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Program MQLVTHXYZ:  
Computer inversion of three-component, time-domain,  
magnetic-field sounding data  
generated using an electric wire source

by

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DISCLAIMER.

This program was written in Fortran IV for a Honeywell Multics 68/80 system\*. Although program tests have been made, no guarantee (expressed or implied) is made by the author regarding accuracy or proper functioning of this program on all computer systems.

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\* Brand or manufacturers' names used in this report are for descriptive purposes only and do not constitute endorsement by the U.S. Geological Survey.

By James P. Kauahikaua

## INTRODUCTION.

Program MQLVTHXYZ is a general purpose program for inversion of time-domain electromagnetic (TDEM) sounding data when a grounded electric wire source is employed. Details of the actual computations are given in other papers (Anderson, 1974, 1975, 1977, 1979a; Kauahikaua and Anderson, 1977; Kauahikaua, 1978). An IMSL (International Mathematical and Statistical Library, 1977) derivative-free Levenburg-Marquardt (Brown-Dennis, 1972) nonlinear least squares subprogram (ZXSSQ) is used for inversion of the TDEM sounding data. See appendix 2 notes for conversion to other computer systems where the IMSL library may not be available.

The following program options are currently available:

- (1) Simultaneous (or Joint) inversion of three components of TDEM data and/or Schlumberger apparent resistivity sounding data.
- (2) Scaling parameter and observation spaces to constrain the solution space and to reduce round-off effects.
- (3) Weighted observations.
- (4) Holding certain parameters fixed (constrained).
- (5) Object-time format control for reading the observed data matrix.
- (6) An infinitesimal- or finite-length wire source may be modelled.
- (7) The impulse or step response may be modelled (Kauahikaua and Anderson, 1977). (1)
- (8) A nonincreasing frequency function may be convolved with the model to simulate an arbitrary source function or filtering in the receiver.
- (9) Amplitude shift parameters may be used to automatically

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(1) The terms "impulse" and "step" response refer to the manner in which the wire source is energized and the resulting magnetic fields are measured. If the wire is driven with a spike current (instantly on and off), then the EM fields observed are impulse responses. On the other hand, if the wire is driven with a step current (on at zero time and kept on), then the EM fields observed are step responses. These two are the most commonly used source current waveforms. If the magnetic field TDEM data are measured with a wire loop, then the data are actually the time-derivatives of the actual fields. In this case, an impulse response would be measured for a source wire energized with a current step because the time-derivative of a step response is an impulse response. Modification of the program to accommodate other current source waveforms can be done using the user-defined function FLT which is controlled by \$init parameters ifltx, ifly, and ifltz.

- scale the models to match the data magnitudes.
- (10) Orientation parameters may be used to automatically rotate the models for discrepancies in orientation of the measurement axes with respect to the wire.

Much of the form and wording of this report has been adopted from a series of recent USGS Open-File Reports by Anderson (1979b, for example) to provide as much timely program information as possible in a fairly standardized format. These reports have no mathematical formulation section, but the interested reader may consult the cited references for more information on the mathematics.

## PARAMETERS AND DATA REQUIRED.

Parameters that are required by program MQLVTHXYZ are read using Fortran namelist read statements with specific names: \$parms and \$init. Default values are used whenever a corresponding parameter is omitted in a namelist. The input data matrix is read from an optional alternate file (unless overridden) using a Fortran object-time format. Preceding the \$parms statement is a required 80 (or less) character title.

The general input order read by program MQLVTHXYZ is:

1. Title line (always required, max. 80 characters).
2. \$parms --non-default parameters--\$  
(note \$parms may begin in col. 1 on Multics).
3. (Object-time format) statement defining the given format of the input data matrix. The object format begins with "(" placed in col. 1 and ends with ")" before col. 73.
4. Optionally, the data matrix read under the object format may be inserted here if the alternate data file is not used (see parameter ialt below).
5. \$init --non-default parameters--\$
6. Optionally, subsequent runs using the same data matrix but with changed \$parms and \$init parameters may be made by repeating steps 1,2,3, and 5 (provided parameters istop=0 and ialt is not 5).

The above general input order is required whether the job is being run in time-sharing or batch modes (see job operating instructions below).

## PROGRAM FILES.

- |        |  |
|--------|--|
| file05 | title, input parameters \$parms, object format (for reading data matrix on unit ialt=10--default), and \$init parameters.  |
| file06 | output on-line printer file (see file16 for more detail output).   |
| file10 | default input data matrix file read under the object format given in file05. Parameter ialt=10 (default) may be changed to any file number other than 06,13, or 16. Note ialt=05 will mean the data matrix is included immediately after the object-time format on file05. |
| file13 | output scratch disk file used as required during execution of MQLVTHXYZ.   |
| file16 | output master print-type disk file--contains complete printable output.  |

DETAIL PARAMETER AND DATA DEFINITIONS.

\$parms parameters (with defaults and cross-references):

[names below prefixed with a "\*" are not used by MQLVTHXYZ, but are included for conversion compatibility if the CALL IMSLMQ is replaced by CALL MARQRT (see appendix 2 paragraph 6 on this type of conversion)]

n=            Number of observed data points  $y(i), i=1, \dots, n$ , where  $n \leq 200$ .

k=            Total number of parameters ( $1 \leq k \leq 20, k \leq n$ ). The value of k must be equal to  $2*mm$  if \$init parameter iob=1,2,3, equal to  $2*mm+2$  if iob=4, and equal to  $2*mm+5$  if iob=5, where \$init parameter  $mm > 0$  is the number of layers in the model and iob is the observation type of the data.  
(cref: \$init parameter mm, iob and \$parms n, b).

if=           Number of omitted parameters; i.e., number of parameters held fixed or constrained via array ib() to initial input values given in array b(). Default if=0 with the restrictions that  $if \leq k$  and  $n \geq k - if$ .  
(cref: \$parms k, n, ib(), and b).

m=            Number of independent variables ( $m \leq 2$ ) given in the data matrix  $(y(i), x(i, j), j=1, m), i=1, n$ . The value of m must be given as follows:  
= 1 when \$init parameter iob  $\leq 3$  (defines specific observation type in  $y(i)$ );  
= 2 when \$init parameter iob=4,5 (defines mixed observation types in  $y(i)$  via  $x(i, 2)$ ).  
(cref: \$parms iwt, \$init iob, and DATA MATRIX NOTES below for all definitions of  $x(i, m)$  used).

ialt=          Input data matrix alternate logical unit number (default 10) for reading the data under the object-time format specified in file05. The value of ialt can be any value the operating system supports, but cannot be equal to 6, 13, or 16. If ialt=5 is used, then the data matrix  $((y(i), x(i, j), j=1, m), i=1, n)$  will immediately follow the object format on file05.  
(cref: \$parms n, m, \$init iob).

istop= 0 to continue processing after completion of the current problem (i.e., a total restart) with the same data matrix as last used, but by using a revised title, \$parms, object-time format, and \$init parameters. Note that istop=0 can only be

used whenever ialt is not 5 (since file ialt is rewound and read again). Also, all \$parms and \$init parameters previously used will be assumed, with the exception of array b(J) which must always be given.

= 1 (default) to stop the run after completion of the current problem.  
(cref: \$parms b,ialt).

iwt= 0 (default) for unweighted observations; i.e., all n observations  $y(i), i=1, \dots, n$  will be weighted unity (with assumed standard deviations equal to 1.0).  
= 1 for weighted observations given by the formula  $wt(i)=1.0/x(i,m+1)**2$ , where  $x(i,m+1)$  is the standard deviation augmented to the data matrix for the given  $m \leq 2$ . Note: to avoid division by zero,  $wt(i)=1.0$  is stored automatically if  $iwt=0$  or when  $iwt=1$  and  $x(i,m+1)=0.0$ .  
(cref: \$parms n,m, \$init iob, and DATA MATRIX NOTES).

\* ider= 0 (default) to use analytic derivatives, which calls both forward problem (fcode) and analytic derivative (rcode) subroutines.  
= 1 to use estimated derivatives, which calls only subroutine fcode. [if converting to subprogram MARQRT (as in appendix 2), then ider=1 must always be used, since rcode is a dummy routine].  
(cref: \$parms del).

iprt= 0 (default) for standard abbreviated printout format for each iteration. Note scaled values of parameters b(J) and phi (sum of squares) will be given via parameter scales.  
= 1 for detail printout format for each iteration, which includes the parameter changes from the Marquardt algorithm. [note iprt=1 behaves like iprt=-2, unless converting to subprogram MARQRT].  
= -1 (recommended if scales>0 used) for abbreviated printout format for each iteration with printed unscaled values of b(J) but scaled values of phi.  
= -2 same as iprt=-1 but also prints on file06 n-observational lines containing: observed value (obs=y(i)), calculated value (cal), residual (res), and x(i,1). Note file16 will always contain the complete obs-cal-res and x(i,m) data printout. Option iprt=-2 may be useful for time-sharing runs to examine on-line the final solution and residuals.  
(cref: \$parms iout,sp and DATA MATRIX NOTES).



- \* niter= Maximum number of iterations allowed before accepting the results as "forced off" (default niter=10). Four different types of convergence tests are possible one of which is termed "forced off", which will occur whenever niter has been reached and one of the other convergence criteria has not been achieved. Using a small niter may be useful to monitor the progress for a large problem, and as an aid for achieving a convenient restarting procedure with the last b-vector as a new initial estimate.  
(cref: \$parms b and Marquardt (1963) for convergence tests used).
- \* inon= 1 (default) to omit nonlinear confidence region calculations.  
= 0 to compute nonlinear confidence regions after the last iteration. This option calls subroutine fcode many times, and is not recommended for general use with program MQLVTHXYZ unless one is interested in a detailed nonlinear statistical analysis of the final solution.  
(see IBM Share Program No. 1428 for more details on this option).
- \* ff= Variance F-ratio statistic (default 4.0) used to compute linear support-plane confidence limits and nonlinear (if inon=0) confidence limits after convergence or niter iterations. The default value is adequate for most applications.
- \* t= Student's t-statistic (default 2.0) used to compute one-parameter linear confidence limits after convergence or niter iterations. The default value is adequate for most applications.
- \* e= Convergence criterion test parameter (default 0.5e-4). For example, for 2-figure accuracy, use e=.01; for 3-figure accuracy, use e=.001, etc. [for MQLVTHXYZ, e is equivalent to \$parms eps (see below)].  
(cref: Marquardt, 1963).
- \* tau= Convergence criterion test parameter (default 1e-3).  
(cref: Marquardt, 1963).
- \* xl= Initial Marquardt's lambda factor (default .01) to be added to the diagonal of the Jacobian transpose times Jacobian matrix. For some very ill-conditioned problems, or for poor initial parameter estimates, a larger xl (e.g., 1.0) may

prove to be advantageous.  
(cref: Marquardt, 1963 and IBM Share Program No. 1428).

\* modlam= 1 (default) to use a modified Marquardt lambda method at each iteration as described in Tabata and Ito (1973).  
= 0 to use the original Marquardt (1963) lambda method at each iteration.

\* samcr= Marquardt's critical angle between the gradient and adjustment vectors (default 45.0 degrees). The value of samcr should not be set greater than 90 degrees. The default value is usually adequate for most applications.  
(cref: Marquardt, 1963).

\* del= Factor used in finite-difference equations (default 1e-5). Note del is used only when ider=1 for estimated partial derivative calculations.  
(cref: \$parms ider).

\* zeta= Singularity criterion for matrix inversion (default 1e-31), which may be selected greater than or equal to the machine smallest exponent range.

\* iout= Printout file06 and file16 control.  
= 1 (default) for printable output to both file06 and file16.  
= 0 for print output only on file06.  
Note: file16 output may be useful for deferred output when running the job from a time-sharing terminal; also, file16 may be used as an input file for other processing programs (e.g., plot routines). In this version of the program, output to file06 has been purposely reduced to take less time to printout on a time-sharing terminal; however, for iout=1 (default), a complete printable output is always given on file16.  
(cref: \$parms iert).

sp= scaler (equivalent names) is a parameter scaling option.  
= 0 (default) to ignore parameter scaling (i.e., to use unscaled parameters).  
= 1 (recommended for program MQLVTHXYZ) to scale parameters  $b(J)$  using  $\ln(b(J))$ , provided the initial  $b(J) > 0$  for all  $J=1,2,\dots,k$ . Note scaler=1 will automatically constrain the final solution space such that  $b(J) > 0$  for all  $J$  in  $(1,k)$ .  
= 2 to scale parameters  $b(J)$  using  $\operatorname{arcsinh}(b(J))$ .

This option allows for log-type parameter scaling whenever  $b(j)$  is positive or negative for any  $j$  in  $(1,k)$ . However, for program MQLVTHXYZ (\$init parameter iob $\leq$ 4), the initial parameters  $b(j)>0$  must be given; hence  $sp=2$  should not be used ( $sp=2$  is defined here for the case where \$init iob=5 or for possible use in other applications).  
(cref: \$parms b,k).

\* sy=        scaley (equivalent names) is an observation scaling option.  
= 0 (default) to ignore observation scaling (i.e., to use unscaled observations  $y(i)$ ).  
= 1 to scale observations  $y(i)$  using  $\ln(y(i))$ , provided  $y(i)>0$  for all  $i=1,2,\dots,n$ .  
= 2 to scale observations  $y(i)$  using  $\operatorname{arcsinh}(y(i))$ . This option allows for log-type observation scaling whenever  $y(i)$  is positive, negative, or zero for any  $i$  in  $(1,n)$ .  
(cref: \$init iob, \$parms n and DATA MATRIX NOTES)

b()=        Array of initial guesses for all k-parameters. These values must be supplied greater than zero for program MQLVTHXYZ (i.e., positive conductivities and thicknesses), unless \$init parameter iob=5. The default values are set to  $b(j)=0$  for all  $j=1$  to  $k$ , and would result in an error condition if any  $b(j)$  was not supplied greater than zero.

For iob $\leq$ 3, the parameter order must be given as:

$b(1)$  is the amplitude shift parameter,

$b(2), b(3), \dots, b(mm+1)$  are the  $mm$  layer conductivities (in mhos/meter), and

$b(mm+2), b(mm+3), \dots, b(2*mm)$  are the  $mm-1$  layer thicknesses (in meters).

For iob=4, the parameter order must be given as:

$b(1), b(2), b(3)$  are the x-, y-, and z-component amplitude shift parameters, respectively (any unused ones should be constrained via \$parms parameters ip and ib()),

$b(4), b(5), \dots, b(mm+3)$  are the  $mm$  layer conductivities (in mhos/meter), and

$b(mm+4), b(mm+5), \dots, b(2*mm+2)$  are the  $mm-1$  layer thicknesses, in meters.

For `iob=5`, the parameter order must be given as:

`b(1),b(2),b(3)` are the x-, y-, and z-component amplitude shift parameters, respectively (any unused ones should be constrained via `$parms` parameters `ip` and `ib()`),

`b(4),b(5),b(6)` are the orientation parameters, angles `theta`, `phi`, and `omega`, where  

$$z_{new} = z \cos(\theta) + \sin(\theta) * (x \cos(\phi) + y \sin(\phi))$$
  

$$x_{new} = x \cos(\omega) + y \sin(\omega)$$
  

$$y_{new} = y \cos(\omega) - x \sin(\omega)$$
  
 where `xprime` and `yprime` are defined by  

$$x_{prime} = x \cos(\theta) + \sin(\theta) * (y \sin(\phi) - z \cos(\phi))$$
  

$$y_{prime} = y \cos(\theta) - \sin(\theta) * (x \sin(\phi) + z \cos(\phi))$$

`b(7),b(8),...,b(mm+6)` are the `mm` layer conductivities (in mhos/meter), and

`b(mm+7),b(mm+8),...,b(2*mm+5)` are the `mm-1` layer thicknesses in meters.  
 (cref: `$parms k,ip,ib` and `$init mm,iob`).

`ib()`= Array of `ip`-indices (in any order) corresponding to any `b()` parameter to hold fixed to its input value. e.g., `ip=2,ib(1)=3,ib(2)=5` will hold fixed `b(3), b(5)` in the least squares. If `ip=0` (default), leave out array `ib` in the namelist.  
 (cref: `$parms ip,b`).

[the following `$parms` are parameters used only by IMSL subprogram `ZXSSQ`, and cannot be used if converting to subprogram `MARQRT` as described in appendix 2].

`iopt`= 1 (default) implies strict descent of the sum of squares is desired in the derivative-free Marquardt algorithm (`ZXSSQ`), with default values used in the input array `parm()`.  
 = 0 implies strict descent is not necessary (i.e., the "best" or optimum Marquardt parameter used may not yield a strict decreasing sum of squares at each iteration).  
 = 2 implies strict descent is desired with user parameter choices as given (or assumed) in input array `parm()`.  
 (cref: `$parms parm()`).

`parm()`= Array of length 4 required only when `iopt=2`. The default is `parm(=.01,2.,120.,.1)`, where each

element is defined by the corresponding index as follows:

- i=1, the initial value of the Marquardt parameter used to scale the diagonal of the approximate Hessian matrix,  $xJtJ$ , by the factor  $(1.0+\text{parm}(1))$ . A small value gives a Newton step, while a large value gives a steepest descent step. (default  $\text{parm}(1)=.01$ ).
- i=2, the scaling factor used to modify the Marquardt parameter, which is decreased by  $\text{parm}(2)$  after an immediately successful descent direction, and increased by the square of  $\text{parm}(2)$  if not. (default  $\text{parm}(2)=2$  where  $\text{parm}(2)>1$  must be used).
- i=3, an upper bound for increasing the Marquardt parameter. The search for a descent point is abandoned if  $\text{parm}(3)$  is exceeded.  $\text{parm}(3)>100$  is recommended. (default  $\text{parm}(3)=120$ ).
- i=4, value for indicating when central rather than forward differencing is to be used for calculating the Jacobian (partial derivatives). The switch is made when the norm of the gradient of the sum of squares function becomes smaller than  $\text{parm}(4)$ . Central differencing is good in the vicinity of the solution, so  $\text{parm}(4)$  should be small. (default  $\text{parm}(4)=.1$ ).  
(cref: \$parms ioft).

nsis= The first convergence criterion. Convergence is satisfied if on 2 successive iterations, the parameter estimates agree, component by component, to nsis digits. (default  $\text{nsis}=3$ ; using  $\text{nsis}>5$  may not converge since single precision is used).

eps= The second convergence criterion. Convergence is satisfied if on 2 successive iterations the residual sum of squares estimates have relative differences  $\leq \text{eps}$ . (default  $\text{eps}=0.0$ ).  
(cref: \$parms e, which is equivalent to eps).

delta= The third convergence criterion. Convergence is satisfied if the Euclidean norm of the approximate gradient is  $\leq \text{delta}$ . (default  $\text{delta}=0.0$ ).

Note: The Marquardt iteration is terminated, and convergence is considered achieved, if any one of the three convergence conditions (nsis, eps, or delta) is satisfied.

maxfn= The maximum number of function evaluations (i.e., calls to subroutine FUNC in ZXSSQ) allowed. The actual number of calls to FUNC may exceed maxfn

slightly. Note: unless  $\text{maxfn} > 0$  is given,  $\text{maxfn} = 2 * k * \text{niter}$  is used as the default value.  
(cref: \$parms k, niter, where default niter=10).

\$end [end of \$parms namelist]

\$init Parameters (with defaults and cross-references):

iob= observation-type defined for  $y(i)$ :  
= 1 defines  $y(i)$  as x-component magnetic field TDEM data, in amps/m (parallel to wire source).  
= 2 defines  $y(i)$  as y-component magnetic field TDEM data, in amps/m (perpendicular to the wire source).  
= 3 defines  $y(i)$  as z-component magnetic field TDEM data, in amps/m (vertical).  
(note: for  $\text{iob} \leq 3$ ,  $m=1$  must also be given in \$parms).  
= 4 defines mixed observation-type soundings where the i-th observation type is given by  $x(i,2)=1.0$  for x-component,  $=2.0$  for y-component,  $=3.0$  for z-component, and  $=4.0$  for Schlumberger apparent resistivities.  
= 5 behaves like  $\text{iob}=4$  except that the orientation parameters may be used. It is advisable to use the  $\text{iob}=5$  option only after the best solution has been obtained with the appropriate  $\text{iob} \leq 4$ . Then when the  $\text{iob}=5$  run is made, \$parms sp should be set to zero to allow the angles to be positive or negative.  
(note: for  $\text{iob}=4,5$ ,  $m=2$  must also be given in \$parms).  
(cref: \$parms m, b(), \$init mm, and DATA MATRIX NOTES).  
  
mm= number of layers in the model ( $1 \leq \text{mm} \leq 10$ ; default  $\text{mm}=1$ ).  
Note: make sure \$parms  $k=2 * \text{mm}$  for  $\text{iob} \leq 3$ ,  $k=2 * \text{mm} + 2$  for  $\text{iob}=4$ , and  $k=2 * \text{mm} + 5$  for  $\text{iob}=5$ .  
(cref: \$parms k, b(), \$init iob).  
  
ister= selects which of the source current waveforms is to be used.  
= 0 (default) for the impulse response.  
= 1 for the step response.  
  
method= selects the numerical technique for computing the step response (only used if \$init ister=1).  
= 1 computed as the integral from 0 to t of the impulse response (see Kaahikaua and Anderson,

1977).

= 2 (default) computed as the transform of the field frequency response divided by the frequency.

ifltx= filter option parameter for the x-component computations (default ifltx=0). If ifltx is different from zero, the magnetic field TDEM response will be computed as the transform of the x-component frequency response multiplied by a user-defined complex function FLT(IFLTx,F) where F is the frequency in Hertz. For multicomponent inversion (\$init iob=4,5), ifltx may be used to differentiate between a call to FLT(IFLTx,F) and either FLT(IFLTy,F) or FLT(IFLTz,F) if desired, simply by including the appropriate FORTRAN statements in the user-written COMPLEX FUNCTION FLT. See example routine FLT listed in appendix 1.

iflty= similar to ifltx except for the y-component (default iflty=0).

ifltz= similar to ifltx except for the z-component (default ifltz=0).

x= x-coordinate of observation position assuming that the wire source is centered at the origin and oriented along the x-axis ( $x \geq 0$ , observation position cannot be along the source-wire).

y= y-coordinate of observation position assuming that the wire source is centered at the origin and oriented along the x-axis ( $y \geq 0$ , observation position cannot be along the source-wire).

ci= current in the source wire in amps (default ci=1).

sl= total length of the source wire in meters (default sl=1). The type of wire source used in the calculations is defined by \$init parameter icase. (cref: \$init icase).

blwr= lower normalized frequency used to compute the field frequency response before the transformation to the time domain (default blwr=.005).

bufr= upper normalized frequency used to compute the field frequency response before the transformation to the time domain (default bufr=10000).

tol= relative error desired for all Hankel, cosine, and sine transform calculations (default tol=1.e-4).

nf= number of frequencies per decade at which to compute the magnetic field frequency response between \$init blwr and buwr (default nf=12). It is recommended that preliminary inversions be done with nf=4 or 5 and the final one be done with nf=12 to insure sufficient accuracy in the final result without using more computer time than is necessary.  
(cref: \$init blwr, buwr).

icase= selects whether an infinitesimal or finite-length wire source model is to be used.  
= 1 (default) infinitesimal wire source (horizontal electric dipole).  
= 2 finite-length wire source, with wire length specified in \$init parameter sl.  
(cref: \$init sl).

cnctol= relative error desired for adaptive integration in finite-length wire model calculation (default cnctol=1.e-5).  
(cref: \$init icase, intype).

mev= maximum number of function evaluations to be allowed for the finite-length wire integration (default mev=300). Setting \$init cnctol to a value smaller than the default may require mev to be set to a number larger than 300.  
(cref: \$init cnctol, intype).

intype= type of integration algorithm (subprogram cnc4) and convergence test desired for finite-length wire integration.  
=1,2,3 uses Newton-Cotes no. 4 quadrature:  
= 1 for absolute error test (not generally recommended),  
= 2 for "1-one" type error test,  
= 3 for "1-infinity" type error test,  
  
= 4 (default) for relative error test using adaptive Gaussian quadrature, and  
= 5 for relative error test using non-adaptive Gaussian quadrature.  
Note: The selected intype convergence test must be satisfied by both the real and the imaginary parts of the complex integral simultaneously.  
(cref: \$init cnctol).

nrun= number of spline nodes to be calculated per digital filter interval for the finite-length wire integration (default nrun=1). Increasing nrun from 1 to 2 roughly doubles the execution time of



MQLVTHXYZ, but yields more accurate field value and is recommended for soundings made close to a long wire.

\$end [end of \$init parameters]

#### DATA MATRIX NOTES.

The data matrix is defined as the sequence of ordered rows:  $(y(i), x(i, j), j=1, m^*)$ , where  $i$ =row number  $1, 2, \dots, n$ , and  $m^*=m+1$  if  $iwt=1$ , otherwise  $m^*=m \leq 2$ . The data matrix is read on logical unit  $ialt$  (default 10) using an object-time format statement (see any Fortran manual). The number of items read depends on \$parms  $m, iwt$  and \$init  $iob$  as previously defined. The various data matrix options are summarized as follows:

- (a) Specific observation component, TDEM soundings ( $iob \leq 3$ ,  $m=1$ , and max. 3 items per record):
  - 1.  $y(i)$  =  $i$ -th observation, where \$init  $iob \leq 3$  defines the particular component.
  - 2.  $x(i, 1)$  =  $i$ -th time ( $x(i, 1) > 0.0$  seconds).
  - 3.  $x(i, 2)$  = standard deviation of observation  $i$  (include only if  $iwt=1$ ).
- (b) Mixed observation types:  $x$ -,  $y$ -, or  $z$ -component TDEM soundings and/or Schlumberger soundings data ( $iob=4$  or  $5$ ,  $m=2$ , and max. 4 items per record):
  - 1.  $y(i)$  =  $i$ -th observation (where actual type is defined by  $x(i, 2)$ ).
  - 2.  $x(i, 1)$  =  $i$ -th time ( $x(i, 1) > 0.0$  seconds) if  $x(i, 2) \leq 3.0$  or corresponding AB/2 for  $x(i, 2)=4.0$  ( $x(i, 1) > 0.0$  meters).
  - 3.  $x(i, 2)$  = observation type in  $y(i)$ ; use  $x(i, 2) = 1.0$  for  $x$ -component TDEM data,  $=2.0$  for  $y$ -component TDEM data,  $=3.0$  for  $z$ -component TDEM data, or  $=4.0$  for Schlumberger apparent resistivity data.
  - 4.  $x(i, 3)$  = standard deviation of observation  $i$  (include only if  $iwt=1$ ). Note: for joint inversion of Schlumberger apparent resistivity and TDEM data, a weighted least squares should be used ( $iwt=1$  option) to produce residuals of near-equal magnitude.

# EXAMPLES OF INPUT PARAMETERS AND DATA ORDERING.

1. Vertical magnetic field TDEM soundings (default iob=3, ister=0):

```
example 1.
$parms n=60,k=6,m=1,iprt=-1,sp=1,ialt=5,
b=1e0,.01,.2,.01,100,200$
(2e14.5)
    0.20961e-08    0.55166e-02
    0.69697e-08    0.18316e-01
--(etc. for 58 more observations)--
$init mm=3,y=1500,icase=1$
```

2. Mixed observation types (iob=4), y-component TDEM (step response) and Schlumberger soundings data, and weighted observations (iwt=1):

```
example 2
$parms n=100,k=8,m=2,iprt=-2,sp=1,iwt=1,ialt=5,ip=2,ib=1,3,
b=1e0,1e9,1e0,.01,.2,.01,100,200$
(4f10.0)
20.1      .05      2.      .05
29.87     .06      2.      .05
--(etc. for rest of TDEM soundings data)--
108.      10.      4.      5.
120.      13.      4.      5.
--(etc. for rest of Schlumberger soundings data)--
$init mm=3,iob=4,icase=1,ister=1,y=1000$
```

3. Vertical magnetic field TDEM soundings (default ister=0), orientation option desired:

```
example 3
$parms n=60,k=9,m=1,iprt=-1,sp=0,ialt=5,ip=2,ib=1,2,
b=1e0,1e0,1e0,1e-6,1e-6,1e-6,.01,.2,.01,100,200$
(2e14.5)
    0.20961e-08    0.55166e-02
    0.69697e-08    0.18316e-01
--(etc. for 58 more observations)--
$init mm=3,y=1500,icase=1,iob=5$
```

## SPECIAL OBJECT FORMAT PHRASES.

If an existing data matrix file does not have the properly defined column ordering in the form (y(i),x(i,j),j=1,m)), then the Fortran "tn" format phrase may be used to begin at any column n in the data record. For example, the format (t41,f10.0,t1,3f10.0) will select y(i) using col.41-50 and x(i,1) beginning at col.1.

### MULTICS OPERATING INSTRUCTIONS.

1. Initially, one should add the following libraries (via the command "asr") to his search rules on the Denver Multics system after the working directory:  
>add>Emodl\_iny>JKauhikaua>exec\_sess,  
>add>Emodl\_iny>WAnderson>lib\_em,  
>add>Emodl\_iny>WAnderson>lib\_l, and >iml>imsl.
2. Either attach "file05" to a predetermined ascii (stream) parameter file, or let file05 default to "user\_input" (i.e., the user's terminal). The order of parameters and data on file05 must be given as defined in the section PARAMETERS AND DATA REQUIRED above. To attach file05, type:  
io attach file05 vfile\_ parameter\_file\_name
3. Attach "file10" to an input data matrix ascii file if ialt=10 (default) is used. If ialt=5 is selected, then ignore this step, but include the data matrix following the object-time format on "file05"--see examples 1 and 2 above. In practice, it is usually best to use distinct files file05 and file10 for parameters and data respectively. To attach file10, type:  
io attach file10 vfile\_ data\_file\_name
4. Set the underflow condition handler off by typing:  
set\_lufl -off
5. Execute Program MQLVTHXYZ by typing: mqlvthxyz

If file05 was not attached, then the user must anticipate the required title, \$parms, object format, and \$init to be typed on "user\_input". Prompt messages are not printed on the terminal.

Note "file16" is the complete print file (normally disk on Multics), and "file06" is always the on-line terminal print file. File16 should either be deleted or derprinted to a line-printer after running program MQLVTHXYZ. Also, file13 (if used) should be deleted after running the program. To submit the job as a batch job (called absentee on Multics), prepare step 1-5 above in a segment with .absin suffix and use the "enter\_abs\_request" command.

### ERROR MESSAGES.

Most parameter and/or data errors are noted by self-explanatory messages appearing in the printed file(s), and the job is terminated. For example, the message

"error--some \$parms out of range" means that a violation (or omission) of a required parameter range has been committed in the \$parms namelist. Check all \$parms values, correct, and resubmit the job.

Exponent underflow may occur when the argument is less than  $10^{*-38}$  on Multics; this is not fatal since 0.0 replaces all underflows. To suppress the underflow messages, the command "set\_ufl -off" can be used prior to executing MQLVTHXYZ.

Exponent overflow and/or arithmetic overflow messages will terminate the run under Multics control. An overflow condition usually means a very poor initial parameter estimate was given in array b() for the model (mm) chosen. First check that all \$parms, \$init, data matrix values, and object-time format are correct. If no errors are found, then try to revise the model (mm) and/or use better guessed estimates for the starting parameters in array b().

If any parameter begins to approach zero or become unbounded during the least squares iterations, then one may fix (constrain) the parameter to a reasonable value, and restart the program to obtain a constrained least squares solution. This is usually required when the data are not sufficient to resolve all the parameters for the model mm chosen.

