Preliminary report on electromagnetic model studies

by

F. C. Frischknecht and G. B. Mangan
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Abstract

More than 70 response curves for various models have been obtained using the slingram and turam electromagnetic methods. Results show that for the slingram method, horizontal co-planar coils are usually more sensitive than vertical, co-axial or vertical, co-planar coils. The shape of the anomaly usually is simpler for the vertical coils.
Introduction

Electromagnetic measurements furnish a useful means of prospecting for ore deposits and are becoming increasingly important for geologic mapping. Results are usually interpreted by comparing the data with reference curves established by previous experience or with curves obtained from model studies in the laboratory, but few such curves have been published.

Since 1955, the U. S. Geological Survey has experimented with various types of electromagnetic methods in many areas. The present curves show the results of typical model studies undertaken for interpreting field observations.

Some of the results were obtained by Frischknecht in the laboratories of Geofysisk Malmleting, in Trondheim, Norway. The others were obtained by Frischknecht and Mangan in the Survey laboratories in Denver, Colorado.

Acknowledgments

The authors wish to thank Geofysisk Malmleting, Trondheim, Norway for the use of their model laboratory, and the staff of Geofysisk Malmleting for their advice and assistance.
Theory

The conditions of electrodynamic similitude are well known (Sinclair, 1948). If displacement currents can be neglected, as is usually permissible in low-frequency prospecting, the only requirement for similitude is that the conductivity parameter, \( \sigma \omega L^2 \), shall have the same value in the model and in the earth, that is,

\[
\sigma_1 \mu_1 \omega_1 L_1^2 = \sigma_2 \mu_2 \omega_2 L_2^2
\]

where:

- \( \sigma \) is the conductivity
- \( \mu \) is the magnetic permeability
- \( \omega \) is the angular frequency
- \( L \) is the length of a selected segment, and

index 1 refers to the field condition and

index 2 refers to the model.

On the assumption that in both cases, the magnetic permeability is the same as that of free space, \( \mu_1 = \mu_2 = \mu_0 \), then:

\[
\sigma_1 \omega_1 L_1^2 = \sigma_2 \omega_2 L_2^2
\]

If the linear dimensions in the field are 1,000 times those in the model, \( (L_1 = 1,000 L_2) \), then:

\[
\sigma_2 \omega_2 = \sigma_1 \omega_1 \times 10^6
\]

For a thin conducting sheet and low frequencies, the electromagnetic response depends on the parameter \( \sigma t \mu_0 \omega L \) (Wait, 1953), where \( t \) is the thickness of the sheet and the other symbols have been defined. Within proper limits, a conducting sheet may be substituted for another if \( \sigma t \) is the same for both.
For purely inductive electromagnetic methods where the primary field is set-up non-galvanically, the effect of country rock and overburden is often small. Most model studies, therefore, have been made using metallic models placed in air. The conductivity of metallic ores covers a wide range. A representative value for sulphide ores might be taken as 100 mhos/meter (Parasnis, 1956). The conductivity of aluminum, which is commonly used in model experiments, is about $3.45 \times 10^7$ mhos/meter or $3.45 \times 10^5$ times that of ore. If the frequency used in the model studies is the same as that used in the field, then the dimensions of an aluminum model should be $\frac{1}{\sqrt{(3.45 \times 10^5)^2}}$ or 1:590 that of the field situation. Scales of from 1:500 to 1:1,000 are convenient, and with the use of field frequencies in the model studies some of the components used in the field can be utilized.
Slingram and turam methods

The slingram method utilizes two, small, portable coils; one serves as a transmitter and the other as a receiver (Frischknecht, 1959). A reference voltage is brought from the transmitting coil to the receiving coil with a cable. The ratio of the mutual impedance between the two coils is the presence of the earth to their mutual impedance in free space is measured by finding the complex ratio between the voltage induced in the receiving coil and the reference voltage. The coils are moved together at a fixed separation which, in practice is usually between 100 and 300 feet. Commonly, the coils are oriented so that they are co-planar and horizontal; however, occasionally the coils are held in perpendicular, vertical, co-axial, or co-planar positions. The field frequency ranges from 500 to 8,000 cycles per second.

