-2524702.702	2102542.641
HVO7	HVO7	-5443443.287	-2557471.217	2116435.666
KAENA POINT ²	KAENA PT	-5463732.308	-2533690.143	2092766.937
KAIWIKI	HAWAII 1210 FEET	-5448549.199	-2525466.395	2142425.664
KALALUA	iron rod	-5457770.802	-2537400.189	2105661.971
KALOLI-2	KALOLI 2	-5444567.086	-2545063.058	2128318.679
KAMAKAIA	HVO128	-5474740.771	-2509853.291	2095095.162
KAMOAMOA	HVO158	-5459919.843	-2538708.025	2096614.956
KAPAPALA ¹	KAPAPALA 1949	-5479877.125	-2503425.017	2088384.626
KAPUKAPU	US COAST + GEOD		too many cycle slips	
KEAAU	KEAAU 1949	-5449690.942	-2535471.975	2127198.360
KEAKAPULU FLATS	HVO 146	-5475056.854	-2504291.545	2102271.274
KOAE	iron rod	-5470945.407	-2513760.934	2100840.817
KULANI ¹	iron rod	-5464987.193	-2513732.093	2118309.705
MAUNA LOA STRIP ¹	HVO 87-108	-5470031.250	-2506030.587	2115499.990
MILOLI	NO 3 1973	-5501158.825	-2459964.749	2082660.333
MOANA HUAUE ²	MOANA HUAUE	-5453129.971	-2548539.545	2102293.276
MOUNTAIN VIEW	HVO 87-101	-5454498.572	-2531143.579	2120875.223
NALI	NALI	-5476894.449	-2511431.940	2085450.362
PALI	HVO111	-5468120.434	-2520350.115	2100336.740
PAPAALOA	HAWAII 1912	-5445482.138	-2512895.990	2164470.593
SANDHILL	HVO119	-5468453.448	-2516197.499	2104808.300
ULAULA	(none)		too many cycle slips	
UWEKAHUNA	HVO113	-5467410.052	-2516254.159	2107790.371
WUNG RANCH ¹	HVO 87-106	-5460266.860	-2526844.826	2112234.315

Table 7. WGS-84 Cartesian coordinates—Continued.

Station Name	Benchmark	X	Y	Z
August 1988				
LYMAN2	LYMAN NO. 2	-5445971.060	-2533159.910	2138839.199
66YY	66YY RESET	-5451325.344	-2548417.297	2107739.281
*APUA POINT	APUA POINT	-5467567.254	-2527222.859	2090533.605
BM80-1	80-1	-5465080.020	-2528993.892	2096703.340
*CAPTAIN COOK	HVO 88-12	-5491390.756	-2455768.505	2114392.958
*HAWAIIAN ACRES	HVO 87-102	-5451577.189	-2539136.473	2118338.281
*HAWAIIAN BEACHES	HVO 87-103	-5446938.744	-2548835.762	2118100.236
*HILINA PALI	HILINA RESET 1975	-5472049.262	-2516015.193	2094380.277
*HP6	HP-6 EL 124.42	-5468952.469	-2455489.146	2170430.817
*HULUHULU	HULUHULU	-5465315.635	-2524702.846	2102542.669
HVO7 ³	HVO7	-5443443.246	-2557471.171	2116435.634
KAENA POINT	KAENA PT	-5463732.443	-2533690.202	2092766.894
KAILUA	HVO 88-11	-5489953.972	-2443731.460	2130483.489
*KALALUA	iron rod	-5457770.667	-2537400.132	2105661.884
*KALOLI-2	KALOLI 2	-5444567.019	-2545063.082	2128318.688
*KAMAKAIA	HVO128	-5474740.772	-2509853.226	2095095.101
KAMOAMOAS ³	HVO158	-5459919.938	-2538708.062	2096614.939
*KAPUKAPU	US COAST + GEOD	-5470259.728	-2520715.707	2092292.353
KEAAU ⁴	KEAAU 1949	-5449691.003	-2535472.008	2127198.369
KEAKAPULU FLATS ⁵	HVO 146	-5475056.872	-2504291.571	2102271.122
KEEI	KEEI NO BASE 1948	-5492297.155	-2454606.114	2112006.028
*KOAE	iron rod	-5470945.298	-2513760.942	2100840.738
*KULANI	iron rod	-5464987.225	-2513732.122	2118309.733
*MAUNA LOA STRIP	HVO 87-108	-5470031.158	-2506030.527	2115499.937
*MILOLI	NO 3 1973	-5501158.943	-2459964.773	2082660.384
*ML1 ⁶	ML1	-5482189.891	-2487576.651	2111928.098
*MOANA HUAE	MOANA HUAE	-5453130.093	-2548539.625	2102293.331
MOUNTAIN VIEW	HVO 87-101	-5454498.531	-2531143.567	2120875.216
*OUO	76-16	-5483781.073	-2476836.254	2116261.294
*PALI	HVO111	-5468120.483	-2520350.105	2100336.739
POLIAHU	HVO 88-14	-5464796.210	-2492640.467	2150664.398
SANDHILL	HVO119	-5468453.371	-2516197.525	2104808.228
ULAULA	(none)		too many cycle slips	
UWEKAHUNA	HVO113	-5467410.125	-2516254.206	2107790.329
*WUNG RANCH	HVO 87-106	-5460266.860	-2526844.777	2112234.281
August 1989				
LYMAN2	LYMAN NO. 2	-5445971.060	-2533159.910	2138839.199
*1899	1899	-5473028.975	-2495131.859	2123112.472
66YY	66YY RESET	-5451325.206	-2548417.264	2107739.012
AHUA	HVO 114	-5467762.194	-2518810.862	2103350.702
APUA POINT	APUA POINT	-5467568.214	-2527222.856	2090533.550
BM80-1	80-1	-5465079.968	-2528993.943	2096703.241
CAPTAIN COOK	HVO 88-12	-5491390.780	-2455768.482	2114392.986
FERN FOREST	HVO 89-1	-5458401.521	-2531794.233	2111447.523
GOAT	(none)		too many cycle slips	
*HALONA	HALONA	-5446655.682	-2546628.266	2121413.203
HAWAIIAN ACRES	HVO 87-102	-5451577.256	-2539136.571	2118338.230
HAWAIIAN BEACHES	HVO 87-103	-5446938.791	-2548835.809	2118100.191
HEIHELAHULU	unmarked pipe	-5453581.821	-2544183.836	2107868.654
HILINA PALI	HILINA RESET 1975	-5472049.310	-2516015.261	2094380.281
*HP6	HP-6 EL 124.42	-5468952.458	-2455489.178	2170430.801
HULUHULU	HULUHULU	-5465315.541	-2524702.753	2102542.539
HVO7	HVO7	-5443443.225	-2557471.169	2116435.583
KAENA POINT	KAENA PT	-5463732.379	-2533690.308	2092766.772
KAILUA	HVO 88-11	-5489953.905	-2443731.458	2130483.521
KALALUA	iron rod	-5457770.435	-2537400.232	2105661.541
KALOLI-2	KALOLI 2	-5444567.061	-2545163.049	2128318.653
KAMAKAIA	HVO128	-5474740.739	-2509853.306	2095095.133
KAMOAMOAS	HVO158	-5459919.888	-2538708.170	2096614.736
KAPUKAPU	US COAST + GEOD	-5470259.819	-2520715.914	2092292.421
KEAAU	KEAAU 1949	-5449690.933	-2535471.995	2127198.346
KEAKAPULU FLATS	HVO 146	-5475056.844	-2504291.566	2102271.243
KEEI	KEEI NO BASE 1948	-5492297.052	-2454606.041	2112006.005
*KOAE	iron rod	-5470945.340	-2513761.059	2100840.712
KULANI	iron rod	-5464987.184	-2513732.054	2118309.681
MAUNA KEA SUMMIT	SUMMIT 1955	-5464366.269	-2493933.083	2150467.594

Table 7. WGS-84 Cartesian coordinates—Continued.

Station Name	Benchmark	X	Y	Z
August 1989—Continued				
*MAUNA LOA STRIP	HVO 87-108	-5470031.266	-2506030.612	2115500.001
MILOLI	NO 3 1973	-5501158.841	-2459964.734	2082660.358
MLI ⁷	MLI	-5482189.849	-2487576.633	2111928.084
*MLO	STAIR 1955	-5477995.864	-2487729.829	2120552.036
MOANA HUAUE	MOANA HUAUE	-5453130.035	-2548539.796	2102293.102
MOUNTAIN VIEW	HVO 87-101	-5454498.510	-2531143.587	2120875.187
*NALI	NALI	-5476894.565	-2511431.968	2085450.341
OOU	76-16	-5483781.114	-2476836.302	2116261.342
PALI	HVO111	-5468120.382	-2520350.139	2100336.671
POLIAHU ⁸	HVO 88-14	-5464796.225	-2492640.410	2150664.397
SANDHILL	HVO119	-5468453.271	-2516197.535	2104808.141
*ULAULA	(none)	-5480137.507	-2505453.017	2084773.267
UWEKAHUNA	HVO113	-5467410.090	-2516254.227	2107790.279
WUNG RANCH	HVO 87-106	-5460266.904	-2526844.876	2112234.303
August 1990				
LYMAN2	LYMAN NO. 2	-5445971.060	-2533159.910	2138839.199
1899 CONE	1899	-5473028.901	-2495131.848	2123112.458
66YY	66YY RESET	-5451325.099	-2548417.226	2107738.975
AHUA	HVO 114	-5467762.082	-2518810.858	2103350.659
APUA POINT	APUA POINT	-5467568.274	-2527222.933	2090533.506
CAPTAIN COOK	HVO 88-12	-5491390.749	-2455768.481	2114392.971
ELEELE	PUU ELEELE 1976	-5478438.231	-2494590.287	2110845.607
FERN FOREST	HVO 89-1	-5458401.501	-2531794.227	2111447.505
HAWAIIAN ACRES	HVO 87-102	-5451577.159	-2539136.504	2118338.180
HAWAIIAN BEACHES	HVO 87-103	-5446938.735	-2548835.790	2118100.164
HEIHEIAHULU	unmarked pipe	-5453581.870	-2544183.873	2107868.643
HILINA PALI	HILINA RESET 1975	-5472049.341	-2516015.326	2094380.269
HP6	HP-6 EL 124.42	-5468952.522	-2455489.177	2170430.841
HULUHULU	HULUHULU	-5465315.402	-2524702.752	2102542.450
HVO7	HVO7	-5443443.291	-2557471.211	2116435.619
August 1990				
KAENA POINT	KAENA PT	-5463732.427	-2533690.370	2092766.722
KAILUA	HVO 88-11	-5489953.952	-2443731.463	2130483.521
KALALUA	iron rod	-5457770.357	-2537400.255	2105661.487
KALOLI-2	KALOLI 2	-5444567.092	-2545063.022	2128318.663
KAMOAMOA	HVO158	-5459919.910	-2538708.316	2096614.692
KEAAU	KEAAU 1949	-5449690.867	-2535471.949	2127198.322
KEEI	KEEI NO BASE 1948	-5492297.105	-2454606.052	2112006.018
KULANI	iron rod	-5464987.154	-2513732.018	2118309.662
MAUNA LOA STRIP	HVO 87-108	-5470031.229	-2506030.590	2115499.970
MILOLI	NO 3 1973	-5501159.002	-2459964.743	2082660.394
MLI ⁹	MLI	-5482189.851	-2487576.616	2111928.065
MLO	STAIR 1955	-5477995.802	-2487729.798	2120552.010
MOANA HUAUE	MOANA HUAUE	-5453129.996	-2548539.786	2102293.050
MOUNTAIN VIEW	HVO 87-101	-5454498.581	-2531143.638	2120875.207
OOU	76-16	-5483781.016	-2476836.353	2116261.327
PALI	HVO111	-5468120.269	-2520350.184	2100336.629
POLIAHU	HVO 88-14	-5464796.254	-2492640.440	2150664.422
SANDHILL	HVO119	-5468453.199	-2516197.620	2104808.089
UWEKAHUNA	HVO113	-5467410.042	-2516254.240	2107790.215
WUNG RANCH	HVO 87-106	-5460266.821	-2526844.867	2112234.270

*Loss of satellite 9, so daily observing sessions shortened to 4.2 hours.