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Appendix 1.-- Source listing

The attached subprograms are listed with beginnings line numbers in the following order:

C*****	PROGRAM MQLVTHXYZ	*****	00000010
	SUBROUTINE ETHXYZ(Y,X,B,K,NN,TITLE,IOUT)		00000150
	SUBROUTINE ITHXYZ(DV,XM,B,PRNT,NPRNT,N,TITLE,IOUT)		00000670
	SUBROUTINE FCODE(DV,XM,BPARMS,PRNT,F,IF,IDER)		00003050
	SUBROUTINE HXYZ(B2,HX,MY,HZ,I0B)		00005300
	COMPLEX FUNCTION FLT(IFLAG,F)		00006060
	SUBROUTINE TRNSI(FUNC,TMAX,TMIN,NT,T,U,MTD)		00006250
	SUBROUTINE SCHSDG(SIG1,XMAX,XMIN,AB2,RH0A,NRHO,TOL)		00006700
	REAL FUNCTION SPLINT(T,A,B,C,N,X,Y)		00007090
	COMPLEX FUNCTION DCKERN(AMBDA)		00007260
	COMPLEX FUNCTION CSPLN(RT)		00007750
	COMPLEX FUNCTION FINHX(B)		00008130
	COMPLEX FUNCTION FINHY(B)		00008390
	COMPLEX FUNCTION FINHZ(B)		00008800
	COMPLEX FUNCTION F3(G)		00008930
	COMPLEX FUNCTION F4(G)		00009010
	SUBROUTINE RECURS(G,V1,F1)		00009090
	SUBROUTINE FINF3(B1,B2,F31,F32)		00009350
	COMPLEX FUNCTION FINITE(FUNC,BFIN)		00009460
	COMPLEX FUNCTION ZHY(B,NEW,R)		00010440
	COMPLEX FUNCTION ZHZ(B,NEW,R)		00010620
	COMPLEX FUNCTION FUNINT(X)		00010770
	COMPLEX FUNCTION I1K1(B8)		00010930
	SUBROUTINE SPLIN1(M,H,X,Y,A,B,C,IT,D,P,S)		00011230
	COMPLEX FUNCTION ZLAGH0(X,FUN,TOL,L,NEW)		00012430
	COMPLEX FUNCTION ZLAGH1(X,FUN,TOL,L,NEW)		00014670
	COMPLEX FUNCTION ZLAGF0(X,FUN,TOL,L,NEW)		00017030
	COMPLEX FUNCTION ZLAGF1(X,FUN,TOL,L,NEW)		00019500
	SUBROUTINE IKS(B8,I1K1,IKDIF)		00021940
	SUBROUTINE KELVIN(X,M,B)		00022580
	SUBROUTINE QUINT(NY,Y,B,C,D,E,F)		00024380
	SUBROUTINE QPOINT(NY,Y,B,C,D,E,F,X1,DELX,XX,YY)		00025150
	COMPLEX FUNCTION CANC4(A1,B1,EP,M,N,FUN,MF,ESUM)		00025340
	SUBROUTINE CQUAD(A,B,RESULT,K,EPSIL,NPTS,ICHECK,F,MEV)		00026910
	COMPLEX FUNCTION CQSUB(A,B,EPSIL,NPTS,ICHECK,RELERR,F,MEV)		00030430
	COMPLEX FUNCTION CQSUBA(A,B,EPSIL,NPTS,ICHECK,RELERR,F,MEV)		00031960
	SUBROUTINE IMSLMQ(SUBZ,SUBEND)		00033370
	SUBROUTINE FFXSSQ(C,N,KIP,F)		00036580
	SUBROUTINE LNXSSQ(C,N,KIP,F)		00036910
	SUBROUTINE SAVER(I,J)		00037040
	COMPLEX FUNCTION ZHANKS(N,B,FUN,TOL,NF,NEW)		00037230
	SUBROUTINE ERRMSG(MSG,M5,I6,I9)		00040650
	SUBROUTINE WARN(MSG,M5,I6,I9,*)		00040880

### Source Availability

The current version of the source code may be obtained by writing directly to the author. A magnetic tape copy of the source code will be sent to requestors to be copied and returned to the author. This method of releasing the program was selected in order to satisfy requests for the latest updated version. The magnetic tape will be recorded in the following mode (unless otherwise requested):

Industry compatible: 9-track, unlabeled, EBCDIC mode, odd-parity, 800 bpi density, 80-character records (unblocked card images), and contained on one file.

Note: The source code for all IMSL Library routines used (ZXSSQ, LEQT1P, LUDECP, LUELMP, LINV1P, and UERTST) are only available from International Mathematical and Statistical Libraries (1977), whose address is given in the references.

### Copyright Notices

- (1). Subprogram QUINT was converted from ALGOL to FORTRAN as published by Herriot and Reinsch (1976): Copyright 1976, Association for Computing Machinery, Inc.; permission to republish, all or in part, granted by ACM. ALGOL to FORTRAN conversion was done by Walt Anderson, USGS.
- (2). Subprograms CQUAD, CQSUB, and CQSUBA are modified versions of subprograms QUAD, QSUB, and QSUBA, respectively, as published by Patterson (1973): Copyright 1973, Association for Computing Machinery, Inc., permission to republish, all or in part, granted by ACM.

```

***** PROGRAM MQLVTHXYZ *****                                00000010
NONLINEAR LEAST SQUARES INVERSION OF THREE COMPONENT            00000020
MAGNETIC FIELD (TDEM) DATA USING A MODIFIED                   00000030
MARQUARDT-LEVENBURG ALGORITHM (FROM IMSL LIBRARY)              00000040
                                                                    00000050
WRITTEN BY JIM KAUAHIKAU, USGS, DENVER, COLORADO               00000060
LAST MODIFIED: NOVEMBER, 1978                                   00000070
                                                                    00000080
EXTERNAL ITHXYZ,ETHXYZ                                          00000090
CALL INITREF('>UDD>EMODL_INV>JKAUAHIKAU>ARCHIVES','HXYZINV_OLIB',00000100
1 'FCODE')                                                       00000110
CALL IMSLMQ(ITHXYZ,ETHXYZ)                                       00000120
STOP                                                             00000130
END                                                               00000140

                                                                    00000150
SUBROUTINE ETHXYZ(Y,X,B,K,NN,TITLE,IOUT)                        00000160
                                                                    00000170
TERMINATION ROUTINE FOR COMPUTER INVERSION OF                   00000180
THREE-COMPONENT MAGNETIC FIELD TDEM DATA                       00000190
                                                                    00000200
CHARACTER*5 TITLE                                              00000210
DIMENSION Y(1),X(200,5),B(1),TITLE(16)                       00000220
COMMON/CXYZ/A1,A2,J1,J2,JN(3),A6,A7,A8,A9,A10,A11,SCALE,U1,U2,J3, 00000230
$ IOB,NEXTRA,NPARMS,B1,B2,B3,B4,B5,J4,J5,J6                   00000240
DATA DCON/57.295779/                                           00000250
WRITE(6,10) TITLE                                              00000260
IF(IOUT.EQ.1) WRITE(16,10) TITLE                                00000270
10 FORMAT(12H1T H X Y Z--,5X,16A5//)                           00000280
IF(NEXTRA.LT.6) GO TO 100                                       00000290
THETA=B(4)*DCON                                                 00000300
PHI=B(5)*DCON                                                    00000310
OMEGA=B(6)*DCON                                                  00000320
WRITE(6,20) THETA,PHI,OMEGA                                     00000330
IF(IOUT.EQ.1) WRITE(16,20) THETA,PHI,OMEGA                     00000340
20 FORMAT(// " ORIENTATION OF MEASUREMENT AXES WITH RESPECT TO WIRE", 00000350
$ " AXES"/                                                       00000360
$ " SPHERICAL COORDS OF Z MSMT AXIS: THETA=",F10.6," DEGREES"/ 00000370
$ 36X,"PHI=",F10.6," DEGREES"/                                  00000380
$ " ROTATION AROUND Z AXIS: OMEGA=",F10.6," DEGREES"//)        00000390
100 N=1                                                         00000400
IF(IOB.GT.3) N=3                                                00000410
WRITE(6,110) (B(I),I=1,N)                                       00000420
IF(IOUT.EQ.1) WRITE(16,110) (B(I),I=1,N)                       00000430
110 FORMAT(" PRIMARY FIELD FACTORS:", 3E16.8//)                00000440
N=(NPARMS+1)/2                                                  00000450
WRITE(6,130)                                                     00000460
IF(IOUT.EQ.1) WRITE(16,130)                                     00000470
130 FORMAT(28H FINAL UNSCALED PARAMETERS--/                     00000480
$ 32X,11HRESISTIVITY,2X,3HLYR,10X,5HDEPTH/)                   00000490
DO 150 I=1,N                                                    00000500
    RHO=1./B(NEXTRA+I)                                           00000510
    WRITE(6,140) I,B(NEXTRA+I),RHO

```



	IF(IOUT.EQ.1) WRITE(16,140) I,B(NEXTRA+I),RHO	00000520
140	FORMAT(5X,I3,4X,2E16.8)	00000530
150	CONTINUE	00000540
	IF(NPARMS.EQ.1) GO TO 300	00000550
	M2=N+1	00000560
	D=0.0	00000570
	DO 170 I=M2,NPARMS	00000580
	D=D+B(NEXTRA+I)	00000590
	L=I-N	00000600
	WRITE(6,160) I,B(NEXTRA+I),L,D	00000610
	IF(IOUT.EQ.1) WRITE(16,160) I,B(NEXTRA+I),L,D	00000620
160	FORMAT(5X,I3,4X,E16.8,16X,I3,4X,E16.8)	00000630
170	CONTINUE	00000640
300	RETURN	00000650
	END	00000660

SUBROUTINE ITHXYZ(DV,XM,B,FRNT,NFRNT,N,TITLE,IOUT) 00000670

```
INITIALIZATION ROUTINE FOR PROGRAM MQLVTHXYZ 00000690
```

CHARACTER\*5 TITLE 00000710

```
DIMENSION DV(1),XM(200,5),B(1),FRNT(5),TITLE(16),ALPH(3),
```

```
$ PRED(2),DT(50),AV(50) 00000730
```

COMPLEX ESUM 00000740

```
COMMON/MODEL/RK(10),D(9),NLAYER                                00000750
```

COMMON/FARM/ISTEP,XX,YY,RR,S,BNYQ,MM,TOL 00000760

COMMON/FIN/R1,R2,R,SL,SIG1,X,Y 00000770

COMMON/FINERR/HTOL,CNCTOL,INTYPE,NRUN,NEV,MEV,ESUM,LW 00000780

COMMON/DCSAV/ARHO(100),BRHO(100),DRHO(100),AB2(100),RHOA(100),NRHO00000790

```
$ ,ABMAX, AEMIN                                00000800
```

COMMON/CXYZ/FNYQ,SLL,METHOD,NF,NCOMP(3),TOX,TNX,TOY,TNY,TOZ,TNZ, 00000810

1SCALE,BL,BU,ND,IOB,NEXTRA,NPARMS,GX,GY,GZ,GT,XO,IFLTX,IFLTY,IFLTZ 00000820

INPUT PARAMETERS ARE: 00000830

TOL - RELATIVE TOLERANCE USED IN HANKEL 00000850

TRANSFORM CALCULATION 00000860

METHOD - CALCULATE STEP RESPONSE BY 00000870

TIME INTEGRAL OF IMPULSE REPONSE IF METHOD=1 00000880

TRANSFORM OF F(W)/W IF METHOD=2 00000890

```
NF      - CALCULATE TRANSIENT MODEL AND DERIVATIVES      00000900
```

USING FREQUENCY FUNCTION EVALUATED AT NF 00000910

POINTS PER DECADE FREQUENCY. IF NF=0 OR 00000920

NF>12 THE COSINE OR SINE ROUTINE WILL EVALUATE 00000930

THE FREQUENCY FUNCTION DIRECTLY 00000940

CNCTOL - RELATIVE TOLERANCE USED IN FINITE WIRE 00000950

INTEGRATION 00000960

INTYPE - 00000970

DENSITY OF NODES FOR FREQUENCY FUNCTION 00000980

```
SPLINE INTERPOLATION                                00000990
```

```
MEV      - MAXIMUM NUMBER OF FUNCTION EVALUATIONS      00001000
```

BY INTEGRATING ROUTINE 00001010

00001020

EQUIVALENCE (M,MM),(L,ICASE),(BL,BLWR),(BU,BUPR)	00001030
NAMelist/INIT/TOL,METHOD,CNCTOL,INTYPE,NRUN,MEV	00001040
1,NF,ISTEP,X,Y,CI,SL,MM,M,IFLTX,IFLTY,IFLTZ,IOB,L,ICASE,BLWR,BUPR	00001050
C	00001060
C CALL DELETE_EXTERNAL_VARIABLES('SAVEC')	00001070
C	00001080
WRITE(6,100) TITLE	00001090
100 FORMAT(12H1T H X Y Z--,5X,16A5/)	00001100
IF(IOUT.EQ.1) WRITE(16,100) TITLE	00001110
C--SET DEFAULTS	00001120
M=1	00001130
ND=N	00001140
L=1	00001150
BLWR=-1E0	00001160
BUPR=-1E0	00001170
CI=1.0	00001180
SL=1.0	00001190
TOL=1.E-4	00001200
METHOD=2	00001210
MEV=300	00001220
NRUN=1	00001230
INTYPE=4	00001240
CNCTOL=1.E-5	00001250
ISTEP=0	00001260
FNYQ=1200	00001270
BNYQ=1E29	00001280
C	00001290
C FNYQ IS SET TO HAVE NO EFFECT AND IS NOT A PARAMETER. FOR INFO	00001300
C ON ITS ORIGINAL PURPOSE, SEE KAUAHIKAUA AND ANDERSON, 1977	00001310
C	00001320
NF=0	00001330
IFLTX=0	00001340
IFLTY=0	00001350
IFLTZ=0	00001360
IOB=3	00001370
C	00001380
READ(5,INIT)	00001390
C	00001400
IF(IOB.GT.0.AND.IOB.LE.6.AND.(L.EQ.1.OR.L.EQ.2).AND.SL.GE.0.0.AND.	00001410
\$ CI.GT.0.0.AND.(ISTEP.EQ.1.OR.ISTEP.EQ.0).AND.X.GE.0.0.AND.Y.GE.	00001420
\$ 0.0.AND.FNYQ.GT.0.0.AND.M.GT.0.AND.M.LT.10.AND.TOL.GE.0.0.AND.	00001430
\$ (METHOD.EQ.1.OR.METHOD.EQ.2).AND.CNCTOL.GE.0.0.AND.INTYPE.GT.0.	00001440
\$ AND.INTYPE.LE.4.AND.NRUN.GT.0.AND.MEV.GT.0) GO TO 4	00001450
WRITE(6,2)	00001460
2 FORMAT(" SOME \$INIT PARMS OUT OF RANGE...")	00001470
STOP	00001480
4 R=SQRT(X*X+Y*Y)	00001490
SL=SL/2.	00001500
C	00001510
IF(BLWR.LT.0E0) BLWR=.005	00001520
IF(BUPR.LT.0E0) BUPR=1E4	00001530
C	00001540

```

C--CALCULATE ESTIMATE OF PRIMARY FIELD STRENGTH          00001550
C FROM DATA                                              00001560
C                                                         00001570
      R12=(X+SL)**2+Y*Y                                   00001580
      R22=(X-SL)**2+Y*Y                                   00001590
      R1=SQRT(R12)                                        00001600
      R2=SQRT(R22)                                        00001610
      GX=CI*(1./R22-1./R12)*Y/12.56637062                00001620
      GX0=X*Y/(6.28318531*R**4)                          00001630
      GY=-CI*((X-SL)/R22-(X+SL)/R12)/12.56637062        00001640
      GY0=-(X*X-Y*Y)/(12.56637062*R**4)                 00001650
      GZ=CI*((X+SL)/R1-(X-SL)/R2)/(12.56637062*Y)       00001660
      GZ0=Y/(12.56637062*R**3)                          00001670
      NRHO=0                                              00001680
      DO 1 I=1,3                                         00001690
1      NCOMP(I)=0                                         00001700
      TOX=0E0                                             00001710
      TNX=0E0                                             00001720
      TOY=0E0                                             00001730
      TNY=0E0                                             00001740
      TOZ=0E0                                             00001750
      TNZ=0E0                                             00001760
      NPRNT=2                                             00001770
      IF(IOB.GT.3) GO TO 5                               00001780
      IS=IOB                                              00001790
      IM=IOB                                              00001800
      GO TO 6                                             00001810
5      IS=1                                              00001820
      IM=4                                              00001830
      NPRNT=3                                             00001840
6      DO 30 I=IS,IM                                     00001850
          KOUNT=0                                         00001860
          DO 16 J=1,N                                     00001870
              IF(IOB.LE.3) GO TO 15                     00001880
C                                                         00001890
C CHECK XM(J,2) VALUES FOR PROPER RANGE                00001900
C                                                         00001910
              IF(XM(J,2).GE.1.,.OR,XM(J,2).LE.4.,.OR,I.GT.IS) GO TO 14 00001920
              WRITE(6,13) J                               00001930
13             FORMAT(" DATA MATRIX ENTRY (",I3," ",2) OUT OF RANGE") 00001940
              STOP                                         00001950
14             IF(IFIX(XM(J,2)).NE.I) GO TO 16           00001960
15             KOUNT=KOUNT+1                               00001970
              DT(KOUNT)=XM(J,1)                          00001980
              AV(KOUNT)=DV(J)                             00001990
16             CONTINUE                                   00002000
              IF(KOUNT.EQ.0) GO TO 30                    00002010
              GO TO (17,18,19,20),I                      00002020
17             TOX=DT(1)                                   00002030
              TNX=DT(KOUNT)                               00002040
              NCOMP(1)=KOUNT                             00002050
              GO TO 30                                    00002060

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18	TOY=DT(1)	00002070
	TNY=DT(KOUNT)	00002080
	NCOMP(2)=KOUNT	00002090
	GO TO 30	00002100
19	TOZ=DT(1)	00002110
	TNZ=DT(KOUNT)	00002120
	NCOMP(3)=KOUNT	00002130
	GO TO 30	00002140
20	NRHO=KOUNT	00002150
	ABMIN=DT(1)	00002160
	ABMAX=DT(KOUNT)	00002170
30	CONTINUE	00002180
	IF(IOB.LT.5) GO TO 40	00002190
	DO 35 I=1,3	00002200
35	NCOMP(I)=1	00002210
	TMAX=AMAX1(TNX,TNY,TNZ)	00002220
	TNX=TMAX	00002230
	TNY=TMAX	00002240
	TNZ=TMAX	00002250
	TMIN=TMAX	00002260
	IF(TOX.LT.TMIN.AND.TOX.GT.OEO) TMIN=TOX	00002270
	IF(TOY.LT.TMIN.AND.TOY.GT.OEO) TMIN=TOY	00002280
	IF(TOZ.LT.TMIN.AND.TOZ.GT.OEO) TMIN=TOZ	00002290
	TOX=TMIN	00002300
	TOY=TMIN	00002310
	TOZ=TMIN	00002320
40	SLL=2.*SL	00002330
C		00002340
C	SET UNUSED IFLTX, IFLTY, IFLTZ TO ZERO	00002350
C		00002360
45	GO TO (46,47,48,47,49,49),IOB	00002370
46	IFLTY=0	00002380
47	IFLTZ=0	00002390
	IF(IOB.EQ.4.OR.IOB.EQ.1) GO TO 49	00002400
48	IFLTX=0	00002410
	IF(IOB.EQ.2) GO TO 49	00002420
	IFLTY=0	00002430
49	CONTINUE	00002440
	WRITE(6,55) ISTEP,X,Y,R,CI,SLL,L,IFLTX,IFLTY,IFLTZ	00002450
	IF(IOUT.EQ.1) WRITE(16,55) ISTEP,X,Y,R,CI,SLL,L,IFLTX,IFLTY,IFLTZ	00002460
55	FORMAT(/19H DATA SET PARMS ARE/7H ISTEP=,I2,2X,2HX=,E12.4,	00002470
	12X,2HY=,E12.4,2X,2HR=,E12.4,2X,8HCURRENT=,E12.4/	00002480
	215H SOURCE LENGTH=,E12.4,2X,3H L=,I2/	00002490
	4 8H IFLTX=,I2,8H IFLTY=,I2,8H IFLTZ=,I2)	00002500
	SCALE=CI	00002510
	IF(L.EQ.2) GO TO 56	00002520
	SL=0.0	00002530
	SCALE=SCALE*SLL	00002540
	GX=GX0*CI*SLL	00002550
	GY=GY0*CI*SLL	00002560
	GZ=GZ0*CI*SLL	00002570
C--	SET EQUIVALENT VALUES FOR INITIALIZING COMMON AREAS	00002580

56 XX=X	00002590
YY=Y	00002600
S=SIG1	00002610
RR=R	00002620
HTOL=TOL	00002630
SLL=SL	00002640
NLAYER=M	00002650
NPARMS=2*M-1	00002660
NEXTRA=1	00002670
IF(IOB.EQ.4) NEXTRA=3	00002680
IF(IOB.EQ.5) NEXTRA=6	00002690
C--GX,GY,GZ ARE PRIMARY FIELD VALUES PASSED TO MODEL ROUTINES	00002700
C GT IS SCALING FACTOR FOR TIME AND FREQUENCY	00002710
GT=2./(R*R*12.56637062E-7)	00002720
WRITE(6,60) TOL,NF,IOB	00002730
IF(IOUT.EQ.1) WRITE(16,60) TOL,NF,IOB	00002740
60 FORMAT(/18H CONTROL PARMS ARE/5H TOL=,E12.4,2X,4HNF =,I4,	00002750
1 2X,5HI0B =,I4)	00002760
IF(L.EQ.1.OR.IOB.EQ.1) GO TO 66	00002770
WRITE(6,65) CNCTOL,INTYPE,NRUN,MEV	00002780
IF(IOUT.EQ.1) WRITE(16,65) CNCTOL,INTYPE,NRUN,MEV	00002790
65 FORMAT(8H CNCTOL=,E12.4,2X,8HINTYPE =,I5,6X,6HNRUN =,I5,8X,	00002800
15HMEV =,I5)	00002810
66 IF(ISTEP.EQ.1) WRITE(6,70) METHOD	00002820
IF(IOUT.EQ.1.AND.ISTEP.EQ.1) WRITE(16,70) METHOD	00002830
70 FORMAT(8H METHOD=,I5//)	00002840
C	00002850
C IF IOB.EQ.5, THE ORIENTATION OPTION HAS BEEN CHOSEN AND NEXTRA IS	00002860
C SET TO 6 TO ACCOMMODATE 3 SCALING FACTORS AND 3 ORIENTATION PARMS.	00002870
C FINALLY IOB IS SET TO 4 TO CAUSE ALL 3 FIELD COMPONENTS TO	00002880
C BE COMPUTED	00002890
C	00002900
IF(IOB.EQ.5) IOB=4	00002910
C	00002920
C CHECK B(I) FOR VALID VALUES	00002930
C	00002940
K=NEXTRA+NPARMS	00002950
DO 110 I=1,K	00002960
IF(B(I).GT.0E0) GO TO 110	00002970
IF(NEXTRA.EQ.6.AND.I.GE.3.AND.I.LE.6) GO TO 110	00002980
WRITE(6,99) I	00002990
99 FORMAT(" B(",I2,") .LE. 0E0")	00003000
STOP	00003010
110 CONTINUE	00003020
RETURN	00003030
END	00003040
SUBROUTINE FCODE(DV,XM,BPARMS,PRNT,F,IF,IDER)	00003050
C	00003060
C FCODE CALLED BY MQLVTHXYZ	00003070
C FCODE CALCULATES HX, HY, AND HZ (STEP OR IMPULSE)	00003080
C TRANSIENT SOUNDING MODELS FOR AN INFINITESIMAL AND	00003090

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C FINITE LENGTH WIRE SOURCE. 00003100
C 00003110
C T,VX,VY,VZ WORK ARRAYS INTERNAL TO FCODE 00003120
C DV VOLTAGE DATA ARRAY 00003130
C XM(1,I) TIMES ARRAY 00003140
C XM(2,I) WEIGHTS ARRAY IF IOB.LE.3 00003150
C INDICES ARRAY IF IOB.GT.3 00003160
C (1=HX, 2=HY, 3=HZ, 4=RHOA) 00003170
C XM(3,I) WEIGHTS ARRAY IF IOB.GT.3 00003180
C ND NUMBER OF DATA POINTS 00003190
C P,S,PS WORK ARRAYS REQUIRED BY SPLIN1 00003200
C 00003210
C THE PARAMETER IOB CONTROLS THE OPERATION OF FCODE: 00003220
C 00003230
C IOB=1 CALCULATE X-COMPONENT ONLY 00003240
C IOB=2 CALCULATE Y-COMPONENT ONLY 00003250
C IOB=3 CALCULATE Z-COMPONENT ONLY 00003260
C IOB=4 CALCULATE MIXED COMPONENTS, INCLUDING SCHLUMBERGER RHOA 00003270
C IOB=5 SAME AS IOB=4 WITH ORIENTATION PARAMETERS. 00003280
C 00003290
C WRITTEN BY JIM KAUAHIKAWA, USGS, DENVER, COLORADO 00003300
C LAST MODIFIED NOVEMBER, 1978 00003310
C 00003320
C DIMENSION BPARMS(1),P(50),S(50),DV(1),XM(200,5),PS(2) 00003330
C COMMON/MODEL/K,DD,NLAYER 00003340
C COMMON/THICK/D 00003350
C COMMON/PASS/CHX 00003360
C COMMON/PARM/ISTEP,XX,YY,R,SIG1,BNYQ,M,TOL 00003370
C COMMON/FIN/A1,A2,A3,A4,SIGG1,A6,A7 00003380
C COMMON/SPLXYZ/AX(100),BX(100),DX(100),AY(100),BY(100),DY(100), 00003390
C $ AZ(100),BZ(100),DZ(100),NB,B(100),SPX(100),SPY(100),SPZ(100),IW 00003400
C COMMON/CXYZ/FN,SL,MTD,NF,NCDMP(3),TOX,TNX,TOY,TNY,TOZ,TNZ,SCALE, 00003410
C $ BLWR,BUPR,ND,IOB,NEXTRA,NPARMS,GX,GY,GZ,GT,XO,IFLTX,IFLTY,IFLTZ 00003420
C COMMON/DCSAV/ARHO(100),BRHO(100),DRHO(100),AB2(100),RHOA(100),NRHO 00003430
C $ ,ABMAX,ABMIN 00003440
C COMMON/SAVEC/TX(50),VX(50),NTX,TY(50),VY(50),NTY,TZ(50),VZ(50), 00003450
C $ NTZ,CPX,CPY,CPZ,PARMS(20) 00003460
C 00003470
C GX,GY, AND GZ ARE THE PREDICTED PRIMARY FIELDS (FROM ITHXYZ) 00003480
C SL IS HALF SOURCE LENGTH IF FINITE WIRE MODELS ARE TO BE USED, 00003490
C IS ZERO OTHERWISE. 00003500
C 00003510
C REAL K(10),D(9),DD(9),PRNT(5) 00003520
C EXTERNAL CSPLN 00003530
C COMPLEX COMPL,FINHX,FINHY,FINHZ,CHX,CHY,CHZ,FLT 00003540
C DATA PS/0.0,0.0/ 00003550
C 00003560
C IF(IF.GT.1) GO TO 150 00003570
C 00003580
C MODELS ARE CALCULATED ONLY IF IF=1, OTHERWISE THEY ARE RETRIEVED 00003590
C FROM STORAGE IN COMMON BLOCK /SAVEC/ 00003600
C 00003610

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      ISKIP=1                                00003620
C                                           00003630
C CHECK BPARMS TO SEE IF SAME AS LAST PARMS 00003640
C                                           00003650
      DO 5 I=1,NPARMS                       00003660
          IF(PARMS(I).NE.BPARMS(NEXTRA+I)) ISKIP=0 00003670
5      PARMS(I)=BPARMS(NEXTRA+I)           00003680
      IF(IOB.EQ.1.OR.IOB.GT.3) CPX=BPARMS(1) 00003690
      IF(IOB.EQ.2) CPY=BPARMS(1)           00003700
      IF(IOB.GT.3) CPY=BPARMS(2)           00003710
      IF(IOB.EQ.3) CPZ=BPARMS(1)           00003720
      IF(IOB.GT.3) CPZ=BPARMS(3)           00003730
C                                           00003740
C IF BPARMS SAME AS LAST PARMS, SKIP MODEL COMPUTATION 00003750
C                                           00003760
      IF(ISKIP.EQ.1) GO TO 150              00003770
      SIG1=PARMS(1)                        00003780
      SIGG1=SIG1                           00003790
      M1=M-1                               00003800
      BMIN=1.0                             00003810
      BMAX=1.0                             00003820
      DO 10 I=1,M1                         00003830
          K(I)=PARMS(I)/SIG1                00003840
C--MAXIMUM NORMALIZED FREQUENCY, BMAX, IS DETERMINED BY SMALLEST 00003850
C CONDUCTIVITY CONTRAST IN MODEL OR BY THE NYQUIST FREQUENCY, FN. 00003860
          BMAX=AMIN1(BMAX,K(I))             00003870
C--MINIMUM NORMALIZED FREQUENCY, BMIN, IS DETERMINED BY LARGEST 00003880
C CONDUCTIVITY CONTRAST IN MODEL          00003890
          BMIN=AMAX1(BMIN,K(I))             00003900
      10 D(I)=PARMS(M+I)                   00003910
          K(M)=PARMS(M)/SIG1                00003920
          BMIN=AMAX1(BMIN,K(M))             00003930
          BMAX=AMIN1(BMAX,K(M))             00003940
C                                           00003950
      CONT=GT/SIG1                          00003960
      XTMAX=CONT*TNX*1.15                   00003970
      XTMIN=CONT*TOX                        00003980
      YTMAX=CONT*TNX*1.15                   00003990
      YTMIN=CONT*TOY                        00004000
      ZTMAX=CONT*TNZ*1.15                   00004010
      ZTMIN=CONT*TOZ                        00004020
C                                           00004030
      VX(1)=1.0                             00004040
      VY(1)=1.0                             00004050
      VZ(1)=3.*CONT*GZ                      00004060
C                                           00004070
C                                           00004080
      IF(NF.GT.12.OR.NF.LE.0) NF=12        00004090
C                                           00004100
C--MODEL CALCULATED ON A SPLINE INTERPOLATED FREQUENCY FUNCTION 00004110
C COMPUTED AT NF FREQUENCIES PER DECADE  00004120
C RANGE AUTOMATICALLY DETERMINED FROM THE MAXIMUM AND MINIMUM 00004130

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C CONDUCTIVITIES IN MODEL 00004140
C 00004150
C 00004160
    BMAX=BUFR/BMAX 00004170
    BMIN=BLWR/BMIN 00004180
C 00004190
15 NB=AIN(T(NF*ALOG10(BMAX/BMIN)))+2 00004200
    NB1=NB+1 00004210
    X0=ALOG10(BMAX)+0.25 00004220
    ISAV=ISTEP 00004230
    IF(MTD,EQ.1) ISTEP=0 00004240
    IF(NB,LE.100) GO TO 18 00004250
C 00004260
C NB MAY NOT EXCEED THE SIZE OF THE ARRAYS IN COMMON BLOCK /SPLXYZ/ 00004270
C 00004280
    WRITE(6,95) NB 00004290
95 FORMAT(" FCODE:  NB,GT.100, NB=",I5) 00004300
    STOP 00004310
18 DO 1 J=1,NB 00004320
    I=NB1-J 00004330
    X=X0-J/FLOAT(NF) 00004340
    B(I)=X 00004350
    X=10E0**X 00004360
    F=X*CONT/6.2831853 00004370
    IF(SL,EQ.0E0) CALL HXYZ(X,CHX,CHY,CHZ,IOB) 00004380
    GO TO (17,20,40,20,20),IOB 00004390
17 IF(SL,GT.0E0) CHX=FINHX(X) 00004400
20 IF(SL,GT.0E0,AND,IOB,GT.1) CHY=FINHY(X) 00004410
    IF(IFLTX,NE.0) CHX=CHX*FLT(IFLTX,F) 00004420
    SPX(I)=REAL(CHX) 00004430
    IF(IOB,EQ.1) GO TO 1 00004440
    IF(IFLTY,NE.0) CHY=CHY*FLT(IFLTY,F) 00004450
    SPY(I)=REAL(CHY) 00004460
    IF(IOB,LT.3) GO TO 1 00004470
40 IF(SL,GT.0E0) CHZ=FINHZ(X) 00004480
    IF(IFLTZ,NE.0) CHZ=CHZ*FLT(IFLTZ,F) 00004490
    SPZ(I)=REAL(CHZ) 00004500
    1 CONTINUE 00004510
    ISTEP=ISAV 00004520
C 00004530
C NOTE:  B() ARRAY IS ACTUALLY ALOG10(B) 00004540
C 00004550
    IF(NCOMP(1),NE.0) CALL SPLIN1(NB,0,B,SPX,AX,BX,DX,0,PS,P,S) 00004560
    IF(NCOMP(2),NE.0) CALL SPLIN1(NB,0,B,SPY,AY,BY,DY,0,PS,P,S) 00004570
    IF(NCOMP(3),NE.0) CALL SPLIN1(NB,0,B,SPZ,AZ,BZ,DZ,0,PS,P,S) 00004580
C 00004590
C THE SWITCH IW WORKS WITH COMMON BLOCK /SPLXYZ/ IN ROUTINE CSPLN 00004600
C TO INTERPOLATE EITHER THE X, Y, OR Z COMPONENT 00004610
C 00004620
    IW=1 00004630
    IF(NCOMP(1),NE.0) CALL TRNSI(CSPLN,XTMAX,XTMIN,NTX,TX,VX,MTD) 00004640
    IW=2 00004650

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IF(NCOMP(2).NE.0) CALL TRNSI(CSPLN,YTMAX,YTMIN,NTY,TY,VY,MTD) 00004660
IW=3 00004670
IF(NCOMP(3).NE.0) CALL TRNSI(CSPLN,ZTMAX,ZTMIN,NTZ,TZ,VZ,MTD) 00004680
C 00004690
IF(IOB.LE.3.OR.NRHO.EQ.0) GO TO 3 00004700
CALL SCHSDG(SIG1,ABMAX,ABMIN,AB2,RHOA,NRHO,TOL) 00004710
DO 2 I=1,NRHO 00004720
2 AB2(I)=ALOG(AB2(I)) 00004730
CALL SPLIN1(NRHO,0,AB2,RHOA,ARHO,BRHO,DRHO,0,PS,P,S) 00004740
C 00004750
3 NT=MAX0(NTX,NTY,NTZ) 00004760
IF(ISTEP.EQ.0.OR.MTD.EQ.1) GO TO 35 00004770
DO 30 I=1,NT 00004780
IF(NCOMP(1).NE.0) VX(I)=VX(I)*SCALE+GX 00004790
IF(NCOMP(2).NE.0) VY(I)=VY(I)*SCALE+GY 00004800
30 IF(NCOMP(3).NE.0) VZ(I)=VZ(I)*SCALE+GZ 00004810
35 DO 50 I=1,NT 00004820
IF(I.LE.NTX) TX(I)=ALOG(TX(I)) 00004830
IF(I.LE.NTY) TY(I)=ALOG(TY(I)) 00004840
IF(I.LE.NTZ) TZ(I)=ALOG(TZ(I)) 00004850
50 CONTINUE 00004860
IF(NCOMP(1).NE.0) CALL SPLIN1(NTX,0,TX,VX,AX,BX,DX,0,PS,P,S) 00004870
IF(NCOMP(2).NE.0) CALL SPLIN1(NTY,0,TY,VY,AY,BY,DY,0,PS,P,S) 00004880
IF(NCOMP(3).NE.0) CALL SPLIN1(NTZ,0,TZ,VZ,AZ,BZ,DZ,0,PS,P,S) 00004890
C 00004900
150 TAU=CONT*XM(IF,1) 00004910
TAU=ALOG(TAU) 00004920
INDEX=IOB 00004930
IF(IOB.GT.3) INDEX=IFIX(XM(IF,2)) 00004940
IF(INDEX.EQ.4) GO TO 188 00004950
IF(NEXTRA.EQ.6) GO TO 180 00004960
IF(INDEX.EQ.1) F=CPX*SPLINT(TAU,AX,BX,DX,NTX,TX,VX) 00004970
IF(INDEX.EQ.2) F=CPY*SPLINT(TAU,AY,BY,DY,NTY,TY,VY) 00004980
IF(INDEX.EQ.3) F=CPZ*SPLINT(TAU,AZ,BZ,DZ,NTZ,TZ,VZ) 00004990
GO TO 190 00005000
C 00005010
C ORIENTATION PARAMETERS OPTION HAS BEEN CHOSEN 00005020
C 00005030
180 FX=CPX*SPLINT(TAU,AX,BX,DX,NTX,TX,VX) 00005040
FY=CPY*SPLINT(TAU,AY,BY,DY,NTY,TY,VY) 00005050
FZ=CPZ*SPLINT(TAU,AZ,BZ,DZ,NTZ,TZ,VZ) 00005060
CS1=COS(BPARMS(4)) 00005070
SN1=SIN(BPARMS(4)) 00005080
CS2=COS(BPARMS(5)) 00005090
SN2=SIN(BPARMS(5)) 00005100
CS3=COS(BPARMS(6)) 00005110
SN3=SIN(BPARMS(6)) 00005120
IF(INDEX.EQ.3) GO TO 185 00005130
FXP=FX*CS1+SN1*(-FZ*CS2+FY*SN2) 00005140
FYP=FY*CS1-SN1*(FZ*CS2+FX*SN2) 00005150
IF(INDEX.EQ.1) F=FXP*CS3+FYP*SN3 00005160
IF(INDEX.EQ.2) F=FYP*CS3-FXP*SN3 00005170

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      GO TO 190                                00005180
185 F=FZ*CS1+SN1*(FX*CS2+FY*SN2)              00005190
      GO TO 190                                00005200
C                                              00005210
188 F=SPLINT(ALOG(XM(IF,1)),ARHO,BRHO,DRHO,NRHO,AB2,RHOA) 00005220
C                                              00005230
190 IIMAX=2                                    00005240
      IF(IOB.GT.3) IIMAX=3                    00005250
      DO 200 II=1,IIMAX                      00005260
200      PRNT(II)=XM(IF,II)                  00005270
      RETURN                                  00005280
      END                                     00005290

      SUBROUTINE HXYZ(B2,HX,HY,HZ,IOB)          00005300
C                                              00005310
C HXYZ CALCULATES THREE COMPONENTS OF THE MAGNETIC FIELD 00005320
C OF AN ELECTRIC DIPOLE AT THE ORIGIN AND ORIENTED ALONG THE X-AXIS. 00005330
C                                              00005340
C IOB=1 FOR HX ONLY                          00005350
C IOB=2 FOR HY ONLY                          00005360
C IOB=3 FOR HZ ONLY                          00005370
C IOB=4,5 FOR MIXED COMPONENTS.             00005380
C                                              00005390
C CALLS ZHANKS,SAVER,F3,F4,IKS               00005400
C                                              00005410
      COMPLEX F3,F4,ZHANKS,XX,YY,ZZ,HX,HY,HZ,ONE,ZERO,I1K1,IKDIF,CB 00005420
      COMMON/PAARM/ISTEP,X,Y,R,SIG1,BNYQ,M,TOL 00005430
      COMMON/MODEL/K,DD,NLAYER                00005440
      COMMON/THICK/D                          00005450
      EXTERNAL F3,F4                          00005460
      REAL K(10),D(9),DD(9)                  00005470
      DOUBLE PRECISION B8                     00005480
      DATA ONE,ZERO/(1.0,0.0),(0.0,0.0)/    00005490
      B=SQRT(B2)                              00005500
      HX=ZERO                                 00005510
      HY=ZERO                                 00005520
      HZ=ZERO                                 00005530
      R2=R*R                                  00005540
      C=Y/(R2*R)                              00005550
      XR2=X*X/R2                              00005560
      CB=CMPLX(B,B)                          00005570
      IF(M.EQ.1) GO TO 10                     00005580
      M1=M-1                                  00005590
      DEL=R/B                                 00005600
      DEL2=DEL*DEL                            00005610
      DO 4 I=1,M1                             00005620
4      DD(I)=2.*D(I)/DEL                      00005630
C                                              00005640
C HX AND HY REQUIRE THE SAME TWO HANKEL TRANSFORMS 00005650
C                                              00005660
      NEW=1                                    00005670
      IF(IOB.EQ.3) GO TO 5                    00005680

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NEW=0	00005690
YY=ZHANKS(1,B,F3,TOL,LW,1)	00005700
CALL SAVER(1,1)	00005710
XX=ZHANKS(0,B,F4,TOL,LW,0)	00005720
HX=2.*(2.*YY/B-XX)*X*Y/(DEL2*R2)	00005730
HY=(XR2-1.)*2.*XX/DEL2+2.*(1.-2.*XR2)*YY/(R*DEL)	00005740
IF(IOB.LT.3) GO TO 10	00005750
5 HZ=ZHANKS(1,B,F4,TOL,LW,NEW)*CMPLX(2.0*B2*C,0.0)	00005760
10 B8=.70710678118654D0*B	00005770
C	00005780
C CALCULATE THE MODIFIED BESSEL FUNCTIONS OF THE FIRST AND	00005790
C SECOND KINDS FOR THE HX AND HY HALFSPACE RESPONSES.	00005800
C	00005810
IF(IOB.NE.3) CALL IKS(B8,I1K1,IKDIF)	00005820
ZZ=ZERO	00005830
IF(IOB.LT.3) GO TO 12	00005840
ZZ=ONE-(ONE+CB+CMPLX(OE0,2E0*B2/3E0))*CEXP(-CB)	00005850
ZZ=ZZ*CMPLX(OE0,-3E0*C/B2)	00005860
C	00005870
C SUBTRACT THE PRIMARY FIELD VALUES IF ISTEP = 1	00005880
C	00005890
12 IF(ISTEP.EQ.0) GO TO 20	00005900
IF(IOB.EQ.3) GO TO 15	00005910
IKDIF=IKDIF-CMPLX(1.0,0.0)	00005920
I1K1=I1K1-CMPLX(0.5,0.0)	00005930
IF(IOB.LT.3) GO TO 20	00005940
15 ZZ=ZZ-CMPLX(C,0.0)	00005950
C	00005960
20 HX=HX+2.*X*Y*IKDIF/(R2*R2)	00005970
HY=HY+2.*(Y*Y*IKDIF/R2-I1K1)/R2	00005980
HZ=HZ+ZZ	00005990
DENOM=12.56637062*B2**ISTEP	00006000
HX=HX/DENOM	00006010
HY=HY/DENOM	00006020
HZ=HZ/DENOM	00006030
RETURN	00006040
END	00006050
COMPLEX FUNCTION FLT(IFLAG,F)	00006060
C	00006070
C USER-DEFINED FUNCTION	00006080
C IFLAG IS A PARAMETER PASSED FROM MQLVTHXYZ VIA \$INIT	00006090
C PARMS IFLTX, IFLTY, OR IFLTZ	00006100
C F IS THE FREQUENCY IN HERTZ	00006110
C	00006120
COMPLEX ONE	00006130
DATA ONE/(1E0,0E0)/	00006140
IF(IFLAG.EQ.0) RETURN	00006150
C	00006160
C EXAMPLE: SINGLE-POLE LOW PASS FILTER WHERE	00006170
C IFLAG IS USED AS THE CORNER FREQUENCY	00006180
C	00006190

CF=IFLAG*6.283185	00006200
OMEGA=F*6.283185	00006210
FLT=ONE/CMPLX(-CF,OMEGA)	00006220
RETURN	00006230
END	00006240
SUBROUTINE TRNSI(FUNC,TMAX,TMIN,NT,T,V,MTD)	00006250
C IF ISTEP = 0, THE COSINE TRANSFORM OF THE REAL	00006260
C PART OF FUNC IS CALCULATED USING THE LAGGED	00006270
C CONVOLUTION OPERATOR ZLAGF0 TO YIELD THE	00006280
C IMPULSE RESPONSE.	00006290
C IF ISTEP = 1, THE STEP RESPONSE IS CALCULATED AS	00006300
C - THE INTEGRAL OVER TIME OF THE IMPULSE	00006310
C RESPONSE IF MTD = 1,	00006320
C - THE SINE TRANSFORM OF THE REAL PART OF FUNC	00006330
C DIVIDED BY THE FREQUENCY USING THE LAGGED	00006340
C CONVOLUTION OPERATOR ZLAGF1 IF MTD = 2,	00006350
C ***** ZLAGF0 AND ZLAGF1 FROM ANDERSON 1975 *****	00006360
C	00006370
DIMENSION T(100),V(100)	00006380
EXTERNAL FUNC	00006390
COMPLEX FUNC,ZLAGF0,ZLAGF1,CON	00006400
COMMON/PAARM/ISTEP,XX,YY,R,SIG1,BNYQ,M,TOL	00006410
NT=AIN(0.5+5.*ALOG(TMAX/TMIN))+1	00006420
NT1=NT+1	00006430
X0=ALOG(TMAX)+0.2	00006440
C=4.0E-7*3.1415927	00006450
XI=C*SIG1*R*R/2.	00006460
C=2./(XI*3.1415927)	00006470
V0=V(1)	00006480
NEW=1	00006490
ISAV=ISTEP	00006500
IF(MTD.EQ.1) ISTEP=0	00006510
DO 2 J=1,NT	00006520
I=NT1-J	00006530
X=X0-0.2*J	00006540
V(I)=0.0	00006550
T(I)=EXP(X)	00006560
IF(ISTEP.EQ.1) GO TO 3	00006570
CON=C*ZLAGF0(X,FUNC,TOL,LW,NEW)/T(I)	00006580
GO TO 4	00006590
3 CON=C*XI*ZLAGF1(X,FUNC,TOL,LW,NEW)/T(I)	00006600
4 V(I)=REAL(CON)	00006610
2 NEW=0	00006620
ISTEP=ISAV	00006630
IF(MTD.EQ.2.OR.ISTEP.EQ.0) GO TO 10	00006640
CALL INTEG1(NT,T,V,V0)	00006650
DO 9 I=1,NT	00006660
9 V(I)=V(I)*XI	00006670
10 RETURN	00006680
END	00006690