In the turam method, a long grounded wire or a large, horizontal, insulated loop is used as the transmitter (Frischknecht, 1959). The field frequency ranges from 100 to 800 cycles per second. Measurements are made along traverses at intervals of 25 to 100 feet using two small receiving coils, the lagging coil being placed at the position previously occupied by the leading coil. The complex ratio of the voltages induced in the two coils is measured. The ratios measured in the field are normalized by dividing by theoretical ratios calculated from free space considerations. When significant anomalies occur in the ratios, the actual normalized fields are calculated by beginning with a measured, or an assumed value, for the field at a point near the cable, and successively multiplying this value by the normalized ratios.
Equipment and techniques

The studies were made using a frequency of 500 cycles per second. The ratiometer and amplifier (fig. 1) were made by Geofysisk Malmleting

Figure 1.--Block diagram of equipment for slingram model experiments.

for turam field measurements. The slingram and the turam receiving coils had several hundred turns of copper wire wound on plastic forms about 1 cm in diameter. The reference coil was wound on the same form as the transmitting coil. Because the coils had a Q of only 2 at the selected frequency, they were not tuned. It was not necessary to use electrostatic shielding around the coils, as would be required at higher frequencies or with larger coils. For the turam measurements, the transmitting loop was a single turn of wire in a 100 cm x 170 cm rectangle.

Under good conditions, the ratiometer could be read to 0.1 percent but interference from the ninth harmonic of the power line frequency usually prevented reading closer than 0.2 percent. The drift of the instruments was small and could usually be eliminated by resetting the zero before each run. If the drift was not negligible, it was assumed to be linear during the run and the readings were adjusted accordingly. The greatest instrumental error in the measurement is probably less than 0.5 percent, with either sign, although larger errors may occur for large anomalies because of errors in determining the positions of the models.
Figure 1. Block diagram of equipment for slingram model experiments
Data

Some of the curves presented in this report represent a systematic attempt to study horizontal sheets of various dimensions. Others represent attempts to reproduce conditions found in field measurements. Frequently, dimensions were selected according to the materials at hand.

Most of the curves were obtained for the slingram method, but a few were obtained for the turam method. The turam curves correspond to normalized field curves. Most of the slingram curves are for horizontal, co-planar coil arrangements and all of the turam curves were for horizontal coils. Profiles were observed for at least three heights above most of the models. Most of the profiles were made along traverses which pass over the midpoint and are perpendicular to the longest dimensions of the model. For all of the profiles taken in this fashion, an end view of the model is shown. For profiles where the traverse did not pass over the midpoint or was not perpendicular to the longest dimension of the model, a plan view of the model and the position of the traverse are shown.

Thin sheets are described in terms of their two largest dimensions and the product, $\sigma t$, which has the dimensions of mhos and which was actually measured in the laboratory. For the other models, all dimensions are specified and no attempt was made to measure their conductivity.
Figure 2: Slingram coils horizontal and co-planar

Frequency = 500 c.p.s.
Coil separation = 10 cm

Sheet 670 mesh 120 cm x 30 cm

Out-of-phase components, in percent

In-phase components, in percent
4 sheets, 670 mhos 120 x 30 cm each plus 4 sheets, 670 mhos 50 x 30 cm each

Coil separation = 10 cm

Frequency = 500 c.p.s.
Figure 9: Slingram Coils Horizontal and Co-Planar

Frequency = 500 c.p.s.
Coil Separation = 10 cm

Out-of-Phase Components, in Percent

In-Phase Components, in Percent

Sheet A: 0.8 cm x 2 cm x 30 cm

H = 1 cm
FIGURE 10
SLINGRAM COILS HORIZONTAL AND CO-PLANAR

Coil separation = 10 cm
Frequency = 500 c.p.s.

h = 1 cm

4 Sheets 580 mhos 20 cm x 30 cm each

IN PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT
IN-PHASE COMPONENTS IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT
IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT
IN-PHASE COMPONENTS IN PERCENT

OUT-OF-PHASE COMPONENTS IN PERCENT

FIGURE 15
SLINGRAM COILS
HORIZONTAL AND CO-PLANAR

Sheet Cu. 0.76 cm x 2.7 cm x 14.3 cm

Coil separation = 10 cm
Frequency = 500 c.p.s.

h = 1 cm

h = 1 cm
Figure 17 Slingram coils horizontal and co-planar

Frequency = 500 c.p.s.
Coil separation = 10 cm

Out-of-phase components, in percent

In-phase components, in percent

Frequency = 500 c.p.s.
Coil separation = 10 cm

Out-of-phase components, in percent

In-phase components, in percent

Frequency = 500 c.p.s.
Coil separation = 10 cm

Out-of-phase components, in percent

In-phase components, in percent
FIGURE 18
SLINGRAM COILS
HORIZONTAL AND CO-PLANAR

Coil separation = 10 cm
Frequency = 500 c.p.s.

