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### Two-step adaptive management for choosing between two management actions

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1 *Running head:* Two-step adaptive management

2 **Two-step Adaptive Management for choosing between two management**  
3 **actions**

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19

20 ABSTRACT

21 Adaptive management is widely advocated to improve environmental management. Derivations  
22 of optimal strategies for adaptive management, however, tend to be case specific and time  
23 consuming. In contrast, managers might seek relatively simple guidance, such as insight into  
24 when a new potential management action should be considered, and how much effort should be  
25 expended on trialing such an action.

26 We constructed a two time-step scenario where a manager is choosing between two possible  
27 management actions. The manager has a total budget which can be split between a learning phase  
28 and an implementation phase. We use this scenario to investigate when and how much a manager  
29 should invest in learning about the management actions available. The optimal investment in  
30 learning can be understood intuitively by accounting for the expected value of sample  
31 information, the benefits that accrue during learning, the direct costs of learning, and the  
32 opportunity costs of learning.

33 We find that the optimal proportion of the budget to spend on learning is characterized by several  
34 critical thresholds that mark a jump from spending a large proportion of the budget on learning to  
35 spending nothing. For example, as sampling variance increases it is optimal to spend a larger  
36 proportion of the budget on learning, up to a point - if the sampling variance passes a critical  
37 threshold, it is no longer beneficial to invest in learning. Similar thresholds are observed as a  
38 function of the total budget and the difference in the expected performance of the two actions.

39 We illustrate how this model can be applied using a case study of choosing between alternative  
40 rearing diets for hihi, an endangered New Zealand passerine.

41 Although the model presented is a simplified scenario, we believe it is relevant to many  
42 management situations. Managers often have relatively short time horizons for management, and  
43 might be reluctant to consider further investment in learning and monitoring beyond collecting  
44 data from a single time period.

45 **KEYWORDS:** adaptive management, decision analysis, monitoring costs, expected value of perfect  
46 and sample information, Bayesian experimental design.

47 INTRODUCTION

48 Adaptive management is widely advocated to improve environmental management, and to help  
49 determine appropriate levels of monitoring effort to support better management decisions  
50 (Walters and Hilborn 1978, Walters and Holling 1990, Johnson and Williams 2015). Adaptive  
51 management aims to strike a balance between learning about the system being managed, and  
52 actually managing it (Holling 1978, Walters 1986), a balance referred to as the “dual-control  
53 problem” in the literature on operations research (Wittenmark 1995). Learning about a system  
54 entails both monitoring costs and lost opportunity costs, since experiments in which two or more  
55 actions are trialed concurrently inevitably means that a sub-optimal action will be at least partly  
56 implemented. Thus, learning about the system will draw on resources that might be used for  
57 management. However, the information gained from monitoring and experimentation might  
58 improve management in the future. Adaptive management aims to balance the longer-term  
59 benefits of learning with its shorter-term costs, helping to determine the appropriate investment in  
60 learning.

61 The academic literature on adaptive management has proliferated, yet examples of successful  
62 implementation are rare (Johnson and Williams 2015). Various reasons restrict the use of  
63 adaptive management including lack of institutional support and commitment, and insufficient  
64 funding for adequate monitoring programs (Walters 2007, Johnson and Williams 2015). The  
65 computational burden required to optimize adaptive management is another potential concern  
66 (Martell and Walters 2008). Further, the academic literature tends to emphasize solutions to  
67 specific adaptive management problems (e.g. Gregory et al. 2006, Tyre et al. 2011, Shea et al.  
68 2014), and drawing general conclusions appears difficult. In contrast, managers might seek  
69 relatively simple guidance, such as insight into when a new potential management action should

70 be considered, and how much effort should be expended on trialing such actions (Walters and  
71 Green 1997, McDonald-Madden et al. 2010).

72 To help generalize adaptive management beyond individual case studies, we constructed an  
73 adaptive management problem where a manager is choosing between two possible management  
74 actions in two decision phases – a learning phase and a final decision phase. The manager has a  
75 total budget to spend over these two phases. In the first time period, both actions can be  
76 implemented and the results monitored. At the end of this learning phase, the remaining budget  
77 will be spent on implementing the action with the highest expected efficiency. The management  
78 goal is to maximize the total expected benefit over the two phases. We use this framework to  
79 investigate the following questions. First, when should we invest in learning more about the value  
80 of the management actions? Second, if investing in a learning phase is expected to be beneficial,  
81 how much of the total budget should we invest? Third, how should the amount spent on the  
82 learning phase be split between the two available actions given their current expected  
83 performance and our uncertainty about these values? Finally, when do we expect the largest  
84 benefits from investing in learning?

85 While this is a simplified scenario, we believe it is relevant to many management situations (e.g.  
86 see the frameworks proposed by Walters and Green 1997, MacGregor et al. 2002). The two  
87 phases will at best approximate sequential decisions over many time-steps, however, managers  
88 often have relatively short time horizons for management, and might be reluctant to consider  
89 further investment in experimentation and monitoring beyond collecting data from a single time  
90 period. As we show in this paper, one advantage of this simplified scenario is that analytical  
91 expressions for the optimal level of experimentation (i.e. optimal number of samples of each

92 management action during the first phase) can be obtained for particular special cases, and  
93 numerical solutions can be obtained efficiently in other cases.

94 There exists a substantial literature addressing the optimal sample size when choosing between  
95 two, or more, treatments in clinical trials, when the objective is to maximize the total number of  
96 successful treatments (Hardwick and Stout 2002, Ghosh et al. 2011). However, we found that  
97 these studies consider scenarios that differ from that considered here in one or more of the  
98 following four respects: (i) the cost of performing experiments is ignored (e.g. Colton 1963), (ii)  
99 the number of trials is assumed to be the same for the two treatments (e.g. Canner 1970, Willan  
100 and Kowgier 2008), (iii) they consider dichotomous responses (success or failure) from the trials  
101 (e.g. Cheng 1996, Hardwick and Stout 2002, Cheng et al. 2003), or (iv) they consider testing a  
102 new action against a known one (e.g. Grundy et al. 1954). As far as we are aware, the scenario  
103 considered in this study (including sample costs, unequal allocation of trials during the  
104 experimental phase, a measure of benefit size obtained from each trial, and two uncertain actions)  
105 has not been addressed in this literature nor in the literature on natural resource management.

106 Another approach to evaluating the expected value of experimentation is value of information  
107 (VOI) analysis (Raiffa and Schlaiffer 1961). VOI is a broad term for an analysis that estimates  
108 the expected potential value of gaining new information about a system. VOI has been used in  
109 various disciplines to determine the maximum amount that should be invested in gaining  
110 information before making a decision (Maxwell et al. 2015). In particular, VOI has been applied  
111 to environmental management dilemmas to determine the potential management benefit of  
112 resolving uncertainty both for one off (Runge et al. 2011, Maxwell et al. 2015) and dynamic  
113 decision processes (Williams et al. 2011, Williams and Johnson 2015), and to determine whether  
114 or not monitoring should be performed (Hauser et al. 2006, McDonald-Madden et al. 2010).

115 VOI analyses may consider the value of resolving all uncertainty about a system (Expected Value  
116 of Perfect Information, EVPI), the value of resolving some sources of uncertainty (expected value  
117 of partial information), or the value of resolving some of the uncertainty via additional sampling  
118 (expected value of sample information, EVSI) (Runge et al. 2011). Such analyses provide an  
119 upper bound on how much should be invested in gathering information before taking a  
120 management decision, and can identify when the benefits of learning are expected to be the  
121 greatest. However, such analysis does not tell us the optimal amount to invest in learning when  
122 accounting for monitoring and lost opportunity costs.

123 At least two decision phases must be considered to capture the trade-off between the expected  
124 benefits and costs of experimentation. We relate the solution of our two time-step process to the  
125 EVSI, and highlight the trade-off between the value of sample information and lost opportunity  
126 costs. By nesting the experimental design question within a decision question, we take the same  
127 approach as in Bayesian experimental design (Chaloner and Verdinelli 1995); indeed, EVSI is  
128 very closely related to a Bayesian preposterior analysis, and provides similarly relevant  
129 information to a decision maker.

130

## 131 METHODS

132 We consider the case when a manager has two actions to choose from,  $i = \{1, 2\}$ . The manager  
133 has a total budget  $B$  to spend on implementing the actions. For each action, one unit of  
134 management costs  $c_i$  and results in a benefit  $x_i$ . We assume that the benefit of each action is  
135 uncertain such that  $x_i$  is an unknown random variable, with the uncertainty represented by a  
136 normal distribution with mean  $m_i$  and standard deviation  $s_i$ .