```

SUBROUTINE SCHSDG(SIG1,XMAX,XMIN,AB2,RHOA,NRHO,TOL)      00006700
C                                                         00006710
C COMPUTE SCHLUMBERGER APPARENT RESISTIVITY SOUNDING CURVE USING 00006720
C LAGGED CONVOLUTION                                     00006730
C                                                         00006740
C     DIMENSION AB2(1),RHOA(1)                           00006750
C     COMPLEX ZLAGH1,CMP                                  00006760
C     COMMON/MODEL/RK(10),DNORM(9),M                     00006770
C     COMMON/THICK/D(9)                                   00006780
C                                                         00006790
C MUST TRANSFER MODEL FROM EM COMMON BLOCK, MODEL,      00006800
C TO DC COMMON BLOCK DCMDL.                              00006810
C                                                         00006820
C     COMMON/DCMDL/SIG(10),DDC(9),NLYR,INDEX             00006830
C     EXTERNAL DCKERN                                     00006840
C                                                         00006850
C     NRHO=AIN(5E0*ALOG(XMAX/XMIN))+2                    00006860
C     NRHO1=NRHO+1                                       00006870
C     X0=ALOG(XMAX)+0.25                                 00006880
C     NLYR=M                                             00006890
C     RHO1=1E0/SIG1                                     00006900
C     DO 10 I=1,M                                       00006910
C         DDC(I)=D(I)                                   00006920
C     10     SIG(I)=SIG1*RK(I)                           00006930
C                                                         00006940
C     INDEX=0                                           00006950
C     NEW=1                                             00006960
C     CMP=CMPLX(0E0,0E0)                               00006970
C     DO 20 J=1,NRHO                                   00006980
C         I=NRHO1-J                                     00006990
C         XX=X0-0.2*J                                   00007000
C         AB2(I)=EXP(XX)                                00007010
C         A2=EXP(2E0*XX)                                00007020
C         IF(M.EQ.1) GO TO 19                           00007030
C         CMP=ZLAGH1(XX,DCKERN,TOL,LW,NEW)/AB2(I)       00007040
C     19     RHOA(I)=RHO1+A2*REAL(CMP)                  00007050
C     20     NEW=0                                       00007060
C     RETURN                                           00007070
C     END                                               00007080
C                                                         00007090
REAL FUNCTION SPLINT(T,A,B,C,N,X,Y)                    00007090
C--CUBIC SPLINE INTERPOLATION ROUTINE                  00007100
C ASSUMES PRIOR CALL TO SPLIN1                          00007110
C     DIMENSION A(1),B(1),C(1),X(1),Y(1)              00007120
C     IF(T.LT.X(1).OR.T.GT.X(N)) GO TO 9               00007130
C     N1=N-1                                           00007140
C     DO 1 I=1,N1                                       00007150
C         J=I                                           00007160
C         IF(T.LT.X(I+1)) GO TO 2                       00007170
C     1 CONTINUE                                       00007180
C     9 SPLINT=0.0                                       00007190
C     IF(T.LT.X(1)) SPLINT=Y(1)                        00007200

```

RETURN	00007210
2 Z=T-X(J)	00007220
SPLINT=Y(J)+((C(J)*Z+B(J))*Z+A(J))*Z	00007230
RETURN	00007240
END	00007250
COMPLEX FUNCTION DCKERN(AMBDA)	00007260
C	00007270
C RESISTIVITY KERNEL FUNCTION CALLED BY SCHSDG	00007280
C	00007290
C FOR INDEX = 0 RETURNS (KERNEL,PDIF W/R RHO(M))	00007300
C WHERE PDIF = PARTIAL DERIVATIVE	00007310
C FOR INDEX = I RETURNS (PDIF KERNEL W/R D(I),	00007320
C PDIF KERNEL W/R RHO(I))	00007330
C M > I > 0	00007340
C	00007350
C ALGORITHM FOR PARTIALS FROM:	00007360
C JOHANSEN, H.K., 1975, AN INTERACTIVE COMPUTER GRAPHICS-	00007370
C DISPLAY-TERMINAL SYSTEM FOR INTERPRETATION OF RESISTIVITY SOUNDING	00007380
C GEOPHYSICAL PROSPECTING, 23: 449-458.	00007390
C	00007400
C PROGRAMMED BY JKAUAHIKAUA, USGS, DENVER, COLO, 1977.	00007410
C	00007420
COMMON/DCMDL/SIG(10),D(9),M,INDEX	00007430
REAL LM,LN,L2	00007440
PSIG=0E0	00007450
PD=0E0	00007460
L=M	00007470
LM=1E0	00007480
10 L1=L-1	00007490
E=EXP_(-2E0*AMBDA*D(L1))	00007500
EN=(1E0-E)/(1E0+E)	00007510
DENOM=SIG(L)+SIG(L1)*LM*EN	00007520
IF(L.EQ.2) L2=LM	00007530
IF(L.EQ.2) E1=E	00007540
LN=(SIG(L1)*LM+SIG(L)*EN)/DENOM	00007550
IF(INDEX+1.LT.M.AND.L-2.EQ.INDEX) PSIG=(1E0-EN*LN)*LM/DENOM	00007560
IF(INDEX-L1) 15,13,14	00007570
13 PSIG=((EN-LN)+(1E0-EN*LN)*SIG(L1)*PSIG)/DENOM	00007580
PD=(1E0+EN)*(SIG(L)-LN*LM*SIG(L1))*2E0*AMBDA*E/(DENOM*(1E0+E))	00007590
GO TO 15	00007600
14 X=(1E0-LN*EN)*SIG(L1)/DENOM	00007610
PSIG=PSIG*X	00007620
PD=PD*X	00007630
15 L=L-1	00007640
LM=LN	00007650
IF(L.GT.1) GO TO 10	00007660
IF(INDEX.GT.0) GO TO 20	00007670
PL1=L2*(1E0-E1*LM)*AMBDA/DENOM	00007680
LM=AMBDA*(LM-1E0)	00007690
DCKERN=CMPLX(LM,PL1)	00007700
RETURN	00007710

```

20 DCKERN=CMPLX(AMBDA*PD,AMBDA*PSIG)                                00007720
   RETURN                                                            00007730
   END                                                                00007740

      COMPLEX FUNCTION CSPLN(RT)                                     00007750
C---CUBIC SPLINE INTERPOLATION ROUTINE                             00007760
C RETURNS A COMPLEX RESULT (IMAG PART = 0)                         00007770
C CALLED WITH TRNSI BY FTHXYZ                                     00007780
C ASSUMES PREVIOUS CALL TO SPLIN1                                 00007790
C                                                                    00007800
C IW USED AS FLAG (SET BY CALLING ROUTINE):                       00007810
C   IW=1 - USE AX, BX, AND CX TO INTERPOLATE SPX                  00007820
C   IW=2 - USE AY, BY, AND CY TO INTERPOLATE SPY                  00007830
C   IW=3 - USE AZ, BZ, AND CZ TO INTERPOLATE SPZ                  00007840
C                                                                    00007850
      COMMON/SPLXYZ/AX(100),BX(100),CX(100),AY(100),BY(100),CY(100),
1  AZ(100),BZ(100),CZ(100),NB,B(100),SPX(100),SPY(100),SPZ(100),IW 00007860
C                                                                    00007870
C NOTE THAT THE FUNCTION BEING SPLINED IS A FUNCTION               00007880
C OF B() = ALOG(B)                                                 00007890
C                                                                    00007900
C                                                                    00007910
      T=ALOG10(RT)                                                  00007920
      IF(T.LT.B(1).OR.T.GT.B(NB)) GO TO 20                         00007930
      N1=NB-1                                                       00007940
      DO 10 I=1,N1                                                  00007950
          J=I                                                         00007960
          IF(T.LT.B(I+1)) GO TO 30                                   00007970
10      CONTINUE                                                    00007980
20      CS=0.0                                                       00007990
          IF(T.GE.B(1)) GO TO 25                                     00008000
          IF(IW.EQ.1) CS=SPX(1)                                       00008010
          IF(IW.EQ.2) CS=SPY(1)                                       00008020
          IF(IW.EQ.3) CS=SPZ(1)                                       00008030
25      CSPLN=CMPLX(CS,0.0)                                         00008040
          RETURN                                                      00008050
30      Z=T-B(J)                                                     00008060
          IF(IW.EQ.1) CS=SPX(J)+((CX(J)*Z+BX(J))*Z+AX(J))*Z         00008070
          IF(IW.EQ.2) CS=SPY(J)+((CY(J)*Z+BY(J))*Z+AY(J))*Z         00008080
          IF(IW.EQ.3) CS=SPZ(J)+((CZ(J)*Z+BZ(J))*Z+AZ(J))*Z         00008090
          CSPLN=CMPLX(CS,0.0)                                         00008100
          RETURN                                                      00008110
          END                                                         00008120

      COMPLEX FUNCTION FINHX(B)                                     00008130
C---HX FIELD OF FINITE ELECTRIC WIRE                               00008140
      COMMON/PAFM/ISTEP,A1,A2,A3,A4,BNYQ,A5,A6                     00008150
      COMMON/FIN/R1,R2,R,L,SIG1,X,Y                               00008160
      COMMON/THICK/D(9)                                             00008170
      COMMON/MODEL/K(10),DD(9),M                                    00008180
      REAL L,K                                                       00008190
      DOUBLE PRECISION BB                                           00008200
      COMPLEX F31,F32,I1K1                                          00008210

```

SB=SQRT(B)	00008220
FINHX=CMPLX(0.0,0.0)	00008230
IF(SB.GT.BNYQ) RETURN	00008240
DEL=R/SB	00008250
IF(M.EQ.1) GO TO 12	00008260
R1=R1/DEL	00008270
B2=R2/DEL	00008280
M1=M-1	00008290
DO 1 I=1,M1	00008300
1 DD(I)=2.*D(I)/DEL	00008310
CALL FINF3(B1,B2,F31,F32)	00008320
FINHX=CMPLX(1./DEL,0.0)*(F31/R1-F32/R2)	00008330
12 B8=0.7071067811865475D0/DEL	00008340
FINHX=FINHX+(I1K1(B8*R1)/R1**2-I1K1(B8*R2)/R2**2)	00008350
FINHX=-FINHX*CMPLX(Y/6.2838153,0.0)	00008360
RETURN	00008370
END	00008380
COMPLEX FUNCTION FINHY(B)	00008390
C--HY FIELD OF FINITE ELECTRIC WIRE	00008400
C PASSES HX IN COMMON BLOCK 'PASS'	00008410
EXTERNAL ZHY	00008420
COMMON/FIN/R1,R2,R,L,SIG1,X,Y	00008430
COMMON/CONST/DEL,DEL2,Z	00008440
COMMON/PASS/FINHX	00008450
COMMON/PAARM/ISTEP,A1,A2,A3,A4,BNYQ,M,A6	00008460
COMPLEX FINITE,F31,F32,FINHX,Z,I1K1,IK1,IK2	00008470
DOUBLE PRECISION B8	00008480
REAL L	00008490
SB=SQRT(B)	00008500
FINHX=CMPLX(0.0,0.0)	00008510
FINHY=CMPLX(0.0,0.0)	00008520
IF(SB.GT.BNYQ) RETURN	00008530
DEL=R/SB	00008540
DEL2=DEL*DEL	00008550
FINHY=FINITE(ZHY,B)	00008560
IF(M.EQ.1) GO TO 10	00008570
B1=R1/DEL	00008580
B2=R2/DEL	00008590
CALL FINF3(B1,B2,F31,F32)	00008600
FINHY=FINHY-((X+L)*F31/R1-(X-L)*F32/R2)*CMPLX(1./DEL,0.0)	00008610
10 B8=0.7071067811865475D0/DEL	00008620
R12=R1*R1	00008630
R22=R2*R2	00008640
IK1=I1K1(B8*R1)/R12	00008650
IK2=I1K1(B8*R2)/R22	00008660
C REMOVE PRIMARY FIELD IF ISTEP=1	00008670
IF(ISTEP.EQ.1) IK1=IK1-CMPLX(0.5/R12,0.0)	00008680
IF(ISTEP.EQ.1) IK2=IK2-CMPLX(0.5/R22,0.0)	00008690
FINHY=-(FINHY-((X+L)*IK1-(X-L)*IK2))*CMPLX(1./6.2831853,0.0)	00008700
IF(X*Y.EQ.0.0) GO TO 20	00008710
IF(M.EQ.1) GO TO 15	00008720



```

FINHX=(F31/R1-F32/R2)*CMPLX(1./DEL,0.0)
15 FINHX=-(FINHX+(IK1-IK2))*CMPLX(Y/6.2831853,0.0)
20 IF(ISTEP.EQ.0) GO TO 30
    FINHY=FINHY/B
    FINHX=FINHX/B
30 RETURN
END

COMPLEX FUNCTION FINHZ(B)
C--HZ FIELD OF FINITE ELECTRIC WIRE
COMPLEX FINITE
EXTERNAL ZHZ
COMMON/PAARM/ISTEP,A1,A2,A3,A4,BNYQ,M,A6
COMMON/FIN/R1,R2,R,RL,SIG1,X,Y
SB=SQRT(B)
FINHZ=CMPLX(0.0,0.0)
IF(SB.GT.BNYQ) RETURN
FINHZ=FINITE(ZHZ,B)*CMPLX(Y/12.5663706,0.0)
IF(ISTEP.EQ.1) FINHZ=FINHZ/B
RETURN
END

COMPLEX FUNCTION F3(G)
COMPLEX V1,F1,C,ONE
DATA ONE/(1.0,0.0)/
CALL RECURS(G,V1,F1)
C=G
F3=(V1*C*(ONE-F1))/((C+V1*F1)*(C+V1))
RETURN
END

COMPLEX FUNCTION F4(G)
COMPLEX V1,F1,C,ONE
DATA ONE/(1.0,0.0)/
CALL RECURS(G,V1,F1)
C=G
F4=(V1*C*C*(ONE-F1))/((C+V1*F1)*(C+V1))
RETURN
END

SUBROUTINE RECURS(G,V1,F1)
C
C      RECURS ALGORITHM FROM ANDERSON(1974)
C
COMPLEX C,VM,V1,F1,EVD,ONE,T
REAL K(10),D(9)
COMMON/MODEL/K,D,M
DATA ONE/(1.0,0.0)/
F1=ONE
G2=G*G
VM=CSQRT(CMPLX(G2,2.0*K(M)))
IF(M.EQ.1) GO TO 30

```

```

      J=M-1                                00009210
10  V1=CSQRT(CMPLX(G2,2.0*K(J)))          00009220
      EVD=-V1*D(J)                        00009230
      EVD=CEXP(EVD)                      00009240
20  C=(ONE-EVD)/(ONE+EVD)                00009250
      T=VM*F1                            00009260
      F1=(T+V1*C)/(V1+T*C)              00009270
      IF(J,EQ,1) GO TO 40                00009280
      J=J-1                              00009290
      VM=V1                              00009300
      GO TO 10                           00009310
30  V1=VM                                00009320
40  RETURN                               00009330
      END                                00009340

      SUBROUTINE FINF3(B1,B2,F31,F32)      00009350
      COMMON/FINERR/TOL,T,IT,N,NEV,MEV,ES,LW 00009360
      COMPLEX F31,F32,ZHANKS,ES           00009370
      EXTERNAL F3                         00009380
      F31=ZHANKS(1,B1,F3,TOL,LW,1)       00009390
      IF(B1,EQ,B2) GO TO 10              00009400
      F32=ZHANKS(1,B2,F3,TOL,LW,1)       00009410
      RETURN                             00009420
10  F32=F31                             00009430
      RETURN                             00009440
      END                                00009450

      COMPLEX FUNCTION FINITE(FUNC,BFIN)   00009460
C---COMPUTE FINITE INTEGRAL OVER (-L,L) OF COMPLEX FIELD FUNCTION 00009470
C BY LAG-CONVOLUTION AND QUINTIC SPLINE INTERPOLATION PRIOR TO    00009480
C AUTOMATIC INTEGRATION BY SUBR 'CANC4'. 00009490
C 'FINITE' CALLS 'FUNC' (WHICH CALLS 'ZLAGH1 OR ZLAGH0'), 'QUINT', AND 00009500
C 'CANC4' (WHICH CALLS 'FUNINT' AND 'QPOINT'). 00009510
C 00009520
C PARAMETERS: 00009530
C 00009540
C FUNC = EXTERNAL DECLARED COMPLEX FUNCTION DEFINING THE DIPOLE FIELD 00009550
C FUNCTION WITH CALLING SEQ: FUNC(B,NEW,R), WHERE 00009560
C B = ANY IND. NO. 00009570
C NEW = 1 FIRST TIME, 0 OTHERWISE (REF: ZLAGH1 OR ZLAGH0) 00009580
C R = B*DEL FOR ANY B OR DEL (SKIN DEPTH). 00009590
C BFIN = FIXED IND. NO. FOR THE FINITE INTEGRAL (BFIN.GT.0). 00009600
C 00009610
C---COMMON PARAMMETERS (INPUT) REQUIRED: 00009620
C 00009630
C HAKTOL = REQUESTED HANKEL TRANSFORM (ZLAG) TOLERANCE. 00009640
C USE HAKTOL.LE.1.E-6*EPS, EPS=ACTUAL HANKEL REL. ERROR. 00009650
C FINTOL = REQUESTED FINITE INTEGRAL (CANC4) TOLERANCE. 00009660
C USE FINTOL.LE.1.E-3*EP, EP=ACTUAL FINITE REL. ERROR. 00009670
C INTYPE = INTEGRATION TYPE FOR CANC4 (NORMALLY, INTYPE=2 OR 4). 00009680
C NFIN = 1 TO USE 1-PASS ZLAG, =2 FOR 2-PASS, ETC. 00009690
C NOTE: NFIN.GT.1 TAKES 'NFIN TIMES' AS LONG TO RUN, BUT 00009700

```

		WILL GIVE ADDITIONAL ACCURACY, IF NEEDED.	00009710
C	MEV	= MAX. FUNCT EVAL'S FOR CANC4 (NORMALLY MEV>300)	00009720
C	R1	= MAX SPACING FROM WIRE END TO RECEIVER POINT (XX,YY)	00009730
C		= SQRT((XX+L)**2+YY*YY)	00009740
C	R2	= MIN SPACING FROM WIRE END TO RECEIVER POINT (XX,YY)	00009750
C		= SQRT((XX-L)**2+YY*YY)	00009760
C	R0	= SPACING FROM WIRE CENTER TO RECEIVER POINT (XX,YY)	00009770
C		= SQRT(XX*XX+YY*YY)	00009780
C	D(9)	= THICKNESS OF M-LAYERS IN MODEL. (METERS)	00009790
C	K(10)	= CONDUCTIVITY RATIO SIG(I)/SIG(1)	00009800
C		FOR I=1,M	00009810
C	M	= NO. LAYERS IN MODEL (M.GE.1.AND.M.LT.10)	00009820
C			00009830
	COMMON/FINERR/HAKTOL,FINTOL,INTYPE,NFIN,NEV,MEV,ESUM,LW		00009840
	COMMON/SPLN80/FDR(80),AR(80),BR(80),CR(80),DR(80),ER(80),		00009850
	& FDI(80),AI(80),BI(80),CI(80),DI(80),EI(80),RLM1,DELRLM,NB		00009860
	COMMON/FIN/R1,R2,R0,L,SIG1,X,Y		00009870
	COMMON/THICK/D(9)		00009880
	COMMON/MODEL/K(10),DD(9),M		00009890
	COMMON/CONST/DEL,DEL2,Z2DEL3		00009900
	REAL L,K		00009910
	COMPLEX FUNC,ESUM,FD,FUNINT,CANC4,Z2DEL3		00009920
	EXTERNAL FUNINT		00009930
C	ISIZE IS THE MAXIMUM POSSIBLE NUMBER OF NODES IN QUINTIC SPLINE.		00009940
	DATA ISIZE/80/		00009950
	DEL=R0/SQRT(BFIN)		00009960
	DEL2=DEL*DEL		00009970
	Z2DEL3=CMPLX(0.0,2./((DEL2*DEL))		00009980
	M1=M-1		00009990
	DO 1 I=1,M1		00010000
1	DD(I)=2.*D(I)/DEL		00010010
	BMAX=R1/DEL		00010020
	BMIN=R2/DEL		00010030
	IF(X.LE.L) BMIN=Y/DEL		00010040
	NB=AIN(5.*ALOG(BMAX/BMIN))+2		00010050
	NB=MAX(NB,3)		00010060
	X0=ALOG(BMIN)+NB*0.2		00010070
	NB=NB+3		00010080
	NRMAX=ISIZE/NB		00010090
	IF(NFIN.LE.NRMAX) GO TO 3		00010100
	IF(NRMAX.GT.0.0) GO TO 2		00010110
	PRINT, 'ERROR IN FINITE: INSUFFICIENT SPLINE NODES'		00010120
	STOP		00010130
2	NFIN=NRMAX		00010140
	PRINT, 'ERROR IN FINITE: NFIN TOO LARGE, RESET TO ',NFIN		00010150
3	DELRLM=.2/FLOAT(NFIN)		00010160
	X0=X0-DELRLM		00010170
	DO 5 ITIME=1,NFIN		00010180
	NEW=1		00010190
	X0=X0+DELRLM		00010200
	DO 5 J=1,NB		00010210
	I=(NB+1)-J		00010220