Coil separation = 10 cm
Frequency = 500 c.p.s.

IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT
Figure 14: Slings gram Coils Horizontal and Co-Planar

Frequency = 500 c.p.s.
Coil Separation = 10 cm

Out-of-Phase Components, in Percent

In-Phase Components, in Percent

Coil separation = 10 cm
Frequency = 500 c.p.s.
FIGURE 20
SLINGRAM COIL HORIZONTAL AND CO-PLANAR

Coil separation = 10 cm
Frequency = 500 c.p.s.
Figure 2: Slingram Coils Horizontal and Co-planar

IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT

Coil separation = 10 cm
Frequency = 500 c.p.s.
Figure 4.1: Silverman, Coil's Horizontal and Co-planar Components, percent.

Frequency = 500 C.P.S.
Coi1 separation = 10 cm

Projectile Al. 0.81 cm x 10 cm x 30 cm
Figure 5.1: Slingram coils horizontal and co-planar

- Frequency = 500 c.p.s.
- Coil separation = 10 cm
- Sheet = 0.08 cm x 30 cm x 20 cm

Graph showing out-of-phase components in percent for various coil separations.
IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT

FIGURE 26
SLINGGRAM COILS
HORIZONTAL AND CO-PLANAR

2 Sheets Al. 0.081 cm x 10 cm x 30 cm

Frequency = 500 c.p.s.
IN-PHASE COMPONENTS IN PERCENT

Figure 2.7 Slingram Coils Horizontal and Co-planar

Frequency = 500 c.p.s.
Coil separation = 10 cm

2 Sheets. 481 cm x 10 cm x 30 cm

OUT-OF-PHASE COMPONENTS, IN PERCENT

IN-PHASE COMPONENTS, IN PERCENT

47159
Figure 4. Slilegram coils horizontal and co-planar CM 15

Frequency = 500 c.p.s.
Coil separation = 10 cm

3 Sheets Al 0.01 cm x 10 cm x 30 cm

Out-of-phase components, in percent

In-phase components, in percent
Figure 3: Silgram Coils Horizontal and Co-planar

- Frequency = 500 c.p.s.
- Coil separation = 10 cm

Out-of-Phase Components, In Percent

In-Phase Components, In Percent

- Sheet 1

- 0.081 cm x 20 cm x 74.8 cm
Coil separation = 10 cm
Frequency = 500 c.p.s.

FIGURE 38
SLINGRAGM COILS HORIZONTAL AND CO-PLANAR
Figure 39: Slingram coils horizontal and co-planar

Frequency = 500 c.p.s.
Coil separation = 10 cm

OUT-OF-PHASE COMPONENTS IN PERCENT

IN-PHASE COMPONENTS IN PERCENT

Dipping vertically

 Traverse

1 Sheet 1.081 cm x 20 cm x 7.08 cm
FIGURE 4.6 SLINGGRAM COILS HORIZONTAL AND CO-PLANAR

Coil separation = 10 cm
Frequency = 500 c.p.s.

4 Sheets Al 0.081 cm x 20 cm x 6.4 cm
Coil separation = 10 cm

Frequency = 500 c.p.s.

FIGURE 4/ Slingogram Coils Horizontal and Co-planar

IN-PHASE COMPONENTS IN PERCENT

OUT-OF-PHASE COMPONENTS IN PERCENT
Figure 43: Sinogram coils horizontal and co-planar.

Frequency = 500 c.p.s.
Coil separation = 10 cm

Out-of-phase components, in percent

In-phase components, in percent

4 sheets Al 0.081 cm x 20 cm x 64.1 cm
Dipping vertically
4 Sheets Al 0.081 cm x 20 cm x 64.1 cm dipping vertically

Frequency = 500 c.p.s.
Coil separation = 10 cm

CM 40 30 20 10 0

FIGURE 10

OUT-OF-PHASE COMPONENT, IN PERCENT

IN-PHASE COMPONENT, IN PERCENT

0.0 0.1 0.2 0.3 0.4 0.5

0 2 cm 4 cm 6 cm 8 cm
Coil separation = 10 cm  
Frequency = 500 c.p.s.
Coil separation = 10 cm
Frequency = 500 c.p.s.
Figure 47: Slingram Coils: Horizontal and Co-Planar

Frequency = 500 c.p.s.
Coil Separation = 10 cm
Dipping 45°

 Traverse

1 Sheet A1 0.081 cm x 20 cm x 74.8 cm

In-Phase Components in Percent

Out-of-Phase Components, in Percent
Figure 20: Silicram coils horizontal and co-planar.