137 Before presenting the two-step adaptive management model, we first consider the expected value  
 138 of sample information. This gives us the expected benefit of information acquired from a  
 139 particular experimental design. EVSI essentially ignores costs associated with obtaining the  
 140 experimental results; whether or not experimentation occurs, the same amount will be invested in  
 141 implementing the expected best action. We then consider a two-step adaptive management (AM)  
 142 scenario, made up of an experimental phase and an implementation phase. We use this  
 143 framework to investigate the trade-off between investing in experimentation and saving resources  
 144 to implement the best action. We highlight the relationship between the AM solution and EVSI.

145 *Expected Value of Sample Information*

146 In the case that the manager must choose between the two actions in the absence of any further  
 147 information, or reduction in uncertainty, the optimal decision is to invest the entire budget in the  
 148 action  $i$  that maximizes the expected net benefit, with the expectation taken over the prior  
 149 distribution. The expected net benefit in the face of uncertainty is

150 
$$E_u = \max_i E \left[ B \frac{x_i}{c_i} \right] = B \max \left( \frac{m_1}{c_1}, \frac{m_2}{c_2} \right) = B \left\{ \frac{m_1}{2c_1} + \frac{m_2}{2c_2} + \frac{1}{2} \left| \frac{m_1}{c_1} - \frac{m_2}{c_2} \right| \right\}. \quad (1)$$

151 The expected value of sample information (EVSI) is the difference between the expected value  
 152 after a given sampling regime is implemented (reduction but not elimination of uncertainty) and  
 153 the expected value in the face of uncertainty. Hence, to calculate EVSI, we need to calculate the  
 154 pre-posterior distribution, that is, the expected net benefit from having additional information,  
 155 taken with respect to the prior distribution.

156 Suppose that our sampling design is to observe  $n_1$  units of action 1 and  $n_2$  units of action 2. We  
 157 then observe a mean response  $p_i$  for the units under action  $i$ , and these have an individual  
 158 variation of  $\sigma_i^2$ . We assume the  $p_i$  are independently distributed according to

$$159 \quad p_i | x_i \sim N \left( x_i, \sqrt{\sigma_i^2 / n_i} \right) \quad (2)$$

160 and the unconditional distribution, given the prior for  $x_i$ , is

$$161 \quad p_i \sim N \left( m_i, \sqrt{\sigma_i^2 / n_i + s_i^2} \right). \quad (3)$$

162 Combining the prior and the observed data, using Bayes' Theorem, the posterior distribution for  
 163 the per-unit benefit,  $y_i$ , is normal with mean

$$164 \quad m_i' = \frac{p_i n_i s_i^2 + m_i \sigma_i^2}{n_i s_i^2 + \sigma_i^2} \quad (4)$$

165 and variance

$$166 \quad \sigma_i'^2 = \frac{\sigma_i^2 s_i^2}{n_i s_i^2 + \sigma_i^2}. \quad (5)$$

167 After observing the new information, we would choose the action with the highest expected  
 168 efficiency, with the expectation taken over the posterior distribution,

$$169 \quad \max \left( E_{posterior} \left[ \frac{y_1}{c_1}, \frac{y_2}{c_2} \right] \right) = \max \left( \frac{p_1 n_1 s_1^2 + m_1 \sigma_1^2}{c_1 (n_1 s_1^2 + \sigma_1^2)}, \frac{p_2 n_2 s_2^2 + m_2 \sigma_2^2}{c_2 (n_2 s_2^2 + \sigma_2^2)} \right)$$

$$170 \quad = \frac{1}{2} \left( \frac{p_1 n_1 s_1^2 + m_1 \sigma_1^2}{c_1 (n_1 s_1^2 + \sigma_1^2)} + \frac{p_2 n_2 s_2^2 + m_2 \sigma_2^2}{c_2 (n_2 s_2^2 + \sigma_2^2)} + \left| \frac{p_1 n_1 s_1^2 + m_1 \sigma_1^2}{c_1 (n_1 s_1^2 + \sigma_1^2)} - \frac{p_2 n_2 s_2^2 + m_2 \sigma_2^2}{c_2 (n_2 s_2^2 + \sigma_2^2)} \right| \right). \quad (6)$$

171 Because we wish to estimate this value prior to making the observation of  $\{p_1, p_2\}$ , we now need  
 172 to take the expectation of this quantity with respect to the prior distribution. The only random  
 173 variables are  $p_1$  and  $p_2$ . Thus, the pre-posterior expectation for the maximum efficiency is

$$174 \quad E_e = \frac{1}{2} \left( \frac{E[p_1]n_1s_1^2 + m_1\sigma_1^2}{c_1(n_1s_1^2 + \sigma_1^2)} + \frac{E[p_2]n_2s_2^2 + m_2\sigma_2^2}{c_2(n_2s_2^2 + \sigma_2^2)} + E[|\Delta|] \right) = \frac{1}{2} \left( \frac{m_1}{c_1} + \frac{m_2}{c_2} + E[|\Delta|] \right) \quad (7)$$

175 where

$$176 \quad \Delta = \frac{p_1n_1s_1^2 + m_1\sigma_1^2}{c_1(n_1s_1^2 + \sigma_1^2)} - \frac{p_2n_2s_2^2 + m_2\sigma_2^2}{c_2(n_2s_2^2 + \sigma_2^2)} \quad (8)$$

177 is normally distributed with mean

$$178 \quad \mu = \frac{m_1}{c_1} - \frac{m_2}{c_2} \quad (9)$$

179 and variance

$$180 \quad \Theta^2 = \left( \frac{s_1}{c_1} \right)^2 \frac{n_1s_1^2}{n_1s_1^2 + \sigma_1^2} + \left( \frac{s_2}{c_2} \right)^2 \frac{n_2s_2^2}{n_2s_2^2 + \sigma_2^2}. \quad (10)$$

181 Because  $\Delta$  is normally distributed, the modulus (absolute value) of  $\Delta$  has a folded-normal  
 182 distribution. Thus,

$$183 \quad E_e = \frac{1}{2} \left( \frac{m_1}{c_1} + \frac{m_2}{c_2} + \Theta \sqrt{\frac{2}{\pi}} e^{-\mu^2/2\Theta^2} + \mu \operatorname{erf} \left( \frac{\mu}{\Theta\sqrt{2}} \right) \right). \quad (11)$$

184 In the case that sampling is obtained for free and the entire budget  $B$  is spent on implementing the  
 185 action with the highest expected posterior efficiency, the total expected benefit with sampling is

$$186 \quad E_s = B * E_e,$$

187 
$$= \frac{B}{2} \left( \frac{m_1}{c_1} + \frac{m_2}{c_2} + \Theta \sqrt{\frac{2}{\pi}} e^{-\mu^2/2\Theta^2} + \mu \operatorname{erf} \left( \frac{\mu}{\Theta\sqrt{2}} \right) \right). \quad (12)$$

188 The expected value of sample information (EVSI) is the difference between the expected benefit  
 189 with sampling and the expected benefit in the face of uncertainty:

190 
$$EVSI = E_S - E_u,$$

191 
$$= \frac{B}{2} \left\{ \frac{m_1}{c_1} + \frac{m_2}{c_2} + \Theta \sqrt{\frac{2}{\pi}} e^{-\mu^2/2\Theta^2} + \mu \operatorname{erf} \left( \frac{\mu}{\Theta\sqrt{2}} \right) \right\} - \frac{B}{2} \left\{ \frac{m_1}{c_1} + \frac{m_2}{c_2} + \left| \frac{m_1}{c_1} - \frac{m_2}{c_2} \right| \right\},$$

192 
$$= \frac{B}{2} \left\{ \Theta \sqrt{\frac{2}{\pi}} e^{-\mu^2/2\Theta^2} + \mu \operatorname{erf} \left( \frac{\mu}{\Theta\sqrt{2}} \right) - |\mu| \right\}, \quad (13)$$

193 where  $\mu = \frac{m_1}{c_1} - \frac{m_2}{c_2}$ , and  $\Theta^2 = \left( \frac{s_1}{c_1} \right)^2 \frac{n_1 s_1^2}{n_1 s_1^2 + \sigma_1^2} + \left( \frac{s_2}{c_2} \right)^2 \frac{n_2 s_2^2}{n_2 s_2^2 + \sigma_2^2}$  (Eqs. 9 and 10). The derivation of  
 194 the expected value of perfect information (EVPI) and a comparison with EVSI can be found in  
 195 Appendix S1.