```

I=NFIN*(I-1)+ITIME                                00010230
XX=X0-0.2*J                                         00010240
BM=EXP(XX)                                           00010250
RM=BM*DEL                                            00010260
IF(I.EQ.1) RLM1=ALOG(RM)                           00010270
FD=FUNC(BM,NEW,RM)                                 00010280
FDR(I)=REAL(FD)                                     00010290
FDI(I)=AIMAG(FD)                                    00010300
5 NEW=0                                              00010310
NB=NFIN*NB                                           00010320
CALL QUINT(NB,FDR,AR,BR,CR,DR,ER)                 00010330
CALL QUINT(NB,FDI,AI,BI,CI,DI,EI)                 00010340
IF(X.LT.L) GO TO 8                                  00010350
FINITE=CANC4(X-L,X+L,FINTOL,NEV,INTYPE,FUNINT,MEV,ESUM) 00010360
GO TO 10                                             00010370
8 FINITE=2.*CANC4(0.,ABS(X-L),FINTOL,NEV,INTYPE,FUNINT,MEV,ESUM) 00010380
IF(X.EQ.0.0) GO TO 10                               00010390
FINITE=FINITE+CANC4(ABS(X-L),X+L,FINTOL,NEV,INTYPE,FUNINT,MEV,
& ESUM)                                             00010400
10 RETURN                                           00010410
END                                                  00010420
                                                    00010430

COMPLEX FUNCTION ZHY(B,NEW,R)                       00010440
COMPLEX ZLAGH0,Z,I1K1,IKDIF                         00010450
DOUBLE PRECISION B8                                 00010460
EXTERNAL F4                                          00010470
COMMON/PAARM/ISTEP,A1,A2,A3,A4,A5,M,TOL             00010480
COMMON/CONST/DEL,DEL2,Z                           00010490
ZHY=CMPLX(0.0,0.0)                                  00010500
IF(M.EQ.1) GO TO 2                                  00010510
ZHY=ZLAGH0(ALOG(B),F4,TOL,LW,NEW)/B                 00010520
2 B8=0.70710678118654D0*B                           00010530
CALL IKS(B8,I1K1,IKDIF)                             00010540
IF(ISTEP.EQ.0) GO TO 5                              00010550
C REMOVE THE PRIMARY FIELD IF ISTEP=1               00010560
I1K1=I1K1-CMPLX(0.5,0.0)                             00010570
IKDIF=IKDIF-CMPLX(1.0,0.0)                           00010580
5 ZHY=ZHY*CMPLX(1./DEL2,0.0)-(IKDIF-2.*I1K1)/R**2    00010590
RETURN                                              00010600
END                                                  00010610

COMPLEX FUNCTION ZHZ(B,NEW,R)                       00010620
COMPLEX ZLAGH1,HAF,ONE,Z                           00010630
EXTERNAL F4                                          00010640
COMMON/PAARM/ISTEP,A1,A2,A3,A4,A5,M,TOL             00010650
COMMON/CONST/DEL,DEL2,Z                           00010660
DATA ONE/(1.0,0.0)/                                00010670
ZHZ=CMPLX(0.0,0.0)                                  00010680
IF(M.EQ.1) GO TO 2                                  00010690
ZHZ=ZLAGH1(ALOG(B),F4,TOL,LW,NEW)*CMPLX(2./(B*R*DEL2),0.0) 00010700
2 HAF=ONE-(ONE+CMPLX(B,B)+CMPLX(0.0,2.*B*B/3.))*CEXP(CMPLX(-B,-B)) 00010710
ZHZ=ZHZ-HAF*CMPLX(0.0,3./(R**3*B*B))               00010720

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C	REMOVE THE PRIMARY FIELD IF ISTEP=1	00010730
	IF(ISTEP.EQ.1) ZHZ=ZHZ-CMPLX(1./R**3,0.0)	00010740
	RETURN	00010750
	END	00010760
	COMPLEX FUNCTION FUNINT(X)	00010770
C--	COMPLEX FUNCTION INTERPOLATION BY QUINTIC SPLINE VIA	00010780
C	CALL TO 'QPOINT', WHERE THE QUINTIC SPLINE	00010790
C	COEFFICIENTS AR,BR,CR,DR,ER, AI,BI,CI,DI,EI WERE	00010800
C	PREVIOUSLY OBTAINED BY SUBR 'QUINT'.	00010810
C		00010820
	DIMENSION SR(80),AR(80),BR(80),CR(80),DR(80),ER(80),	00010830
	& SI(80),AI(80),BI(80),CI(80),DI(80),EI(80)	00010840
	COMMON/SPLN80/SR,AR,BR,CR,DR,ER,SI,AI,BI,CI,DI,EI,RLM1,DELRLM,NL	00010850
	COMMON/FIN/R1,R2,R0,XL,SIG1,XX,Y	00010860
	R=ALOG(SQRT(X*X+Y*Y))	00010870
	CALL QPOINT(NL,SR,AR,BR,CR,DR,ER,RLM1,DELRLM,R,YR)	00010880
	CALL QPOINT(NL,SI,AI,BI,CI,DI,EI,RLM1,DELRLM,R,YI)	00010890
	FUNINT=CMPLX(YR,YI)	00010900
	RETURN	00010910
	END	00010920
	COMPLEX FUNCTION I1K1(B8)	00010930
C--	COMPUTE MODIFIED BESSEL FUNCTION PRODUCT I1*K1 FOR	00010940
C	PARAMETERS	00010950
C	B8 = DOUBLE PRECISION ARGUMENT (=B/DSQRT(2.0D0) HERE)	00010960
C	I1K1 = I1*K1 COMPLEX RESULT	00010970
C		00010980
C--	SUBR KELVIN CALLED AND D.P. USED BEFORE CMPLX*ING	00010990
C		00011000
	COMPLEX Z,Z2,TERM1	00011010
	DOUBLE PRECISION B8,BB(8),Q1,Q2	00011020
	IF(B8.GT.20.0D0) GO TO 1	00011030
	CALL KELVIN(B8,8,BB)	00011040
	Q1=-BB(6)*BB(8)+BB(5)*BB(7)	00011050
	Q2= BB(5)*BB(8)+BB(6)*BB(7)	00011060
	I1K1=CMPLX(SNGL(Q1),SNGL(Q2))	00011070
	RETURN	00011080
1	B=0.70710678*SNGL(B8)	00011090
	Z=CMPLX(B,B)	00011100
	K=-1	00011110
	Z2=4.*Z*Z	00011120
	TERM1=CMPLX(1.0,0.0)	00011130
	I1K1=TERM1	00011140
2	K=K+2	00011150
	COM=-K/(Z2*(K+1))	00011160
	TERM1=TERM1*COM*(4.-K*K)	00011170
	I1K1=I1K1+TERM1	00011180
	IF(CABS(TERM1)/CABS(I1K1).GT.1.E-6) GO TO 2	00011190
	I1K1=I1K1/(2.*Z)	00011200
	RETURN	00011210
	END	00011220

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SUBROUTINE SPLINI(M,H,X,Y,A,B,C,IT,D,P,S)                                00011230
C--ONE DIMENSIONAL CUBIC SPLINE COEFFICIENT DETERMINATION.              00011240
C                                                                           00011250
C    BY W.L.ANDERSON, U.S. GEOLOGICAL SURVEY, DENVER, COLORADO          00011260
C                                                                           00011270
C  PARMS--- M= NUMBER OF DATA POINTS .GT. 2                            00011280
C            H= EQUAL INTERVAL OPTION WHEN H.GT.0. (USE DUMMY X HERE),    00011290
C            UNEQUAL INTERVALS IF H=0. (X REQUIRED STORAGE)                00011300
C            X= INDEP.VAR WHEN H=0. (DIM .GE. M).                        00011310
C            Y= DEPENDENT VARIABLE (DIM .GE. M).                        00011320
C            A,B,C=COEFF.ARRAYS (EACH DIM .GE. M)                        00011330
C            RESULTS ARE RETURNED IN 1ST(M-1) ELEMENTS OF A,B,&C.        00011340
C            ALSO USED AS WORK ARRAYS DURING EXECUTION.                  00011350
C            IT= TYPE OF BOUNDARY CONDITION SUPPLIED IN D ARRAY. USE     00011360
C            IT=1 IF 1ST DERIVATIVES GIVEN AT END POINTS, OR            00011370
C            IT=0 IF 2ND DERIVATIVES GIVEN AT END POINTS.                00011380
C            D= BOUNDARY ARRAY (DIM 2) AT POINT 1 AND M RESPECTIVELY.    00011390
C            P,S= WORK ARRAYS (EACH DIM=M).                              00011400
C--ERROR RETURN WITH M=-(ABS(M)) IF ANY FARM OUT OF RANGE.              00011410
C  THE RESULTING CUBIC SPLINE IS OF THE FORM:                            00011420
C    Y=Y(I)+A(I)*(X-X(I))+B(I)*(X-X(I))**2+C(I)*(X-X(I))**3            00011430
C    FOR I=1,2,...,M-1                                                  00011440
C                                                                           00011450
C                                                                           00011460
C    REAL*4  X(1),Y(1),A(1),B(1),C(1),D(2),P(1),S(1),MUL                00011470
C    IF(IT.LT.0.OR.IT.GT.1.OR.H.LT.0..OR.M.LT.3) GO TO 999              00011480
C    N=M-1                                                                00011490
C    IF(IT.EQ.0) GO TO 20                                                 00011500
C--1ST DERIVATIVE BOUNDARIES GIVEN                                       00011510
C    NE=N-1                                                                00011520
C    IF(H) 999,11,1                                                       00011530
C--EQUAL SPACING H .GT. 0. AND IT=1                                     00011540
C    1 HH=3.0/H                                                            00011550
C    DO 2 I=1,NE                                                          00011560
C      B(I)=4.0                                                            00011570
C      C(I)=1.0                                                            00011580
C      A(I)=1.0                                                            00011590
C    2 F(I)=HH*(Y(I+2)-Y(I))                                              00011600
C      F(1)=F(1)-D(1)                                                      00011610
C      F(NE)=F(NE)-D(2)                                                    00011620
C--SOLUTION OF TRIDIAGONAL MATRIX EQ. OF ORDER NE                     00011630
C    3 C(1)=C(1)/B(1)                                                      00011640
C      F(1)=F(1)/B(1)                                                      00011650
C      DO 4 I=2,NE                                                         00011660
C        MUL=1.0/(B(I)-A(I)*C(I-1))                                        00011670
C        C(I)=MUL*C(I)                                                    00011680
C    4 F(I)=MUL*(F(I)-A(I)*F(I-1))                                        00011690
C--OBTAIN SPLINE COEFFICIENTS                                           00011700
C    A(NE+IT)=F(NE)                                                       00011710
C    I=NE-1                                                                00011720
C    5 A(I+IT)=P(I)-C(I)*A(I+IT+1)                                        00011730

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I=I-1	00011740
IF(I,GE,1) GO TO 5	00011750
IF(IT,EQ,0) GO TO 6	00011760
A(1)=D(1)	00011770
A(M)=D(2)	00011780
6 IF(H,EQ,0.) GO TO 14	00011790
HH=1.0/H	00011800
DO 7 I=1,N	00011810
MUL=HH*(Y(I+1)-Y(I))	00011820
B(I)=HH*(3.0*MUL-(A(I+1)+2.0*A(I)))	00011830
7 C(I)=HH*HH*(-2.0*MUL+A(I+1)+A(I))	00011840
RETURN	00011850
C--UNEQUAL SPACING H=0., AND IT=1	00011860
11 DO 12 I=1,N	00011870
12 S(I+1)=X(I+1)-X(I)	00011880
DO 13 I=1,NE	00011890
B(I)=2.0*(S(I+1)+S(I+2))	00011900
C(I)=S(I+1)	00011910
A(I)=S(I+2)	00011920
13 P(I)=3.0*(S(I+1)**2*(Y(I+2)-Y(I+1))+S(I+2)**2*(Y(I+1)-Y(I)))/	00011930
* (S(I+1)*S(I+2))	00011940
P(1)=P(1)-S(3)*D(1)	00011950
P(NE)=P(NE)-S(N)*D(2)	00011960
GO TO 3	00011970
14 DO 15 I=1,N	00011980
HH=1.0/S(I+1)	00011990
MUL=(Y(I+1)-Y(I))*HH**2	00012000
B(I)=3.0*MUL-(A(I+1)+2.0*A(I))*HH	00012010
15 C(I)=-2.0*MUL*HH+(A(I+1)+A(I))*HH**2	00012020
RETURN	00012030
C--2ND DERIVATIVE BOUNDARIES GIVEN	00012040
20 NE=N+1	00012050
IF(H) 999,31,21	00012060
C--EQUAL SPACING H .GT. 0 AND IT=0	00012070
21 HH=3.0/H	00012080
DO 22 I=2,N	00012090
B(I)=4.0	00012100
C(I)=1.0	00012110
A(I)=1.0	00012120
22 P(I)=HH*(Y(I+1)-Y(I-1))	00012130
B(1)=2.0	00012140
B(NE)=2.0	00012150
C(1)=1.0	00012160
C(NE)=1.0	00012170
A(NE)=1.0	00012180
P(1)=HH*(Y(2)-Y(1))-0.5*H*D(1)	00012190
P(NE)=HH*(Y(M)-Y(N))+0.5*H*D(2)	00012200
GO TO 3	00012210
C--UNEQUAL SPACING H=0 AND IT=0	00012220
31 DO 32 I=1,N	00012230
32 S(I+1)=X(I+1)-X(I)	00012240
N1=N-1	00012250

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DO 33 I=1,N1                                00012260
B(I+1)=2.0*(S(I+1)+S(I+2))                  00012270
C(I+1)=S(I+1)                                00012280
A(I+1)=S(I+2)                                00012290
33 P(I+1)=3.0*(S(I+1)**2*(Y(I+2)-Y(I+1))+S(I+2)**2*(Y(I+1)-Y(I)))/ 00012300
*      (S(I+1)*S(I+2))                      00012310
B(1)=2.0                                    00012320
B(NE)=2.0                                    00012330
C(1)=1.0                                    00012340
C(NE)=1.0                                    00012350
A(NE)=1.0                                    00012360
P(1)=3.0*(Y(2)-Y(1))/S(2)-0.5*S(2)*D(1)    00012370
P(NE)=3.0*(Y(M)-Y(N))/S(M)+0.5*S(M)*D(2)    00012380
GO TO 3                                       00012390
999 M=-IABS(M)                              00012400
RETURN                                       00012410
END                                           00012420

      COMPLEX FUNCTION ZLAGHO(X,FUN,TOL,L,NEW) 00012430
C---*** A SPECIAL LAGGED* CONVOLUTION METHOD TO COMPUTE THE 00012440
C INTEGRAL FROM 0 TO INFINITY OF 'FUN(G)*JO(G*B)*DG' DEFINED AS THE 00012450
C COMPLEX HANKEL TRANSFORM OF ORDER 0 AND ARGUMENT X(=ALOG(B)) 00012460
C BY CONVOLUTION FILTERING WITH COMPLEX FUNCTION 'FUN'---AND 00012470
C USING A VARIABLE CUT-OFF METHOD WITH EXTENDED FILTER TAILS... 00012480
C                                           00012490
C---REF: ANDERSON, W.L., 1975, NTIS REPT. PB-242-800. 00012500
C                                           00012510
C---PARAMETERS: 00012520
C                                           00012530
C      * X      = REAL ARGUMENT(=ALOG(B) AT CALL) OF THE HANKEL TRANSFORM 00012540
C                  'ZLAGHO' IS USEFUL ONLY WHEN X=(LAST X)-.20 *** I.E., 00012550
C                  SPACED SAME AS FILTER USED---IF THIS IS NOT CONVENIENT, 00012560
C                  THEN SUBPROGRAM 'ZHANKO' IS ADVISED FOR GENERAL USE. 00012570
C                  (ALSO SEE PARM 'NEW' & NOTES (2)-(4) BELOW). 00012580
C      FUN(G)= EXTERNAL DECLARED COMPLEX FUNCTION NAME (USER SUPPLIED) 00012590
C                  OF A REAL ARGUMENT G. 00012600
C      NOTE: IF PARMS OTHER THAN G ARE REQUIRED, USE COMMON IN 00012610
C                  CALLING PROGRAM AND IN SUBPROGRAM FUN. 00012620
C                  THE COMPLEX FUNCTION FUN SHOULD BE A MONOTONE 00012630
C                  DECREASING FUNCTION AS THE ARGUMENT G BECOMES LARGE... 00012640
C                  FOR REAL-ONLY FUNCTIONS, SUBPROGRAM 'RLAGHO' IS ADVISED; 00012650
C                  HOWEVER, TWO REAL-FUNCTIONS F1(G),F2(G) MAY BE 00012660
C                  INTEGRATED IN PARALLEL BY WRITING FUN=CMPLX(F1(G),F2(G)) 00012670
C      TOL=      REAL TOLERANCE EXCEPTED AT CONVOLVED TAILS---I.E., 00012680
C                  IF FILTER*FUN<TOL*MAX, THEN REST OF TAIL IS TRUNCATED. 00012690
C                  THIS IS DONE AT BOTH ENDS OF FILTER.  TYPICALLY, 00012700
C                  TOL <= .0001 IS USUALLY OK---BUT THIS DEPENDS ON 00012710
C                  THE FUNCTION FUN AND PARAMETER X...IN GENERAL, 00012720
C                  A 'SMALLER TOL' WILL USUALLY RESULT IN 'MORE ACCURACY' 00012730
C                  BUT WITH 'MORE WEIGHTS' BEING USED.  TOL IS NOT DIRECTLY 00012740
C                  RELATED TO TRUNCATION ERROR, BUT GENERALLY SERVES AS AN 00012750
C                  APPROXIMATION INDICATOR... FOR VERY LARGE OR SMALL B, 00012760

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C      ONE SHOULD USE A SMALLER TOL THAN RECOMMENDED ABOVE... 00012770
C      L=      RESULTING NO. FILTER WTS. USED IN THE VARIABLE 00012780
C              CONVOLUTION (L DEPENDS ON TOL AND FUN). 00012790
C      MIN.L=20 AND MAX.L=193--WHICH COULD 00012800
C              OCCUR IF TOL IS VERY SMALL AND/OR FUN NOT DECREASING 00012810
C              VERY FAST... 00012820
C      * NEW= 1 IS NECESSARY 1ST TIME OR BRAND NEW X. 00012830
C              0 FOR ALL SUBSEQUENT CALLS WHERE X=(LAST X)-0.20 00012840
C              IS ASSUMED INTERNALLY BY THIS ROUTINE. 00012850
C              NOTE: IF THIS IS NOT TRUE, ROUTINE WILL 00012860
C              STILL ASSUME X=(LAST X)-0.20 ANYWAY... 00012870
C              IT IS THE USERS RESPONSIBILITY TO NORMALIZE 00012880
C              BY CORRECT B=EXP(X) OUTSIDE OF CALL (SEE USAGE BELOW). 00012890
C      THE LAGGED CONVOLUTION METHOD PICKS UP SIGNIFICANT 00012900
C      TIME IMPROVEMENTS WHEN THE KERNEL IS NOT A 00012910
C      SIMPLE ELEMENTARY FUNCTION...DUE TO INTERNALLY SAVING 00012920
C      ALL KERNEL FUNCTION EVALUATIONS WHEN NEW=1... 00012930
C      THEN WHEN NEW=0, ALL PREVIOUSLY CALCULATED 00012940
C      KERNELS WILL BE USED IN THE LAGGED CONVOLUTION 00012950
C      WHERE POSSIBLE, ONLY ADDING NEW KERNEL EVALUATIONS 00012960
C      WHEN NEEDED (DEPENDS ON PARMS TOL AND FUN) 00012970
C 00012980
C--THE RESULTING COMPLEX CONVOLUTION SUM IS GIVEN IN ZLAGH0; THE HANKEL 00012990
C TRANSFORM IS THEN ZLAGH0/B WHICH IS TO BE COMPUTED AFTER EXIT FROM 00013000
C THIS ROUTINE.... WHERE B=EXP(X), X=ARGUMENT USED IN CALL... 00013010
C 00013020
C--USAGE-- 'ZLAGH0' IS CALLED AS FOLLOWS: 00013030
C ... 00013040
C COMPLEX Z,ZLAGH0,ZF 00013050
C EXTERNAL ZF 00013060
C ... 00013070
C Z=ZLAGH0(ALOG(B),ZF,TOL,L,NEW)/B 00013080
C ... 00013090
C END 00013100
C COMPLEX FUNCTION ZF(G) 00013110
C ...USER SUPPLIED CODE... 00013120
C END 00013130
C 00013140
C--NOTES: 00013150
C (1). EXP-UNDERFLOW'S MAY OCCUR IN EXECUTING THE SUBPROGRAM 00013160
C BELOW; HOWEVER, THIS IS OK PROVIDED THE MACHINE SYSTEM SETS 00013170
C ANY & ALL EXP-UNDERFLOW'S TO 0.0.... 00013180
C (2). AS AN AID TO UNDERSTANDING & USING THE LAGGED CONVOLUTION 00013190
C METHOD, LET BMAX>=BMIN>0 BE GIVEN. THEN IT CAN BE SHOWN 00013200
C THAT THE ACTUAL NUMBER OF B'S IS NB=AIN(5.*ALOG(BMAX/BMIN))+1, 00013210
C PROVIDED BMAX/BMIN>=1. THE USER MAY THEN ASSUME AN 'ADJUSTED' 00013220
C BMINA=BMAX*EXP(-.2*(NB-1)). THE METHOD GENERATES THE DECREASING 00013230
C ARGUMENTS SPACED AS X=ALOG(BMAX),X-.2,X-.2*2,...,ALOG(BMINA), 00013240
C FOR EXAMPLE, ONE MAY CONTROL THIS WITH THE CODE: 00013250
C ... 00013260
C NB=AIN(5.*ALOG(BMAX/BMIN))+1 00013270
C NB1=NB+1 00013280

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C      X0=ALOG(BMAX)+.2      00013290
C      NEW=1      00013300
C      DO 1 J=1,NB      00013310
C      I=NB1-J      00013320
C      X=X0-.2*J      00013330
C      ARG(I)=EXP(X)      00013340
C      Z(I)=ZLAGH(X,ZF,TOL,L,NEW)/ARG(I)      00013350
C      1      NEW=0      00013360
C      ***      00013370
C      (3). IF RESULTS ARE STORED IN ARRAYS ARG(I),Z(I),I=1,NB FOR      00013380
C      ARG IN (BMINA,BMAX), THEN THESE ARRAYS MAY BE USED, FOR EXAMPLE,      00013390
C      TO SPLINE-INTERPOLATE AT A DIFFERENT (LARGER OR SMALLER)      00013400
C      SPACING THAN USED IN THE LAGGED CONVOLUTION METHOD.      00013410
C      (4). IF A DIFFERENT RANGE OF B IS DESIRED, THEN ONE MAY      00013420
C      ALWAYS RESTART THE ABOVE PROCEDURE IN (2) WITH A NEW      00013430
C      BMAX,BMIN AND BY SETTING NEW=1,...      00013440
C      (5). ABSCISSA CORRESPONDING TO WEIGHT IS GENERATED TO SAVE STORAGE      00013450
C      00013460
C      00013470
C      COMPLEX FUN,C,CMAX,SAVE      00013480
C      DIMENSION KEY(193),SAVE(193),T(2),TMAX(2)      00013490
C      DIMENSION YT(193),Y1(76),Y2(76),Y3(41)      00013500
C      EQUIVALENCE (C,T(1)),(CMAX,TMAX(1))      00013510
C      EQUIVALENCE (YT(1),Y1(1)),(YT(77),Y2(1)),(YT(153),Y3(1))      00013520
C--JO--EXTENDED FILTER WEIGHT ARRAYS:      00013530
C      DATA Y1/      00013540
C      1 5.8565723E-08, 7.1143477E-11,-7.8395565E-11, 8.7489547E-11,      00013550
C      2-8.9007811E-11, 9.8790055E-11,-9.8675347E-11, 1.1118797E-10,      00013560
C      3-1.0893474E-10, 1.2543400E-10,-1.1979399E-10, 1.4200767E-10,      00013570
C      4-1.3106341E-10, 1.6153229E-10,-1.4238602E-10, 1.8486236E-10,      00013580
C      5-1.5315381E-10, 2.1319755E-10,-1.6238115E-10, 2.4824144E-10,      00013590
C      6-1.6850378E-10, 2.9243813E-10,-1.6909302E-10, 3.4934366E-10,      00013600
C      7-1.6043759E-10, 4.2417082E-10,-1.3690001E-10, 5.2458440E-10,      00013610
C      8-8.9946096E-11, 6.6188220E-10,-6.6964033E-12, 8.5276151E-10,      00013620
C      9 1.3222770E-10, 1.1219600E-09, 3.5591442E-10, 1.5061956E-09,      00013630
C      1 7.0795382E-10, 2.0600379E-09, 1.2535947E-09, 2.8646623E-09,      00013640
C      2 2.0904225E-09, 4.0409101E-09, 3.3642886E-09, 5.7687700E-09,      00013650
C      3 5.2930786E-09, 8.3164338E-09, 8.2021809E-09, 1.2083635E-08,      00013660
C      4 1.2577400E-08, 1.7666303E-08, 1.9143895E-08, 2.5953011E-08,      00013670
C      5 2.8983953E-08, 3.8268851E-08, 4.3712685E-08, 5.6590075E-08,      00013680
C      6 6.5740136E-08, 8.3864288E-08, 9.8662323E-08, 1.2448811E-07,      00013690
C      7 1.4784461E-07, 1.8501974E-07, 2.2129198E-07, 2.7524203E-07,      00013700
C      8 3.3094739E-07, 4.0974828E-07, 4.9462868E-07, 6.1030809E-07,      00013710
C      9 7.3891802E-07, 9.0939667E-07, 1.1034727E-06, 1.3554600E-06,      00013720
C      1 1.6474556E-06, 2.0207696E-06, 2.4591294E-06, 3.0131400E-06/      00013730
C      DATA Y2/      00013740
C      1 3.6701680E-06, 4.4934101E-06, 5.4770076E-06, 6.7015208E-06,      00013750
C      2 8.1726989E-06, 9.9954201E-06, 1.2194425E-05, 1.4909101E-05,      00013760
C      3 1.8194388E-05, 2.2239184E-05, 2.7145562E-05, 3.3174088E-05,      00013770
C      4 4.0499452E-05, 4.9486730E-05, 6.0421440E-05, 7.3822001E-05,      00013780
C      5 9.0141902E-05, 1.1012552E-04, 1.3448017E-04, 1.6428337E-04,      00013790
C      6 2.0062570E-04, 2.4507680E-04, 2.9930366E-04, 3.6560582E-04,      00013800

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7 4.4651421E-04, 5.4541300E-04, 6.6612648E-04, 8.1365181E-04, 00013810
8 9.9374786E-04, 1.2138120E-03, 1.4824945E-03, 1.8107657E-03, 00013820
9 2.2115938E-03, 2.7012675E-03, 3.2991969E-03, 4.0295817E-03, 00013830
1 4.9214244E-03, 6.0106700E-03, 7.3405529E-03, 8.9643708E-03, 00013840
2 1.0946310E-02, 1.3365017E-02, 1.6314985E-02, 1.9910907E-02, 00013850
3 2.4289325E-02, 2.9612896E-02, 3.6070402E-02, 4.3876936E-02, 00013860
4 5.3264829E-02, 6.4465091E-02, 7.7664144E-02, 9.2918324E-02, 00013870
5 1.1000121E-01, 1.2811102E-01, 1.4543025E-01, 1.5832248E-01, 00013880
6 1.6049224E-01, 1.4170064E-01, 8.8788108E-02, -1.1330934E-02, 00013890
7 -1.5331864E-01, -2.9094670E-01, -2.9084655E-01, -2.9708834E-02, 00013900
8 3.9009601E-01, 1.7999785E-01, -4.1858139E-01, 1.5317216E-01, 00013910
9 6.5184953E-02, -1.0751806E-01, 7.8429567E-02, -4.6019124E-02, 00013920
1 2.5309571E-02, -1.3904823E-02, 7.8187120E-03, -4.5190369E-03/ 00013930
  DATA Y3/ 00013940
1 2.6729062E-03, -1.6073718E-03, 9.7715622E-04, -5.9804407E-04, 00013950
2 3.6749320E-04, -2.2635296E-04, 1.3960805E-04, -8.6172618E-05, 00013960
3 5.3212947E-05, -3.2867888E-05, 2.0304203E-05, -1.2543926E-05, 00013970
4 7.7499633E-06, -4.7882430E-06, 2.9584108E-06, -1.8278645E-06, 00013980
5 1.1293571E-06, -6.9778174E-07, 4.3113019E-07, -2.6637753E-07, 00013990
6 1.6458373E-07, -1.0168954E-07, 6.2829807E-08, -3.8819969E-08, 00014000
7 2.3985272E-08, -1.4819520E-08, 9.1563774E-09, -5.6573541E-09, 00014010
8 3.4954514E-09, -2.1597005E-09, 1.3343946E-09, -8.2447148E-10, 00014020
9 5.0941033E-10, -3.1474631E-10, 1.9447072E-10, -1.2015685E-10, 00014030
1 7.4241055E-11, -4.5871468E-11, 2.8343095E-11, -1.7513137E-11, 00014040
2 6.9049613E-12/ 00014050
C--$$ENDATA 00014060
C 00014070
  IF(NEW) 10,30,10 00014080
10 LAG=-1 00014090
  X0=-X-26.30455704 00014100
  DO 20 IR=1,193 00014110
20 KEY(IR)=0 00014120
30 LAG=LAG+1 00014130
  ZLAGH0=(0.0,0.0) 00014140
  CMAX=(0.0,0.0) 00014150
  L=0 00014160
  ASSIGN 110 TO M 00014170
  I=129 00014180
  GO TO 200 00014190
110 TMAX(1)=AMAX1(ABS(T(1)),TMAX(1)) 00014200
  TMAX(2)=AMAX1(ABS(T(2)),TMAX(2)) 00014210
  I=I+1 00014220
  IF(I.LE.146) GO TO 200 00014230
  IF(TMAX(1).EQ.0.0.AND.TMAX(2).EQ.0.0) GO TO 150 00014240
  CMAX=TOL*CMAX 00014250
  ASSIGN 120 TO M 00014260
  I=128 00014270
  GO TO 200 00014280
120 IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 130 00014290
  I=I-1 00014300
  IF(I.GT.0) GO TO 200 00014310
130 ASSIGN 140 TO M 00014320