¹Measured with respect to UWEKAHUNA coordinates in this table.

²Measured with respect to KAMOAMOA coordinates in this table.

³Measured with respect to KAENA POINT coordinates in this table.

⁴Measured with respect to 66YY coordinates in this table.

⁵Measured with respect to KEAAU coordinates in this table.

⁶Measured with respect to OOU coordinates in this table.

⁷Relative to the 1988 location of OOU coordinates in this table.

⁸Relative to HP6 coordinates in this table.

⁹Relative to the 1988 location of OOU coordinates in this table.

Table 8. Latitude, longitude, and height.

Station Name	Latitude	Longitude	Height, M
April 1987			
LYMAN2	19° 43' 21.90783"	-155° 3' 17.26675"	26.030
66YY	19 25 25.86693	-154 56 40.48070	254.948
AINAPO TRAIL	19 22 24.01569	-155 27 28.90794	1570.134
APUA POINT	19 15 35.48955	-155 11 33.52729	24.242
BM80-1	19 19 1.14017	-155 10 2.70305	632.265
GOAT	19 19 35.31428	-155 13 41.10818	829.716
HALONA	19 33 19.18200	-154 56 28.23862	114.842
HAWAIIAN ACRES	19 31 30.89500	-155 1 32.49825	303.809
HAWAIIAN BEACHES	19 31 24.68650	-154 55 23.76130	129.953
HEIHEIAHULU	19 25 27.10891	-154 59 24.68727	537.243
HILINA PALI	19 17 40.25410	-155 18 26.33012	706.368
HP6	20 1 33.92022	-155 49 13.92297	59.044
HULUHULU	19 22 17.38996	-155 12 19.52065	1069.214
HVO7	19 30 28.21852	-154 50 4.70910	46.267
KAENA POINT	19 16 52.24748	-155 7 17.34985	40.369
KAIWIKI	19 45 21.58620	-155 7 54.20832	388.607
KALALUA	19 24 9.32973	-155 3 56.05541	683.630
KALOLI-2	19 37 18.60751	-154 56 46.53846	23.016
KAMAKAIA	19 18 3.53623	-155 22 16.57665	824.707
KAMOAMOA	19 19 4.80949	-155 3 46.46580	43.199
KAPAPALA	19 14 16.13163	-155 26 49.92369	493.848
KEAAU	19 36 37.84746	-155 2 59.16437	202.708
KEAKAPULU FLATS	19 22 5.55002	-155 25 14.29943	1286.773
KOAE	19 21 19.41793	-155 19 20.69906	1009.501
KULANI	19 31 13.73647	-155 17 56.29830	1706.544
MAUNA LOA STRIP	19 29 32.74787	-155 23 8.42127	2060.734
MILOLII	19 11 4.37055	-155 54 25.69945	19.580
MOANA HAUAE	19 22 20.59660	-154 57 2.87443	36.977
MOUNTAIN VIEW	19 32 59.47906	-155 6 23.34643	473.112
NALI	19 12 39.38878	-155 21 58.17556	113.283
PALI	19 21 1.92384	-155 15 15.18000	1020.165
PAPAALOA	19 58 4.84899	-155 13 42.09289	297.567
SANDHILL	19 23 34.56079	-155 17 29.18271	1150.027
UWEKAHUNA	19 25 15.99833	-155 17 12.47169	1269.244
WUNG RANCH	19 27 54.42314	-155 10 0.26728	817.255
August 1988			
LYMAN2	19° 43' 21.90783"	-155° 3' 17.26675"	26.030
66YY	19 25 25.86689	-154 56 40.48052	254.887
*APUA POINT	19 15 35.48697	-155 11 33.52584	24.372
BM80-1	19 19 1.13815	-155 10 2.70181	632.444
*CAPTAIN COOK	19 29 12.57364	-155 54 20.32293	495.816
*HAWAIIAN ACRES	19 31 30.89547	-155 1 32.49904	303.722
*HAWAIIAN BEACHES	19 31 24.68600	-154 55 23.76171	129.939
*HILINA PALI	19 17 40.25281	-155 18 26.33075	706.419
*HP6	20 1 33.92088	-155 49 13.92436	59.133
*HULUHULU	19 22 17.38969	-155 12 19.51686	1069.323
HVO7	19 30 28.21816	-154 50 4.70995	46.203
KAENA POINT	19 16 52.24456	-155 7 17.34995	40.494
KAILUA	19 38 33.31370	-156 0 17.35709	26.383
*KALALUA	19 24 9.32864	-155 3 56.05523	683.464
*KALOLI-2	19 37 18.60833	-154 56 46.53672	22.971
*KAMAKAIA	19 18 3.53465	-155 22 16.57870	824.662
KAMOAMOA	19 19 4.80787	-155 3 46.46602	43.290
*KAPUKAPU	19 16 32.51575	-155 15 34.47644	337.607
KEAAU	19 36 37.84701	-155 2 59.16423	202.776
KEAKAPULU FLATS	19 22 5.54907	-155 25 14.29885	1286.750
KEEI	19 27 55.56504	-155 55 9.39249	32.842
*KOAE	19 21 19.41653	-155 19 20.69725	1009.384
*KULANI	19 31 13.73690	-155 17 56.29784	1706.592
*MAUNA LOA STRIP	19 29 32.74741	-155 23 8.42185	2060.614
*MILOLII	19 11 4.37086	-155 54 25.70035	19.708
*MLI	19 27 6.36432	-155 35 36.75375	4082.388
*MOANA HAUAE	19 22 20.59685	-154 57 2.87359	37.123
MOUNTAIN VIEW	19 32 56.47930	-155 6 23.34622	473.069
*OUO	19 29 51.44276	-155 41 34.56397	2717.557
*PALI	19 21 1.92337	-155 15 15.18101	1020.203
POLIAHU	19 49 22.06399	-155 28 51.58572	4163.806
SANDHILL	19 23 34.55921	-155 17 29.18083	1149.948
UWEKAHUNA	19 25 15.99605	-155 17 12.47124	1269.314
*WUNG RANCH	19 27 54.42234	-155 10 0.26878	817.224

SURVEY RESULTS

Table 8. Latitude, longitude, and height—Continued.

Station Name	Latitude		Longitude		Height, M		
August 1989							
LYMAN2	19°	43'	21.90783"	-155°	3'	17.26675"	26.030
*1899 CONE	19	33	45.58037	-155	29	31.01566	2905.298
66YY	19	25	25.86013	-154	56	40.47954	254.666
AHUA	19	22	44.83449	-155	15	57.93868	1104.856
APUA POINT	19	15	35.48568	-155	11	33.52536	24.317
BM80-1	19	19	1.13539	-155	10	2.69946	632.387
CAPTAIN COOK	19	29	12.57439	-155	54	20.32370	495.838
FERN FOREST	19	27	29.01491	-155	6	55.14843	667.009
*HALONA	19	33	19.18108	-154	56	28.23701	114.913
HAWAIIAN ACRES	19	31	30.89280	-155	1	32.49694	303.801
HAWAIIAN BEACHES	19	31	24.68393	-154	55	23.76096	129.984
HEIHEIAHULU	19	25	27.09634	-154	59	24.68409	536.697
HILINA PALI	19	17	40.25215	-155	18	26.32933	706.488
*HP6	20	1	33.92032	-155	49	13.92322	59.130
HULUHULU	19	22	17.38703	-155	12	19.51841	1069.162
HVO7	19	30	28.21680	-154	50	4.70968	46.167
KAENA POINT	19	16	52.24098	-155	7	17.34576	40.441
KAILUA	19	38	33.31535	-156	0	17.35622	26.336
KALALUA	19	24	9.31995	-155	3	56.04878	683.191
KALOLI-2	19	37	18.60701	-154	56	46.53835	22.982
KAKAKAIA	19	18	3.53560	-155	22	16.57571	824.676
KAMOAMOA	19	19	4.80163	-155	3	46.46197	43.222
KAPUKAPU	19	16	32.51604	-155	15	34.47131	337.789
KEAAU	19	36	37.84703	-155	2	59.16361	202.704
KEAKAPULU FLATS	19	22	5.54907	-155	25	14.29865	1286.763
KEEI	19	27	55.56566	-155	55	9.39334	32.716
*KOEAE	19	21	19.41479	-155	19	20.69422	1009.457
KULANI	19	31	13.73601	-155	17	56.29937	1706.513
MAUNA KEA SUMMIT	19	49	14.44472	-155	28	5.07329	4233.867
*MAUNA LOA STRIP	19	29	32.74793	-155	23	8.42073	2060.761
MILOLII	19	11	4.37124	-155	54	25.70015	19.596
MLI	19	27	6.36441	-155	35	36.75371	4082.341
*MLO	19	32	11.32361	-155	34	32.55787	3419.922
MOANA HAUAE	19	22	20.58948	-154	57	2.86756	37.074
MOUNTAIN VIEW	19	32	56.47853	-155	6	23.34528	473.049
*NALI	19	12	39.38688	-155	21	58.17634	113.386
OUO	19	29	51.44362	-155	41	34.56306	2717.627
PALI	19	21	1.92213	-155	15	15.17851	1020.108
POLLAHU	19	49	22.06400	-155	28	51.58774	4163.796
SANDHILL	19	23	34.55749	-155	17	29.17907	1149.837
*ULAULA	19	12	13.67753	-155	25	50.48436	324.550
UWEKAHUNA	19	25	15.99483	-155	17	12.47012	1269.273
WUNG RANCH	19	27	54.42212	-155	10	0.26635	817.308
August 1990							
LYMAN2	19°	43'	21.90783"	-155°	3'	17.26675"	26.030
1899 CONE	19	33	45.58072	-155	29	31.01500	2905.228
66YY	19	25	25.86015	-154	56	40.47914	254.550
AHUA	19	22	44.83425	-155	15	57.93720	1104.746
APUA POINT	19	15	35.48332	-155	11	33.52381	24.386
CAPTAIN COOK	19	29	12.57422	-155	54	20.32358	495.807
ELEELE	19	26	38.74070	-155	31	4.78759	3238.165
FERN FOREST	19	27	29.01455	-155	6	55.14833	666.986
HAWAIIAN ACRES	19	31	30.89248	-155	1	32.49760	303.676
HAWAIIAN BEACHES	19	31	24.68369	-154	55	23.76070	129.921
HEIHEIAHULU	19	25	27.09528	-154	59	24.68368	536.752
HILINA PALI	19	17	40.25111	-155	18	26.32776	706.538
HP6	20	1	33.92097	-155	49	13.92411	59.201
HULUHULU	19	22	17.38562	-155	12	19.51643	1069.015
HVO7	19	30	28.21704	-154	50	4.70936	46.254
KAENA POINT	19	16	52.23860	-155	7	17.34453	40.492
KAILUA	19	38	33.31487	-156	0	17.35674	26.380
KALALUA	19	24	9.31890	-155	3	56.04694	683.116
KALOLI-2	19	37	18.60710	-154	56	46.53964	23.003
KAMOAMOA	19	19	4.79935	-155	3	46.45774	43.287
KEAAU	19	36	37.84717	-155	2	59.16408	202.623
KEEI	19	27	55.56544	-155	55	9.39374	32.772
KULANI	19	31	13.73584	-155	17	56.30004	1706.468
MAUNA LOA STRIP	19	29	32.74742	-155	23	8.42089	2060.713
MILOLII	19	11	4.37063	-155	54	25.70209	19.752
MLI	19	27	6.36386	-155	35	36.75424	4082.331
MLO	19	32	11.32353	-155	34	32.55794	3419.850

Table 8. Latitude, longitude, and height—Continued.