196 *Two-step Adaptive Management*

197 To calculate the EVSI we assumed that we knew the sampling design; the number of units  $n_i$  of  
 198 each action to be trialed. The EVSI tells us the maximum *additional* amount we could spend on a  
 199 particular sampling design to achieve the same expected net benefit. However, in the case that we  
 200 have a total budget  $B$  to spend on both experimentation and implementation, EVSI does not tell  
 201 us how much of that budget to invest in monitored trials. The more we invest in experimentation,  
 202 the more likely we are to finally choose the best management action, but experimentation incurs  
 203 additional monitoring costs (resulting in less money to spend on implementation) and lost  
 204 opportunity costs of trialing the worst action.

205 To analyze this trade-off we consider a two-step adaptive management process, made up of an  
 206 experimental phase, consisting of monitored trials, and an implementation phase, in which the  
 207 remaining funds are used to implement the action with the largest posterior efficiency. During the  
 208 experimental phase, the additional cost of monitoring the outcome of each trial is  $k_i$  for each unit  
 209 of management. We assume that the data will have a standard deviation of  $\sigma_i$ , representing the  
 210 observed variation in benefit among different units of management.

211 The total expected net benefit over the two time-steps is the expected benefit from the  
 212 experimental phase plus the expected benefit of spending the remaining funds on the action that  
 213 is found to have the highest expected efficiency (equation 11),

$$\begin{aligned}
 214 \quad L &= n_1 m_1 + n_2 m_2 + (B - n_1(c_1 + k_1) - n_2(c_2 + k_2))E_e, \\
 215 \quad &= n_1 m_1 + n_2 m_2 + (B - n_1(c_1 + k_1) - n_2(c_2 + k_2)) \frac{1}{2} \left\{ \frac{m_1}{c_1} + \frac{m_2}{c_2} + \Theta \sqrt{\frac{2}{\pi}} e^{-\mu^2/2\Theta^2} + \mu \operatorname{erf}\left(\frac{\mu}{\Theta\sqrt{2}}\right) \right\}, \\
 216 & \tag{14}
 \end{aligned}$$

217 Let the total cost of the experimental phase be given by  $C_{\text{experiment}} = (c_1+k_1)n_1 + (c_2+k_2)n_2$ .

218 Equation (14) can be re-written as

$$\begin{aligned}
 219 \quad L &= n_1 m_1 + n_2 m_2 + \left(1 - \frac{C_{\text{experiment}}}{B}\right) E_s \\
 220 \quad &= n_1 m_1 + n_2 m_2 + E_s - \frac{C_{\text{experiment}}}{B} E_s \\
 221 \quad &= n_1 m_1 + n_2 m_2 + E_u + EVSI - \frac{C_{\text{experiment}}}{B} E_s \\
 222 \quad &= E_u + EVSI + n_1 m_1 + n_2 m_2 - \frac{C_{\text{experiment}}}{B} E_s. \tag{15}
 \end{aligned}$$

223 Written in this way we can more easily see the trade-off between investing in experimentation  
224 and saving resources for implementing the best action; the more we spend on the experimental  
225 phase, the larger the expected value of sample information (EVSI) and the larger the incidental  
226 benefits of experimentation ( $n_1m_1+n_2m_2$ ). However, the lost opportunity costs incurred by using  
227 up resources during sampling,  $(C_{\text{experiment}}/B)E_s$ , are also greater.

228 The number of trials of each action that maximizes the total net benefit can be found efficiently  
229 using numerical methods. We generated the numerical results using Wolfram Mathematica  
230 V8.0.4 (Inc. 2014)). We used a built in optimization function, FindMaximum, to find the optimal  
231 non-zero allocation to the learning phase and compared this to the expected reward under no  
232 experimentation (Data S1). We also derived explicit analytic solutions for several special cases  
233 (Appendix S2).

234 *Example: Choosing between supplementary feeding options for hihi nestlings*

235 We illustrate the model by determining the optimal proportion of the total budget to use on  
236 trialing two supplemental feeding treatments for hihi (*Notiomystis cincta*) nestlings, an endangered  
237 New Zealand bird whose recovery program is based on supplementary feeding (Walker et al.  
238 2013). There is evidence that sugar water improves adult survival (Armstrong and Ewan 2001;  
239 Chauvenet et al 2012); sugar water is currently provided to five out of six extant populations  
240 (L.Walker, personal observations). An alternative full dietary supplement (Wombaroo™  
241 Lorikeet & Honeyeater Food, Wombaroo Food Products, Glen Osmond, SA, Australia) has also  
242 been trialed in both adult and, more recently, juvenile populations (Armstrong et al. 2007, Walker  
243 et al. 2013). Walker et al. (2013) investigated experimentally the effects of neonatal  
244 supplementary feeding using four alternative treatments on nestling growth, nestling survival and

245 juvenile survival to breeding age (recruitment). The following illustrative example is based on  
246 data and cost estimates from Walker et al.'s study.

247 Consider the case when management has a total budget  $B$  to spend on supplementary feeding  
248 over  $T$  years. The manager has two possible supplementary feeding treatments: sugar water (N-)  
249 and Wombaroo™ Lorikeet & Honeyeater Food (N+). The goal is to determine the proportion of  
250 the budget to spend on trialing the two treatments in the first year. The management benefit of  
251 each treatment is measured as the mean additional weight at age 20 days; where additional is in  
252 reference to the expected average weight with no supplementary feeding. We consider the  
253 management units to be birds and consider costs in units of hours per bird per year.

254 We assume that sugar water is provided using general feeding stations in all situations (i.e. during  
255 the experiment and during the management only phase). During the experimental phase, the  
256 managers additionally feed the dietary supplement to the nestlings directly. If sugar water (N-) is  
257 found to be the preferable treatment, then it would be administered only via the general feeding  
258 stations, as it is known to be provisioned to nestlings by parents (Walker et al. 2013; Thorogood  
259 et al. 2008). However, for Wombaroo (N+), it is unclear whether it would be possible to  
260 administer the supplement via the feeders or if it would be necessary to continue directly feeding  
261 juveniles in the nests (L. Walker, personal observations). Therefore, we considered two scenarios.

262 In scenario (i) we assumed that the full dietary supplement (N+) will continue to be administered  
263 to juveniles directly. In scenario (ii) we assumed that after the experimental phase N+ could be  
264 administered via the general feeding stations. In this case a larger quantity of the dietary  
265 supplement would be required, but the cost associated with administering the supplement would  
266 be much less.

267 Estimates for the cost of implementing both management options (general feeders and direct  
268 feeding of nestlings), together with estimates of the cost of monitoring the results were obtained  
269 from data provided by L. Walker and A. Baxter (unpublished data; personal communication). A  
270 summary of the parameters used for the results presented are given in Table 1, while an overview  
271 of the cost data can be found in Appendix S3.

## 272 RESULTS

### 273 *When and how much should we invest in learning?*

274 Recall that  $E_u$  is the expected benefit in the face of uncertainty, that is, if no experimentation  
275 occurs. Consequently, from Equation (15) we see that it is beneficial to invest in experimentation  
276 if there exists a sampling design  $\{n_1, n_2\}$  (not =  $\{0,0\}$ ) such that the expected benefit from the  
277 experimentation phase outweighs the lost opportunity costs incurred by using resources for  
278 experimentation, i.e. when

$$279 \quad EVSI + n_1 m_1 + n_2 m_2 > \frac{c_{\text{experiment}}}{B} E_s. \quad (16)$$

280 There is no simple rule for when learning is worthwhile due to the large number of parameters  
281 involved in determining the threshold. Nonetheless, general tendencies can be observed  
282 (summarized in Box 1 and Table 2).

283 If monitoring costs are negligible it is nearly always optimal to spend some of the budget on  
284 learning (Figs. 1-3: Panels a and c, Appendix S4: Fig. S1a). Note that if both actions are  
285 uncertain, trialing the expected best action will never be worse than directly implementing it, but  
286 there may be no expected advantage when the means are very different. In the case that the  
287 benefit of one action is known, if the uncertain action is expected to be worse, then whether or



288 not it is worth trialing it will depend on how uncertain we are about its performance, the budget  
289 and the monitoring precision (Figs. 1-3: Panel c, Fig. S2).

290 If monitoring costs are significant, it is not beneficial to invest in learning if: one action is  
291 expected to be much better than the other, monitoring variance is large, monitoring costs are large  
292 or the budget is small (Figs. 1-3: Panels b and d). For example, if the expected benefit of the two  
293 actions differs, then investing in learning is worthwhile only when the budget is sufficiently large  
294 (Fig. 2b and 2d).