FREQUENCY = 500 c.p.s.
Coil separation = 10 cm

Bar A: 3.8 cm x 10.2 cm x 104.2 cm

OUT-OF-PHASE COMPONENT IN PERCENT

IN-PHASE COMPONENT IN PERCENT
Figure 5.2: Si InGraM Coil's HorizontaL AND Co-PlanAR

- Frequency = 500 c.p.s.
- Coil Separation = 10 cm

Traverse dipping vertically

<table>
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<tr>
<th>Bar</th>
<th>1 Bar 3.8 cm x 10.3 cm x 104.2 cm</th>
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- Traverse Coils separation = 10 cm
- Frequency = 500 c.p.s.

Graph showing out-of-phase components in percent for different coil separations.
Figure 54: Stringram Coils Horizontal and Co-planar

- Frequency = 500 c.p.s.
- Cell Separation = 10 cm

Out-of-Phase Components, in Percent

In-Phase Components, in Percent
Coil separation = 10 cm
Frequency = 500 c.p.s.

Traverse A: 3.8 cm x 10.3 cm x 104.2 cm
dipping vertically

Coil separation = 10 cm
Frequency = 500 c.p.s.

Traverse A: 3.8 cm x 10.3 cm x 104.2 cm
dipping vertically
Block lead: 5.1 cm x 10.2 cm x 20.3 cm

Coil separation: 10 cm

Frequency = 500 c.p.s.

Figure S: Slingram coils horizontal and co-planar.

Cell separation = 10 cm

Frequency = 500 c.p.s.
Coil separation = 10 cm
Frequency = 500 c.p.s.

FIGURE S9
SLINGRAM COILS HORIZONTAL AND CO-P L A N A R
FIGURE 6
SLINGRAM COILS HORIZONTAL AND CO-PLANAR

Rectangular loop 12 Cu. wire 30 cm x 20 cm

IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT

Coil separation = 10 cm
Frequency = 500 c.p.s.
47759

![Graph of SLINGEGRAM COILS VERTICAL AND CO-AXIAL](image)

- Frequency: 500 c.p.s.
- Coil separation: 10 cm
- 4 sheets, 670 mhos, 120 x 30 cm each

**FIGURE SL**

OUT-OF-PHASE COMPONENTS, IN PERCENT

IN-PHASE COMPONENTS, IN PERCENT

- h = 2 cm
- 4 cm
- 4 cm
FIGURE 65
SLINGRAM COILS VERTICAL AND CO-AXIAL

Sheet Al. 0.81 cm x 20 cm x 30 cm

Coil separation = 10 cm
Frequency: 500 c.p.s.

IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT
Figure 6. Slingram Coils Vertical and Co-Axial

Coil separation = 10 cm
Frequency = 500 c.p.s.

In-phase components, in percent

Out-of-phase components, in percent

Sheet A1, 0.81 cm x 30 cm x 20 cm

Coil separation = 10 cm
I Block lead 5.1 cm x 10.2 cm x 20.3 cm
Coil separation 5 cm x 10.2 cm x 20.3 cm
Frequency = 500 c.p.s.
Figure 6.9: Slingram coils, vertical and coaxial.

Mid Tensile Block Al, 15.4 cm long.

Coil separation = 10 cm
Frequency = 500 c.p.s.

IN-PHASE COMPONENTS, IN PERCENT

OUT-OF-PHASE COMPONENTS, IN PERCENT
OUT-OF-PHASE COMPONENTS IN PERCENT

IN-PHASE COMPONENTS, IN PERCENT

FIGURE 7: SLINGRAM COILS VERTICAL AND COPLANAR

Sheet Al, 0.81 cm x 20 cm x 30 cm

Coil separation = 10 cm
Frequency = 500 c.p.s.
Figure 74 Transmitt ing loop traverse. Frequency = 500 c.p.s.

DISTANCE FROM EDGE OF TRANSMITTING LOOP

OUT-OF-PHASE COMPONENTS IN PERCENT

IN-PHASE COMPONENTS IN PERCENT

COILS HORIZONTAL 100 CM

I Sheet Al 0.81cm x 20cm x 30cm

47759
FIGURE 30
TURAN
COILS
HORIZONTAL

CM 20  25  30  35  40  45  50 CM
DISTANCE FROM EDGE OF TRANSMITTING LOOP

2cm x 2cm
square loop

4cm x 20cm x 50cm box filled with powdered magnetite

h=3 cm box vertical
h=6 cm box vertical
h=6 cm box dipping 70°