Station Name	Latitude		Longitude		Height, M		
August 1990—Continued							
MOANA HAUAE	19°	22'	20.58828	-154°	57'	2.86731	37.022
MOUNTAIN VIEW	19	32	56.47818	-155	6	23.34470	473.139
OOU	19	29	51.44385	-155	41	34.56007	2717.559
PALI	19	21	1.92166	-155	15	15.17548	1020.016
POLIAHU	19	49	22.06443	-155	28	51.58721	4163.844
SANDHILL	19	23	34.55619	-155	17	29.17539	1149.793
UWEKAHUNA	19	25	15.99323	-155	17	12.46904	1269.218
WUNG RANCH	19	27	54.42194	-155	10	0.26545	817.224

*Loss of satellite 9, so daily observing sessions shortened to 4.4 hours.

above the reference ellipsoid defined in table 2. (At the latitude of Hawaii, 0.01" of latitude or longitude is about 0.3 m.) Also given in table 7 is the name stamped on the benchmark or the type of mark used, such as an iron rod at KALALUA. All station coordinates in tables 7 and 8 are relative to the position of LYMAN2 computed for the April 1987 survey using NSWC orbits and listed in the bottom half of table 4.

Most station positions were computed from baselines that included LYMAN2 as one endpoint. The exceptions are given in a footnote. For example, for the 1987 survey, the position of HULUHULU was computed from a baseline that had HULUHULU and UWEKAHUNA as endpoints. If in some future re-analysis of these surveys the position of UWEKAHUNA is adjusted, then the position of HULUHULU must be adjusted by the same amount. During the 1989 and 1990 surveys, LYMAN2 was occupied every day.

The loss of satellite 9 during a major portion of the 1988 and 1989 surveys reduced the duration of our daily observing sessions, which resulted in less accurate measurements. Asterisks in tables 7 and 8 identify the stations surveyed when satellite 9 was unavailable.

The position of a few stations, such as KAPUKAPU in 1987, could not be determined because of a large number of cycle slips, mostly in L2-carrier phase measurements. As a result, no coordinates are given for a few stations.

Differences in measured station positions of four pairs of surveys are listed in table 9. The first three survey pairs are for successive annual surveys between 1987 and 1990. The last pair is for the full four years from 1987 to 1990. A positive difference means a measured change to the north, east, or up. At the bottom of table 9, an uncertainty for each component for each survey pair was computed as the square root of the sum of the squares of the uncertainties given in table 5 for the appropriate component and survey. For example, the daily variation in measuring the north/south component was 8 mm in 1987 and 27 mm in 1988. (As mentioned in an earlier section, we assume these daily variations are the accuracy of each survey.) The uncertainty in computing the difference

in north/south positions between 1987 and 1988 was $\sqrt{27^2 + 8^2} = 28\text{mm}$.

COMPARISON OF GPS AND TRILATERATION MEASUREMENTS

Trilateration measurements were made in the summit area of Kilauea at about the same time as the GPS surveys. The station-to-station distances measured using a laser instrument and GPS are listed in table 10 and plotted in figure 10. (The 1990 trilateration measurements of ML-Strip were not to the GPS benchmark (MAUNA LOA STRIP), but to another benchmark (stamped ML STRIP) located about 200 m east. Trilateration measurements were also made to ML STRIP in August 1989, and so a change in line length measured to ML STRIP between August 1989 and October 1990 was assumed to be the same as a change in line length to the GPS benchmark.)

Distances computed from our laser measurements are almost always longer than those computed from GPS (figs. 10 and 11 and last column in table 10) because an inadequate refraction correction has been made to the laser measurements. Air temperatures that were measured only at the endpoints, used to compute a refraction correction, are higher than the air temperature averaged along the line-of-sight, and so computed distances are slightly too long. To illustrate this bias, we have plotted in figure 11 the differences between laser and GPS measurements as a function of baseline distance. The dashed line indicates a bias of 5 ppm, which means, on average, endpoint temperatures overestimate average line-of-sight temperatures by about 5°C. (When air temperatures are measured along the entire line between two stations, distances determined by laser and GPS measurements agree to within 0.2 ppm (Prescott and others, 1989).)

In studying active volcanoes, we are concerned with changes in station positions, not absolute positions, and so for our purposes, the bias between laser and GPS measurements is not as great as indicated by figure 11. Furthermore, on active volcanoes we are more apt to measure changes of ten

Table 9. Coordinate differences between GPS surveys.

[Values expressed in millimeters]

Station name	1988-1987			1989-1988			1990-1989			1990-1987		
	N/S	E/W	U/D									
1899 CONE												
66YY	-1	6	-61	-208	28	-221	11	19	-70			
AHUA							2	12	-116	-207	46	-398
APUA POINT	-79	42	130	-40	14	55	-6	44	-20			
BM80-1	-62	36	179	-85	69	-57	-70	45	69	-189	101	144
CAPTAIN COOK				22	-31	22	-4	11	-9			
FERN FOREST							-9	3	-23			
HAWAIIAN ACRES	14	-23	-87	-82	61	79	-9	-20	-125	-77	18	-133
HAWAIIAN BEACHES	-15	-12	-13	-64	22	45	-6	7	-63	-85	17	-31
HEIHEIAHULU							-31	12	55	-418	104	-491
HILINA PALI	-40	-22	51	-20	41	69	-30	46	50	-90	69	170
HP6	20	-40	89	-17	32	-37	18	-25	72	21	-33	157
HULUHULU	-8	111	109	-82	-45	-161	-41	57	-147	-131	123	-199
HVO7	-11	-24	-64	-42	7	-36	-9	10	87	-44	-7	-13
KAENA POINT	-89	-3	125	-110	122	-53	-71	35	51	-270	154	129
KAILUA				51	25	-47	-15	-15	44			
KALALUA	-33	5	-166	-268	188	-273	-30	53	-75	-331	246	-514
KALOLI-2	25	50	-45	-41	-47	11	4	-37	21	-12	-34	-13
KAMAKAIA	-49	-60	-45	28	87	14						
KAMOAMOAO	-51	-6	91	-191	118	-68	-69	123	65	-311	235	88
KAPUKAPU				9	150	182						
KEAAU	-13	4	68	0	18	-72	5	-14	-81	-8	8	-85
KEAKAPULU FLATS	-29	17	-23	0	5	13						
KEEI				24	-13	-37	-6	-11	56			
KOAE	-43	53	-117	-53	88	73						
KULANI	14	13	48	-28	-44	-79	-4	-20	-45	-18	-51	-76
MAUNA LOA STRIP	14	-17	-120	-16	32	147	15	-4	-48	13	11	-21
MILOLII	9	-26	128	12	6	-112	-17	-57	196	4	-77	172
ML1				3	1	-46	-17	-15	-9			
MLO							-1	-2	-72			
MOANA HAUAE	8	24	145	-227	176	-49	-35	7	-52	-254	207	44
MOUNTAIN VIEW	8	5	-43	-24	28	-20	-10	16	90	-26	49	27
OOU				26	27	70	9	87	-68			
PALI	-15	-30	38	-38	73	-95	-12	88	-92	-65	131	-149
POLIAHU				1	-58	-11	11	15	49			
SANDHILL	-48	55	-79	-53	51	-111	-39	107	-44	-140	213	-234
UWEKAHUNA	-70	14	69	-38	32	-40	-47	32	-56	-155	78	-27
WUNG RANCH	-24	-44	-31	-7	71	84	-5	26	-84	-36	53	-31
¹ Uncertainties	(28)	(44)	(82)	(34)	(47)	(96)	(22)	(32)	(89)	(12)	(28)	(74)

¹Uncertainties are the square root of the sum of the squares of the uncertainties given for the appropriate component for each survey in table 5. For example, for the 1988 and 1987 surveys, the uncertainty of the difference of the N/S component was [$\sqrt{27^2 + 8^2} = 28$].

parts per million or more, in which case laser and GPS measurements record similar changes in line lengths (fig. 12).

STABLE BASELINES

Annual measurements across three baselines, which did not span areas of seismic or volcanic activity, are shown in figure 13A. The range of north/south or east/west positions is usually within 30 mm, with the 1988 measurement showing the largest variation. The range of vertical positions is

70 mm or more. There appears to be a trend of increasing elevation difference between LYMAN2 and HP6, which may represent a mistake in measuring antenna height in 1987 or 1990 or illustrate the limitation of the single-parameter tropospheric model and the lack of water vapor measurements. (LYMAN2 is on the windward side of the island where annual rainfall is 180 inches (5 m); HP6 is on the arid leeward side where annual rainfall is less than 0.1 m.) Although there is a 4,000-m-elevation difference between LYMAN2 and POLIAHU, this baseline has the same repeatability as the other two stable baselines.

Table 10. Comparison of trilateration and GPS measurements.

Stations	Trilateration		GPS Survey		Difference m
	Date	Length, m	Date	Length, m	
Uwekahuna - Sandhill	Nov. 5, 1986	3159.911	Apr 1987	3159.847	0.064
	Aug. 4, 1988	3159.883	Aug 1988	3159.826	0.057
	Aug. 18, 1989	3159.850	Aug 1989	3159.840	0.010
	Oct. 2, 1990	3159.856	Aug 1990	3159.845	0.011
Uwekahuna - Pali	Nov. 5, 1986	8534.568	Apr 1987	8534.525	0.043
	Aug. 4, 1988	8534.524	Aug 1988	8534.460	0.064
	Aug. 18, 1989	8534.491	Aug 1989	8534.476	0.015
	Oct. 2, 1990	8534.489	Aug 1990	8534.467	0.022
Uwekahuna - Kulani	Nov. 4, 1986	11085.428	Apr 1987	11085.461	-0.033
	Aug. 4, 1988	11085.582	Aug 1988	11085.541	0.041
	Aug. 18, 1989	11085.601	Aug 1989	11085.560	0.041
	Oct. 2, 1990	11085.645	Aug 1990	11085.610	0.035
Uwekahuna - MLStrip	Jul. 2, 1987	13070.316	Apr 1987	13070.208	0.108
	Aug. 4, 1988	13070.380	Aug 1988	13070.252	0.128
	Aug. 18, 1989	13070.378	Aug 1989	13070.298	0.080
	Oct. 18, 1990	13070.430*	Aug 1990	13070.347	0.083
Sandhill - Pali	Nov. 5, 1986	6111.516	Apr 1987	6111.462	0.054
	Aug. 4, 1988	6111.460	Aug 1988	6111.378	0.082
	Aug. 18, 1989	6111.370	Aug 1989	6111.381	-0.011
	Oct. 19, 1990	6111.335	Aug 1990	6111.349	-0.014
Sandhill - Kulani	Nov. 4, 1986	14155.598	Apr 1987	14155.603	-0.005
	Aug. 4, 1988	14155.735	Aug 1988	14155.671	0.064
	Aug. 18, 1989	14155.743	Aug 1989	14155.703	0.040
	Oct. 2, 1990	14155.744	Aug 1990	14155.746	-0.002
Sandhill - MLStrip	Jul. 2, 1987	14838.157	Apr 1987	14838.052	0.105
	Aug. 4, 1988	14838.238	Aug 1988	14838.123	0.115
	Aug. 18, 1989	14838.284	Aug 1989	14838.203	0.081
	Oct. 18, 1990	14838.338*	Aug 1990	14838.295	0.043
Pali - MLStrip	Jul. 2, 1987	20943.477	Apr 1987	20943.358	0.119
	Aug. 4, 1988	20943.527	Aug 1988	20943.342	0.185
	Aug. 18, 1989	20943.511	Aug 1989	20943.422	0.089
	Oct. 18, 1990	20943.546*	Aug 1990	20943.482	0.064

*Change relative to trilateration benchmark.