295 Note that the graphs in Figure 1 are not perfectly symmetric around  $m_2 - m_1 = 0$ . When the benefit  
296 of action 1 is known with certainty (Fig. 1c-d), it is optimal to spend less on the learning phase if  
297 the expected benefit of action 2 is less than the expected benefit of action 1 than if it is greater  
298 (see also Figs. 2c-d and 3c-d). Intuitively, this is because there is a smaller probability that action  
299 2 is better than action 1. When both actions are uncertain, this argument no longer applies: there  
300 is the same probability that the expected worse action will be found to be better. In this case, we  
301 observe the opposite behavior: it is optimal to spend a larger proportion of the budget on the  
302 learning phase when the expected value of action 2 is 5 units smaller than action 1 than when it is  
303 5 units larger (Figs. 1-3: Panels a-b). This is primarily because the solution depends substantially  
304 on the ratio of the means to prior variances: the optimal proportion to spend on the learning phase  
305 is a decreasing function of the ratio of the prior expected benefit to prior standard deviation  
306 (Appendix S4: Fig. S11).

307 The solution for the optimal proportion to spend on the learning phase displays a number of  
308 interesting critical thresholds (Figs. 1-3). For example, as the difference in the expected prior  
309 benefit of the two actions increases, a point is eventually reached beyond which it is not worth

310 investing in learning (Fig. 1). At this point, the optimal solution drops suddenly from spending a  
311 large amount on learning to nothing at all. Where this point occurs depends notably on the prior  
312 variance of each action. The more uncertain we are about the performance of each action, the  
313 greater the difference between the prior mean benefits before we stop investing in learning, since  
314 if the overlap between the two prior distributions is small the best action is known with high  
315 probability. Similar thresholds are observed for the budget (Fig. 2 and Appendix S4: Fig. S1),  
316 monitoring cost (Appendix S4: Fig. S1) and monitoring variance (Fig. 3). These thresholds are  
317 more prevalent when monitoring costs are significant.

318 This threshold behavior can be better understood by observing that the optimal (non-zero)  
319 investment in experimentation is a local, but not necessarily global, optimum (Fig. 4). The  
320 expected net benefit (ENB = Expected benefit *without* experimentation - expected benefit *with*  
321 experimentation) is a concave function of the amount invested in the experiment. Note that no  
322 experimentation results in zero expected net benefit. When the expected net benefit of  
323 experimentation is positive, the optimal solution is found at the maximum of this curve (e.g., at  
324 an investment of ~50 in Fig. 4a). However, as, for example, the sampling variance increases,  
325 EVSI and also the expected net benefit decrease, but an optimal allocation can still be found,  
326 until the whole curve drops below 0 (Fig. 4b), in which case, no investment in learning is  
327 warranted.

328 Analytical results for the optimal number of trials can be derived for several, potentially  
329 common, special cases (Appendix S2). These analytic solutions suggest a maximum of 1/3 of the  
330 budget should be spent on the learning phase. Numerical results showed that this limit is  
331 occasionally exceeded when: monitoring costs are negligible, means differ, and either sampling  
332 variance is (reasonably) high or the budget is small (Figs. 2 and 3). However, for the parameter

333 ranges we explored, it is usually optimal to spend less than 20% of the budget on learning. When  
334 monitoring costs are significant, the optimal allocation of effort to the learning phase is always  
335 less than a third. Moreover, in this case the analytic solution derived assuming identical  
336 parameters (Appendix S2: Eq. S3) is an upper bound.

337 For both negligible and significant monitoring costs, the highest proportion of the budget is spent  
338 on learning when the budget is fairly small (Fig. 2, Appendix S2: Eq. S3). As the budget  
339 increases relative to implementation and monitoring costs, we spend more on monitoring in an  
340 absolute sense, but a smaller fraction of the total budget. For example, in the hihi supplementary  
341 feeding example below, as the budget increases the optimal number of trials of each treatment  
342 increases, but the total proportion spent on the learning phase decreases (Fig. 6 and Appendix S4:  
343 Fig. S10).

344 For a fixed budget, the optimal proportion to spend on learning is an increasing function of  
345 monitoring costs when parameters are equal and the prior expected benefits are zero (Appendix  
346 S2). This is because although the optimal number of trials is a decreasing function of monitoring  
347 cost, it does not decrease as fast as monitoring and implementation costs increase. Interestingly,  
348 when the prior mean benefits are positive, the optimal number of trials decreases more quickly  
349 than when they can be assumed to be zero (Appendix S4: Fig. S3). Consequently, when the  
350 management actions are expected to have a large benefit ( $> \sim 4$  for the default parameters), the  
351 optimal proportion of the budget to spend on the learning phase is a decreasing, rather than  
352 increasing, function of monitoring costs (Appendix S4: Fig. S3).

353 When monitoring costs are negligible, the amount spent on the learning phase is an increasing  
354 function of the difference in the prior mean benefit (until the threshold is reached) (Fig. 1a and

355 1c). Consequently, the largest percentage of the budget is invested in experimentation when the  
356 prior means are different, but not too different. In contrast, when monitoring costs are significant  
357 the largest percentage is spent on learning when the prior mean benefits are the same (Fig. 1b and  
358 1d).

359 When all other parameters are equal, we spend the maximum proportion of the budget on  
360 learning when the prior standard deviations of the two actions are the same (Fig. S4). That is, if  
361 we are more confident about one action than the other, we will tend to spend less on  
362 experimenting. In Appendix S2, we derive an analytic solution for the case when the benefit of  
363 one action is well known ( $s_1 = 0$ ), the prior mean benefits are the same and either  $m_2$  or  $k_2$  is zero  
364 (Appendix S2: Eq. S6). We also show that this solution is a good approximation for non-zero  $m_2$   
365 and  $k_2$  if the prior variance is large relative to the expected benefit  $m_2$ . Our numerical results  
366 support this finding: in general, if we fix the uncertainty about one action and increase the  
367 uncertainty about the other, the amount spent on learning converges to the analytical solution  
368 derived (Appendix S4: Fig. S4). Presumably we are only entertaining the second action because  
369 we think that its performance is roughly the same as action 1, but we are not sure whether it will  
370 do much better or much worse. In this case,  $s_2$  will be large (relative to  $m_2$ ). Hence, the analytical  
371 result gives us a rough rule of thumb of investment in assessing a very uncertain action against a  
372 known outcome.

373 As highlighted by the analytic results (Appendix S2), the ratio of sampling variance to prior  
374 variance also plays an important role in determining when to invest in learning. As the sampling  
375 variance increases, more sampling is required to be similarly confident about the benefit of each  
376 action, initially increasing the amount spent on the learning phase. However, the percentage gain  
377 from investing in learning is a decreasing function of sample variance (Appendix S4: Fig. S5).

378 Consequently, when the expected performance differs between actions or monitoring costs are  
379 significant, investing in learning is eventually no longer beneficial. At this critical threshold, the  
380 optimal strategy switches from investing a significant amount in learning to investing nothing  
381 (Figs. 1 and 3).

382 *If we invest in learning, what is the split between the two actions?*

383 When only the prior mean efficiency differs between actions, it is optimal to spend a larger  
384 proportion of the learning-phase budget on the action with the highest expected performance  
385 (Fig. 5a-b,  $s_2 = 10$ ). When the two actions are expected to perform equally well but the  
386 uncertainty about their performance differs, it is optimal to spend more on the most uncertain  
387 action (Fig. 5a-b,  $m_2 - m_1 = 0$ ). When the prior mean efficiencies and prior variances both differ, the  
388 split is weighted toward the action with the highest expected return (Fig. 5a-b). That is, even if  
389 we are more uncertain about action 2, we may still spend more on trialing action 1 if we believe it  
390 is expected to be the better action.

391 When the prior distributions differ, it is sometimes optimal to only trial one of the actions if the  
392 budget is small or sampling variance is large, relative to the prior variance, (Fig. 5, Appendix S4:  
393 Figs. S6 and S7). In these situations, investing in learning may still be optimal, but lost  
394 opportunity costs are minimized by only trialing the expected best action.

395 *When do we get the largest benefits from investing in learning?*

396 The largest percentage gains in the objective function are observed when the budget is large  
397 (Appendix S4: Figs. S8b and S9), the means are similar (Appendix S4: Figs. S5, S6a and S9), the  
398 efficiency of each action is uncertain (Appendix S4: Fig. S8c), and sampling provides precise  
399 results (Appendix S4: Figs. S5 and S8d).