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      I=147                                00014330
      GO TO 200                            00014340
140   IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 190 00014350
      I=I+1                                00014360
      IF(I.LE.193) GO TO 200               00014370
      GO TO 190                            00014380
150   ASSIGN 160 TO M                      00014390
      I=1                                  00014400
      GO TO 200                            00014410
160   IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 170 00014420
      I=I+1                                00014430
      IF(I.LE.128) GO TO 200              00014440
170   ASSIGN 180 TO M                      00014450
      I=193                                00014460
      GO TO 200                            00014470
180   IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 190 00014480
      I=I-1                                00014490
      IF(I.GE.147) GO TO 200              00014500
190   RETURN                              00014510
C--STORE/RETRIEVE ROUTINE (DONE INTERNALLY TO SAVE CALL'S) 00014520
200   LOOK=I+LAG                           00014530
      IQ=LOOK/194                           00014540
      IR=MOD(LOOK,194)                     00014550
      IF(IR.EQ.0) IR=1                     00014560
      IROLL=IQ*193                         00014570
      IF(KEY(IR).LE.IROLL) GO TO 220       00014580
210   C=SAVE(IR)*YT(I)                     00014590
      ZLAGH0=ZLAGH0+C                      00014600
      L=L+1                                00014610
      GO TO M,(110,120,140,160,180)       00014620
220   KEY(IR)=IROLL+IR                     00014630
      SAVE(IR)=FUN(EXP(X0+FLOAT(LOOK)*.20)) 00014640
      GO TO 210                            00014650
      END                                  00014660

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      COMPLEX FUNCTION ZLAGH1(X,FUN,TOL,L,NEW) 00014670
C--*** A SPECIAL LAGGED* CONVOLUTION METHOD TO COMPUTE THE 00014680
C  INTEGRAL FROM 0 TO INFINITY OF 'FUN(G)*J1(G*B)*DG' DEFINED AS THE 00014690
C  COMPLEX HANKEL TRANSFORM OF ORDER 1 AND ARGUMENT X(=ALOG(B)) 00014700
C  BY CONVOLUTION FILTERING WITH COMPLEX FUNCTION 'FUN'--AND 00014710
C  USING A VARIABLE CUT-OFF METHOD WITH EXTENDED FILTER TAILS... 00014720
C  00014730
C--REF: ANDERSON, W.L., 1975, NTIS REPT. PB-242-800. 00014740
C  00014750
C--PARAMETERS: 00014760
C  00014770
C    * X      = REAL ARGUMENT(=ALOG(B) AT CALL) OF THE HANKEL TRANSFORM 00014780
C               'ZLAGH1' IS USEFUL ONLY WHEN X=(LAST X)-.20 *** I.E., 00014790
C               SPACED SAME AS FILTER USED--IF THIS IS NOT CONVENIENT, 00014800
C               THEN SUBPROGRAM 'ZHANK1' IS ADVISED FOR GENERAL USE. 00014810
C               (ALSO SEE PARM 'NEW' & NOTES (2)-(3) BELOW), 00014820
C    FUN(G)= EXTERNAL DECLARED COMPLEX FUNCTION NAME (USER SUPPLIED) 00014830

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C      OF A REAL ARGUMENT G.                                00014840
C      NOTE: IF PARMS OTHER THAN G ARE REQUIRED, USE COMMON IN 00014850
C      CALLING PROGRAM AND IN SUBPROGRAM FUN.                00014860
C      THE COMPLEX FUNCTION FUN SHOULD BE A MONOTONE         00014870
C      DECREASING FUNCTION AS THE ARGUMENT G BECOMES LARGE... 00014880
C      FOR REAL-ONLY FUNCTIONS, SUBPROGRAM 'RLAGH1' IS ADVISED; 00014890
C      HOWEVER, TWO REAL-FUNCTIONS F1(G),F2(G) MAY BE         00014900
C      INTEGRATED IN PARALLEL BY WRITING FUN=CMPLX(F1(G),F2(G)) 00014910
C      TOL= REAL TOLERANCE EXCEPTED AT CONVOLVED TAILS--I.E., 00014920
C      IF FILTER*FUN<TOL*MAX, THEN REST OF TAIL IS TRUNCATED. 00014930
C      THIS IS DONE AT BOTH ENDS OF FILTER. TYPICALLY,        00014940
C      TOL <= .0001 IS USUALLY OK--BUT THIS DEPENDS ON        00014950
C      THE FUNCTION FUN AND PARAMETER X...IN GENERAL,          00014960
C      A 'SMALLER TOL' WILL USUALLY RESULT IN 'MORE ACCURACY' 00014970
C      BUT WITH 'MORE WEIGHTS' BEING USED. TOL IS NOT DIRECTLY 00014980
C      RELATED TO TRUNCATION ERROR, BUT GENERALLY SERVES AS AN 00014990
C      APPROXIMATION INDICATOR... FOR VERY LARGE OR SMALL B,    00015000
C      ONE SHOULD USE A SMALLER TOL THAN RECOMMENDED ABOVE... 00015010
C      L= RESULTING NO. FILTER WTS. USED IN THE VARIABLE       00015020
C      CONVOLUTION (L DEPENDS ON TOL AND FUN).                 00015030
C      MIN.L=15 AND MAX.L=236--WHICH COULD                    00015040
C      OCCUR IF TOL IS VERY SMALL AND/OR FUN NOT DECREASING   00015050
C      VERY FAST...                                            00015060
C      * NEW= 1 IS NECESSARY 1ST TIME OR BRAND NEW X.          00015070
C      0 FOR ALL SUBSEQUENT CALLS WHERE X=(LAST X)-0.20        00015080
C      IS ASSUMED INTERNALLY BY THIS ROUTINE.                  00015090
C      NOTE: IF THIS IS NOT TRUE, ROUTINE WILL                 00015100
C      STILL ASSUME X=(LAST X)-0.20 ANYWAY...                  00015110
C      IT IS THE USERS RESPONSIBILITY TO NORMALIZE             00015120
C      BY CORRECT B=EXP(X) OUTSIDE OF CALL (SEE USAGE BELOW). 00015130
C      THE LAGGED CONVOLUTION METHOD PICKS UP SIGNIFICANT       00015140
C      TIME IMPROVEMENTS WHEN THE KERNEL IS NOT A             00015150
C      SIMPLE ELEMENTARY FUNCTION...DUE TO INTERNALLY SAVING   00015160
C      ALL KERNEL FUNCTION EVALUATIONS WHEN NEW=1...          00015170
C      THEN WHEN NEW=0, ALL PREVIOUSLY CALCULATED              00015180
C      KERNELS WILL BE USED IN THE LAGGED CONVOLUTION          00015190
C      WHERE POSSIBLE, ONLY ADDING NEW KERNEL EVALUATIONS      00015200
C      WHEN NEEDED (DEPENDS ON PARMS TOL AND FUN)              00015210
C      00015220
C      C--THE RESULTING COMPLEX CONVOLUTION SUM IS GIVEN IN ZLAGH1; THE HANKEL 00015230
C      TRANSFORM IS THEN ZLAGH1/B WHICH IS TO BE COMPUTED AFTER EXIT FROM 00015240
C      THIS ROUTINE.... WHERE B=EXP(X), X=ARGUMENT USED IN CALL... 00015250
C      00015260
C      C--USAGE-- 'ZLAGH1' IS CALLED AS FOLLOWS:              00015270
C      ...                                                      00015280
C      COMPLEX Z,ZLAGH1,ZF                                       00015290
C      EXTERNAL ZF                                               00015300
C      ...                                                      00015310
C      Z=ZLAGH1(ALOG(B),ZF,TOL,L,NEW)/B                          00015320
C      ...                                                      00015330
C      END                                                       00015340
C      COMPLEX FUNCTION ZF(G)                                    00015350

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C      ...USER SUPPLIED CODE...                                00015360
C      END                                                        00015370
C                                                                00015380
C--NOTES:                                                         00015390
C      (1). EXP-UNDERFLOW'S MAY OCCUR IN EXECUTING THE SUBPROGRAM 00015400
C      BELOW; HOWEVER, THIS IS OK PROVIDED THE MACHINE SYSTEM SETS 00015410
C      ANY & ALL EXP-UNDERFLOW'S TO 0.0....                     00015420
C      (2). AS AN AID TO UNDERSTANDING & USING THE LAGGED CONVOLUTION 00015430
C      METHOD, LET BMAX>=BMIN>0 BE GIVEN. THEN IT CAN BE SHOWN     00015440
C      THAT THE ACTUAL NUMBER OF B'S IS NB=AIN(5.*ALOG(BMAX/BMIN))+1, 00015450
C      PROVIDED BMAX/BMIN>=1. THE USER MAY THEN ASSUME AN 'ADJUSTED' 00015460
C      BMINA=BMAX*EXP(-.2*(NB-1)). THE METHOD GENERATES THE DECREASING 00015470
C      ARGUMENTS SPACED AS X=ALOG(BMAX),X-.2,X-.2*2,...,ALOG(BMINA), 00015480
C      FOR EXAMPLE, ONE MAY CONTROL THIS WITH THE CODE:           00015490
C                                                                00015500
C      ...                                                         00015510
C      NB=AIN(5.*ALOG(BMAX/BMIN))+1                               00015520
C      NB1=NB+1                                                    00015530
C      X0=ALOG(BMAX)+.2                                            00015540
C      NEW=1                                                        00015550
C      DO 1 J=1,NB                                                 00015560
C      I=NB1-J                                                      00015570
C      X=X0-.2*J                                                    00015580
C      ARG(I)=EXP(X)                                                00015590
C      Z(I)=ZLAGH1(X,ZF,TOL,L,NEW)/ARG(I)                         00015600
C      1 NEW=0                                                       00015610
C      ...                                                         00015620
C      (3). IF RESULTS ARE STORED IN ARRAYS ARG(I),Z(I),I=1,NB FOR 00015630
C      ARG IN (BMINA,BMAX), THEN THESE ARRAYS MAY BE USED, FOR EXAMPLE, 00015640
C      TO SPLINE-INTERPOLATE AT A DIFFERENT (LARGER OR SMALLER)     00015650
C      SPACING THAN USED IN THE LAGGED CONVOLUTION METHOD.          00015660
C      (4). IF A DIFFERENT RANGE OF B IS DESIRED, THEN ONE MAY     00015670
C      ALWAYS RESTART THE ABOVE PROCEDURE IN (2) WITH A NEW        00015680
C      BMAX,BMIN AND BY SETTING NEW=1....                          00015690
C      (5). ABSCISSA CORRESPONDING TO WEIGHT IS GENERATED TO SAVE STORAGE 00015700
C                                                                00015710
C      COMPLEX FUN,C,CMAX,SAVE                                     00015720
C      DIMENSION KEY(236),SAVE(236),T(2),TMAX(2)                  00015730
C      DIMENSION WT(236),W1(76),W2(76),W3(76),W4(8)              00015740
C      EQUIVALENCE (C,T(1)),(CMAX,TMAX(1))                        00015750
C      EQUIVALENCE (WT(1),W1(1)),(WT(77),W2(1)),(WT(153),W3(1)), 00015760
C      1 (WT(229),W4(1))                                           00015770
C--J1-EXTENDED FILTER WEIGHT ARRAYS:                               00015780
C      DATA W1/                                                    00015790
C      1-8.8863805E-10, 1.1293811E-09,-1.2050872E-09, 1.2696232E-09, 00015800
C      2-1.3223909E-09, 1.3642393E-09,-1.3969439E-09, 1.4225941E-09, 00015810
C      3-1.4427475E-09, 1.4580582E-09,-1.4682563E-09, 1.4732179E-09, 00015820
C      4-1.4735606E-09, 1.4719870E-09,-1.4727091E-09, 1.4828225E-09, 00015830
C      5-1.5102619E-09, 1.5667752E-09,-1.6634522E-09, 1.8172900E-09, 00015840
C      6-2.0412753E-09, 2.3595230E-09,-2.7861077E-09, 3.3592871E-09, 00015850
C      7-4.0940172E-09, 5.0571015E-09,-6.2604109E-09, 7.8269461E-09, 00015860
C      8-9.7514701E-09, 1.2267639E-08,-1.5312389E-08, 1.9339924E-08, 00015870

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9-2.4126297E-08, 3.0576829E-08, -3.8060204E-08, 4.8423732E-08, 00015880
1-6.0051116E-08, 7.6787475E-08, -9.4700993E-08, 1.2192844E-07, 00015890
2-1.4918997E-07, 1.9392737E-07, -2.3464786E-07, 3.0911127E-07, 00015900
3-3.6815394E-07, 4.9413800E-07, -5.7554168E-07, 7.9301529E-07, 00015910
4-8.9502818E-07, 1.2794292E-06, -1.3811469E-06, 2.0789668E-06, 00015920
5-2.1069398E-06, 3.4103188E-06, -3.1584463E-06, 5.6639045E-06, 00015930
6-4.6059955E-06, 9.5561672E-06, -6.4142855E-06, 1.6440205E-05, 00015940
7-8.2010619E-06, 2.8945217E-05, -8.6348466E-06, 5.2317398E-05, 00015950
8-3.9915035E-06, 9.7273612E-05, 1.5220520E-05, 1.8614373E-04, 00015960
9 7.2023760E-05, 3.6620099E-04, 2.2062958E-04, 7.3874539E-04, 00015970
1 5.8623480E-04, 1.5226779E-03, 1.4538718E-03, 3.1930365E-03/ 00015980
DATA W2/ 00015990
1 3.4640868E-03, 6.7790882E-03, 8.0328420E-03, 1.4484339E-02, 00016000
2 1.8201316E-02, 3.0866143E-02, 4.0106549E-02, 6.4527872E-02, 00016010
3 8.4285526E-02, 1.2773175E-01, 1.6020907E-01, 2.1948043E-01, 00016020
4 2.3636305E-01, 2.4895051E-01, 1.2586300E-01, -5.1060445E-02, 00016030
5-3.4376222E-01, -2.9042175E-01, 1.1564736E-01, 4.9253231E-01, 00016040
6-4.6748595E-01, 1.5280945E-01, 3.3348541E-02, -8.2485252E-02, 00016050
7 7.9740630E-02, -6.6934498E-02, 5.5150465E-02, -4.5868721E-02, 00016060
8 3.8651958E-02, -3.2935834E-02, 2.8303994E-02, -2.4475127E-02, 00016070
9 2.1259541E-02, -1.8526278E-02, 1.6182037E-02, -1.4158101E-02, 00016080
1 1.2402225E-02, -1.0873526E-02, 9.5392016E-03, -8.3723743E-03, 00016090
2 7.3506490E-03, -6.4551136E-03, 5.6696335E-03, -4.9803353E-03, 00016100
3 4.3752213E-03, -3.8438703E-03, 3.3772023E-03, -2.9672872E-03, 00016110
4 2.6071877E-03, -2.2908274E-03, 2.0128794E-03, -1.7686706E-03, 00016120
5 1.5540998E-03, -1.3655666E-03, 1.1999089E-03, -1.0543497E-03, 00016130
6 9.2644973E-04, -8.1406593E-04, 7.1531559E-04, -6.2854459E-04, 00016140
7 5.5229955E-04, -4.8530352E-04, 4.2643446E-04, -3.7470650E-04, 00016150
8 3.2925334E-04, -2.8931382E-04, 2.5421910E-04, -2.2338147E-04, 00016160
9 1.9628455E-04, -1.7247455E-04, 1.5155278E-04, -1.3316889E-04, 00016170
1 1.1701502E-04, -1.0282066E-04, 9.0348135E-05, -7.9388568E-05/ 00016180
DATA W3/ 00016190
1 6.9758436E-05, -6.1296474E-05, 5.3860978E-05, -4.7327436E-05, 00016200
2 4.1586435E-05, -3.6541840E-05, 3.2109174E-05, -2.8214208E-05, 00016210
3 2.4791718E-05, -2.1784390E-05, 1.9141864E-05, -1.6819888E-05, 00016220
4 1.4779578E-05, -1.2986765E-05, 1.1411426E-05, -1.0027182E-05, 00016230
5 8.8108499E-06, -7.7420630E-06, 6.8029235E-06, -5.9777053E-06, 00016240
6 5.2525892E-06, -4.6154325E-06, 4.0555653E-06, -3.5636118E-06, 00016250
7 3.1313335E-06, -2.7514911E-06, 2.4177236E-06, -2.1244417E-06, 00016260
8 1.8667342E-06, -1.6402859E-06, 1.4413051E-06, -1.2664597E-06, 00016270
9 1.1128220E-06, -9.7781908E-07, 8.5919028E-07, -7.5494920E-07, 00016280
1 6.6335060E-07, -5.8286113E-07, 5.1213358E-07, -4.4998431E-07, 00016290
2 3.9537334E-07, -3.4738689E-07, 3.0522189E-07, -2.6817250E-07, 00016300
3 2.3561831E-07, -2.0701397E-07, 1.8188012E-07, -1.5979545E-07, 00016310
4 1.4038968E-07, -1.2333746E-07, 1.0835294E-07, -9.5185048E-08, 00016320
5 8.3613184E-08, -7.3443411E-08, 6.4505118E-08, -5.6648167E-08, 00016330
6 4.9740428E-08, -4.3665572E-08, 3.8321109E-08, -3.3616717E-08, 00016340
7 2.9472836E-08, -2.5819439E-08, 2.2594957E-08, -1.9745353E-08, 00016350
8 1.7223359E-08, -1.4987869E-08, 1.3003472E-08, -1.1240058E-08, 00016360
9 9.6723739E-09, -8.2794392E-09, 7.0438407E-09, -5.9509676E-09, 00016370
1 4.9882405E-09, -4.1443813E-09, 3.4088114E-09, -2.7712762E-09/ 00016380
DATA W4/ 00016390

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1	2.2217311E-09,-1.7504755E-09, 1.3485207E-09,-1.0080937E-09,	00016400
2	7.2300885E-10,-4.8860666E-10, 3.0121413E-10,-9.1649798E-11/	00016410
C--\$\$ENDATA		00016420
C		00016430
	IF(NEW) 10,30,10	00016440
10	LAG=-1	00016450
	X0=-X-17.0	00016460
	DO 20 IR=1,236	00016470
20	KEY(IR)=0	00016480
30	LAG=LAG+1	00016490
	ZLAGH1=(0.0,0.0)	00016500
	CMAx=(0.0,0.0)	00016510
	L=0	00016520
	ASSIGN 110 TO M	00016530
	I=86	00016540
	GO TO 200	00016550
110	TMAX(1)=AMAX1(ABS(T(1)),TMAX(1))	00016560
	TMAX(2)=AMAX1(ABS(T(2)),TMAX(2))	00016570
	I=I+1	00016580
	IF(I.LE.98) GO TO 200	00016590
	IF(TMAX(1).EQ.0.0.AND.TMAX(2).EQ.0.0) GO TO 150	00016600
	CMAx=TOL*CMAx	00016610
	ASSIGN 120 TO M	00016620
	I=85	00016630
	GO TO 200	00016640
120	IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 130	00016650
	I=I-1	00016660
	IF(I.GT.0) GO TO 200	00016670
130	ASSIGN 140 TO M	00016680
	I=99	00016690
	GO TO 200	00016700
140	IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 190	00016710
	I=I+1	00016720
	IF(I.LE.236) GO TO 200	00016730
	GO TO 190	00016740
150	ASSIGN 160 TO M	00016750
	I=1	00016760
	GO TO 200	00016770
160	IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 170	00016780
	I=I+1	00016790
	IF(I.LE.85) GO TO 200	00016800
170	ASSIGN 180 TO M	00016810
	I=236	00016820
	GO TO 200	00016830
180	IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 190	00016840
	I=I-1	00016850
	IF(I.GE.99) GO TO 200	00016860
190	RETURN	00016870
C--STORE/RETRIEVE ROUTINE (DONE INTERNALLY TO SAVE CALL'S)		00016880
200	LOOK=I+LAG	00016890
	IQ=LOOK/237	00016900
	IR=MOD(LOOK,237)	00016910



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      IF(IR.EQ.0) IR=1                                00016920
      IROLL=IQ*236                                    00016930
      IF(KEY(IR).LE.IROLL) GO TO 220                  00016940
210   C=SAVE(IR)*WT(I)                                00016950
      ZLAGH1=ZLAGH1+C                                00016960
      L=L+1                                            00016970
      GO TO M,(110,120,140,160,180)                  00016980
220   KEY(IR)=IROLL+IR                                00016990
      SAVE(IR)=FUN(EXP(X0+FLOAT(LOOK)*.20))          00017000
      GO TO 210                                       00017010
      END                                             00017020

      COMPLEX FUNCTION ZLAGFO(X,FUN,TOL,L,NEW)          00017030
C---*** A SPECIAL LAGGED* CONVOLUTION METHOD TO COMPUTE THE 00017040
C INTEGRAL FROM 0 TO INFINITY OF 'FUN(G)*COS(G*B)*DG' DEFINED AS THE 00017050
C COMPLEX FOURIER COSINE TRANSFORM WITH ARGUMENT X(=ALOG(B)) 00017060
C BY CONVOLUTION FILTERING WITH COMPLEX FUNCTION 'FUN'---AND 00017070
C USING A VARIABLE CUT-OFF METHOD WITH EXTENDED FILTER TAILS... 00017080
C                                                         00017090
C---REF: ANDERSON, W.L., 1975, NTIS REPT. PB-242-800.    00017100
C                                                         00017110
C---PARAMETERS:                                         00017120
C                                                         00017130
C   * X      = REAL ARGUMENT(=ALOG(B) AT CALL) OF THE FOURIER TRANSFORM 00017140
C               'ZLAGFO' IS USEFUL ONLY WHEN X=(LAST X)-.20 *** I.E., 00017150
C               SPACED SAME AS FILTER USED---IF THIS IS NOT CONVENIENT, 00017160
C               THEN SUBPROGRAM 'ZFOURO' IS ADVISED FOR GENERAL USE. 00017170
C               (ALSO SEE PARM 'NEW' & NOTES (2)-(4) BELOW). 00017180
C   FUN(G)= EXTERNAL DECLARED COMPLEX FUNCTION NAME (USER SUPPLIED) 00017190
C               OF A REAL ARGUMENT G. 00017200
C               NOTE: IF PARMS OTHER THAN G ARE REQUIRED, USE COMMON IN 00017210
C               CALLING PROGRAM AND IN SUBPROGRAM FUN. 00017220
C               THE COMPLEX FUNCTION FUN SHOULD BE A MONOTONE 00017230
C               DECREASING FUNCTION AS THE ARGUMENT G BECOMES LARGE... 00017240
C               FOR REAL-ONLY FUNCTIONS, SUBPROGRAM 'RLAGFO' IS ADVISED; 00017250
C               HOWEVER, TWO REAL-FUNCTIONS F1(G),F2(G) MAY BE 00017260
C               INTEGRATED IN PARALLEL BY WRITING FUN=CMPLX(F1(G),F2(G)) 00017270
C   TOL=      REAL TOLERANCE EXCEPTED AT CONVOLVED TAILS---I.E., 00017280
C               IF FILTER*FUN<TOL*MAX, THEN REST OF TAIL IS TRUNCATED. 00017290
C               THIS IS DONE AT BOTH ENDS OF FILTER. TYPICALLY, 00017300
C               TOL <= .0001 IS USUALLY OK---BUT THIS DEPENDS ON 00017310
C               THE FUNCTION FUN AND PARAMETER X...IN GENERAL, 00017320
C               A 'SMALLER TOL' WILL USUALLY RESULT IN 'MORE ACCURACY' 00017330
C               BUT WITH 'MORE WEIGHTS' BEING USED. TOL IS NOT DIRECTLY 00017340
C               RELATED TO TRUNCATION ERROR, BUT GENERALLY SERVES AS AN 00017350
C               APPROXIMATION INDICATOR... FOR VERY LARGE OR SMALL B, 00017360
C               ONE SHOULD USE A SMALLER TOL THAN RECOMMENDED ABOVE... 00017370
C   L=        RESULTING NO. FILTER WTS. USED IN THE VARIABLE 00017380
C               CONVOLUTION (L DEPENDS ON TOL AND FUN). 00017390
C               MIN.L=24 AND MAX.L=281---WHICH COULD 00017400
C               OCCUR IF TOL IS VERY SMALL AND/OR FUN NOT DECREASING 00017410
C               VERY FAST... 00017420

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C      * NEW=      1 IS NECESSARY 1ST TIME OR BRAND NEW X.      00017430
C                  0 FOR ALL SUBSEQUENT CALLS WHERE X=(LAST X)-0.20 00017440
C                  IS ASSUMED INTERNALLY BY THIS ROUTINE.      00017450
C                  NOTE: IF THIS IS NOT TRUE, ROUTINE WILL      00017460
C                  STILL ASSUME X=(LAST X)-0.20 ANYWAY...      00017470
C                  IT IS THE USERS RESPONSIBILITY TO NORMALIZE 00017480
C                  BY CORRECT B=EXP(X) OUTSIDE OF CALL (SEE USAGE BELOW).00017490
C                  THE LAGGED CONVOLUTION METHOD PICKS UP SIGNIFICANT 00017500
C                  TIME IMPROVEMENTS WHEN THE KERNEL IS NOT A 00017510
C                  SIMPLE ELEMENTARY FUNCTION...DUE TO INTERNALLY SAVING 00017520
C                  ALL KERNEL FUNCTION EVALUATIONS WHEN NEW=1... 00017530
C                  THEN WHEN NEW=0, ALL PREVIOUSLY CALCULATED 00017540
C                  KERNELS WILL BE USED IN THE LAGGED CONVOLUTION 00017550
C                  WHERE POSSIBLE, ONLY ADDING NEW KERNEL EVALUATIONS 00017560
C                  WHEN NEEDED (DEPENDS ON PARMS TOL AND FUN) 00017570
C                  00017580
C--THE RESULTING COMPLEX CONVOLUTION SUM IS GIVEN IN ZLAGFO; THE FOURIER00017590
C TRANSFORM IS THEN ZLAGFO/B WHICH IS TO BE COMPUTED AFTER EXIT FROM 00017600
C THIS ROUTINE.... WHERE B=EXP(X), X=ARGUMENT USED IN CALL... 00017610
C 00017620
C--USAGE-- 'ZLAGFO' IS CALLED AS FOLLOWS: 00017630
C ... 00017640
C COMPLEX Z ZLAGFO,ZF 00017650
C EXTERNAL ZF 00017660
C ... 00017670
C Z=ZLAGFO(ALOG(B),ZF,TOL,L,NEW)/B 00017680
C ... 00017690
C END 00017700
C COMPLEX FUNCTION ZF(G) 00017710
C ...USER SUPPLIED CODE... 00017720
C END 00017730
C 00017740
C--NOTES: 00017750
C (1). EXP-UNDERFLOW'S MAY OCCUR IN EXECUTING THE SUBPROGRAM 00017760
C BELOW; HOWEVER, THIS IS OK PROVIDED THE MACHINE SYSTEM SETS 00017770
C ANY & ALL EXP-UNDERFLOW'S TO 0.0.... 00017780
C (2). AS AN AID TO UNDERSTANDING & USING THE LAGGED CONVOLUTION 00017790
C METHOD, LET BMAX>=BMIN>0 BE GIVEN. THEN IT CAN BE SHOWN 00017800
C THAT THE ACTUAL NUMBER OF B'S IS NB=AIN(5.*ALOG(BMAX/BMIN))+1, 00017810
C PROVIDED BMAX/BMIN>=1. THE USER MAY THEN ASSUME AN 'ADJUSTED' 00017820
C BMINA=BMAX*EXP(-.2*(NB-1)). THE METHOD GENERATES THE DECREASING 00017830
C ARGUMENTS SPACED AS X=ALOG(BMAX),X-.2,X-.2*2,...,ALOG(BMINA). 00017840
C FOR EXAMPLE, ONE MAY CONTROL THIS WITH THE CODE: 00017850
C ... 00017860
C NB=AIN(5.*ALOG(BMAX/BMIN))+1 00017870
C NB1=NB+1 00017880
C X0=ALOG(BMAX)+.2 00017890
C NEW=1 00017900
C DO 1 J=1,NB 00017910
C I=NB1-J 00017920
C X=X0-.2*J 00017930
C ARG(I)=EXP(X) 00017940

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C          Z(I)=ZLAGFO(X,ZF,TOL,L,NEW)/ARG(I)          00017950
C      1      NEW=0          00017960
C          ***          00017970
C      (3). IF RESULTS ARE STORED IN ARRAYS ARG(I),Z(I),I=1,NB FOR 00017980
C      ARG IN (BMINA,BMAX), THEN THESE ARRAYS MAY BE USED, FOR EXAMPLE, 00017990
C      TO SPLINE-INTERPOLATE AT A DIFFERENT (LARGER OR SMALLER) 00018000
C      SPACING THAN USED IN THE LAGGED CONVOLUTION METHOD. 00018010
C      (4). IF A DIFFERENT RANGE OF B IS DESIRED, THEN ONE MAY 00018020
C      ALWAYS RESTART THE ABOVE PROCEDURE IN (2) WITH A NEW 00018030
C      BMAX,BMIN AND BY SETTING NEW=1.... 00018040
C      (5). ABSCISSA CORRESPONDING TO WEIGHT IS GENERATED TO SAVE STORAGE 00018050
C          00018060
C          00018070
C      COMPLEX FUN,C,CMAX,SAVE 00018080
C      DIMENSION KEY(281),SAVE(281),T(2),TMAX(2) 00018090
C      DIMENSION YT(281),Y1(76),Y2(76),Y3(76),Y4(53) 00018100
C      EQUIVALENCE (C,T(1)),(CMAX,TMAX(1)) 00018110
C      EQUIVALENCE (YT(1),Y1(1)),(YT(77),Y2(1)),(YT(153),Y3(1)), 00018120
C      1 (YT(229),Y4(1)) 00018130
C--COS-EXTENDED FILTER WEIGHT ARRAYS: 00018140
C      DATA Y1/ 00018150
C      1 5.1178101E-14, 2.9433849E-14, 2.5492522E-14, 1.9034819E-14, 00018160
C      2 6.4179780E-14, 1.3085746E-15, 1.1989957E-13, -1.2216234E-14, 00018170
C      3 1.7534103E-13, 7.9373498E-15, 2.1235658E-13, 7.9981520E-14, 00018180
C      4 2.3815757E-13, 1.9714260E-13, 2.8920132E-13, 3.4161340E-13, 00018190
C      5 4.0349917E-13, 5.2203885E-13, 5.9837223E-13, 7.8015306E-13, 00018200
C      6 8.8911655E-13, 1.1709731E-12, 1.3165595E-12, 1.7578463E-12, 00018210
C      7 1.9538564E-12, 2.6289768E-12, 2.9167697E-12, 3.9044344E-12, 00018220
C      8 4.3927341E-12, 5.7526904E-12, 6.6569552E-12, 8.4555678E-12, 00018230
C      9 1.0063229E-11, 1.2487964E-11, 1.5134682E-11, 1.8501488E-11, 00018240
C      1 2.2720051E-11, 2.7452598E-11, 3.4025443E-11, 4.0875985E-11, 00018250
C      2 5.0751668E-11, 6.1094382E-11, 7.5492982E-11, 9.1445759E-11, 00018260
C      3 1.1227336E-10, 1.3676464E-10, 1.6720269E-10, 2.0423244E-10, 00018270
C      4 2.4932743E-10, 3.0470661E-10, 3.7198526E-10, 4.5449934E-10, 00018280
C      5 5.5502537E-10, 6.7793669E-10, 8.2810001E-10, 1.0112626E-09, 00018290
C      6 1.2354800E-09, 1.5085255E-09, 1.8432253E-09, 2.2503397E-09, 00018300
C      7 2.7499027E-09, 3.3569525E-09, 4.1025670E-09, 5.0077487E-09, 00018310
C      8 6.1205950E-09, 7.4703399E-09, 9.1312760E-09, 1.1143911E-08, 00018320
C      9 1.3622929E-08, 1.6623917E-08, 2.0324094E-08, 2.4798610E-08, 00018330
C      1 3.0321709E-08, 3.6992986E-08, 4.5237482E-08, 5.5183434E-08/ 00018340
C      DATA Y2/ 00018350
C      1 6.7491070E-08, 8.2317946E-08, 1.0069271E-07, 1.2279375E-07, 00018360
C      2 1.5022907E-07, 1.8316969E-07, 2.2413747E-07, 2.7322865E-07, 00018370
C      3 3.3441046E-07, 4.0756197E-07, 4.9894278E-07, 6.0793233E-07, 00018380
C      4 7.4443665E-07, 9.0679753E-07, 1.1107379E-06, 1.3525651E-06, 00018390
C      5 1.6573073E-06, 2.0174273E-06, 2.4728798E-06, 3.0090445E-06, 00018400
C      6 3.6898816E-06, 4.4879625E-06, 5.5059521E-06, 6.6935820E-06, 00018410
C      7 8.2160716E-06, 9.9828691E-06, 1.2260527E-05, 1.4888061E-05, 00018420
C      8 1.8296530E-05, 2.2202672E-05, 2.7305154E-05, 3.3109672E-05, 00018430
C      9 4.0751046E-05, 4.9372484E-05, 6.0820947E-05, 7.3619571E-05, 00018440
C      1 9.0780005E-05, 1.0976837E-04, 1.3550409E-04, 1.6365676E-04, 00018450
C      2 2.0227521E-04, 2.4398338E-04, 3.0197018E-04, 3.6370760E-04, 00018460