Annual measurements of three shorter baselines are shown in figure 13B. MAUNA LOA STRIP and KEAKAPULU FLATS both lie in the Hilea-Kaoiki seismic area, where several earthquakes greater than 5.0 magnitude occurred between 1981 and 1983. During the four years spanned by our surveys, however, earthquake activity was low, and so for that time period we consider these baselines stable. The range of north/south or east/west positions was within 30 mm; however, the range of vertical positions was more than 100 mm for the baselines that included KULANI and MAUNA LOA STRIP. (If the 1988 survey is excluded, the range of vertical positions for these two baselines was less than 60 mm. Both baselines were measured during the shortened observing sessions in 1988; a six-hour observing session was used to measure the baseline to KEAKAPULU FLATS.) In view of these measurements, as well as the earlier discussion about daily variations in repeating baseline measurements, on average, single-day measurements yield north/south and east/west

positions to within 30 mm and vertical positions to 60 mm. Those baselines measured during shortened observing sessions in 1988 are less accurate by as much as a factor of two.

HEIGHT OF THE GEOID

Though vertical positions are the most difficult to measure with GPS, an accuracy of 100 mm or better is adequate to determine height of the geoid if elevations from leveling surveys are also available. GPS measures geometric heights, the height that would be measured if a long graduated bar extended from Earth's center of mass to the surface. Elevations determined from leveling surveys are orthometric heights, which are influenced by the gravity field. Height of the geoid is the difference between these two elevations, here defined as geometric minus orthometric elevation.

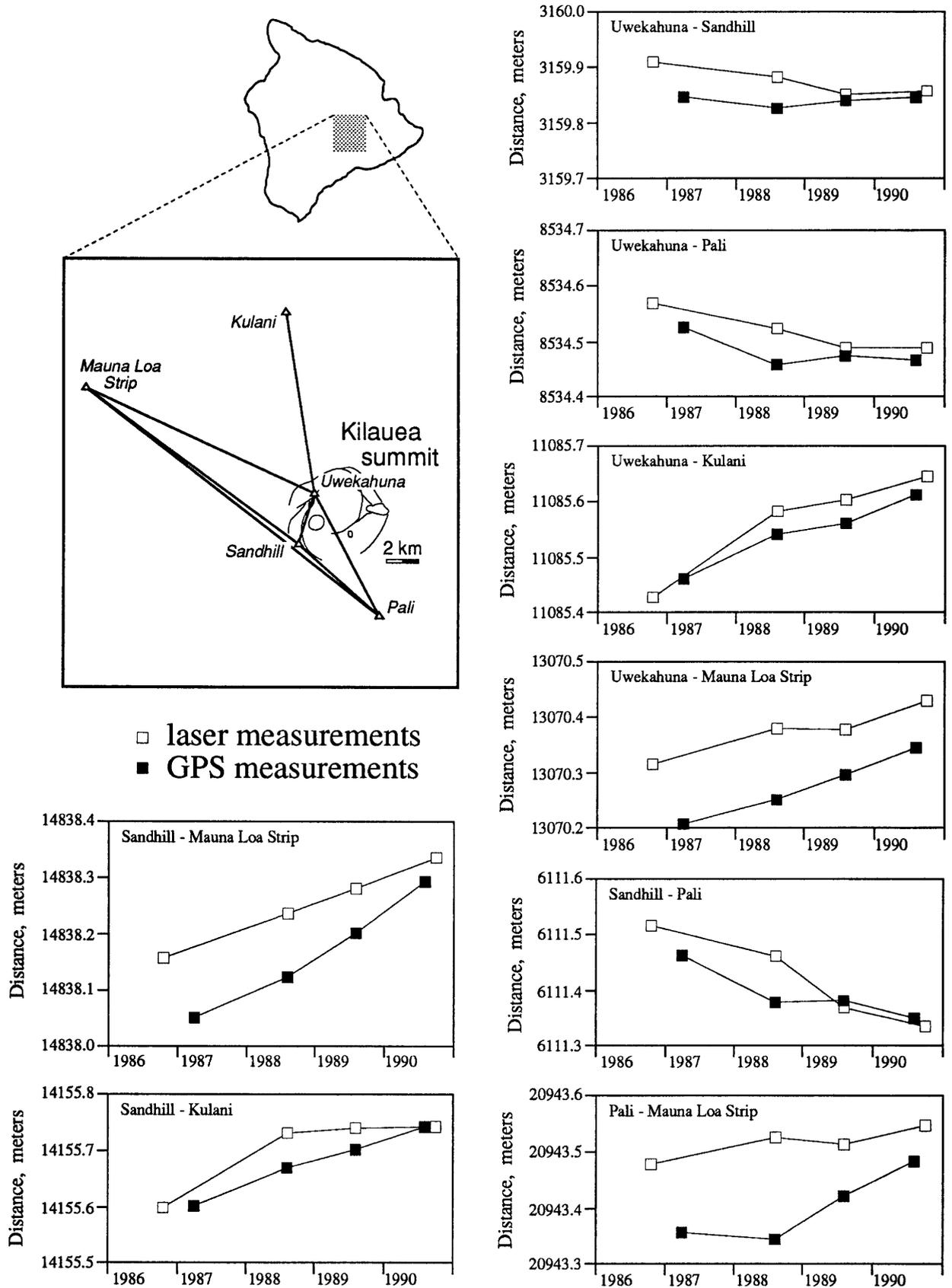


Figure 10. Comparison of baseline distances determined by laser and GPS measurements. Location of each baseline is shown in the upper lefthand corner.

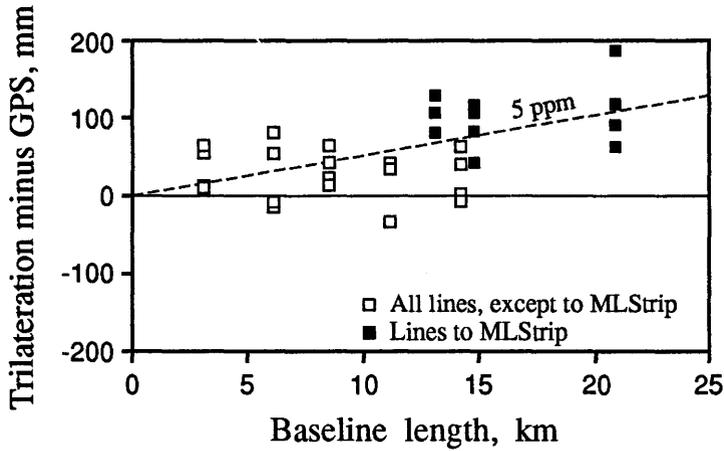


Figure 11. Difference between laser and GPS measurements, plotted as a function of baseline length. A difference of 5 parts per million is shown as a dashed line.

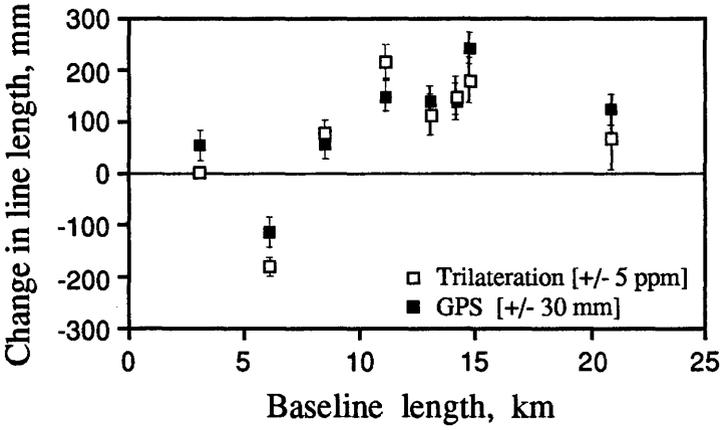


Figure 12. Measured changes in line lengths, determined from laser and GPS measurements, between April 1987 and August 1990.

zontal gradient between Hilo and Mauna Kea of 0.24 m/km. This is similar to the maximum geoid heights determined elsewhere along the Hawaiian island chain, for example across Molokai where the geoid height rises 12 m over a distance of about 100 km (Watts, 1979).

We have determined geoid heights elsewhere on the island of Hawaii using geometric elevations from GPS measurements and orthometric elevations determined either from an extensive leveling survey conducted across Kilauea in February 1989 or orthometric elevations of several GPS benchmarks taken from USGS topographic maps. Relative to LYMAN2, geoid heights are about 11 m in the summit areas of Mauna Kea and Mauna Loa and 5 m in the summit area of Kilauea (fig. 14). LYMAN2, KAPUKAPU, and MILOLII are at nearly the same geoid height.

As suggested by Watts (1979), our map of geoid heights across Hawaii probably reflects two major components: (1) the broad high shape of the island above the sea floor and (2) subsidence of the rigid lithosphere into a viscous asthenosphere caused by the weight of the volcanoes.