400 *Choosing between supplementary feeding options for hihi nestlings*

401 For the parameters used, the total proportion of the budget to spend on the learning phase  
402 depended very little on whether the prior expected benefit of the Wombaroo treatment (N+) was  
403 smaller, larger or the same as the sugar water treatment (N-) (Fig. 6a and Appendix S4: Fig.  
404 S10a). However, the optimal number of trials of each treatment did depend on the expected  
405 benefit of the Wombaroo treatment (Fig. 6b and Appendix S4: Fig. S10b).

406 Interestingly, there was only a small difference between the results for the two different scenarios  
407 (Fig. 6 versus Appendix S4: Fig. S10). That is, for our cost estimates, whether or not Wombaroo  
408 would be fed directly to nestlings or could be administered via feeders, the optimal proportion to  
409 spend on the learning phase was more or less the same.

410 It is worth highlighting that these results depend on the reference weight. The optimal proportion  
411 to spend on experimentation depends on the ratio of the expected benefit to standard deviation of  
412 the prior (Appendix S4: Fig. S11). Consequently, if the reference weight is expected to be large  
413 (so that benefit above reference weight is small), then it will be optimal to spend more on  
414 experimentation than if the reference weight is small.

415 DISCUSSION

416 The formal derivation of the net benefit of two-phase adaptive management for a simple setting  
417 provides some powerful intuitive guidance for thinking about the value of learning in a dynamic  
418 setting. The value of experimentation arises out of two benefits and two costs (Eq. 15): the  
419 benefits associated with applying learning to subsequent management (EVSI); the transient  
420 benefits accrued during the learning phase; the direct costs of learning; and the opportunity costs  
421 of learning (the resources not available for subsequent management). Experimentation will be

422 warranted when the benefits outweigh the costs (Eq. 16); otherwise, management should proceed  
423 in the face of uncertainty. These qualitative insights, derived from quantitative results, provide a  
424 useful framework for evaluating experimentation.

425 More specific guidance for investment in learning becomes complicated quickly (Box 1 and  
426 Table 2). The management scenario we have presented was as simple as we could make it while  
427 including all the relevant factors. Nevertheless, there were still 11 parameters to consider, making  
428 it difficult to extract general insights and tendencies from numerical sensitivity analyses alone.  
429 By considering a simple scenario we were able to derive analytical solutions for several special  
430 cases. These solutions provided greater insight into how parameter combinations drive solution  
431 behavior, and a base against which to compare results when the assumptions leading to an  
432 analytical solution are violated. For example, the analytic solution is a good rule of thumb when  
433 trialing an unknown management action against a known one, even when the prior expected  
434 benefits differ and monitoring costs are significant (contrary to assumptions used to derive the  
435 result)(Appendix S4: Fig. S4). However, when considering two uncertain management actions,  
436 the optimal allocation of resources depends strongly on the parameters that were excluded from  
437 the analytical result.

438 The scenario analyzed gave rise to several unintuitive results. For example, there is a tendency to  
439 think that monitoring large projects is more important than monitoring small projects – sure,  
440 large projects should have more money spent on monitoring, but our results suggest that smaller  
441 projects should have a higher proportion of the budget spent on learning and monitoring. This  
442 also suggests benefits of cooperation and coordination of smaller projects.

443 An interesting feature of the solution is the existence of several critical thresholds that mark a  
444 jump from investing a lot in learning to not learning at all, or vice versa. For example, when the  
445 expected performance of the two actions differ, as sampling variance increases we observe a  
446 critical threshold at which the optimal solution changes from spending a lot on the learning phase  
447 to spending nothing. While it is important for people developing and interpreting adaptive  
448 management models to be aware of such thresholds, managers implementing the policies need  
449 not be too concerned, since, at these thresholds investing a lot or not investing at all yield quite  
450 similar management outcomes. Consequently, it is not crucial to know precisely on which side of  
451 the critical threshold the system lies.

452 The priors for the two management options influence the results quite substantially. That is, the  
453 perceived performance of the two options (the prior means), and the uncertainty about their  
454 performance (the prior standard deviations) will influence the optimal extent of experimentation.  
455 This makes intuitive sense because managers would be expected to entertain the possibility of  
456 experimenting on a new management action only if they thought that it might perform better than  
457 an alternative but were uncertain about its relative performance. However, prior distributions are  
458 rarely used in ecology (Morris et al. 2015), and they can be difficult to specify coherently  
459 (McCarthy 2007) . If one were unwilling to specify a prior distribution, then one could set the  
460 prior standard deviation to be large, which would mean the posterior distribution would have the  
461 same shape as the likelihood function. In this case, the Bayesian estimates of the experimental  
462 results would be numerically equivalent to those of a frequentist analysis, which do not  
463 incorporate priors. However, such a wide prior distribution implies that extremely good (large  
464 positive values for the efficiency of management) or extremely poor outcomes (large negative  
465 values) are conceivable. Inflating the uncertainty in the priors will tend to drive more



466 experimentation than might be warranted, emphasizing the need to specify priors thoughtfully  
467 with available data (McCarthy and Masters 2005) or rigorous methods for expert elicitation  
468 (Speirs-Bridge et al. 2010). Although priors might be difficult to specify, decision-makers are  
469 inherently considering them when they begin to compare different management actions.  
470 Explicitly specifying the anticipated benefits and the degree of uncertainty about action outcomes  
471 can lead to better decisions about experimentation. Hence, specifying priors should not be seen as  
472 an obstacle to the decision making process, but rather a useful tool to improve decisions.

473 Monitoring is the cornerstone of successful adaptive management (Moir and Block 2001).  
474 However, monitoring management outcomes is rarely a trivial task and can account for a large  
475 fraction of the total budget required to implement an adaptive approach to management (Walters  
476 2007). For the two time-step process considered here, including monitoring costs substantially  
477 changed the solution, both in terms of quantitative value and qualitative behavior. For example,  
478 when monitoring costs were negligible, the amount spent on learning increased as the expected  
479 benefit of the two actions differed. In this case, little is to be lost by spending more on the  
480 learning phase and increasing the proportion of the learning-phase budget spent on the expected  
481 best action. However, when monitoring costs were significant the amount spent on  
482 experimentation was largest when the difference in the prior mean benefits was small. This is  
483 because the resulting probability of choosing the best management action without monitoring is  
484 lowest at this point (in contrast, when the expected difference in benefit is large, the probability  
485 the better looking action is actually better is large, hence there is less to gain from monitoring, see  
486 also MacGregor et al. 2002, Maxwell et al. 2015). Further, the critical thresholds play a more  
487 important role when monitoring costs are significant; the minimum budget, maximum difference

488 between prior means and maximum monitoring variance are more likely to be encountered within  
489 feasible parameter ranges.

490 Interestingly, in many ways the optimal solution was simpler when monitoring costs were  
491 substantial. For example, the proportion of the budget spent on learning tended to be fairly  
492 constant across the region in which it was optimal to invest in learning. Further, the analytic  
493 solution derived assuming identical parameters for the two actions (Appendix S2) is an upper-  
494 bound on the optimal proportion to spend on learning. These results highlight the importance of  
495 accounting for monitoring costs when designing adaptive management plans.

496 We found that the largest expected proportional gains in the objective function rarely  
497 corresponded to when the largest proportion of the budget should be spent on learning. For  
498 example, larger proportional gains are expected when sampling variance is low, whereas, in  
499 general, a larger percentage of the budget should be spent on learning when sampling variance is  
500 high because more samples are needed. Similarly, although a larger percentage gain is expected  
501 for large budgets, a larger proportion of the budget should be spent on learning when budgets are  
502 small.

503 We considered a two-step adaptive management approach in which the management horizon is  
504 divided into a learning phase and an implementation phase. Walters and Green (1997) propose a  
505 similar framework for evaluating experimental management actions for ecological systems.

506 These two approaches make a one-off decision about how much to invest in learning. This differs  
507 from many formulations of AM that assume a fixed budget per time-step and look at how to  
508 divide funds between alternative management actions, and monitoring, at each phase (e.g. Moore  
509 and McCarthy 2010, Baxter and Possingham 2011); effectively deciding how much to invest in

510 learning at each time-step. At best, the two time-steps will approximate sequential decisions over  
511 many time-steps. An interesting avenue of future research would be to compare the management  
512 policies derived under the two different modelling approaches.

513 EVSI tells us the expected value of a given sampling design, but it does not take into account lost  
514 opportunity costs associated with experimentation and monitoring. Consequently, while methods  
515 such as EVSI are useful for determining when learning is likely to be beneficial, and can provide  
516 upper bounds on *additional* funds that should be spent on experimentation, further analysis is  
517 needed to determine the fraction of the total budget to invest in learning. In contrast, Adaptive  
518 Management formulations with long time horizons can be computationally challenging and  
519 difficult to implement in the real world. The approach presented here strikes a balance between  
520 complexity and utility. By considering a two-step AM process we are able to capture the trade-off  
521 between the benefit and costs of investing in additional information while remaining relatively  
522 simple.