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3 4.5083748E-04, 5.4213338E-04, 6.7315347E-04, 8.0800951E-04, 00018470
4 1.0051938E-03, 1.2041401E-03, 1.5011708E-03, 1.7942344E-03, 00018480
5 2.2421056E-03, 2.6730676E-03, 3.3490681E-03, 3.9815050E-03, 00018490
6 5.0028666E-03, 5.9285668E-03, 7.4730905E-03, 8.8233510E-03, 00018500
7 1.1160132E-02, 1.3119627E-02, 1.6653199E-02, 1.9472767E-02, 00018510
8 2.4800811E-02, 2.8793704E-02, 3.6762063E-02, 4.2228780E-02, 00018520
9 5.3905163E-02, 6.0804660E-02, 7.7081738E-02, 8.3874501E-02, 00018530
1 1.0377190E-01, 1.0377718E-01, 1.1892208E-01, 9.0437429E-02/ 00018540
  DATA Y3/ 00018550
1 7.1685138E-02,-3.9473064E-02,-1.5078720E-01,-4.0489859E-01, 00018560
2-5.6018995E-01,-6.8050388E-01,-1.5094224E-01, 6.6304064E-01, 00018570
3 1.3766748E+00,-8.0373222E-01,-1.0869629E+00, 1.2812892E+00, 00018580
4-5.0341082E-01,-4.4274455E-02, 2.0913102E-01,-1.9999661E-01, 00018590
5 1.5207664E-01,-1.0920260E-01, 7.8169956E-02,-5.6651561E-02, 00018600
6 4.1611799E-02,-3.0880012E-02, 2.3072559E-02,-1.7311631E-02, 00018610
7 1.3021442E-02,-9.8085025E-03, 7.3943529E-03,-5.5769518E-03, 00018620
8 4.2073164E-03,-3.1745026E-03, 2.3954154E-03,-1.8076122E-03, 00018630
9 1.3640816E-03,-1.0293934E-03, 7.7682952E-04,-5.8623518E-04, 00018640
1 4.4240399E-04,-3.3386183E-04, 2.5195025E-04,-1.9013541E-04, 00018650
2 1.4348659E-04,-1.0828284E-04, 8.1716174E-05,-6.1667509E-05, 00018660
3 4.6537684E-05,-3.5119887E-05, 2.6503388E-05,-2.0000904E-05, 00018670
4 1.5093768E-05,-1.1390572E-05, 8.5959318E-06,-6.4869407E-06, 00018680
5 4.8953713E-06,-3.6942830E-06, 2.7878625E-06,-2.1038241E-06, 00018690
6 1.5875917E-06,-1.1980090E-06, 9.0398030E-07,-6.8208296E-07, 00018700
7 5.1458650E-07,-3.8817581E-07, 2.9272267E-07,-2.2067921E-07, 00018710
8 1.6623514E-07,-1.2514102E-07, 9.4034535E-08,-7.0556837E-08, 00018720
9 5.2741581E-08,-3.9298610E-08, 2.9107255E-08,-2.1413893E-08, 00018730
1 1.5742032E-08,-1.1498608E-08, 8.7561571E-09,-7.2959446E-09/ 00018740
  DATA Y4/ 00018750
1 6.8816619E-09,-8.9679825E-09, 1.4258275E-08,-1.9564299E-08, 00018760
2 2.0235313E-08,-1.4725545E-08, 5.4632820E-09, 3.5995580E-09, 00018770
3-9.5287133E-09, 1.1460041E-08,-1.0250532E-08, 7.4641748E-09, 00018780
4-4.4703465E-09, 2.0499053E-09,-4.4806353E-10,-4.0374336E-10, 00018790
5 7.0321001E-10,-6.7067960E-10, 4.9130404E-10,-2.8840747E-10, 00018800
6 1.2373144E-10,-1.5260443E-11,-4.2027559E-11, 6.1885474E-11, 00018810
7-5.9273937E-11, 4.6588766E-11,-3.2054182E-11, 1.9831637E-11, 00018820
8-1.1210098E-11, 5.9567021E-12,-3.2427812E-12, 2.1353868E-12, 00018830
9-1.8476851E-12, 1.8438474E-12,-1.8362842E-12, 1.7241847E-12, 00018840
1-1.5161479E-12, 1.2627657E-12,-1.0129176E-12, 7.9578625E-13, 00018850
2-6.2131435E-13, 4.8745900E-13,-3.8703630E-13, 3.1172547E-13, 00018860
3-2.5397802E-13, 2.0824130E-13,-1.7123163E-13, 1.4113344E-13, 00018870
4-1.1687986E-13, 9.7664016E-14,-8.2977176E-14, 7.2515267E-14, 00018880
5-5.6047478E-14/ 00018890
C--$ENDATA 00018900
  IF(NEW) 10,30,10 00018910
10 LAG=-1 00018920
  X0=-X-30.30251236 00018930
  DO 20 IR=1,281 00018940
20 KEY(IR)=0 00018950
30 LAG=LAG+1 00018960
  ZLAGF0=(0,0,0,0) 00018970
  CMAX=(0,0,0,0) 00018980

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	L=0	00018990
	ASSIGN 110 TO M	00019000
	I=149	00019010
	GO TO 200	00019020
110	TMAX(1)=AMAX1(ABS(T(1)),TMAX(1))	00019030
	TMAX(2)=AMAX1(ABS(T(2)),TMAX(2))	00019040
	I=I+1	00019050
	IF(I,LE,170) GO TO 200	00019060
	IF(TMAX(1).EQ.0.0.AND.TMAX(2).EQ.0.0) GO TO 150	00019070
	CMAX=TOL*CMAX	00019080
	ASSIGN 120 TO M	00019090
	I=148	00019100
	GO TO 200	00019110
120	IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 130	00019120
	I=I-1	00019130
	IF(I,GT,0) GO TO 200	00019140
130	ASSIGN 140 TO M	00019150
	I=171	00019160
	GO TO 200	00019170
140	IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 190	00019180
	I=I+1	00019190
	IF(I,LE,281) GO TO 200	00019200
	GO TO 190	00019210
150	ASSIGN 160 TO M	00019220
	I=1	00019230
	GO TO 200	00019240
160	IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 170	00019250
	I=I+1	00019260
	IF(I,LE,148) GO TO 200	00019270
170	ASSIGN 180 TO M	00019280
	I=281	00019290
	GO TO 200	00019300
180	IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 190	00019310
	I=I-1	00019320
	IF(I,GE,171) GO TO 200	00019330
190	RETURN	00019340
	C---STORE/RETRIEVE ROUTINE (DONE INTERNALLY TO SAVE CALL'S)	00019350
200	LOOK=I+LAG	00019360
	IQ=LOOK/282	00019370
	IR=MOD(LOOK,282)	00019380
	IF(IR,EQ,0) IR=1	00019390
	IROLL=IQ*281	00019400
	IF(KEY(IR),LE,IROLL) GO TO 220	00019410
210	C=SAVE(IR)*YT(I)	00019420
	ZLAGF0=ZLAGF0+C	00019430
	L=L+1	00019440
	GO TO M,(110,120,140,160,180)	00019450
220	KEY(IR)=IROLL+IR	00019460
	SAVE(IR)=FUN(EXP(X0+FLOAT(LOOK)*.20))	00019470
	GO TO 210	00019480
	END	00019490

COMPLEX FUNCTION ZLAGF1(X,FUN,TOL,L,NEW)

00019500

C---\*\*\* A SPECIAL LAGGED\* CONVOLUTION METHOD TO COMPUTE THE 00019510  
C INTEGRAL FROM 0 TO INFINITY OF 'FUN(G)\*SIN(G\*B)\*DG' DEFINED AS THE 00019520  
C COMPLEX FOURIER SINE TRANSFORM WITH ARGUMENT X(=ALOG(B)) 00019530  
C BY CONVOLUTION FILTERING WITH COMPLEX FUNCTION 'FUN'---AND 00019540  
C USING A VARIABLE CUT-OFF METHOD WITH EXTENDED FILTER TAILS... 00019550  
C 00019560  
C---REF: ANDERSON, W.L., 1975, NTIS REPT. PB-242-800. 00019570  
C 00019580  
C---PARAMETERS: 00019590  
C 00019600  
C \* X = REAL ARGUMENT(=ALOG(B) AT CALL) OF THE FOURIER TRANSFORM 00019610  
C 'ZLAGF1' IS USEFUL ONLY WHEN X=(LAST X)-.20 \*\*\* I.E., 00019620  
C SPACED SAME AS FILTER USED---IF THIS IS NOT CONVENIENT, 00019630  
C THEN SUBPROGRAM 'ZFOUR1' IS ADVISED FOR GENERAL USE. 00019640  
C (ALSO SEE PARM 'NEW' & NOTES (2)-(4) BELOW). 00019650  
C FUN(G)= EXTERNAL DECLARED COMPLEX FUNCTION NAME (USER SUPPLIED) 00019660  
C OF A REAL ARGUMENT G. 00019670  
C NOTE: IF PARMS OTHER THAN G ARE REQUIRED, USE COMMON IN 00019680  
C CALLING PROGRAM AND IN SUBPROGRAM FUN. 00019690  
C THE COMPLEX FUNCTION FUN SHOULD BE A MONOTONE 00019700  
C DECREASING FUNCTION AS THE ARGUMENT G BECOMES LARGE... 00019710  
C FOR REAL-ONLY FUNCTIONS, SUBPROGRAM 'RLAGF1' IS ADVISED; 00019720  
C HOWEVER, TWO REAL-FUNCTIONS F1(G),F2(G) MAY BE 00019730  
C INTEGRATED IN PARALLEL BY WRITING FUN=CMPLX(F1(G),F2(G)) 00019740  
C TOL= REAL TOLERANCE EXCEPTED AT CONVOLVED TAILS---I.E., 00019750  
C IF FILTER\*FUN<TOL\*MAX, THEN REST OF TAIL IS TRUNCATED. 00019760  
C THIS IS DONE AT BOTH ENDS OF FILTER. TYPICALLY, 00019770  
C TOL <= .0001 IS USUALLY OK---BUT THIS DEPENDS ON 00019780  
C THE FUNCTION FUN AND PARAMETER X...IN GENERAL, 00019790  
C A 'SMALLER TOL' WILL USUALLY RESULT IN 'MORE ACCURACY' 00019800  
C BUT WITH 'MORE WEIGHTS' BEING USED. TOL IS NOT DIRECTLY 00019810  
C RELATED TO TRUNCATION ERROR, BUT GENERALLY SERVES AS AN 00019820  
C APPROXIMATION INDICATOR... FOR VERY LARGE OR SMALL B, 00019830  
C ONE SHOULD USE A SMALLER TOL THAN RECOMMENDED ABOVE... 00019840  
C L= RESULTING NO. FILTER WTS. USED IN THE VARIABLE 00019850  
C CONVOLUTION (L DEPENDS ON TOL AND FUN). 00019860  
C MIN.L=20 AND MAX.L=266---WHICH COULD 00019870  
C OCCUR IF TOL IS VERY SMALL AND/OR FUN NOT DECREASING 00019880  
C VERY FAST... 00019890  
C \* NEW= 1 IS NECESSARY 1ST TIME OR BRAND NEW X. 00019900  
C 0 FOR ALL SUBSEQUENT CALLS WHERE X=(LAST X)-0.20 00019910  
C IS ASSUMED INTERNALLY BY THIS ROUTINE. 00019920  
C NOTE: IF THIS IS NOT TRUE, ROUTINE WILL 00019930  
C STILL ASSUME X=(LAST X)-0.20 ANYWAY... 00019940  
C IT IS THE USERS RESPONSIBILITY TO NORMALIZE 00019950  
C BY CORRECT B=EXP(X) OUTSIDE OF CALL (SEE USAGE BELOW). 00019960  
C THE LAGGED CONVOLUTION METHOD PICKS UP SIGNIFICANT 00019970  
C TIME IMPROVEMENTS WHEN THE KERNEL IS NOT A 00019980  
C SIMPLE ELEMENTARY FUNCTION...DUE TO INTERNALLY SAVING 00019990  
C ALL KERNEL FUNCTION EVALUATIONS WHEN NEW=1... 00020000  
C THEN WHEN NEW=0, ALL PREVIOUSLY CALCULATED 00020010