SLOW SUBSIDENCE OF THE SUMMIT AREA OF KILAUEA VOLCANO

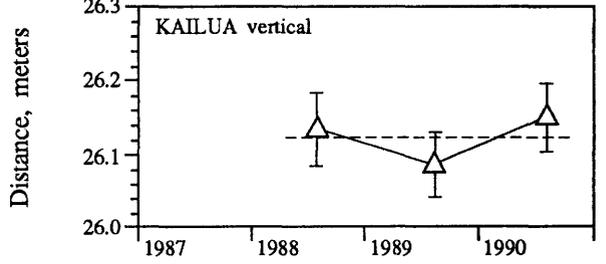
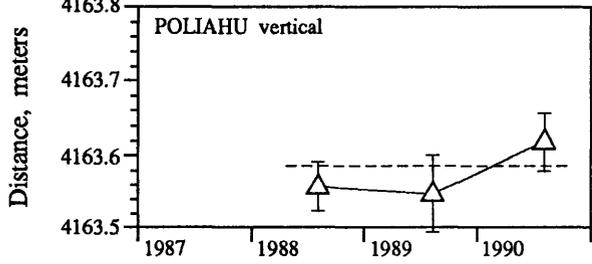
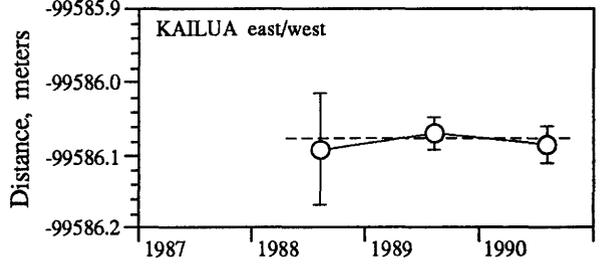
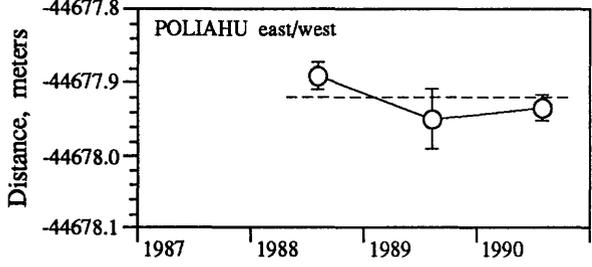
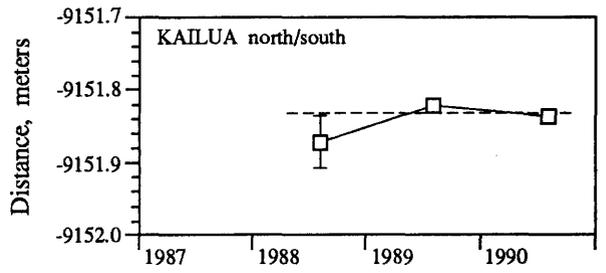
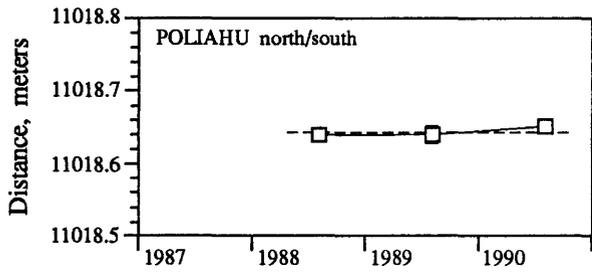
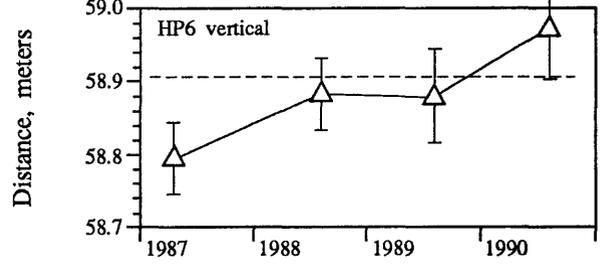
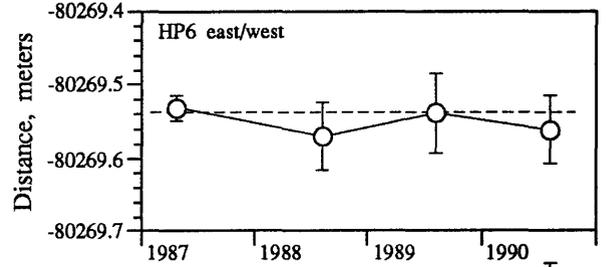
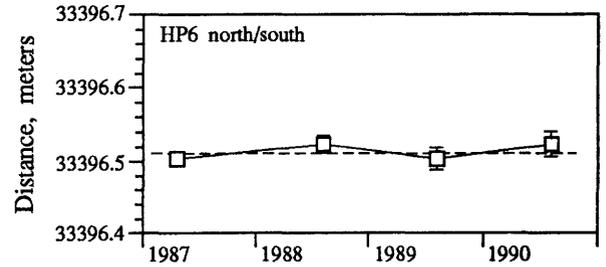
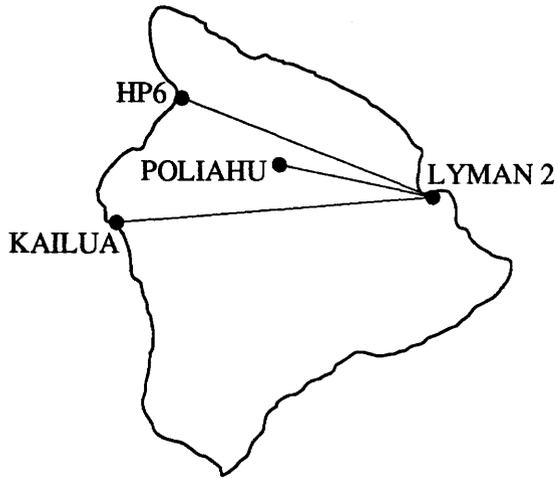
Leveling surveys have shown a slow subsidence of the summit area of Kilauea since the beginning of an eruption along the east rift zone in January 1983. HVO27, a leveling benchmark located near the UWEKHUNA GPS benchmark, 3 km north of the center of subsidence, has subsided at an annual rate of 20 mm/yr since February 1983 (fig. 15). HVO32, located within 2 km of the center of subsidence, has subsided four times faster. Our GPS measurements also recorded the subsidence, as well as contraction of the summit area.

The three-dimensional displacement of UWEKAHUNA and SANDHILL, relative to LYMAN2, are shown in figure 16. Between April 1987 and August 1990, UWEKAHUNA moved south-southeast at a rate of 50 mm/yr, and SANDHILL moved southeast at a faster rate of 80 mm/yr (fig. 16). The subsidence rate of 20 mm/yr near

► **Figure 13.** Measurements of six stable baselines on the island of Hawaii. We suspect these were stable baselines during the period of our surveys because no significant seismic or volcanic activity occurred beneath these lines between 1987 and 1990. A, Baselines between LYMAN2 and HP6, POLIAHU, and KAILUA. B, Baselines between LYMAN2 and KULANI, MAUNA LOA STRIP, and KEAKAPULU FLATS. An error bar is five times the standard error computed using the Bernese software package. Error bars are only shown when they are larger than the symbol. Within the error bars, a horizontal trend, indicated as a dashed line segment, can account for the measured variation of each component, which supports the claim that, within the uncertainty of our measurements, these were stable baselines.

We illustrate geoid height by considering different determinations of the elevation of the summit of Mauna Kea, the highest peak in the Pacific basin. Leveling and triangulation surveys were used to determine the summit of Mauna Kea to be 4,205 meters above sea level (Mauna Kea quadrangle 7.5-minute topographic series, U.S. Geological Survey, 1982). A GPS measurement made on August 25, 1989 was used to compute an elevation difference of 4,207.8 m between LYMAN2 and the benchmark at the true summit of Mauna Kea (stamped SUMMIT 1955). From a 1957 survey, LYMAN2 was 8.2 m above mean high sea level, established at a nearby tide gage in Hilo Bay. If we include a 0.2 m rise of sea level in Hilo Bay since 1957 (Moore, 1987), the present geometric height of the summit of Mauna Kea is 4,215.8 m above mean sea level in Hilo Bay. The difference between geometric and orthometric elevations means the geoid at the summit of Mauna Kea is raised 11 m, which corresponds to a hori-

A



B

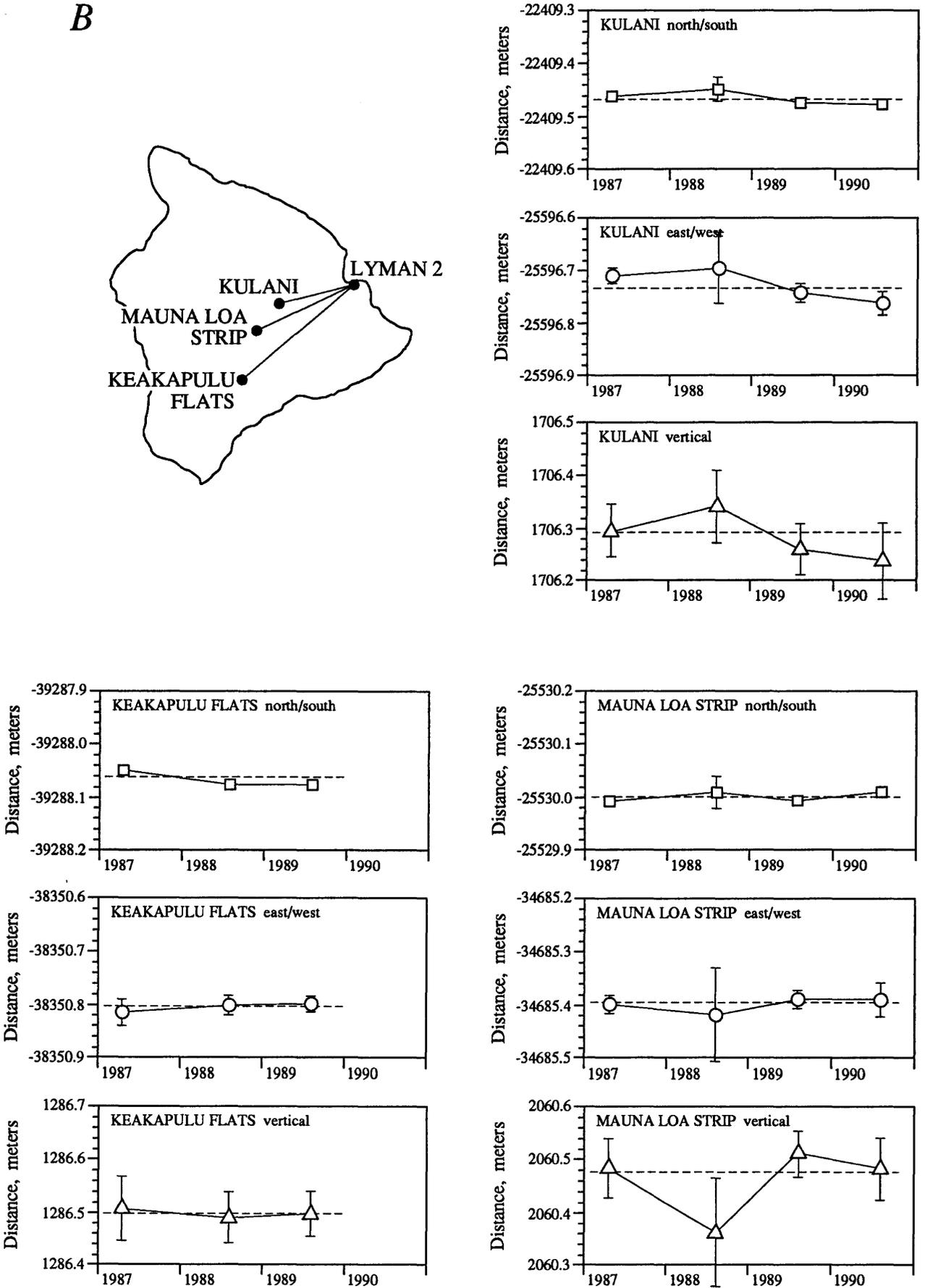


Figure 13.—Continued.

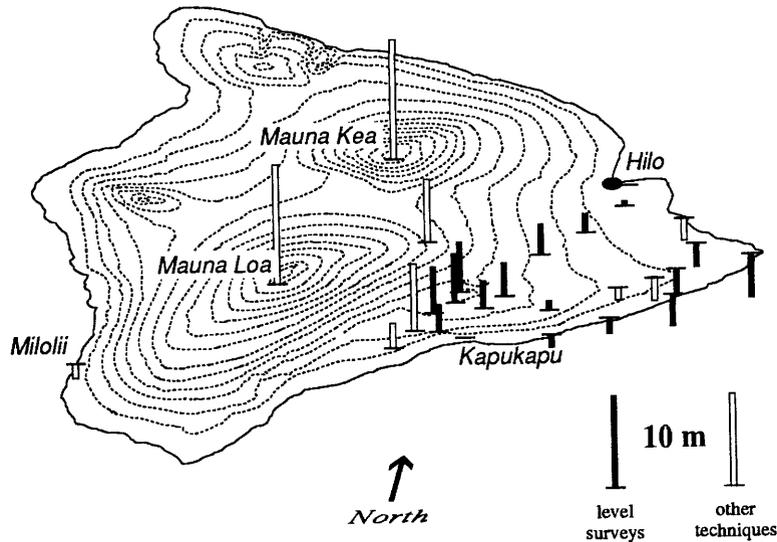


Figure 14. Geoid heights relative to Hilo: difference between geometric and orthometric heights. Geometric heights determined by GPS measurements. Orthometric heights determined either by leveling surveys or elevations of topographic control points on USGS topographic maps.