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611

612

613 Box 1. Summary of key results

614

615 When and how much should we invest in learning? (Figs 1-3, S2 and S4)

616

617 It is worthwhile investing in learning if:

618 
$$EVSI + n_1 m_1 + n_2 m_2 > \frac{c_{\text{experiment}}}{B} E_S,$$

619 for some  $\{n_1, n_2\}$  not equal to 0.

620

621 Analytic solutions suggest a maximum of 1/3 of the budget should be invested in learning. This is  
622 an upper bound when monitoring costs are significant. When monitoring costs are negligible, it  
623 may be optimal to spend more than 1/3 on learning if: the prior mean benefit differs between  
624 actions and either the sampling variance is (reasonably) large or the budget is small.

625

626 The optimal solution is characterized by several interesting critical thresholds.

627

628 Significant monitoring costs result in a higher proportion of the budget being spent on learning  
629 when the expected performance of the two actions is the same. In contrast, when monitoring costs  
630 are negligible a higher proportion of the budget is spent on learning when the expected  
631 performance of the two actions differ (Table 2).

632

633 How should we split the resources spent on learning between the two actions? (Fig 5,6 and S6)

634

635 It is optimal to spend more on the most uncertain or the expected best action.

636

637 If the prior distributions differ, it is sometimes optimal to only trial one of the actions (expected  
638 best or most uncertain) if: the budget is small or sampling variance is large.

639

640



641 **Table 1:** Parameter estimates for the hihi example.

| Parameter   | units         | Treatment N-          | Treatment N+                    |
|---|---------------|-----------------------|---------------------------------|
| Management cost, c  | hrs/bird/year | (i) 1.13<br>(ii) 1.13 | (i) 2.14<br>(ii) 2.651          |
| Monitoring cost, k  | hrs/bird/year | (i) 1.55<br>(ii) 1.55 | (i) 1.55<br>(ii) 0.033          |
| Management effect<br>(weight above<br>reference weight)<br>• Mean<br>• SD | g/bird        | $m_1 = 3$<br>SD = 6   | $m_2 = \{0, 3, 6\}$ g<br>SD = 6 |
| Budget  | hours         | [50, 2000]            |                                 |
| Monitoring<br>SD/accuracy   | g/bird        | SD = 6 g              | SD = 6 g                        |

642

643

644 Table 2: The largest percentage of the budget is spent on learning when:  
 645

| variable   | $k = 0$  | $k > 0$   |
|------------|--|---|
| $m_i$      | $m_1$ and $m_2$ <i>differ</i> ,<br>but difference is $<$ threshold | $m_1$ and $m_2$ <i>are the same</i>   |
| $\sigma_i$ | large, but $<$ threshold   |   |
| $B$        | small, but $>$ threshold   |   |
| $s_i$      | $s_1$ and $s_2$ are the same                                       |   |
| $k_i$      | N/A  | large if $m_i s_i$ are small<br>small if $m_i s_i$ are large  |
| $m_i/s_i$  | constant   | uncertainty about the expected benefit of action $i$ is large relative to the expected benefit, i.e when $m_i/s_i$ is small. (Fig S9) |

646

647

648

649

650 FIGURE LEGENDS

651 Figure 1. Proportion spent on learning as a function of the difference in the prior expected  
652 benefits and sampling standard deviation. Contours indicate the proportion of the budget spent on  
653 the learning phase for various shades of gray (dark gray = 0, white = 1).  $m_1 = 10$  (vary  $m_2$ ),  $B =$   
654  $500$ ,  $c_1 = c_2 = 5$ ,  $\sigma_1 = \sigma_2$ . Panels (a) and (c) assume zero monitoring cost,  $k_1 = k_2 = 0$ , panels (b) and  
655 (d) assume a monitoring cost of 3 units ( $k_1 = k_2 = 3$ ). Panels (a) and (b) assume both actions are  
656 uncertain with  $s_1 = s_2 = 10$ , panels (c) and (d) assume the benefit of one is known,  $s_1 = 0$  and  $s_2 =$   
657  $10$ . See Fig S1 for a cross section of (a) and (b) at  $\sigma_1 = \sigma_2 = 40$ .

658 Figure 2. Proportion spent on learning vs budget. Default parameters:  $m_1 = 10$ ,  $m_2 = \{5, 10, 15\}$ ,  $s_1$   
659  $= s_2 = 10$ ,  $c_1 = c_2 = 5$ ,  $\sigma_1 = \sigma_2 = 20$ . Black dashed:  $m_2 - m_1 = -5$ , thin black:  $m_2 - m_1 = 0$ , thick black:  $m_2 -$   
660  $m_1 = 5$ . The gray line is the corresponding analytic solution assuming parameters are equal and  
661 either monitoring is free or mean benefits are zero.

662 Figure 3. Proportion spent on experimentation as a function of the ratio of sample to prior  
663 variance for action 2.  $B = 500$ ,  $m_1 = 10$ ,  $c_1 = c_2 = 5$ . (a) & (b)  $s_1 = s_2 = 10$ ,  $\sigma_1 = \sigma_2$ . (c) & (d) benefit of  
664 action 1 assumed to be known. Black dashed:  $m_2 = 5$ , thin black:  $m_2 = 10$ , thick black:  $m_2 = 15$ . The  
665 gray line is the corresponding analytic solution assuming parameters are equal and either  
666 monitoring is free or mean benefits are zero.

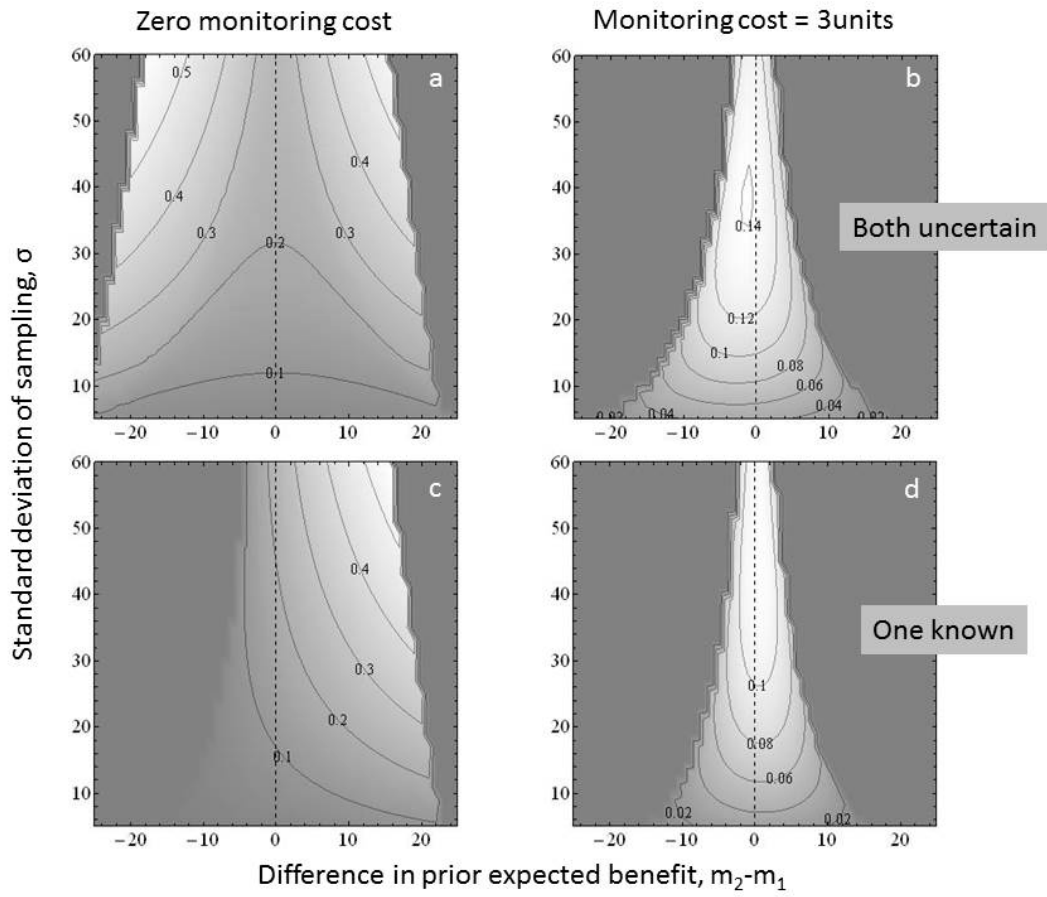
667 Figure 4. Expected net benefit versus the amount invested in experimentation for: two-step AM =  
668  $EVSI + n_1 m_1 + n_2 m_2 - \frac{c_{\text{experiment}}}{B} E_S$  (thick solid line), EVSI (dashed line) and EVPI (thin solid  
669 line).  $c_1 = c_2 = 5$ ;  $k_1 = k_2 = 3$ ;  $s_1 = s_2 = 10$ ;  $m_1 = 10$ ,  $m_2 = 15$ ;  $B = 500$ . (a)  $\sigma_1 = \sigma_2 = 20$  ( $\sigma^2/s^2 = 4$ ),  
670 (b)  $\sigma_1 = \sigma_2 = 37$  ( $\sigma^2/s^2 = 13.7$ ).