C	KERNELS WILL BE USED IN THE LAGGED CONVOLUTION	00020020
C	WHERE POSSIBLE, ONLY ADDING NEW KERNEL EVALUATIONS	00020030
C	WHEN NEEDED (DEPENDS ON PARMS TOL AND FUN)	00020040
C		00020050
C	--THE RESULTING COMPLEX CONVOLUTION SUM IS GIVEN IN ZLAGF1; THE FOURIER	00020060
C	TRANSFORM IS THEN ZLAGF1/B WHICH IS TO BE COMPUTED AFTER EXIT FROM	00020070
C	THIS ROUTINE.... WHERE B=EXP(X), X=ARGUMENT USED IN CALL..	00020080
C		00020090
C	--USAGE-- 'ZLAGF1' IS CALLED AS FOLLOWS:	00020100
C	***	00020110
C	COMPLEX Z,ZLAGF1,ZF	00020120
C	EXTERNAL ZF	00020130
C	***	00020140
C	Z=ZLAGF1(ALOG(B),ZF,TOL,L,NEW)/B	00020150
C	***	00020160
C	END	00020170
C	COMPLEX FUNCTION ZF(G)	00020180
C	...USER SUPPLIED CODE...	00020190
C	END	00020200
C		00020210
C	--NOTES:	00020220
C	(1). EXP-UNDERFLOW'S MAY OCCUR IN EXECUTING THE SUBPROGRAM	00020230
C	BELOW; HOWEVER, THIS IS OK PROVIDED THE MACHINE SYSTEM SETS	00020240
C	ANY & ALL EXP-UNDERFLOW'S TO 0.0....	00020250
C	(2). AS AN AID TO UNDERSTANDING & USING THE LAGGED CONVOLUTION	00020260
C	METHOD, LET BMAX>=BMIN>0 BE GIVEN. THEN IT CAN BE SHOWN	00020270
C	THAT THE ACTUAL NUMBER OF B'S IS NB=AINT(5.*ALOG(BMAX/BMIN))+1,	00020280
C	PROVIDED BMAX/BMIN>=1. THE USER MAY THEN ASSUME AN 'ADJUSTED'	00020290
C	BMINA=BMAX*EXP(-.2*(NB-1)). THE METHOD GENERATES THE DECREASING	00020300
C	ARGUMENTS SPACED AS X=ALOG(BMAX),X-.2,X-.2*2,...,ALOG(BMINA).	00020310
C	FOR EXAMPLE, ONE MAY CONTROL THIS WITH THE CODE:	00020320
C	***	00020330
C	NB=AINT(5.*ALOG(BMAX/BMIN))+1	00020340
C	NB1=NB+1	00020350
C	XO=ALOG(BMAX)+.2	00020360
C	NEW=1	00020370
C	DO 1 J=1,NB	00020380
C	I=NB1-J	00020390
C	X=XO-.2*J	00020400
C	ARG(I)=EXP(X)	00020410
C	Z(I)=ZLAGF1(X,ZF,TOL,L,NEW)/ARG(I)	00020420
C	1 NEW=0	00020430
C	***	00020440
C	(3). IF RESULTS ARE STORED IN ARRAYS ARG(I),Z(I),I=1,NB FOR	00020450
C	ARG IN (BMINA,BMAX), THEN THESE ARRAYS MAY BE USED, FOR EXAMPLE,	00020460
C	TO SPLINE-INTERPOLATE AT A DIFFERENT (LARGER OR SMALLER)	00020470
C	SPACING THAN USED IN THE LAGGED CONVOLUTION METHOD.	00020480
C	(4). IF A DIFFERENT RANGE OF B IS DESIRED, THEN ONE MAY	00020490
C	ALWAYS RESTART THE ABOVE PROCEDURE IN (2) WITH A NEW	00020500
C	BMAX,BMIN AND BY SETTING NEW=1....	00020510
C	(5). ABSCISSA CORRESPONDING TO WEIGHT IS GENERATED TO SAVE STORAGE	00020520
C		00020530

```

C
COMPLEX FUN,C,CMAX,SAVE
DIMENSION KEY(266),SAVE(266),T(2),TMAX(2)
DIMENSION WT(266),W1(76),W2(76),W3(76),W4(38)
EQUIVALENCE (C,T(1)),(CMAX,TMAX(1))
EQUIVALENCE (WT(1),W1(1)),(WT(77),W2(1)),(WT(153),W3(1)),
1 (WT(229),W4(1))
C--SIN-EXTENDED FILTER WEIGHT ARRAYS:
DATA W1/
1-1.1113940E-09,-1.3237246E-12, 1.5091739E-12,-1.6240954E-12,
2 1.7236636E-12,-1.8227727E-12, 1.9255992E-12,-2.0335514E-12,
3 2.1473541E-12,-2.2675549E-12, 2.3946842E-12,-2.5292661E-12,
4 2.6718110E-12,-2.8227693E-12, 2.9825171E-12,-3.1514006E-12,
5 3.3297565E-12,-3.5179095E-12, 3.7163306E-12,-3.9256378E-12,
6 4.1464798E-12,-4.3794552E-12, 4.6252131E-12,-4.8845227E-12,
7 5.1582809E-12,-5.4474462E-12, 5.7530277E-12,-6.0760464E-12,
8 6.4175083E-12,-6.7783691E-12, 7.1595239E-12,-7.5618782E-12,
9 7.9864477E-12,-8.4344110E-12, 8.9072422E-12,-9.4067705E-12,
1 9.9349439E-12,-1.0493731E-11, 1.1084900E-11,-1.1709937E-11,
2 1.2370354E-11,-1.3067414E-11, 1.3802200E-11,-1.4575980E-11,
3 1.5390685E-11,-1.6249313E-11, 1.7155934E-11,-1.8115250E-11,
4 1.9131898E-11,-2.0209795E-11, 2.1352159E-11,-2.2561735E-11,
5 2.3840976E-11,-2.5192263E-11, 2.6618319E-11,-2.8122547E-11,
6 2.9709129E-11,-3.1382870E-11, 3.3149030E-11,-3.5013168E-11,
7 3.6981050E-11,-3.9058553E-11, 4.1251694E-11,-4.3566777E-11,
8 4.6010537E-11,-4.8590396E-11, 5.1314761E-11,-5.4193353E-11,
9 5.7236720E-11,-6.0455911E-11, 6.3861222E-11,-6.7461492E-11,
1 7.1265224E-11,-7.5279775E-11, 7.9512249E-11,-8.3971327E-11/
DATA W2/
1 8.8668961E-11,-9.3621900E-11, 9.8851764E-11,-1.0438319E-10,
2 1.1024087E-10,-1.1644680E-10, 1.2301979E-10,-1.2997646E-10,
3 1.3733244E-10,-1.4510363E-10, 1.5330772E-10,-1.6196550E-10,
4 1.7110130E-10,-1.8074257E-10, 1.9091922E-10,-2.0166306E-10,
5 2.1300756E-10,-2.2498755E-10, 2.3763936E-10,-2.5100098E-10,
6 2.6511250E-10,-2.8001616E-10, 2.9575691E-10,-3.1238237E-10,
7 3.2994314E-10,-3.4849209E-10, 3.6808529E-10,-3.8878042E-10,
8 4.1063982E-10,-4.3372666E-10, 4.5811059E-10,-4.8386049E-10,
9 5.1105728E-10,-5.3977672E-10, 5.7011632E-10,-6.0215516E-10,
1 6.3601273E-10,-6.7175964E-10, 7.0955028E-10,-7.4942601E-10,
2 7.9161025E-10,-8.3606980E-10, 8.8317110E-10,-9.3270330E-10,
3 9.8533749E-10,-1.0404508E-09, 1.0993731E-09,-1.1605442E-09,
4 1.2267391E-09,-1.2942905E-09, 1.3691677E-09,-1.4429912E-09,
5 1.5288164E-09,-1.6077524E-09, 1.7085998E-09,-1.7890471E-09,
6 1.9129068E-09,-1.9857116E-09, 2.1491608E-09,-2.1926779E-09,
7 2.4312660E-09,-2.3959044E-09, 2.7872500E-09,-2.5610596E-09,
8 3.2762318E-09,-2.6082940E-09, 4.0261453E-09,-2.3560563E-09,
9 5.3176554E-09,-1.3960161E-09, 7.7708747E-09, 1.1853546E-09,
1 1.2760851E-08, 7.4264707E-09, 2.3342187E-08, 2.1869851E-08/
DATA W3/
1 4.6306744E-08, 5.4631686E-08, 9.6763087E-08, 1.2823337E-07,
2 2.0832812E-07, 2.9280540E-07, 4.5580888E-07, 6.5992437E-07,
3 1.0056815E-06, 1.4779183E-06, 2.2284335E-06, 3.2994604E-06,

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4 4.9485823E-06, 7.3545473E-06, 1.1001083E-05, 1.6380539E-05, 00021060
5 2.4469550E-05, 3.6469246E-05, 5.4441527E-05, 8.1176726E-05, 00021070
6 1.2113828E-04, 1.8066494E-04, 2.6954609E-04, 4.0202288E-04, 00021080
7 5.9969995E-04, 8.9437312E-04, 1.3338166E-03, 1.9886697E-03, 00021090
8 2.9643943E-03, 4.4168923E-03, 6.5773518E-03, 9.7855105E-03, 00021100
9 1.4539361E-02, 2.1558670E-02, 3.1871864E-02, 4.6903518E-02, 00021110
1 6.8559512E-02, 9.9170152E-02, 1.4120770E-01, 1.9610835E-01, 00021120
2 2.6192603E-01, 3.2743321E-01, 3.6407406E-01, 3.1257559E-01, 00021130
3 9.0460168E-02, -3.6051039E-01, -8.6324760E-01, -8.1178720E-01, 00021140
4 5.2205241E-01, 1.5449873E+00, -1.1817933E+00, -2.6759896E-01, 00021150
5 8.0869203E-01, -6.2757149E-01, 3.4062630E-01, -1.5885304E-01, 00021160
6 7.0472984E-02, -3.1624462E-02, 1.4894068E-02, -7.4821176E-03, 00021170
7 4.0035936E-03, -2.2543784E-03, 1.3160358E-03, -7.8636604E-04, 00021180
8 4.7658745E-04, -2.9125817E-04, 1.7885105E-04, -1.1012416E-04, 00021190
9 6.7910334E-05, -4.1914054E-05, 2.5881544E-05, -1.5985851E-05, 00021200
1 9.8751880E-06, -6.1008526E-06, 3.7692543E-06, -2.3287953E-06/ 00021210
DATA W4/ 00021220
1 1.4388425E-06, -8.8899353E-07, 5.4926991E-07, -3.3937048E-07, 00021230
2 2.0968284E-07, -1.2955437E-07, 8.0046336E-08, -4.9457371E-08, 00021240
3 3.0557711E-08, -1.8880390E-08, 1.1665454E-08, -7.2076428E-09, 00021250
4 4.4533423E-09, -2.7515696E-09, 1.7001092E-09, -1.0504494E-09, 00021260
5 6.4904567E-10, -4.0102999E-10, 2.4778763E-10, -1.5310321E-10, 00021270
6 9.4600354E-11, -5.8453314E-11, 3.6119400E-11, -2.2320056E-11, 00021280
7 1.3793460E-11, -8.5242656E-12, 5.2675102E-12, -3.2543076E-12, 00021290
8 2.0097689E-12, -1.2405412E-12, 7.6530538E-13, -4.7191929E-13, 00021300
9 2.9084993E-13, -1.7923661E-13, 1.1018948E-13, -6.7885902E-14, 00021310
1 4.2025050E-14, -2.1314731E-14/ 00021320
C---$$ENDATA 00021330
C 00021340
IF(NEW) 10,30,10 00021350
10 LAG=-1 00021360
X0=-X-38.30455704 00021370
DO 20 IR=1,266 00021380
20 KEY(IR)=0 00021390
30 LAG=LAG+1 00021400
ZLAGF1=(0.0,0.0) 00021410
CMAX=(0.0,0.0) 00021420
L=0 00021430
ASSIGN 110 TO M 00021440
I=191 00021450
GO TO 200 00021460
110 TMAX(1)=AMAX1(ABS(T(1)),TMAX(1)) 00021470
TMAX(2)=AMAX1(ABS(T(2)),TMAX(2)) 00021480
I=I+1 00021490
IF(I.LE.208) GO TO 200 00021500
IF(TMAX(1).EQ.0.0.AND.TMAX(2).EQ.0.0) GO TO 150 00021510
CMAX=TOL*CMAX 00021520
ASSIGN 120 TO M 00021530
I=190 00021540
GO TO 200 00021550
120 IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 130 00021560
I=I-1 00021570

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	IF(I.GT.0) GO TO 200	00021580
130	ASSIGN 140 TO M	00021590
	I=209	00021600
	GO TO 200	00021610
140	IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 190	00021620
	I=I+1	00021630
	IF(I.LE.266) GO TO 200	00021640
	GO TO 190	00021650
150	ASSIGN 160 TO M	00021660
	I=1	00021670
	GO TO 200	00021680
160	IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 170	00021690
	I=I+1	00021700
	IF(I.LE.190) GO TO 200	00021710
170	ASSIGN 180 TO M	00021720
	I=266	00021730
	GO TO 200	00021740
180	IF(T(1).EQ.0.0.AND.T(2).EQ.0.0) GO TO 190	00021750
	I=I-1	00021760
	IF(I.GE.209) GO TO 200	00021770
190	RETURN	00021780
	C--STORE/RETRIEVE ROUTINE (DONE INTERNALLY TO SAVE CALL'S)	00021790
200	LOOK=I+LAG	00021800
	IQ=LOOK/267	00021810
	IR=MOD(LOOK,267)	00021820
	IF(IR.EQ.0) IR=1	00021830
	IROLL=IQ*266	00021840
	IF(KEY(IR).LE.IROLL) GO TO 220	00021850
210	C=SAVE(IR)*WT(I)	00021860
	ZLAGF1=ZLAGF1+C	00021870
	L=L+1	00021880
	GO TO M,(110,120,140,160,180)	00021890
220	KEY(IR)=IROLL+IR	00021900
	SAVE(IR)=FUN(EXP(X0+FLOAT(LOOK)*.20))	00021910
	GO TO 210	00021920
	END	00021930
	 SUBROUTINE IKS(B8,I1K1,IKDIF)	00021940
	C--COMPUTE MODIFIED BESSEL FUNCTION (I & K) SPECIAL COMBINATIONS FOR	00021950
	C PARAMETERS	00021960
	C B8 = DOUBLE PRECISION ARGUMENT (=B/DSQRT(2.D0) HERE)	00021970
	C I1K1 = I1*K1 COMPLEX RESULT	00021980
	C IKDIF = 4*I1*K1-(B8*DSQRT(I))*(I0*K1-I1*K0) COMPLEX RESULT DONE IN	00021990
	C DP BEFORE CMLX"ING.	00022000
	C--SUBROUTINE KELVIN CALLED	00022010
	C	00022020
	DOUBLE PRECISION B8,BB(8),BETA,Q1,Q2,R1,R2	00022030
	COMPLEX I1K1,IKDIF,CAMBDA,DENOM,DENOM1,TERM0,TERM1,TERM11	00022040
	COMPLEX S11,S10,S11,SK0,SK1,ONE	00022050
	DATA ONE/(1.0,0.0)/	00022060
	IF(B8.GT.20.D0) GO TO 10	00022070
	CALL KELVIN(B8,8,BB)	00022080

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Q1=-BB(6)*BB(8)+BB(5)*BB(7)                                00022090
Q2= BB(5)*BB(8)+BB(6)*BB(7)                                00022100
I1K1=CMPLX(SNGL(Q1),SNGL(Q2))                                00022110
R1=-BB(1)*BB(8)-BB(2)*BB(7) -                                00022120
&    BB(6)*BB(3)-BB(5)*BB(4)                                00022130
R2=-BB(2)*BB(8)+BB(1)*BB(7) +                                00022140
&    BB(5)*BB(3)-BB(6)*BB(4)                                00022150
BETA=.7071067811865475D0*B8                                  00022160
Q1=4.0D0*Q1-BETA*(R1-R2)                                    00022170
Q2=4.0D0*Q2-BETA*(R1+R2)                                    00022180
IKDIF=CMPLX(SNGL(Q1),SNGL(Q2))                                00022190
RETURN                                                         00022200
10 B=SNGL(B8/0.7071067811865475D0)                            00022210
TOL=1.E-6                                                      00022220
C--FOR LARGE ARGUMENTS, USE ABRAMOWITZ AND STEGUN            00022230
C    ASYMPTOTIC FORMULAS FOR LARGE ARGUMENTS                 00022240
C    9.7.1 THROUGH 9.7.5, P. 377-378.                        00022250
CAMBDA=B*CMPLX(1.0,1.0)/2.                                    00022260
IKDIF=CMPLX(100.,0.)                                          00022270
ISIGN=1                                                         00022280
DENOM=8.*CAMBDA                                                00022290
DENOM1=(2.*CAMBDA)**2                                         00022300
NODD=1                                                         00022310
TERM0=ONE                                                       00022320
TERM1=ONE                                                       00022330
TERM11=ONE                                                      00022340
S11=ONE                                                         00022350
S10=ONE                                                         00022360
SI1=ONE                                                         00022370
SK0=ONE                                                         00022380
SK1=ONE                                                         00022390
1 NODD2=NODD*NODD                                              00022400
OIKDIF=CABS(IKDIF)                                             00022410
TERM1=TERM1*CMPLX(4.,-NODD2,0.)/DENOM                        00022420
TERM0=TERM0*CMPLX(-FLOAT(NODD2),0.)/DENOM                    00022430
TERM11=TERM11*CMPLX(NODD*(4.,-NODD2)/(NODD+1),0.)/DENOM1    00022440
ISIGN=-ISIGN                                                   00022450
S11=S11+ISIGN*TERM11                                          00022460
S10=S10+ISIGN*TERM0                                           00022470
SI1=SI1+ISIGN*TERM1                                           00022480
SK0=SK0+TERM0                                                  00022490
SK1=SK1+TERM1                                                  00022500
IKDIF=S10*SK1-SK0*SI1                                         00022510
NODD=NODD+2                                                    00022520
IF(ABS(OIKDIF-CABS(IKDIF)).GT.TOL) GO TO 1                   00022530
I1K1=S11/(CAMBDA*CMPLX(2.,0.))                                00022540
IKDIF=CMPLX(4.,0.)*I1K1-IKDIF/CMPLX(2.,0.)                 00022550
RETURN                                                         00022560
END                                                             00022570

SUBROUTINE KELVIN(X,M,B)                                       00022580
C--COMPUTES M(,LE,8) KELVIN FUNCTIONS (ORDERS 0,1) CONSECUTIVELY STORED 00022590

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C   IN ARRAY B(M) WHERE:                                00022600
C                                                         00022610
C   X      = DF-ARGUMENT ,GT. 0.0D0 (ASYMPTOTIC FORM USED IF X.GE.8.0) 00022620
C   M      = NUMBER OF B'S TO COMPUTE AS DEFINED BELOW (1.GE.M.LE.8) 00022630
C   B(M)    = COMPUTED DF-FUNCTIONS WHERE B IS DEFINED: 00022640
C           B(1) = BER(X)  -- ORDER 0 00022650
C           B(2) = BEI(X)  -- ORDER 0 00022660
C           B(3) = KER(X)  -- ORDER 0 00022670
C           B(4) = KEI(X)  -- ORDER 0 00022680
C           B(5) = BER1(X) -- ORDER 1 00022690
C           B(6) = BEI1(X) -- ORDER 1 00022700
C           B(7) = KER1(X) -- ORDER 1 00022710
C           B(8) = KEI1(X) -- ORDER 1 00022720
C ** ACCURACY GOOD TO AT LEAST 14 FIGURES FOR ALL X ** 00022730
C NOTE: THIS METHOD OF GENERATING MULTIPLE KELVIN FUNCTIONS WAS CHOSEN 00022740
C       TO REDUCE TOTAL CPU-TIME SINCE MOST APPLICATIONS REQUIRE 00022750
C       MULTIPLE FUNCTION USE AND IS THEREFORE ACCOMPLISHED BY ONE CALL. 00022760
C E.G: TO OBTAIN BER(X),BEI(X),KER(X), AND KEI(X): CALL KELVIN(X,4,B) 00022770
C IF X OR M OUT OF RANGE, ROUTINE EXITS WITHOUT ACTION. 00022780
C                                                         00022790
C   IMPLICIT REAL*8 (A-H,O-Z) 00022800
C   REAL*8 B(8),CN(8),SN(8) 00022810
C   DATA CN /,7071067811865475D0,0.D0,-.7071067811865475D0, 00022820
C * -1.D0,-.7071067811865475D0,0.D0,.7071067811865475D0,1.D0/, 00022830
C * SN /,7071067811865475D0,1.D0,.7071067811865475D0,0.D0, 00022840
C * -.7071067811865475D0,-1.D0,-.7071067811865475D0,0.D0/ 00022850
C   DATA PI4/.7853981633974483D0/,R22/,7071067811865475D0/, 00022860
C * E/0.5D-14/, 00022870
C * PI1/.3183098861837907D0/ 00022880
C   IF(M.LT.1.OR.M.GT.8.OR.X.LE.0.0D0) GO TO 9 00022890
C   IF(X.GE.8.0D0) GO TO 8 00022900
C--SERIES METHODS (X.GT.0.0.AND,X.LT.8.0D0) 00022910
C   X2=0.5D0*X 00022920
C   X4=X2**4 00022930
C   T1=-0.25D0*X4 00022940
C   S1=T1 00022950
C   T2=0.0D0 00022960
C   T3=0.0D0 00022970
C   T4=0.0D0 00022980
C   T15=0.0D0 00022990
C   T26=0.0D0 00023000
C   T75=0.0D0 00023010
C   T86=0.0D0 00023020
C   IF(M.EQ.1) GO TO 100 00023030
C   T2=X2**2 00023040
C   S2=T2 00023050
C   IF(M.EQ.2) GO TO 100 00023060
C   T5=1.5D0 00023070
C   S5=T1*T5 00023080
C   IF(M.EQ.3) GO TO 100 00023090
C   T6=1.0D0 00023100
C   S6=T2 00023110

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IF(M.EQ.4) GO TO 100	00023120
T3=-0.5D0*X2**3	00023130
S3=T3	00023140
T4=X2	00023150
S4=T4	00023160
IF(M.LE.6) GO TO 100	00023170
T7=-0.25D0*X2**3	00023180
S7=2.0D0*T7*T5	00023190
T8=X2	00023200
S8=T8	00023210
100 TK=2.0D0	00023220
101 TK2=TK+TK	00023230
TK21=TK2-1.0D0	00023240
TK22=TK2-2.0D0	00023250
RK2=1.0D0/TK2	00023260
RK21=1.0D0/TK21	00023270
RK22=1.0D0/TK22	00023280
R1=-X4*(RK21*RK2)**2	00023290
T1=T1*R1	00023300
S1=S1+T1	00023310
IF(M.EQ.1) GO TO 200	00023320
R2=-X4*(RK22*RK21)**2	00023330
T2=T2*R2	00023340
S2=S2+T2	00023350
IF(M.EQ.2) GO TO 200	00023360
T5=T5+RK21+RK2	00023370
T15=T1*T5	00023380
S5=S5+T15	00023390
IF(M.EQ.3) GO TO 200	00023400
T6=T6+RK22+RK21	00023410
T26=T2*T6	00023420
S6=S6+T26	00023430
IF(M.EQ.4) GO TO 200	00023440
T3=T3*(-X4*(RK22*RK21**2*RK2))	00023450
S3=S3+T3	00023460
T4=T4*(-X4*RK22**2*RK21/(TK2-3.0D0))	00023470
S4=S4+T4	00023480
IF(M.LE.6) GO TO 200	00023490
T7=T7*R1	00023500
T75=TK2*T7*T5	00023510
S7=S7+T75	00023520
T8=T8*R2	00023530
T86=TK21*T8*T6	00023540
S8=S8+T86	00023550
200 TK=TK+1.0D0	00023560
IF(DABS(T1).GT.E.OR.DABS(T2).GT.E.OR.DABS(T15).GT.E.OR.	00023570
* DABS(T26).GT.E.OR.DABS(T3).GT.E.OR.DABS(T4).GT.E.OR.	00023580
* DABS(T75).GT.E.OR.DABS(T86).GT.E) GO TO 101	00023590
B(1)=1.0D0+S1	00023600
IF(M.EQ.1) GO TO 9	00023610
B(2)=S2	00023620
IF(M.EQ.2) GO TO 9	00023630

C=0.1159315156584124D0-DLOG(X)	00023640
B(3)=C*B(1)+PI4*B(2)+S5	00023650
IF(M.EQ.3) GO TO 9	00023660
B(4)=C*B(2)-PI4*B(1)+S6	00023670
IF(M.EQ.4) GO TO 9	00023680
B(5)=R22*(S3-S4)	00023690
IF(M.EQ.5) GO TO 9	00023700
B(6)=R22*(S3+S4)	00023710
IF(M.EQ.6) GO TO 9	00023720
S7=C*S3-B(1)/X+PI4*S4+S7	00023730
S8=C*S4-B(2)/X-PI4*S3+S8	00023740
B(7)=R22*(S7-S8)	00023750
IF(M.EQ.7) GO TO 9	00023760
B(8)=R22*(S7+S8)	00023770
9 RETURN	00023780
C---GENERAL ASYMPTOTIC FORM FOR NU=0,1:	00023790
8 NU=0	00023800
X2=R22*X	00023810
X8=8.0D0*X	00023820
SX=DSQRT(X)	00023830
EX2=DEXP_(-X2)	00023840
C1=1.253314137315500D0*EX2/SX	00023850
C2=1.0D0/(2.506628274631001D0*SX*EX2+1.0D-38)	00023860
MAXK=30	00023870
IF(X.LT.15.0D0) MAXK=X+X	00023880
1 XNU=NU	00023890
XMU=4.0D0*XNU	00023900
ALP=X2+PI4*(XNU+XNU-0.5D0)	00023910
BETA=ALP+PI4	00023920
CB=DCOS(BETA)	00023930
CA=DCOS(ALP)	00023940
SB=DSIN(BETA)	00023950
SA=DSIN(ALP)	00023960
N4=4*NU	00023970
FM=0.0D0	00023980
FP=0.0D0	00023990
GM=0.0D0	00024000
GP=0.0D0	00024010
TM=1.0D0	00024020
TP=1.0D0	00024030
K=1	00024040
2 TK=K	00024050
T=(XMU-(TK+TK-1.0D0)**2)/(TK*X8)	00024060
TPL=DABS(TP)	00024070
TP=-TP*T	00024080
IF(DABS(TP).GT.TPL) GO TO 21	00024090
TM=TM*T	00024100
N=MOD(K,8)	00024110
IF(N.EQ.0) N=8	00024120
T1=TP*CN(N)	00024130
FP=FP+T1	00024140
T2=TM*CN(N)	00024150

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FM=FM+T2                                00024160
T3=TF*SN(N)                             00024170
GP=GP+T3                                00024180
T4=TM*SN(N)                             00024190
GM=GM+T4                                00024200
K=K+1                                    00024210
IF(K.GT.MAXK) GO TO 3                    00024220
GO TO 2                                  00024230
21 FP=FP-T1                              00024240
FM=FM-T2                                00024250
GP=GP-T3                                00024260
GM=GM-T4                                00024270
3 FP=FP+1.0D0                            00024280
FM=FM+1.0D0                             00024290
B(N4+4)=C1*(-FM*SB-GM*CB)                00024300
B(N4+3)=C1*(FM*CB-GM*SB)                00024310
B(N4+2)=C2*(FP*SA-GP*CA)+PI1*B(N4+3)    00024320
B(N4+1)=C2*(FP*CA+GP*SA)-PI1*B(N4+4)    00024330
IF(NU.EQ.1.OR.M.LE.4) GO TO 9           00024340
NU=1                                      00024350
GO TO 1                                  00024360
END                                       00024370

SUBROUTINE QUINT(NY,Y,B,C,D,E,F)         00024380
C---COMPUTES COEFFICIENTS OF A QUINTIC NATURAL SPLINE S(X) GIVEN 00024390
C THE ORDINATES Y(I) AT ASSUMED EQUIDISTANT POINTS X(I),I=1 TO NY. 00024400
C                                     00024410
C TRANSLATED FROM ALGOL TO FORTRAN BY 00024420
C W.L. ANDERSON, U.S. GEOLOGICAL SURVEY, DENVER, COLORADO. 00024430
C REF: ACM TRANSACTIONS ON MATH. SOFTWARE, SEPT 1976, V.2, N. 3, 00024440
C PP.281-289. 00024450
C                                     00024460
C PARAMETERS: 00024470
C                                     00024480
C NY = NUMBER OF DATA POINTS GIVEN IN Y(NY), NY.GT.2. 00024490
C Y()= ARRAY OF NY GIVEN ORDINATES (DIM.GE.NY). 00024500
C Y() POINTS ASSUMED EQUALLY SPACED IN X-DIRECTION. 00024510
C B,C,D,E,F() = RESULTING ARRAYS (EACH DIM.GE.NY) OF 00024520
C QUINTIC SPLINE COEFFICIENTS, WHERE 00024530
C FOR ANY XX IN (X(I),X(I+1)): 00024540
C S(XX)=((((F(I)*T+E(I))*T+D(I))*T+C(I))*T+B(I))*T+Y(I) WITH 00024550
C T=(XX-X(I))/DELX, DELX=(X(I+1)-X(I)) FOR ANY I. 00024560
C NOTE: SEE PROC 'QPOINT' TO EVAL THE QUINTIC SPLINE AFTER 00024570
C 'QUINT' IS CALLED. 00024580
C                                     00024590
C DIMENSION Y(1),B(1),C(1),D(1),E(1),F(1) 00024600
C IF(NY.LE.2) GO TO 4 00024610
N=NY-3 00024620
F=0.0 00024630
Q=0.0 00024640
R=0.0 00024650
S=0.0 00024660

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	T=0.0	00024670
	DO 1 I=1,N	00024680
	U=P*R	00024690
	B(I)=1.0/(66.0-U*R-Q)	00024700
	R=26.0-U	00024710
	C(I)=R	00024720
	D(I)=Y(I+3)-3.0*(Y(I+2)-Y(I+1))-Y(I)-U*S-Q*T	00024730
	Q=P	00024740
	P=B(I)	00024750
	T=S	00024760
	S=D(I)	00024770
1	CONTINUE	00024780
	D(N+2)=0.0	00024790
	N1=N+1	00024800
	D(N1)=0.0	00024810
	DO 2 J=1,N	00024820
	I=N1-J	00024830
	D(I)=(D(I)-C(I)*D(I+1)-D(I+2))*B(I)	00024840
2	CONTINUE	00024850
	N=NY-1	00024860
	Q=0.0	00024870
	V=D(1)	00024880
	T=V	00024890
	R=V	00024900
	DO 3 I=2,N	00024910
	P=Q	00024920
	Q=R	00024930
	R=D(I)	00024940
	S=T	00024950
	T=P-Q-Q+R	00024960
	F(I)=T	00024970
	U=5.0*(-P+Q)	00024980
	E(I)=U	00024990
	D(I)=10.0*(P+Q)	00025000
	C(I)=0.5*(Y(I+1)+Y(I-1)+S-T)-Y(I)-U	00025010
	B(I)=0.5*(Y(I+1)-Y(I-1)-S-T)-D(I)	00025020
3	CONTINUE	00025030
	F(1)=V	00025040
	E(1)=0.0	00025050
	E(NY)=0.0	00025060
	D(1)=0.0	00025070
	D(NY)=0.0	00025080
	C(1)=C(2)-10.0*V	00025090
	C(NY)=C(NY-1)+10.0*T	00025100
	B(1)=Y(2)-Y(1)-C(1)-V	00025110
	B(NY)=Y(NY)-Y(NY-1)+C(NY)-T	00025120
4	RETURN	00025130
	END	00025140
	SUBROUTINE QPOINT(NY,Y,B,C,D,E,F,X1,DELX,XX,YY)	00025150
C	GIVEN THE QUINTIC SPLINE COEFF'S B(*),C(*),D(*),E(*),F(*) AS	00025160
C	OBTAINED FROM SUBR 'QUINT', AND GIVEN NY OBS. DATA Y(NY) EQUALLY	00025170



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C   SPACED BY DELX STARTING AT X1, THEN 'QPOINT' INTERPOLATES      00025180
C   YY AT ANY XX IN (X1,X1+(NY-1)*DELX).                          00025190
C                                                                    00025200
      DIMENSION Y(1),B(1),C(1),D(1),E(1),F(1)                      00025210
      XMAX=X1+(NY-1)*DELX                                           00025220
      IF(XX.LT.X1.OR.XX.GT.XMAX) GO TO 2                            00025230
      I=(XX-X1)/DELX+1                                              00025240
      XI=X1+(I-1)*DELX                                             00025250
      T=(XX-XI)/DELX                                               00025260
      YY=(((((F(I)*T+E(I))*T+D(I))*T+C(I))*T+B(I))*T+Y(I))         00025270
1     RETURN                                                         00025280
2     WRITE(6,3) XX,X1,XMAX                                         00025290
3     FORMAT('QPOINT ERROR-- XX=',E16.8,' NOT IN CLOSED INTERVAL (', 00025300
& E16.8,',',E16.8,')')                                           00025310
      GO TO 1                                                       00025320
      END                                                           00025330

      COMPLEX FUNCTION CANC4(A1,B1,EP,M,N,FUN,MF,ESUM)              00025340
C---COMPLEX FUNCTION DEFINITE INTEGRATION BY                       00025350
C   ADAPTIVE QUADRATURE USING NEWTON-COTES NO. 4 (N=1,2,3), OR     00025360
C   AUTOMATIC GAUSSIAN QUADRATURE (N=4,5)....                     00025370
C   A GENERAL ROUTINE IN SINGLE-PRECISION COMPLEX...              00025380
C   BY W.L.ANDERSON, U.S.GEOLOGICAL SURVEY, DENVER, COLORADO.     00025390
C---PARAMETERS--                                                  00025400
C   A1      = LOWER LIMIT OF INTEGRATION (REAL*4)                  00025410
C   B1      = UPPER LIMIT OF INTEGRATION (REAL*4)                  00025420
C   EP      = DESIRED REL. ERROR (REAL*4) IN COMPLEX RESULT 'CANC4', 00025430
C             (FOR BOTH RE & IM PARTS OF CANC4)                    00025440
C   M       = RESULTING NUMBER OF COMPLEX 'FUN EVALUATIONS'        00025450
C   N       = ERROR TEST TYPE:                                     00025460
C             = 1 FOR ABS. ERROR TEST (NOT GENERALLY RECOMMENDED) 00025470
C             = 2 FOR 'L-ONE' ERROR TEST                           00025480
C             = 3 FOR 'L-INFINITY' ERROR TEST                       00025490
C             = 4 FOR REL. ERROR TEST USING ADAPTIVE GAUSSIAN QUADRATURE 00025500
C             = 5 FOR REL. ERROR TEST USING NON-ADAPTIVE GAUSSIAN QUAD... 00025510
C   NOTE:   N=1,2,OR 3 USES ADAPTIVE NEWTON-COTES QUADRATURE, AND   00025520
C           N=4 OR 5 USES ADAPTIVE OR NON-ADAPTIVE GAUSS QUADRATURES 00025530
C   FUN     = EXTERNAL COMPLEX FUNCTION NAME (COMPLEX*8)          00025540
C   MF      = MAX. FUN EVALUATIONS ALLOWED BEFORE ACCEPTING COMPLEX 00025550
C             RESULT 'CANC4' WITH M.GE.MF....                     00025560
C   ESUM    = ACTUAL COMPLEX ERROR ACHIEVED AT EXIT....            00025570
C---SUBPROGRAMS CALLED: CQSUBA,CQSUB (WHICH CALLS CQUAD)          00025580
C   (THESE ARE FOR N=4 OR 5 GAUSSIAN QUADRATURES)                  00025590
C                                                                    00025600
      COMPLEX FUN,ESUM,TSUM,FA, F,X,Z, CQSUBA,CQSUB,                00025610
1     F1,FS,F3,FM,F2,FT,F4,FB,FTP,FBP,FMAX,FTST,EST,AEST,EST1,EST2,AEST00025620
2     1,AEST2,ABSAR,DELTA,DIFF,DAFT,SUM                            00025630
      DIMENSION F2(30),F4(30),FTP(30),FBP(30),FTST(5),EST2(30),NRTR(30) 00025640
      DIMENSION AEST2(30),XB(30)                                    00025650
      DIMENSION FMX(2)                                              00025660
      EXTERNAL FUN                                                  00025670
      EQUIVALENCE (FMX(1),FMAX)                                     00025680

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C--	STATEMENT FUNCTION GOES HERE ON HONEYWELL MULTICS SYSTEM	00025690
	F(X)=CMPLX(ABS(REAL(X)),ABS(AIMAG(X)))	00025700
C	THE PARAMETER SETUP FOR THE INITIAL CALL	00025710
	IF(N.LE.0)GO TO 210	00025720
	IF(N.GT.5)GO TO 211	00025730
	GO TO (10,10,10,400,500),N	00025740
10	A=A1	00025750
	B=B1	00025760
	EPS=EP*63.0	00025770
	ESUM=(0.0,0.0)	00025780
	TSUM=(0.0,0.0)	00025790
	LVL=1	00025800
	DA=B-A	00025810
	FA=FUN(A)	00025820
	FS=FUN((3.0 *A+B)/4.0 )	00025830
	FM=FUN((A+B)*0.5 )	00025840
	FT=FUN((A+3.0 *B)/4.0 )	00025850
	FB=FUN(B)	00025860
	M=5	00025870
	FMAX=F(FA)	00025880
	FTST(1)=FMAX	00025890
	FTST(2)=F(FS)	00025900
	FTST(3)=F(FM)	00025910
	FTST(4)=F(FT)	00025920
	FTST(5)=F(FB)	00025930
	DO 100 I=2,5	00025940
	IF(FMX(1).GE.REAL(FTST(I)))GO TO 101	00025950
	FMX(1)=REAL(FTST(I))	00025960
101	IF(FMX(2).GE.AIMAG(FTST(I)))GO TO 100	00025970
	FMX(2)=AIMAG(FTST(I))	00025980
100	CONTINUE	00025990
	EST=(7.0 *(FA+FB)+32.0 *(FS+FT)+12.0 *FM)*DA/90.0	00026000
	ABSAR=(7.0 *(FTST(1)+FTST(5))+32.0 *(FTST(2)+FTST(4))+12.0 *FTS	00026010
	1T(3))*DA/90.0	00026020
	AEST=ABSAR	00026030
C	1=RECUR	00026040
1	SX=(DA/(2.0 **LVL))/90.0	00026050
	F1=FUN((7.0 *A+B)/8.0 )	00026060
	F3=FUN((5.0 *A+3.0 *B)/8.0 )	00026070
	F2(LVL)=FUN((3.0 *A+5.0 *B)/8.0 )	00026080
	F4(LVL)=FUN((A+7.0 *B)/8.0 )	00026090
	EST1=SX*(7.0 *(FA+FM)+32.0 *(F1+F3)+12.0 *FS)	00026100
	FBP(LVL)=FB	00026110
	FTP(LVL)=FT	00026120
	XB(LVL)=B	00026130
	EST2(LVL)=SX*(7.0 *(FM+FB)+32.0 *(F2(LVL)+F4(LVL))+12.0 *FT)	00026140
	SUM=EST1+EST2(LVL)	00026150
	FTST(1)=F(F1)	00026160
	FTST(2)=F(F2(LVL))	00026170
	FTST(3)=F(F3)	00026180
	FTST(4)=F(F4(LVL))	00026190
	FTST(5)=F(FM)	00026200

	AEST1=SX*(7.0 *(F(FA) +FTST(5))+32.0 *(FTST(1)+FTST(3))+12.0	00026210
	X*F(FS))	00026220
	AEST2(LVL)=SX*(7.0 *(FTST(5)+F(FB) )+32.0 *(FTST(2)+FTST(4))+100026230	
	X2.0*F(FT))	00026240
	ABSAR=ABSAR-AEST+AEST1+AEST2(LVL)	00026250
	M=M+4	00026260
	IF(M.GE.MF) GO TO 5	00026270
	GO TO (201,200,202),N	00026280
200	DELTA=ABSAR	00026290
	GO TO 205	00026300
210	WRITE(6,39)	00026310
	39 FORMAT(' CANC4- ERROR RETURN-N,LE.0')	00026320
	GO TO 999	00026330
211	WRITE(6,40)	00026340
	40 FORMAT(' CANC4- ERROR RETURN-N,GT.5')	00026350
	GO TO 999	00026360
201	DELTA=(1.0,1.0)	00026370
	GO TO 205	00026380
202	DO 203 I=1,4	00026390
	IF(FMX(1).GE.REAL(FTST(I)))GO TO 2031	00026400
	FMX(1)=REAL(FTST(I))	00026410
2031	IF(FMX(2).GE.AIMAG(FTST(I)))GO TO 203	00026420
	FMX(2)=AIMAG(FTST(I))	00026430
203	CONTINUE	00026440
	DELTA=FMX	00026450
205	DAFT=EST-SUM	00026460
	DIFF=F(DAFT)	00026470
	DAFT=DAFT/63.0	00026480
	Z=DIFF-EPS*DELTA	00026490
	IF(REAL(Z).LE.0.0.AND.AIMAG(Z).LE.0.0) GO TO 6	00026500
	3 IF(LVL-30)4,2,2	00026510
	6 IF(LVL-1)2,4,2	00026520
C	2=UP	00026530
	2 A=B	00026540
	ESUM=ESUM+DAFT	00026550
	TSUM=TSUM+SUM	00026560
	9 LVL=LVL-1	00026570
	L=NRTR(LVL)	00026580
	GO TO (11,12),L	00026590
C	11=R1,12=R2	00026600
	4 NRTR(LVL)=1	00026610
	EST=EST1	00026620
	AEST=AEST1	00026630
	FB=FM	00026640
	FT=F3	00026650
	FM=FS	00026660
	FS=F1	00026670
	B=(A+B)/2.0	00026680
	EPS=EPS/2.0	00026690
	7 LVL=LVL+1	00026700
	GO TO 1	00026710
11	NRTR(LVL)=2	00026720

FA=FB	00026730
FS=F2(LVL)	00026740
FM=FTP(LVL)	00026750
FT=F4(LVL)	00026760
FB=FBP(LVL)	00026770
B=XB(LVL)	00026780
EST=EST2(LVL)	00026790
AEST=AEST2(LVL)	00026800