UWEKAHUNA, indicated by the leveling benchmark HVO27, was not resolved by our GPS; however, our GPS measurements easily resolved the 80 mm/yr subsidence of SANDHILL (fig. 15).

Assuming the subsidence pattern can be modeled as the contraction of a pressure source located 4 km beneath the subsidence center shown in figure 16, which represents a shallow magma reservoir, the subsidence rate at Sandhill corresponds to the removal of 0.01 km³/yr of magma. This rate is 10 percent of the average eruptive rate of 0.1 km³/yr from 1983 to 1986, which is corrected for 20 percent vesiculation of the erupted lava (Heliker and Wright, 1991). If the eruptive rate has continued unchanged through 1990, then only 10 percent of the erupted lava can be accounted for by net removal of magma from the summit reservoir. The other 90 percent must correspond to the rate magma is being supplied to Kilauea from a source deeper than the summit reservoir.

SEAWARD MOVEMENT OF THE SOUTH FLANK OF KILAUEA VOLCANO

Seaward displacement occurs along the most seismically active portion of the south flank, from APUA POINT to KAMOAMOA (fig. 17). Between the 1987 and 1988 surveys and again between the 1989 and 1990 surveys, the coastline from APUA POINT to KAMOAMOA moved seaward at annual rates of 50 to 100 mm/yr. During the same time periods, no significant ground displacement was measured east of KAMOAMOA or along the north flank of Kilauea.

Movement along the south flank was first revealed by triangulation and trilateration surveys conducted since 1914 (Swanson and others, 1976). Seaward displacement is driven by intrusion of pressurized magma into a rift zone, which causes immediate compression of the adjacent section of the south flank. Persistent earthquake zones beneath the south flank reveal the most mobile sections of the south flank, though seaward displacement may also occur, at times, elsewhere on Kilauea, for example southwest of the summit area as indicated by persistent southward displacement at KOAE, KAMAKAIA, and HILINA PALI (fig. 17).

During the four years of GPS measurements, the largest ground displacement were associated with a magnitude 6.1 earthquake on June 26, 1989, beneath the south flank. The epicenter was located a few kilometers north of the KAMOAMOA GPS station, between the axis of the east rift zone and the coastline (fig. 18). The focal mechanism is consistent with seaward displacement of the south flank over older ocean crust (Koyanagi and others, 1989). The pattern of horizontal displacement determined using GPS also indicates seaward displacement of as much as 0.3 m (fig. 18).

The pattern of horizontal displacement can be reproduced by a rectangular fault embedded in a homogeneous, isotropic, elastic half-space with displacement constant across the fault. Analytic expressions for surface displacement were given by Okada (1985). Eight parameters are determined from this model: latitude, longitude, and depth of one corner of the fault; length and width of the fault; dip and strike angle of the fault; and the amount of dip-slip displacement across the fault. The values of these

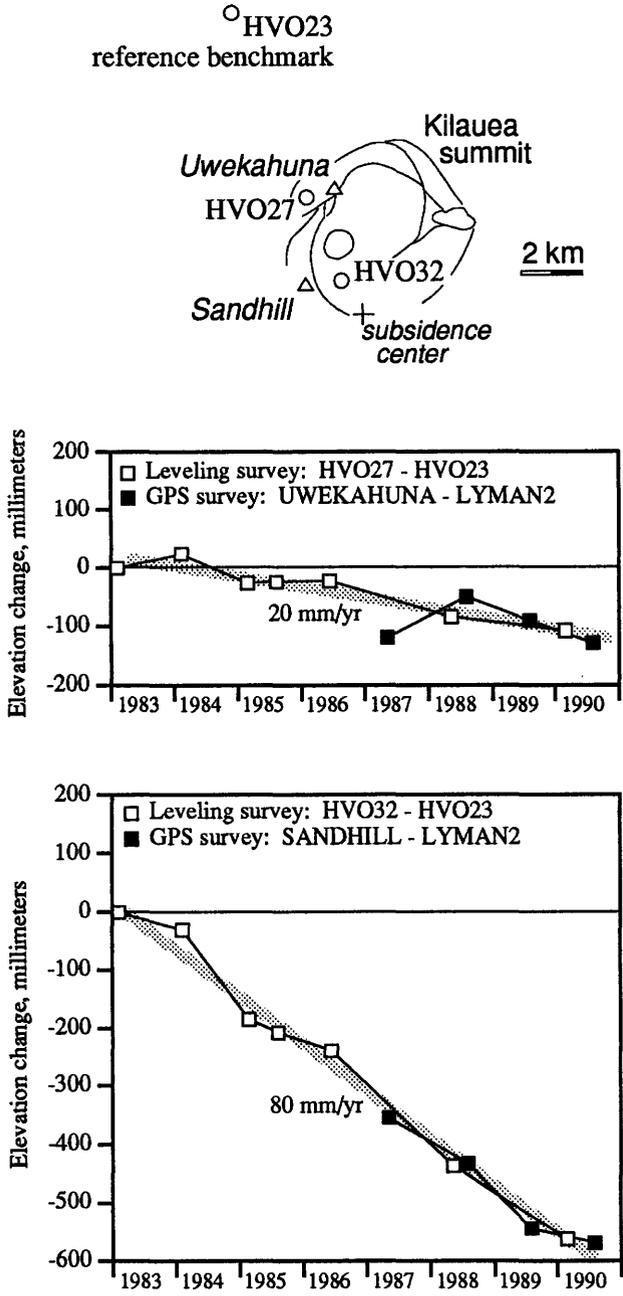
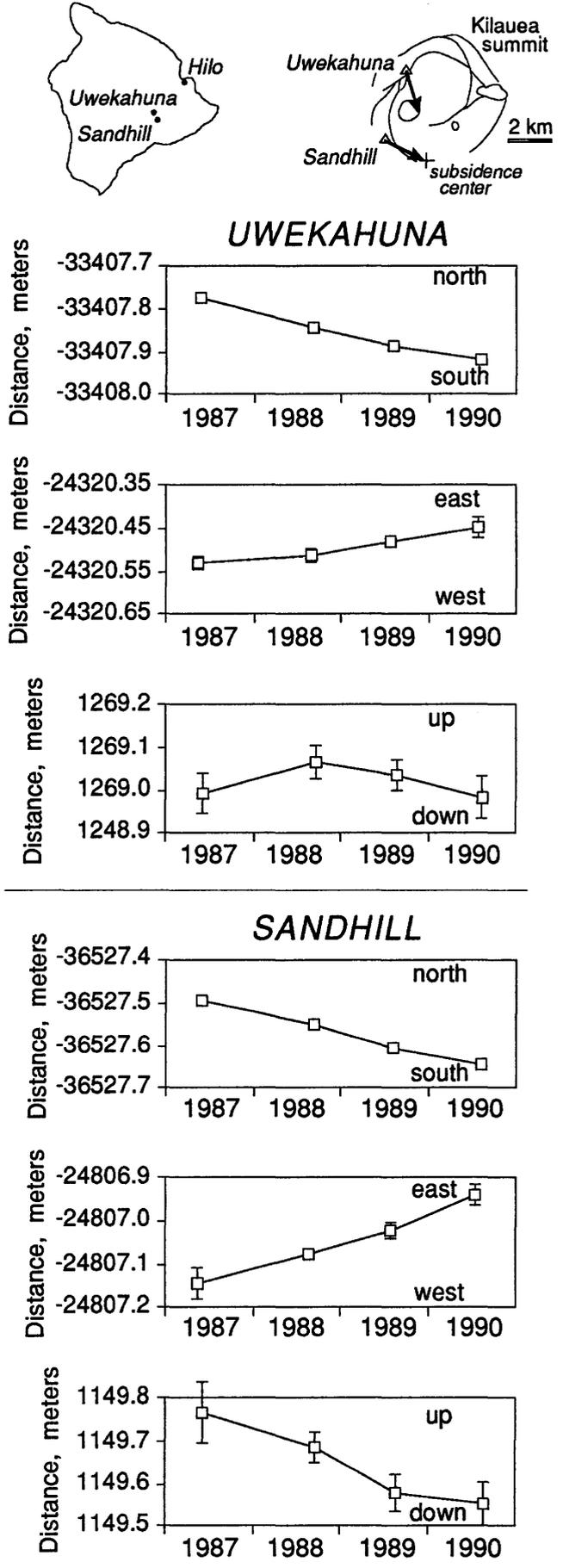


Figure 15. Slow subsidence of summit area of Kilauea, indicated by results of leveling surveys. Locations of leveling benchmarks (circles) and GPS benchmarks (triangles) shown at the top. Upper plot indicates slow subsidence at an average rate of 20 mm/yr of the leveling benchmark HVO27, located near the UWEKAHUNA GPS benchmark. Bottom plot also indicates slow subsidence, relative to HVO23, of the leveling benchmark HVO32 located within 2 km of subsidence center. Changes in vertical positions of the GPS benchmarks UWEKAHUNA and SANDHILL shown as solid squares in the two plots.

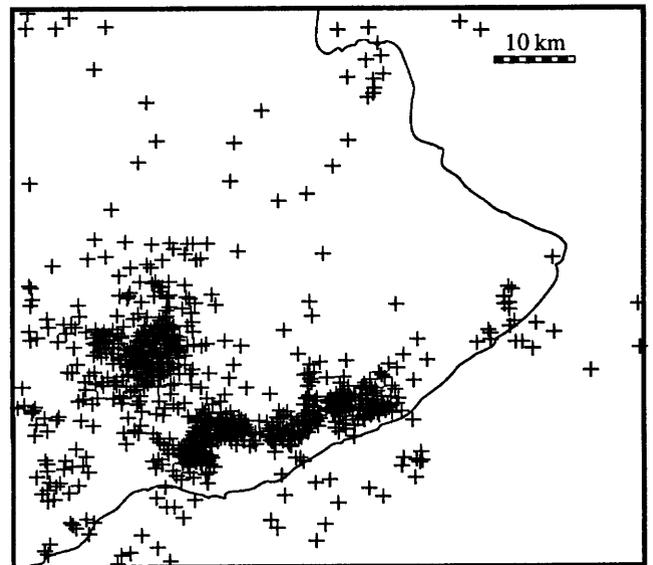
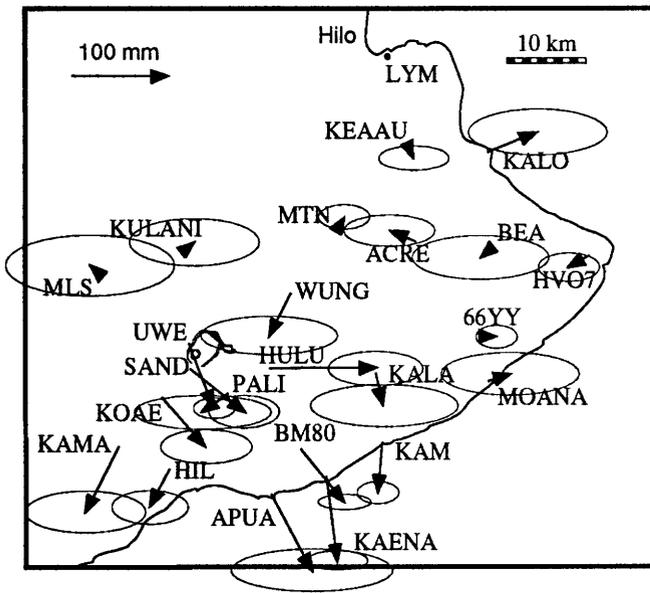
► **Figure 16.** Three-dimensional displacement of two GPS stations in the summit area of Kilauea, UWEKAHUNA and SANDHILL, relative to LYMAN2. Both stations indicate slow subsidence and contraction of summit area, probably the result of slow net withdrawal of magma from summit reservoir.