671 Figure 5. Panels (a) and (b): Optimal proportion to spend on action 2 when the prior means and  
672 standard deviations differ.  $s_1 = 10$ ,  $c_1 = c_2 = 5$ ,  $\sigma_1 = \sigma_2 = 20$ ,  $B = 500$ . Black dashed:  $s_2=5$ , thin  
673 black:  $s_2=10$ , thick black:  $s_2=20$ . A sudden drop to zero corresponds to crossing a threshold above  
674 which none of the budget is spent on the learning phase (see panels (c) and (d): optimal  
675 proportion to spend on the learning phase). In panel (b), when  $s_2 = 5$ , none of the budget is spent  
676 on trialing action 2 as the benefit is reasonably well known, however, some of the budget is spent  
677 on trialing action 1 for some of the parameter space.

678 Figure 6. Hihi supplementary feeding example, scenario (i). Panel (a): Optimal proportion to  
679 spend on the learning phase as a function of the budget (for males). Black dashed:  $m_{N+} = 0$ ,  
680 Black thin:  $m_{N+} = 3 = m_{N-}$ , Black thick:  $m_{N+}=6$ . In this panel, the gray line corresponds to the  
681 approximate solution, calculate assuming parameters are the same and either negligible  
682 monitoring costs or zero expected effect. Panel (b): Corresponding optimal number of trials of  
683 each action. Black (top group of lines) = action N- , gray (bottom group) = action N+. Target  
684 weight = 29.  $s = 6$ ,  $\sigma = 6$ .  $m_{N-} = 3$ .

685 FIGURES

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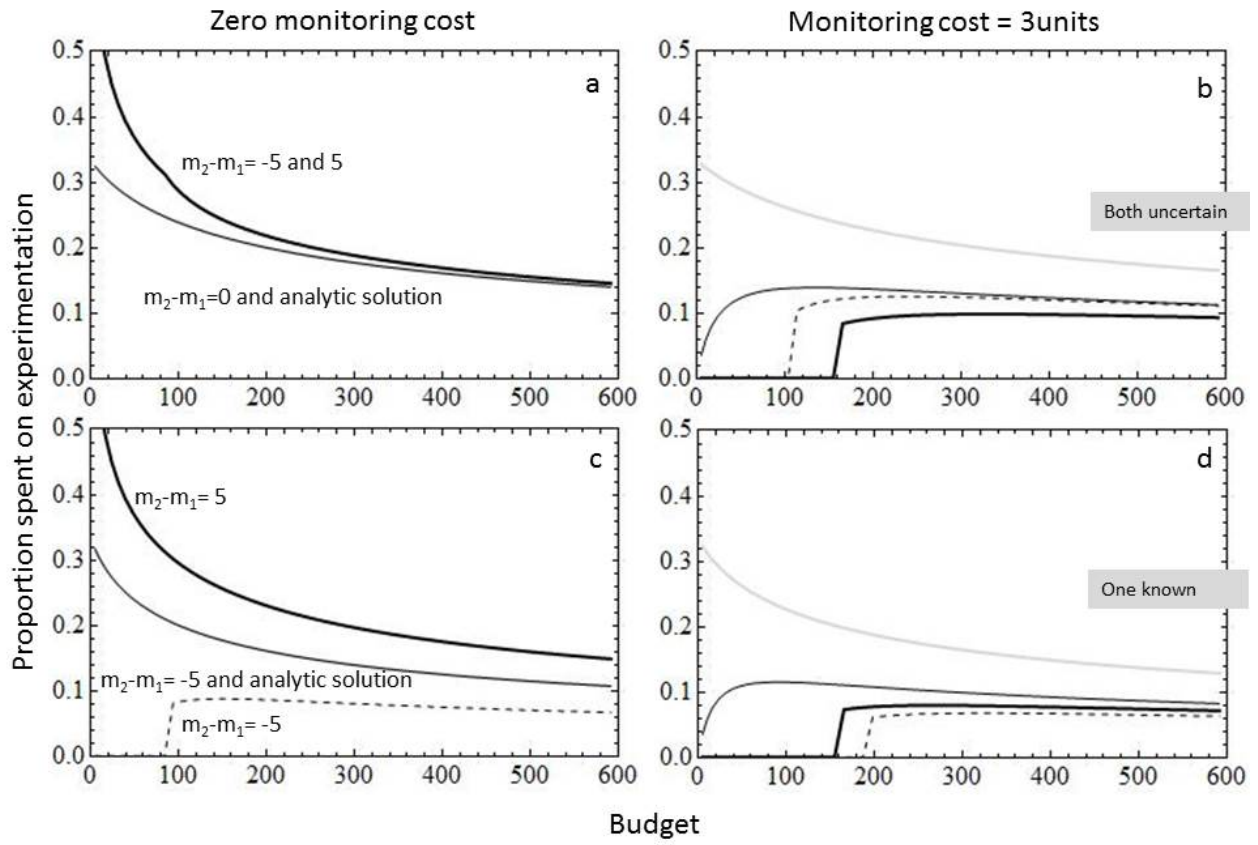


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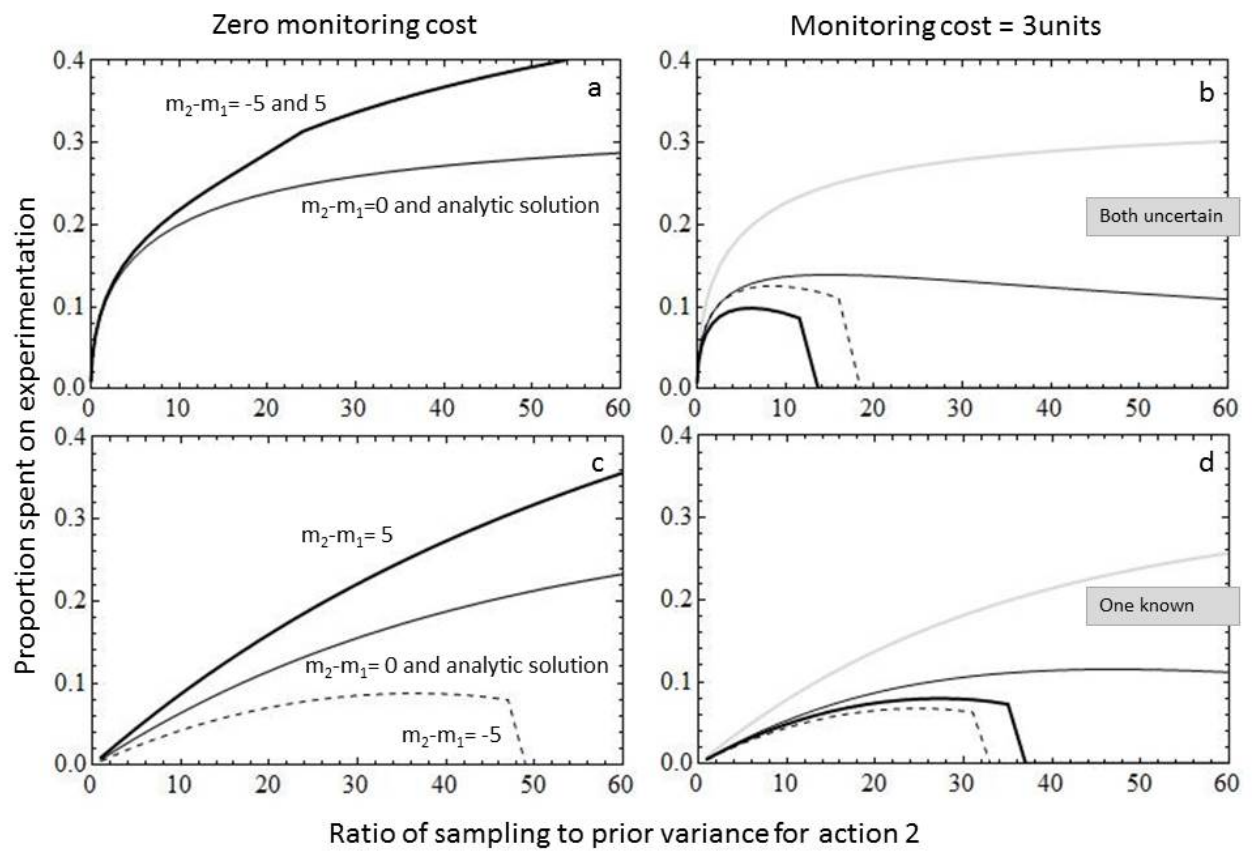
688 Figure 1