Horizontal movements - GPS

Earthquake locations

APRIL 1987 TO AUGUST 1988



AUGUST 1989 TO AUGUST 1990

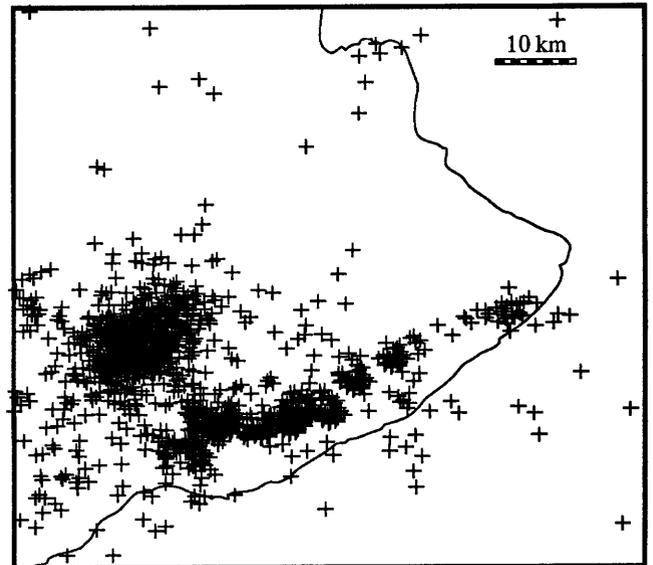
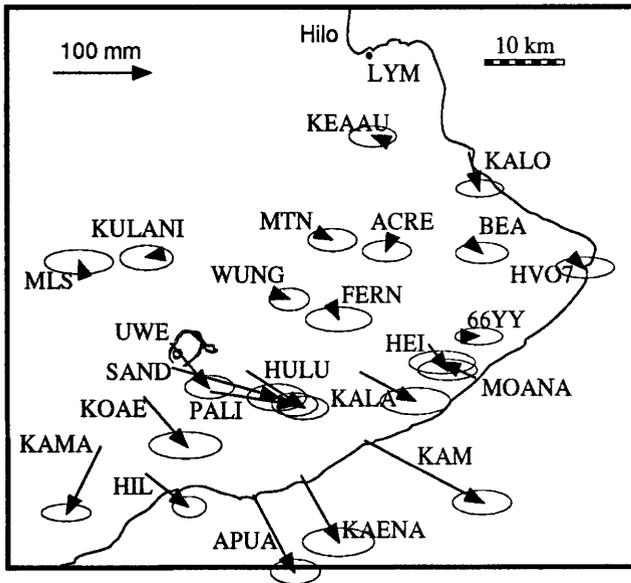


Figure 17. GPS-measured horizontal displacements on Kilauea from April 1987 to August 1988 and from August 1989 to August 1990. Ellipses represent five times standard error computed using Bernese software package. Earthquake locations for same time periods shown at right.

parameters given in table 11 minimize, in the least-squares sense, the difference between measured and modeled horizontal displacement. The measured and modeled horizontal displacements are listed in table 11 and shown in figure 18.

Vertical displacement measured using GPS between August 1988 and August 1989 and computed displacement,

based on the model derived from horizontal displacement, are given in the lower diagram in figure 18. Vertical displacement was also measured along a leveling route that was surveyed in February 1988 and again in February 1990 (fig. 19). Both GPS and leveling surveys show the same pattern of changes and as much as 0.25 m of subsidence, though the results of the leveling surveys are more precise.

SUMMIT AREA OF MAUNA LOA VOLCANO

GPS measurements of Mauna Loa were started in 1988 with one station in the summit area and another on the west

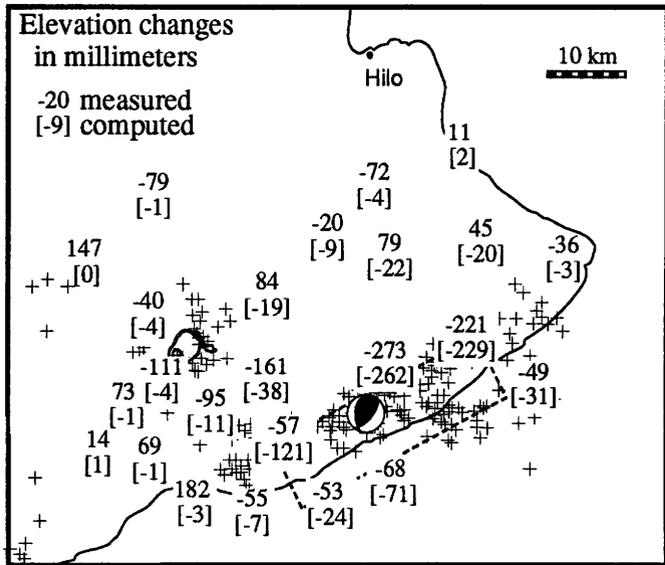
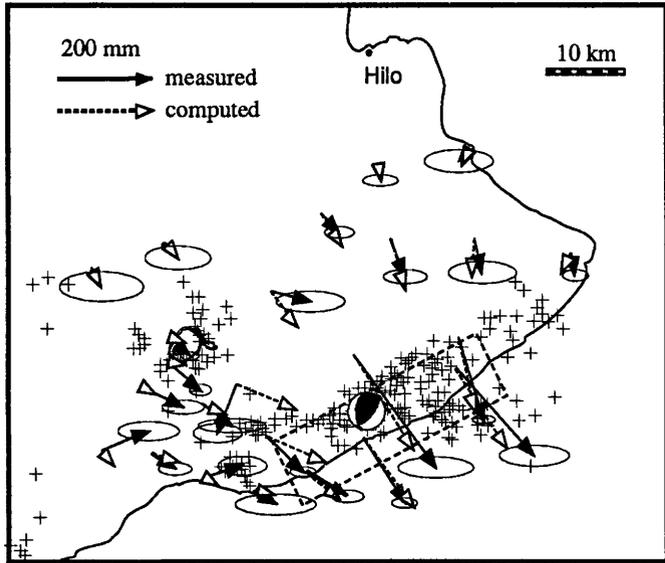


Figure 18. Surface displacements from August 1988 to August 1989 associated with magnitude 6.1 earthquake on June 26, 1989, beneath south flank of Kilauea. All displacements are relative to LYMAN2. Top: Measured horizontal displacements are shown as solid vectors; computed displacements, based on model parameters listed in table 11, shown as dashed vectors. Ellipses represent five times standard error computed using Bernese software package. Surface projection of rectangular sheet model indicated as dashed rectangle. Focal mechanism, located at earthquake epicenter, indicates seaward displacement of the upper portion of south flank. Bottom: Top numbers are measured vertical changes; bottom numbers in brackets are computed vertical changes based on model parameters listed in table 10.

flank at the 2,700-m elevation. In 1989 and 1990 these two stations were remeasured and new stations established on the north and the southeast flanks of the volcano.

Since 1988, the summit station ML1 has moved no more than 20 mm horizontally relative to OOU on the west flank and less than 50 mm vertically (fig. 20). These measured changes are within the accuracy of our surveys, and so no significant ground displacement was measured using GPS. Results of trilateration measurements made across a network that covers the summit area of Mauna Loa indicated ML1 moved less than 20 mm between 1988 and 1990; results of leveling surveys also conducted in the summit area show ML1 was raised 0.17 m since the 1984

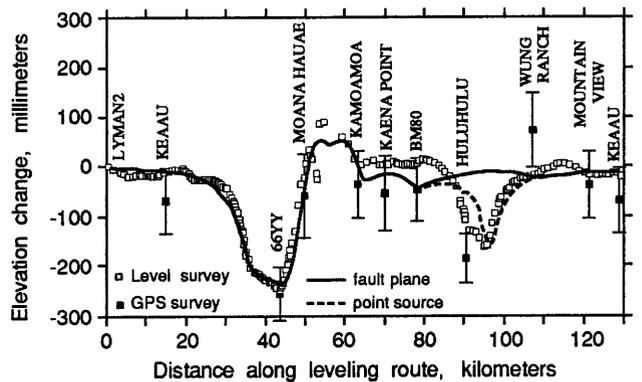
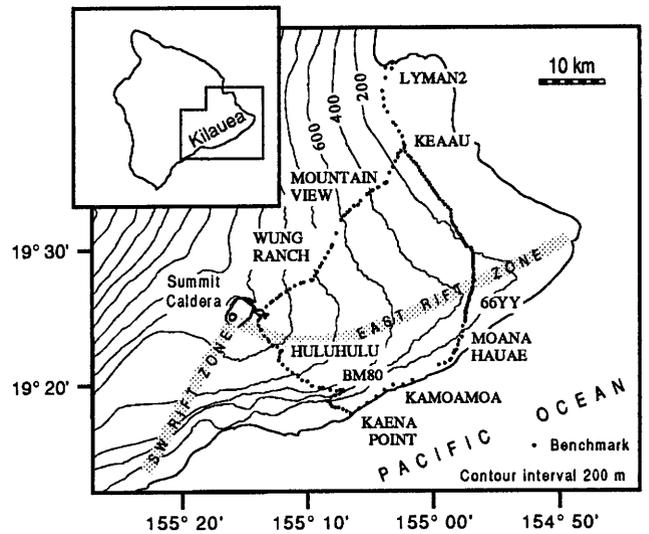


Figure 19. Comparison of measured and computed vertical changes associated with the June 26, 1989, earthquake. Top: Location of leveling route and GPS stations used in bottom diagram. Bottom: Elevation changes as function of distance along leveling route from Hilo. Results of leveling surveys shown as open squares; results of GPS surveys shown as solid squares. (Error bars on GPS measurements are five times standard error computed using Bernese software package.) Solid line is computed vertical changes based on model parameters listed in table 11. In bottom diagram, short, dashed line between HULUHULU and WUNG RANCH includes local subsidence of summit area.

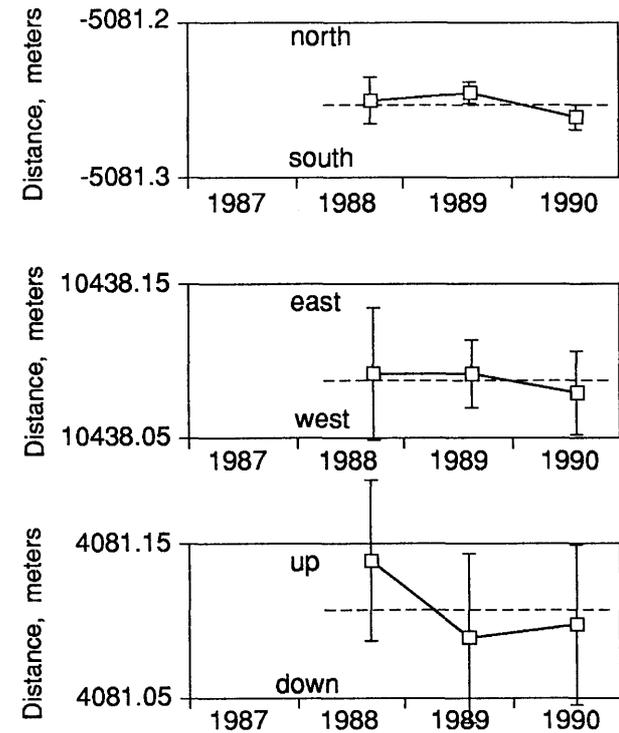
Table 11. Model calculations for the June 1989 earthquake.

Model parameters:	latitude	19.2333	depth to the source	6 km
	longitude	155.1000	length of the source	27 km
	strike angle from north	60°	width of the source	12 km
	dip angle	5°	dip-slip displacement	-1.2 m

	north/south		east/west		up/down	
	measured, mm	model, mm	measured, mm	model, mm	measured, mm	model, mm
LYMAN2*	0	0	0	0	0	0
KEEAU	0	-14	18	3	-72	-4
66YY	-208	-200	28	11	-221	-229
APUA POINT	-40	3	14	27	-55	-7
BM80-1	-85	-28	69	152	-57	-121
HAWAIIAN ACRES	-82	-61	61	15	79	-22
HAWAIIAN BEACHES	-64	-54	21	-17	45	-20
HILINA PALI	-20	7	41	16	69	-1
HULUHULU**	-82	-33	-45	84	-161	-38
HVO7	-42	-11	7	-14	-36	-3
KAENA POINT	-110	-114	122	84	-53	-24
KALALUA	-268	-248	188	152	-273	-262
KALOLI-2	-41	-12	-47	-4	11	-2
KAMAKAIA**	29	7	87	8	14	1
KAMOAMOA	-191	-200	118	127	-68	-71
KAPUKAPU	9	9	150	22	182	-3
KOAE**	-53	4	88	17	73	-1
KULANI	-28	-1	-44	9	-79	-1
MAUNA LOA STRIP	-16	3	32	6	147	0
MOANA HAUAE	-227	-196	176	110	-49	-31
MOUNTAIN VIEW	-24	-26	28	14	-20	-9
PALI	-38	-2	73	43	-95	-11
SANDHILL**	-53	-1	51	23	-111	-4
UWEKAHUNA**	-38	-3	32	21	-40	-4
WUNG RANCH	-7	-39	71	40	84	-19
Root-mean-square differences (measured minus observed)	31		54		77	

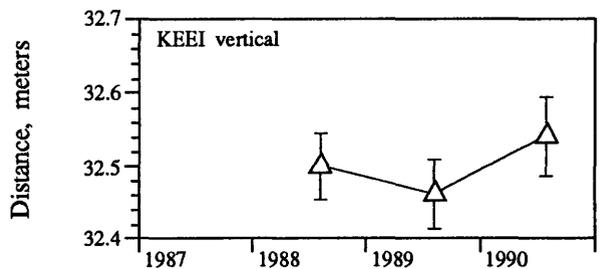
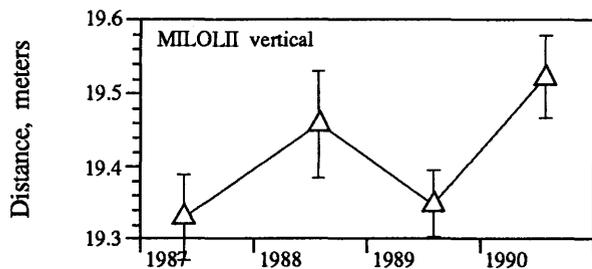
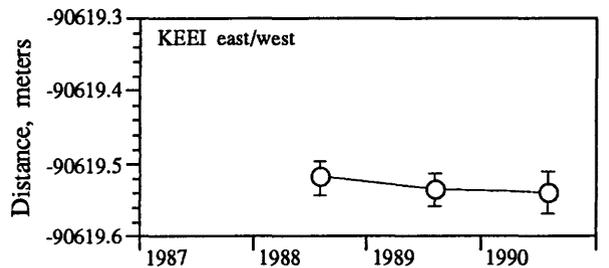
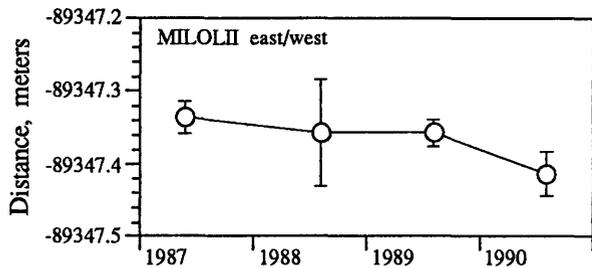
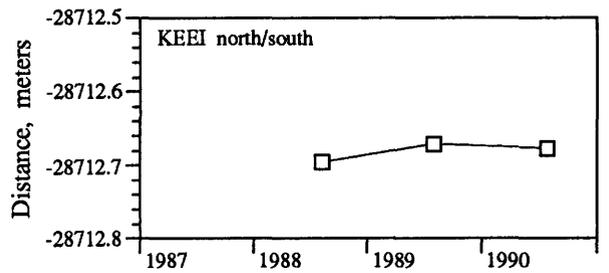
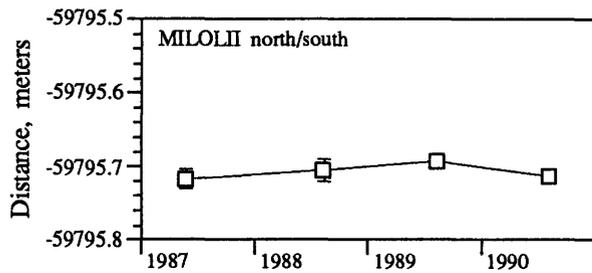
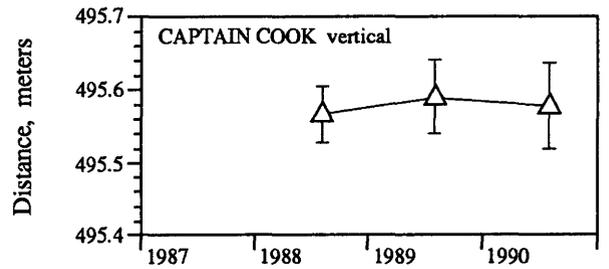
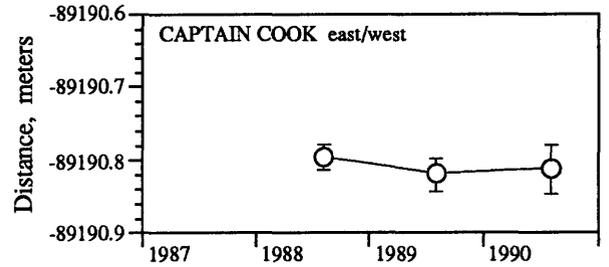
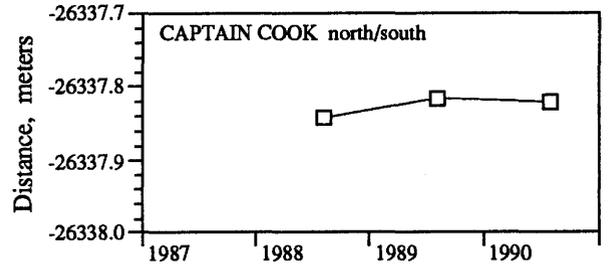
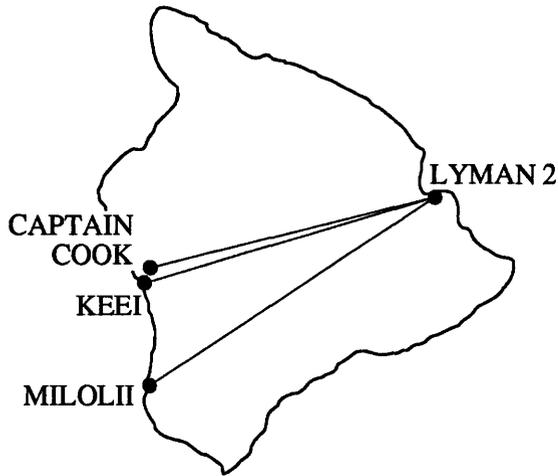
*All displacements, expressed as millimeters, are relative to LYMAN2.

**These stations were not used to compute the root-mean-square values shown at the bottom.



SURVEY RESULTS

Figure 20. Three-dimensional position of ML1 in summit area of Mauna Loa, relative to OUO on west slope of volcano. Dashed horizontal lines indicate no significant changes were measured between ML1 and OUO during period.



eruption of Mauna Loa, though most of the uplift probably occurred before 1986 (Hawaiian Volcano Observatory, unpub. data).

KEALAKEKUA FAULT SYSTEM

Three stations have been measured annually along the southwest coast of Hawaii (fig. 21), along a strip that encompasses the Kealakekua fault system. This fault system on the west flank of Mauna Loa is probably similar in origin and operation to the more active and more pronounced Hilina Pali fault system along the south flank of Kilauea. Both fault systems have arcuate, normal faults that formed during sudden seaward displacement of the flank.

Since 1950, three damaging earthquakes, all believed to be greater than magnitude 6.0, occurred along the west flank of Mauna Loa (Nakata and others, 1990). Continued seismicity at a rate one-quarter to one-half the rate along the south flank of Kilauea suggests ground displacement may be occurring along the southwest coast of Hawaii.

MILOLII may have moved seaward as much as 80 mm between 1987 and 1990. This displacement is consistent with westward slip directions determined by Bryan and Johnson (1991) from focal mechanisms beneath this portion of the island. The vertical positions of MILOLII varied greatly, in part because of the inaccuracy of the 1988 survey and, perhaps, because of an error in measuring the antenna height in 1990. Additional measurements will either confirm, or refute, our apparent detection of seaward displacement along the west coast of Mauna Loa.

GPS AS A TOOL TO STUDY ACTIVE VOLCANOES

Most, if not all, volcanic eruptions are preceded by vertical and horizontal displacement of the Earth's surface, often occurring near the eventual eruptive site. Kilauea volcano in Hawaii is only one of many such examples. Presumably, the displacement is a response of the crust to accumulation of magma or buildup of pressure within a magma reservoir. Measurements made at many different volcanoes show that the displacement may precede an eruption by as much as several years. Often, a rapid increase in rate of displacement occurs a few hours to a few days before the start of eruptive activity. Among the challenges of understanding active volcanoes and predicting their eruptions are those associated with measuring the displacement of the Earth's surface when the amount of displacement is small.

GPS is a new scientific tool that meets this challenge. The ability to record three-dimensional surface displacement at the centimeter level over distances of tens to hundreds of kilometers makes GPS ideal in the study of active volcanoes. Furthermore, GPS stations can be located in remote and rugged terrain and do not require that stations be intervisible. Weather conditions under which GPS measurements can be made are less restrictive than conventional land-surveying techniques.

Besides Hawaiian volcanoes, GPS surveys have also been conducted at Izu Peninsula, Japan (Shimada and others, 1990); Yellowstone caldera, Wyoming (Meertens and others, 1990); Hekla, Iceland (Sigmundsson and others, 1991); Mono Craters, California (Marshall and Stein, 1991) and Taupo Volcanic Zone, New Zealand (Meertens and others, 1991). The number of active volcanoes surveyed by GPS will continue to grow as ground receivers become less expensive and data processing becomes more automatic.

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◀ **Figure 21.** GPS positions of three stations located along southwest coast of Hawaii, along the Kealakekua fault system.

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