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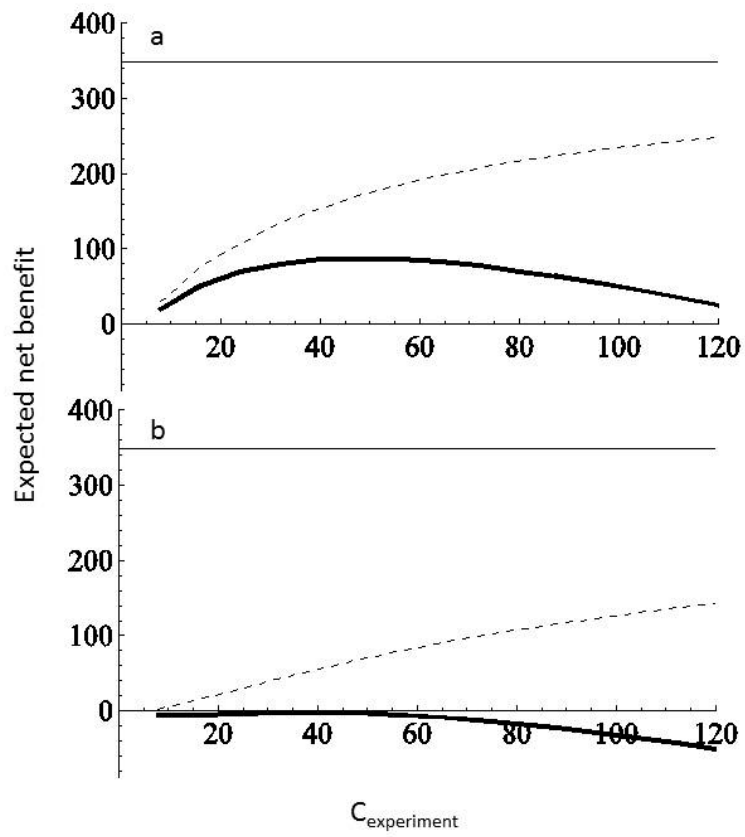
692  
693 Figure 2.



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695 Figure 3.

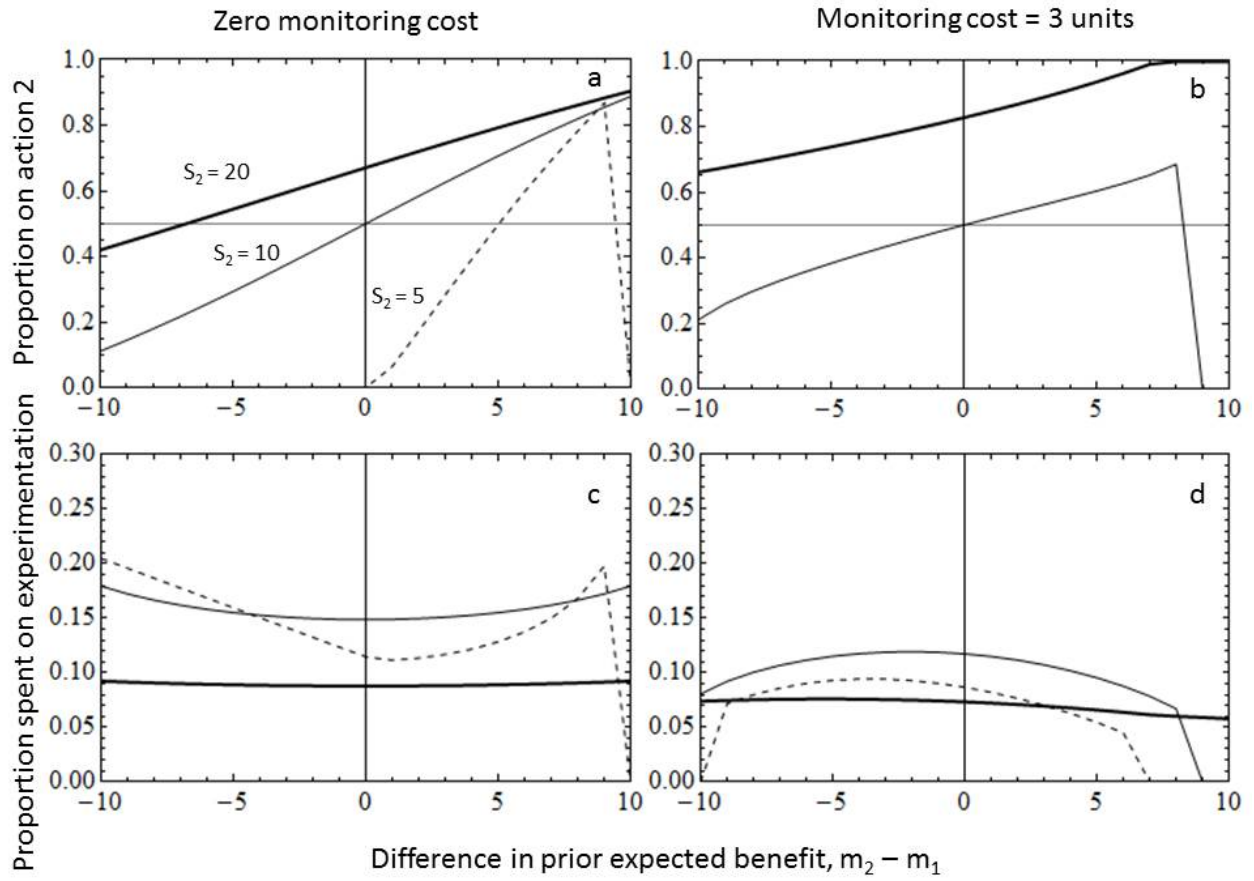
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698 Figure 4.





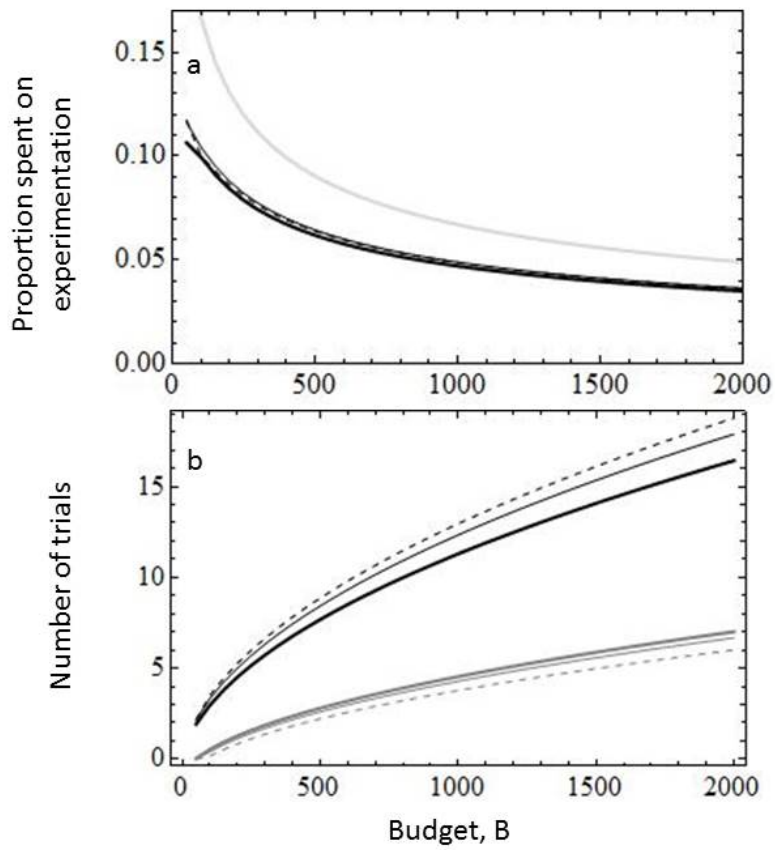
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700 Figure 5.

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704  
705  
706 Figure 6.

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