GO TO 7	00026810
12 EPS=2.0 *EPS	00026820
IF(LVL-1)5,5,9	00026830
5 CANC4=TSUM-ESUM	00026840
GO TO 999	00026850
400 CANC4=CQSUBA(A1,B1,EP,M,ICK,ESUM,FUN,MF)	00026860
GO TO 999	00026870
500 CANC4=CQSUB(A1,B1,EP,M,ICK,ESUM,FUN,MF)	00026880
999 RETURN	00026890
END	00026900
SUBROUTINE CQUAD(A,B,RESULT,K,EPSIL,NPTS,ICHECK,F,MEV)	00026910
C--MODIFIED BY W.L.ANDERSON FOR COMPLEX FUNCTIONS--12/28/73.	00026920
COMPLEX F,RESULT,FUNCT,FZERO,ACUM	00026930
DIMENSION FUNCT(127), P(381), RESULT(8)	00026940
C THIS SUBROUTINE ATTEMPTS TO CALCULATE THE INTEGRAL OF F(X)	00026950
C OVER THE INTERVAL ** TO ** WITH RELATIVE ERROR NOT	00026960
C EXCEEDING *EPSIL*.	00026970
C THE RESULT IS OBTAINED USING A SEQUENCE OF 1,3,7,15,31,63,	00026980
C 127, AND 255 POINT INTERLACING FORMULAE(NO INTEGRAND	00026990
C EVALUATIONS ARE WASTED) OF RESPECTIVE DEGREE 1,5,11,23,	00027000
C 47,95,191 AND 383. THE FORMULAE ARE BASED ON THE OPTIMAL	00027010
C EXTENSION OF THE 3-POINT GAUSS FORMULA. DETAILS OF	00027020
C THE FORMULAE ARE GIVEN IN *THE OPTIMUM ADDITION OF POINTS	00027030
C TO QUADRATURE FORMULAE* BY T.N.L. PATTERSON,MATHS.COMP.	00027040
C VOL 22,847-856,1968.	00027050
C *** INPUT ***	00027060
C A LOWER LIMIT OF INTEGRATION.	00027070
C B UPPER LIMIT OF INTEGRATION.	00027080
C EPSIL RELATIVE ACCURACY REQUIRED. WHEN THE RELATIVE	00027090
C DIFFERENCE OF TWO SUCCESSIVE FORMULAE DOES NOT	00027100
C EXCEED *EPSIL* THE LAST FORMULA COMPUTED IS TAKEN	00027110
C AS THE RESULT.	00027120
C F F(X) IS THE INTEGRAND.	00027130
C *** OUTPUT ***	00027140
C RESULT THIS ARRAY,WHICH SHOULD BE DECLARED TO HAVE AT	00027150
C LEAST 8 ELEMENTS, HOLDS THE RESULTS OBTAINED BY	00027160
C THE 1,3,7, ETC., POINT FORMULAE. THE NUMBER OF	00027170
C FORMULAE COMPUTED DEPENDS ON *EPSIL*.	00027180
C K RESULT(K) HOLDS THE VALUE OF THE INTEGRAL TO THE	00027190
C SPECIFIED RELATIVE ACCURACY.	00027200
C NPTS NUMBER INTEGRAND EVALUATIONS.	00027210
C ICHECK ON EXIT NORMALLY ICHECK=0. HOWEVER IF CONVERGENCE	00027220
C TO THE ACCURACY REQUESTED IS NOT ACHIEVED ICHECK=1	00027230

[illegible]

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* 0.98868475754742947994E 00,0.61155068221172463397E-02,      00027760
* 0.97218287474858179658E 00,0.10498246909621321898E-01,      00027770
* 0.94634285837340290515E 00,0.15406750466559497802E-01,      00027780
* 0.91037115695700429250E 00,0.20594233915912711149E-01,      00027790
* 0.86390793819369047715E 00,0.25869679327214746911E-01,      00027800
* 0.80694053195021761186E 00,0.31073551111687964880E-01,      00027810
* 0.73975604435269475868E 00,0.36064432780782572640E-01,      00027820
* 0.66290966002478059546E 00,0.40715510116944318934E-01,      00027830
* 0.57719571005204581484E 00,0.44914531653632197414E-01,      00027840
* 0.48361802694584102756E 00,0.48564330406673198716E-01/      00027850
DATA      00027860
* P( 85),P( 86),P( 87),P( 88),P( 89),P( 90),P( 91),      00027870
* P( 92),P( 93),P( 94),P( 95),P( 96),P( 97),P( 98),      00027880
* P( 99),P(100),P(101),P(102),P(103),P(104),P(105),      00027890
* P(106),P(107),P(108),P(109),P(110),P(111),P(112)/      00027900
* 0.38335932419873034692E 00,0.51583253952048458777E-01,      00027910
* 0.27774982202182431507E 00,0.53905499335266063927E-01,      00027920
* 0.16823525155220746498E 00,0.55481404356559363988E-01,      00027930
* 0.56344313046592789972E-01,0.56277699831254301273E-01,      00027940
* 0.56377628360384717388E-01,0.16801938574103865271E-01,      00027950
* 0.64519000501757369228E-02,0.25078569652949768707E-01,      00027960
* 0.21088152457266328793E-02,0.11615723319955134727E-01,      00027970
* 0.21438980012503867246E-01,0.27394605263981432516E-01,      00027980
* 0.63260731936263354422E-03,0.41115039786546930472E-02,      00027990
* 0.89892757840641357233E-02,0.14244877372916774306E-01,      00028000
* 0.19219905124727766019E-01,0.23406777495314006201E-01,      00028010
* 0.26417473395058259931E-01,0.27989218255238159704E-01,      00028020
* 0.18073956444538835782E-03,0.12895240826104173921E-02,      00028030
* 0.30577534101755311361E-02,0.52491234548088591251E-02/      00028040
DATA      00028050
* P(113),P(114),P(115),P(116),P(117),P(118),P(119),      00028060
* P(120),P(121),P(122),P(123),P(124),P(125),P(126),      00028070
* P(127),P(128),P(129),P(130),P(131),P(132),P(133),      00028080
* P(134),P(135),P(136),P(137),P(138),P(139),P(140)/      00028090
* 0.77033752332797418482E-02,0.10297116957956355524E-01,      00028100
* 0.12934839663607373455E-01,0.15536775555843982440E-01,      00028110
* 0.18032216390391286320E-01,0.20357755058472159467E-01,      00028120
* 0.22457265826816098707E-01,0.24282165203336599358E-01,      00028130
* 0.25791626976024229388E-01,0.26952749667633031963E-01,      00028140
* 0.27740702178279681994E-01,0.28138849915627150636E-01,      00028150
* 0.99998243035489159858E 00,0.50536095207862517625E-04,      00028160
* 0.99959879967191068325E 00,0.37774664632698466027E-03,      00028170
* 0.99831663531840739253E 00,0.93836984854238150079E-03,      00028180
* 0.99572410469840718851E 00,0.16811428654214699063E-02,      00028190
* 0.99149572117810613240E 00,0.25687649437940203731E-02,      00028200
* 0.98537149959852037111E 00,0.35728927835172996494E-02,      00028210
* 0.97714151463970571416E 00,0.46710503721143217474E-02,      00028220
* 0.96663785155841656709E 00,0.58434498758356395076E-02/      00028230
DATA      00028240
* P(141),P(142),P(143),P(144),P(145),P(146),P(147),      00028250
* P(148),P(149),P(150),P(151),P(152),P(153),P(154),      00028260
* P(155),P(156),P(157),P(158),P(159),P(160),P(161),      00028270

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* P(162),P(163),P(164),P(165),P(166),P(167),P(168)/      00028280
* 0.95373000642576113641E 00,0.70724899954335554680E-02,  00028290
* 0.93832039777959288365E 00,0.83428387539681577056E-02,  00028300
* 0.92034002547001242073E 00,0.96411777297025366953E-02,  00028310
* 0.89974489977694003664E 00,0.10955733387837901648E-01,  00028320
* 0.87651341448470526974E 00,0.12275830560082770087E-01,  00028330
* 0.85064449476835027976E 00,0.13591571009765546790E-01,  00028340
* 0.82215625436498040737E 00,0.14893641664815182035E-01,  00028350
* 0.79108493379984836143E 00,0.16173218729577719942E-01,  00028360
* 0.75748396638051363793E 00,0.17421930159464173747E-01,  00028370
* 0.72142308537009891548E 00,0.18631848256138790186E-01,  00028380
* 0.68298743109107922809E 00,0.19795495048097499488E-01,  00028390
* 0.64227664250975951377E 00,0.20905851445812023852E-01,  00028400
* 0.59940393024224289297E 00,0.21956366305317824939E-01,  00028410
* 0.55449513263193254887E 00,0.22940964229387748761E-01/  00028420
DATA 00028430
* P(169),P(170),P(171),P(172),P(173),P(174),P(175),      00028440
* P(176),P(177),P(178),P(179),P(180),P(181),P(182),      00028450
* P(183),P(184),P(185),P(186),P(187),P(188),P(189),      00028460
* P(190),P(191),P(192),P(193),P(194),P(195),P(196)/      00028470
* 0.50768775753371660215E 00,0.23854052106038540080E-01,  00028480
* 0.45913001198983233287E 00,0.24690524744487676909E-01,  00028490
* 0.40897982122988867241E 00,0.25445769965464765813E-01,  00028500
* 0.35740383783153215238E 00,0.26115673376706097680E-01,  00028510
* 0.30457644155671404334E 00,0.26696622927450359906E-01,  00028520
* 0.25067873030348317661E 00,0.27185513229624791819E-01,  00028530
* 0.19589750271110015392E 00,0.27579749566481873035E-01,  00028540
* 0.14042423315256017459E 00,0.27877251476613701609E-01,  00028550
* 0.84454040083710883710E-01,0.28076455793817246607E-01,  00028560
* 0.28184648949745694339E-01,0.28176319033016602131E-01,  00028570
* 0.28188814180192358694E-01,0.84009692870519326354E-02,  00028580
* 0.32259500250878684614E-02,0.12539284826474884353E-01,  00028590
* 0.10544076228633167722E-02,0.58078616599775673635E-02,  00028600
* 0.10719490006251933623E-01,0.13697302631990716258E-01/  00028610
DATA 00028620
* P(197),P(198),P(199),P(200),P(201),P(202),P(203),      00028630
* P(204),P(205),P(206),P(207),P(208),P(209),P(210),      00028640
* P(211),P(212),P(213),P(214),P(215),P(216),P(217),      00028650
* P(218),P(219),P(220),P(221),P(222),P(223),P(224)/      00028660
* 0.31630366082226447689E-03,0.20557519893273465236E-02,  00028670
* 0.44946378920320678616E-02,0.71224386864583871532E-02,  00028680
* 0.96099525623638830097E-02,0.11703388747657003101E-01,  00028690
* 0.13208736697529129966E-01,0.13994609127619079852E-01,  00028700
* 0.90372734658751149261E-04,0.64476204130572477933E-03,  00028710
* 0.15288767050877655684E-02,0.26245617274044295626E-02,  00028720
* 0.38516876166398709241E-02,0.51485584789781777618E-02,  00028730
* 0.64674198318036867274E-02,0.77683877779219912200E-02,  00028740
* 0.90161081951956431600E-02,0.10178877529236079733E-01,  00028750
* 0.11228632913408049354E-01,0.12141082601668299679E-01,  00028760
* 0.12895813488012114694E-01,0.13476374833816515982E-01,  00028770
* 0.13870351089139840997E-01,0.14069424957813575318E-01,  00028780
* 0.25157870384280661489E-04,0.18887326450650491366E-03,  00028790
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* 0.46918492424785040975E-03,0.84057143271072246365E-03/      00028800
DATA                                                                00028810
* P(225),P(226),P(227),P(228),P(229),P(230),P(231),          00028820
* P(232),P(233),P(234),P(235),P(236),P(237),P(238),          00028830
* P(239),P(240),P(241),P(242),P(243),P(244),P(245),          00028840
* P(246),P(247),P(248),P(249),P(250),P(251),P(252)/          00028850
* 0.12843824718970101768E-02,0.17864463917586498247E-02,    00028860
* 0.23355251860571608737E-02,0.29217249379178197538E-02,    00028870
* 0.35362449977167777340E-02,0.41714193769840788528E-02,    00028880
* 0.48205888648512683476E-02,0.54778666939189508240E-02,    00028890
* 0.61379152800413850435E-02,0.67957855048827733948E-02,    00028900
* 0.74468208324075910174E-02,0.80866093647888599710E-02,    00028910
* 0.87109650797320868736E-02,0.93159241280693950932E-02,    00028920
* 0.98977475240487497440E-02,0.10452925722906011926E-01,    00028930
* 0.10978183152658912470E-01,0.11470482114693874380E-01,    00028940
* 0.11927026053019270040E-01,0.12345262372243838455E-01,    00028950
* 0.12722884982732382906E-01,0.13057836688353048840E-01,    00028960
* 0.13348311463725179953E-01,0.13592756614812395910E-01,    00028970
* 0.13789874783240936517E-01,0.13938625738306850804E-01,    00028980
* 0.14038227896908623303E-01,0.14088159516508301065E-01/    00028990
DATA                                                                00029000
* P(253),P(254),P(255),P(256),P(257),P(258),P(259),          00029010
* P(260),P(261),P(262),P(263),P(264),P(265),P(266),          00029020
* P(267),P(268),P(269),P(270),P(271),P(272),P(273),          00029030
* P(274),P(275),P(276),P(277),P(278),P(279),P(280)/          00029040
* 0.99999759637974846462E 00,0.69379364324108267170E-05,    00029050
* 0.99994399620705437576E 00,0.53275293669780613125E-04,    00029060
* 0.99976049092443204733E 00,0.13575491094922871973E-03,    00029070
* 0.99938033802502358193E 00,0.24921240048299729402E-03,    00029080
* 0.99874561446809511470E 00,0.38974528447328229322E-03,    00029090
* 0.99780535449595727456E 00,0.55429531493037471492E-03,    00029100
* 0.99651414591489027385E 00,0.74028280424450333046E-03,    00029110
* 0.99483150280062100052E 00,0.94536151685852538246E-03,    00029120
* 0.99272134428278861533E 00,0.11674841174299594077E-02,    00029130
* 0.99015137040077015918E 00,0.14049079956551446427E-02,    00029140
* 0.98709252795403406719E 00,0.16561127281544526052E-02,    00029150
* 0.98351865757863272876E 00,0.19197129710138724125E-02,    00029160
* 0.97940628167086268381E 00,0.21944069253638388388E-02,    00029170
* 0.97473445975240266776E 00,0.24789582266575679307E-02/    00029180
DATA                                                                00029190
* P(281),P(282),P(283),P(284),P(285),P(286),P(287),          00029200
* P(288),P(289),P(290),P(291),P(292),P(293),P(294),          00029210
* P(295),P(296),P(297),P(298),P(299),P(300),P(301),          00029220
* P(302),P(303),P(304),P(305),P(306),P(307),P(308)/          00029230
* 0.96948465950245923177E 00,0.27721957645934509940E-02,    00029240
* 0.96364062156981213252E 00,0.30730184347025783234E-02,    00029250
* 0.95718821610986096274E 00,0.33803979910869203823E-02,    00029260
* 0.95011529752129487656E 00,0.36933779170256508183E-02,    00029270
* 0.94241156519108305981E 00,0.40110687240750233989E-02,    00029280
* 0.93406843615772578800E 00,0.43326409680929828545E-02,    00029290
* 0.92507893290707565236E 00,0.46573172997568547773E-02,    00029300
* 0.91543758715576504064E 00,0.49843645647655386012E-02,    00029310
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* 0.90514035881326159519E 00,0.53130866051870565663E-02, 00029320
* 0.89418456833555902286E 00,0.56428181013844441585E-02, 00029330
* 0.88256884024734190684E 00,0.59729195655081658049E-02, 00029340
* 0.87029305554811390585E 00,0.63027734490857587172E-02, 00029350
* 0.85735831088623215653E 00,0.66317812429018878941E-02, 00029360
* 0.84376688267270860104E 00,0.69593614093904229394E-02/ 00029370
DATA 00029380
* P(309),P(310),P(311),P(312),P(313),P(314),P(315), 00029390
* P(316),P(317),P(318),P(319),P(320),P(321),P(322), 00029400
* P(323),P(324),P(325),P(326),P(327),P(328),P(329), 00029410
* P(330),P(331),P(332),P(333),P(334),P(335),P(336)/ 00029420
* 0.82952219463740140018E 00,0.72849479805538070639E-02, 00029430
* 0.81462878765513741344E 00,0.76079896657190565832E-02, 00029440
* 0.79909229096084140180E 00,0.79279493342948491103E-02, 00029450
* 0.78291939411828301639E 00,0.82443037630328680306E-02, 00029460
* 0.76611781930376009072E 00,0.85565435613076896192E-02, 00029470
* 0.74869629361693660282E 00,0.88641732094824942641E-02, 00029480
* 0.73066452124218126133E 00,0.91667111635607884067E-02, 00029490
* 0.71203315536225203459E 00,0.94636899938300652943E-02, 00029500
* 0.69281376977911470289E 00,0.97546565363174114611E-02, 00029510
* 0.67301883023041847920E 00,0.10039172044056840798E-01, 00029520
* 0.65266166541001749610E 00,0.10316812330947621682E-01, 00029530
* 0.63175643771119423041E 00,0.10587167904885197931E-01, 00029540
* 0.61031811371518640016E 00,0.10849844089337314099E-01, 00029550
* 0.58836243444766254143E 00,0.11104461134006926537E-01/ 00029560
DATA 00029570
* P(337),P(338),P(339),P(340),P(341),P(342),P(343), 00029580
* P(344),P(345),P(346),P(347),P(348),P(349),P(350), 00029590
* P(351),P(352),P(353),P(354),P(355),P(356),P(357), 00029600
* P(358),P(359),P(360),P(361),P(362),P(363),P(364)/ 00029610
* 0.56590588542365442262E 00,0.11350654315980596602E-01, 00029620
* 0.54296566649831149049E 00,0.11588074033043952568E-01, 00029630
* 0.51955966153745702199E 00,0.11816385890830235763E-01, 00029640
* 0.49570640791876146017E 00,0.12035270785279562630E-01, 00029650
* 0.47142506587165887693E 00,0.12244424981611985899E-01, 00029660
* 0.44673538766202847374E 00,0.12443560190714035263E-01, 00029670
* 0.42165768662616330006E 00,0.12632403643542078765E-01, 00029680
* 0.39621280605761593918E 00,0.12810698163877361967E-01, 00029690
* 0.37042208795007823014E 00,0.12978202239537399286E-01, 00029700
* 0.34430734159943802278E 00,0.13134690091960152836E-01, 00029710
* 0.31789081206847668318E 00,0.13279951743930530650E-01, 00029720
* 0.29119514851824668196E 00,0.13413793085110098513E-01, 00029730
* 0.26424337241092676194E 00,0.13536035934956213614E-01, 00029740
* 0.23705884558982972721E 00,0.13646518102571291428E-01/ 00029750
DATA 00029760
* P(365),P(366),P(367),P(368),P(369),P(370),P(371), 00029770
* P(372),P(373),P(374),P(375),P(376),P(377),P(378), 00029780
* P(379),P(380),P(381)/ 00029790
* 0.20966523824318119477E 00,0.13745093443001896632E-01, 00029800
* 0.18208649675925219825E 00,0.13831631909506428676E-01, 00029810
* 0.15434681148137810869E 00,0.13906019601325461264E-01, 00029820
* 0.12647058437230196685E 00,0.13968158806516938516E-01, 00029830

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* 0.98482396598119202090E-01,0.14017968039456608810E-01,      00029840
* 0.70406976042855179063E-01,0.14055382072649964277E-01,      00029850
* 0.42269164765363603212E-01,0.14080351962553661325E-01,      00029860
* 0.14093886410782462614E-01,0.14092845069160408355E-01,      00029870
* 0.14094407090096179347E-01/      00029880
  ICHECK = 0      00029890
C CHECK FOR TRIVIAL CASE.      00029900
  IF (A.EQ.B) GO TO 70      00029910
C SCALE FACTORS.      00029920
  SUM = (B+A)/2.0      00029930
  DIFF = (B-A)/2.0      00029940
C 1-POINT GAUSS      00029950
  FZERO = F(SUM)      00029960
  RESULT(1) = 2.0*FZERO*DIFF      00029970
  I = 0      00029980
  IOLD = 0      00029990
  INEW = 1      00030000
  K = 2      00030010
  ACUM = (0.0,0.0)      00030020
  GO TO 30      00030030
10 IF (K.EQ.8) GO TO 50      00030040
  IF(INEW+IOLD.GE.MEV) GO TO 60      00030050
  K = K + 1      00030060
  ACUM = (0.0,0.0)      00030070
C CONTRIBUTION FROM FUNCTION VALUES ALREADY COMPUTED.      00030080
  DO 20 J=1,IOLD      00030090
    I = I + 1      00030100
    ACUM = ACUM + P(I)*FUNCT(J)      00030110
  20 CONTINUE      00030120
C CONTRIBUTION FROM NEW FUNCTION VALUES.      00030130
  30 IOLD = IOLD + INEW      00030140
  DO 40 J=INEW,IOLD      00030150
    I = I + 1      00030160
    X = P(I)*DIFF      00030170
    FUNCT(J) = F(SUM+X) + F(SUM-X)      00030180
    I = I + 1      00030190
    ACUM = ACUM + P(I)*FUNCT(J)      00030200
  40 CONTINUE      00030210
  INEW = IOLD + 1      00030220
  I = I + 1      00030230
  RESULT(K) = (ACUM+P(I)*FZERO)*DIFF      00030240
C CHECK FOR CONVERGENCE.      00030250
  IF(ABS(REAL(RESULT(K))-REAL(RESULT(K-1))),LE.EPSIL*      00030260
  $ABS(REAL(RESULT(K))),AND,      00030270
  $ ABS(AIMAG(RESULT(K))-AIMAG(RESULT(K-1))),LE.EPSIL*      00030280
  $ABS(AIMAG(RESULT(K)))) GO TO 60      00030290
  GO TO 10      00030300
C CONVERGENCE NOT ACHIEVED.      00030310
  50 ICHECK = 1      00030320
C NORMAL TERMINATION.      00030330
  60 NPTS = INEW + IOLD      00030340
  RETURN      00030350

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C TRIVIAL CASE	00030360
70 K = 2	00030370
RESULT(1) = (0.0,0.0)	00030380
RESULT(2) = (0.0,0.0)	00030390
NPTS = 0	00030400
RETURN	00030410
END	00030420
COMPLEX FUNCTION CQSUB(A, B, EPSIL, NPTS, ICHECK, RELERR, F, MEV)	00030430
COMPLEX RELERR, F, RESULT, ESTIM, COMP	00030440
C THIS FUNCTION ROUTINE PERFORMS AUTOMATIC INTEGRATION	00030450
C OVER A FINITE INTERVAL USING THE BASIC INTEGRATION	00030460
C ALGORITHM QUAD, TOGETHER WITH, IF NECESSARY, A NON-	00030470
C ADAPTIVE SUBDIVISION PROCESS.	00030480
C THE CALL TAKES THE FORM	00030490
C CQSUB(A,B,EPSIL,NPTS,ICHECK,RELERR,F,MEV)	00030500
C AND CAUSES F(X) TO BE INTEGRATED OVER (A,B) WITH RELATIVE	00030510
C ERROR HOPEFULLY NOT EXCEEDING EPSIL. SHOULD QUAD CONVERGE	00030520
C (ICHECK=0) THEN QSUB WILL RETURN THE VALUE OBTAINED BY IT	00030530
C OTHERWISE SUBDIVISION WILL BE INVOKED AS A RESCUE	00030540
C OPERATION IN A NON-ADAPTIVE MANNER. THE ARGUMENT RELERR	00030550
C GIVES A CRUDE ESTIMATE OF THE ACTUAL RELATIVE ERROR	00030560
C OBTAINED.	00030570
C THE SUBDIVISION STRATEGY IS AS FOLLOWS	00030580
C LET THE INTERVAL (A,B) BE DIVIDED INTO 2**N PANELS AT STEP	00030590
C N OF THE SUBDIVISION PROCESS. QUAD IS APPLIED FIRST TO	00030600
C THE SUBDIVIDED INTERVAL ON WHICH QUAD LAST FAILED TO	00030610
C CONVERGE AND IF CONVERGENCE IS NOW ACHIEVED THE REMAINING	00030620
C PANELS ARE INTEGRATED. SHOULD A CONVERGENCE FAILURE OCCUR	00030630
C ON ANY PANEL THE INTEGRATION AT THAT POINT IS TERMINATED	00030640
C AND THE PROCEDURE REPEATED WITH N INCREASED BY 1. THE	00030650
C STRATEGY INSURES THAT POSSIBLY DELINQUENT INTERVALS ARE	00030660
C EXAMINED BEFORE WORK, WHICH LATER MIGHT HAVE TO BE	00030670
C DISCARDED, IS INVESTED ON WELL BEHAVED PANELS. THE	00030680
C PROCESS IS COMPLETE WHEN NO CONVERGENCE FAILURE OCCURS ON	00030690
C ANY PANEL AND THE SUM OF THE RESULTS OBTAINED BY QUAD ON	00030700
C EACH PANEL IS TAKEN AS THE VALUE OF THE INTEGRAL.	00030710
C THE PROCESS IS VERY CAUTIOUS IN THAT THE SUBDIVISION OF	00030720
C THE INTERVAL (A,B) IS UNIFORM, THE FINENESS OF WHICH IS	00030730
C CONTROLLED BY THE SUCCESS OF QUAD. IN THIS WAY IT IS	00030740
C RATHER DIFFICULT FOR A SPURIOUS CONVERGENCE TO SLIP	00030750
C THROUGH.	00030760
C THE CONVERGENCE CRITERION OF QUAD IS SLIGHTLY RELAXED	00030770
C IN THAT A PANEL IS DEEMED TO HAVE BEEN SUCCESSFULLY	00030780
C INTEGRATED IF EITHER QUAD CONVERGES OR THE ESTIMATED	00030790
C ABSOLUTE ERROR COMMITTED ON THIS PANEL DOES NOT EXCEED	00030800
C EPSIL TIMES THE ESTIMATED ABSOLUTE VALUE OF THE INTEGRAL	00030810
C OVER (A,B). THIS RELAXATION IS TO TRY TO TAKE ACCOUNT OF	00030820
C A COMMON SITUATION WHERE ONE PARTICULAR PANEL CAUSES	00030830
C SPECIAL DIFFICULTY, PERHAPS DUE TO A SINGULARITY OF SOME	00030840
C TYPE. IN THIS CASE QUAD COULD OBTAIN NEARLY EXACT	00030850
C ANSWERS ON ALL OTHER PANELS AND SO THE RELATIVE ERROR FOR	00030860

C THE TOTAL INTEGRATION WOULD BE ALMOST ENTIRELY DUE TO THE	00030870
C DELINQUENT PANEL. WITHOUT THIS CONDITION THE COMPUTATION	00030880
C MIGHT CONTINUE DESPITE THE REQUESTED RELATIVE ERROR BEING	00030890
C ACHIEVED.	00030900
C THE OUTCOME OF THE INTEGRATION IS INDICATED BY ICHECK.	00030910
C ICHECK=0 - CONVERGENCE OBTAINED WITHOUT INVOKING	00030920
C SUBDIVISION. THIS CORRESPONDS TO THE	00030930
C DIRECT USE OF QUAD.	00030940
C ICHECK=1 - RESULT OBTAINED AFTER INVOKING SUBDIVISION.	00030950
C ICHECK=2 - AS FOR ICHECK=1 BUT AT SOME POINT THE	00030960
C RELAXED CONVERGENCE CRITERION WAS USED.	00030970
C THE RISK OF UNDERESTIMATING THE RELATIVE	00030980
C ERROR WILL BE INCREASED. IF NECESSARY,	00030990
C CONFIDENCE MAY BE RESTORED BY CHECKING	00031000
C EPSIL AND RELERR FOR A SERIOUS DISCREPANCY.	00031010
C ICHECK NEGATIVE	00031020
C IF DURING THE SUBDIVISION PROCESS THE	00031030
C ALLOWED UPPER LIMIT ON THE NUMBER OF PANELS	00031040
C THAT MAY BE GENERATED (PRESENTLY 4096) IS	00031050
C REACHED A RESULT IS OBTAINED WHICH MAY BE	00031060
C UNRELIABLE BY CONTINUING THE INTEGRATION	00031070
C WITHOUT FURTHER SUBDIVISION IGNORING	00031080
C CONVERGENCE FAILURES. THIS OCCURRENCE IS	00031090
C FLAGGED BY RETURNING ICHECK WITH NEGATIVE	00031100
C SIGN.	00031110
C THE RELIABILITY OF THE ALGORITHM WILL DECREASE FOR LARGE	00031120
C VALUES OF EPSIL. IT IS RECOMMENDED THAT EPSIL SHOULD	00031130
C GENERALLY BE LESS THAN ABOUT 0.001.	00031140
DIMENSION RESULT(8)	00031150
INTEGER BAD, OUT	00031160
LOGICAL RHS	00031170
EXTERNAL F	00031180
DATA NMAX/4096/	00031190
CALL CQUAD(A, B, RESULT, K, EPSIL, NPTS, ICHECK, F, MEV)	00031200
CQSUB = RESULT(K)	00031210
RELERR = (0.0,0.0)	00031220
IF (REAL(CQSUB).NE.0.0.AND.AIMAG(CQSUB).NE.0.0) RELERR=	00031230
\$ CMPLX(ABS(REAL(RESULT(K)-RESULT(K-1)))/REAL(CQSUB),	00031240
\$ ABS(AIMAG(RESULT(K)-RESULT(K-1)))/AIMAG(CQSUB))	00031250
C CHECK IF SUBDIVISION IS NEEDED.	00031260
IF (ICHECK.EQ.0) RETURN	00031270
C SUBDIVIDE	00031280
ESTIM=CQSUB*EPSIL	00031290
ESTIM=CMPLX(ABS(REAL(ESTIM)),ABS(AIMAG(ESTIM)))	00031300
IC = 1	00031310
RHS = .FALSE.	00031320
N = 1	00031330
H = B - A	00031340
BAD = 1	00031350
10 CQSUB = (0.0,0.0)	00031360
RELERR = (0.0,0.0)	00031370
H = H*0.5	00031380

N = N + N	00031390
C INTERVAL (A,B) DIVIDED INTO N EQUAL SUBINTERVALS.	00031400
C INTEGRATE OVER SUBINTERVALS BAD TO (BAD+1) WHERE TROUBLE	00031410
C HAS OCCURRED.	00031420
M1 = BAD	00031430
M2 = BAD + 1	00031440
OUT = 1	00031450
GO TO 50	00031460
C INTEGRATE OVER SUBINTERVALS 1 TO (BAD-1)	00031470
20 M1 = 1	00031480
M2 = BAD - 1	00031490
RHS = .FALSE.	00031500
OUT = 2	00031510
GO TO 50	00031520
C INTEGRATE OVER SUBINTERVALS (BAD+2) TO N.	00031530
30 M1 = BAD + 2	00031540
M2 = N	00031550
OUT = 3	00031560
GO TO 50	00031570
C SUBDIVISION RESULT	00031580
40 ICHECK = IC	00031590
RELERR=CMPLX(REAL(RELERR)/ABS(REAL(CQSUB)),	00031600
\$ AIMAG(RELERR)/ABS(AIMAG(CQSUB)))	00031610
RETURN	00031620
C INTEGRATE OVER SUBINTERVALS M1 TO M2.	00031630
50 IF (M1.GT.M2) GO TO 90	00031640
DO 80 JJ=M1,M2	00031650
J = JJ	00031660
C EXAMINE FIRST THE LEFT OR RIGHT HALF OF THE SUBDIVIDED	00031670
C TROUBLESOME INTERVAL DEPENDING ON THE OBSERVED TREND.	00031680
IF (RHS) J = M2 + M1 - JJ	00031690
ALPHA = A + H*(J-1)	00031700
BETA = ALPHA + H	00031710
CALL CQUAD(ALPHA, BETA, RESULT, M, EPSIL, NF, ICHECK, F,MEV)	00031720
COMP = (RESULT(M)-RESULT(M-1))	00031730
COMP=CMPLX(ABS(REAL(COMP)),ABS(AIMAG(COMP)))	00031740
NPTS = NPTS + NF	00031750
IF(NPTS.GE.MEV) GO TO 70	00031760
IF (ICHECK.NE.1) GO TO 70	00031770
IF(REAL(COMP).LE.REAL(ESTIM).AND.	00031780
\$ AIMAG(COMP).LE.AIMAG(ESTIM)) GO TO 100	00031790
C SUBINTERVAL J HAS CAUSED TROUBLE.	00031800
C CHECK IF FURTHER SUBDIVISION SHOULD BE CARRIED OUT.	00031810
IF (N.EQ.NMAX) GO TO 60	00031820
BAD = 2*J - 1	00031830
RHS = .FALSE.	00031840
IF ((J-2*(J/2)).EQ.0) RHS = .TRUE.	00031850
GO TO 10	00031860
60 IC = -IABS(IC)	00031870
70 CQSUB = CQSUB + RESULT(M)	00031880
80 CONTINUE	00031890
RELERR = RELERR + COMP	00031900

90 GO TO (20,30,40), OUT	00031910
C RELAXED CONVERGENCE	00031920
100 IC = ISIGN(2,IC)	00031930
GO TO 70	00031940
END	00031950
COMPLEX FUNCTION CQSUBA(A, B, EPSIL, NPTS, ICHECK, RELERR, F,MEV)	00031960
COMPLEX RELERR,F,RESULT,ESTIM,COMP	00031970
C THIS FUNCTION ROUTINE PERFORMS AUTOMATIC INTEGRATION	00031980
C OVER A FINITE INTERVAL USING THE BASIC INTEGRATION	00031990
C ALGORITHM QUAD TOGETHER WITH, IF NECESSARY AN ADAPTIVE	00032000
C SUBDIVISION PROCESS. IT IS GENERALLY MORE EFFICIENT THAN	00032010
C THE NON-ADAPTIVE ALGORITHM QSUB BUT IS LIKELY TO BE LESS	00032020
C RELIABLE(SEE COMP.J.,14,189,1971).	00032030
C THE CALL TAKES THE FORM	00032040
C CQSUBA(A,B,EPSIL,NPTS,ICHECK,RELERR,F,MEV)	00032050
C AND CAUSES F(X) TO BE INTEGRATED OVER (A,B) WITH RELATIVE	00032060
C ERROR HOPEFULLY NOT EXCEEDING EPSIL. SHOULD QUAD CONVERGE	00032070
C (ICHECK=0) THEN QSUBA WILL RETURN THE VALUE OBTAINED BY IT	00032080
C OTHERWISE SUBDIVISION WILL BE INVOKED AS A RESCUE	00032090
C OPERATION IN AN ADAPTIVE MANNER. THE ARGUMENT RELERR GIVES	00032100
C A CRUDE ESTIMATE OF THE ACTUAL RELATIVE ERROR OBTAINED.	00032110
C THE SUBDIVISION STRATEGY IS AS FOLLOWS	00032120
C AT EACH STAGE OF THE PROCESS AN INTERVAL IS PRESENTED FOR	00032130
C SUBDIVISION (INITIALLY THIS WILL BE THE WHOLE INTERVAL	00032140
C (A,B)). THE INTERVAL IS HALVED AND QUAD APPLIED TO EACH	00032150
C SUBINTERVAL. SHOULD QUAD FAIL ON THE FIRST SUBINTERVAL	00032160
C THE SUBINTERVAL IS STACKED FOR FUTURE SUBDIVISION AND THE	00032170
C SECOND SUBINTERVAL IMMEDIATELY EXAMINED. SHOULD QUAD FAIL	00032180
C ON THE SECOND SUBINTERVAL THE SUBINTERVAL IS	00032190
C IMMEDIATELY SUBDIVIDED AND THE WHOLE PROCESS REPEATED.	00032200
C EACH TIME A CONVERGED RESULT IS OBTAINED IT IS	00032210
C ACCUMULATED AS THE PARTIAL VALUE OF THE INTEGRAL. WHEN	00032220
C QUAD CONVERGES ON BOTH SUBINTERVALS THE INTERVAL LAST	00032230
C STACKED IS CHOSEN NEXT FOR SUBDIVISION AND THE PROCESS	00032240
C REPEATED. A SUBINTERVAL IS NOT EXAMINED AGAIN ONCE A	00032250
C CONVERGED RESULT IS OBTAINED FOR IT SO THAT A SPURIOUS	00032260
C CONVERGENCE IS MORE LIKELY TO SLIP THROUGH THAN FOR THE	00032270
C NON-ADAPTIVE ALGORITHM QSUB.	00032280
C THE CONVERGENCE CRITERION OF QUAD IS SLIGHTLY RELAXED	00032290
C IN THAT A PANEL IS DEEMED TO HAVE BEEN SUCCESSFULLY	00032300
C INTEGRATED IF EITHER QUAD CONVERGES OR THE ESTIMATED	00032310
C ABSOLUTE ERROR COMMITTED ON THIS PANEL DOES NOT EXCEED	00032320
C EPSIL TIMES THE ESTIMATED ABSOLUTE VALUE OF THE INTEGRAL	00032330
C OVER (A,B). THIS RELAXATION IS TO TRY TO TAKE ACCOUNT OF	00032340
C A COMMON SITUATION WHERE ONE PARTICULAR PANEL CAUSES	00032350
C SPECIAL DIFFICULTY, PERHAPS DUE TO A SINGULARITY OF SOME	00032360
C TYPE. IN THIS CASE QUAD COULD OBTAIN NEARLY EXACT	00032370
C ANSWERS ON ALL OTHER PANELS AND SO THE RELATIVE ERROR FOR	00032380
C THE TOTAL INTEGRATION WOULD BE ALMOST ENTIRELY DUE TO THE	00032390
C DELINQUENT PANEL. WITHOUT THIS CONDITION THE COMPUTATION	00032400
C MIGHT CONTINUE DESPITE THE REQUESTED RELATIVE ERROR BEING	00032410

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C ACHIEVED. 00032420
C THE OUTCOME OF THE INTEGRATION IS INDICATED BY ICHECK. 00032430
C ICHECK=0 - CONVERGENCE OBTAINED WITHOUT INVOKING SUB- 00032440
C DIVISION. THIS WOULD CORRESPOND TO THE 00032450
C DIRECT USE OF QUAD. 00032460
C ICHECK=1 - RESULT OBTAINED AFTER INVOKING SUBDIVISION. 00032470
C ICHECK=2 - AS FOR ICHECK=1 BUT AT SOME POINT THE 00032480
C RELAXED CONVERGENCE CRITERION WAS USED. 00032490
C THE RISK OF UNDERESTIMATING THE RELATIVE 00032500
C ERROR WILL BE INCREASED. IF NECESSARY, 00032510
C CONFIDENCE MAY BE RESTORED BY CHECKING 00032520
C EPSIL AND RELERR FOR A SERIOUS DISCREPANCY. 00032530
C ICHECK NEGATIVE 00032540
C IF DURING THE SUBDIVISION PROCESS THE STACK 00032550
C OF DELINQUENT INTERVALS BECOMES FULL (IT IS 00032560
C PRESENTLY SET TO HOLD AT MOST 100 NUMBERS) 00032570
C A RESULT IS OBTAINED BY CONTINUING THE 00032580
C INTEGRATION IGNORING CONVERGENCE FAILURES 00032590
C WHICH CANNOT BE ACCOMMODATED ON THE STACK. 00032600
C THIS OCCURRENCE IS FLAGGED BY RETURNING 00032610
C ICHECK WITH NEGATIVE SIGN. 00032620
C THE RELIABILITY OF THE ALGORITHM WILL DECREASE FOR LARGE 00032630
C VALUES OF EPSIL. IT IS RECOMMENDED THAT EPSIL SHOULD 00032640
C GENERALLY BE LESS THAN ABOUT 0.001. 00032650
    DIMENSION RESULT(8), STACK(100) 00032660
    EXTERNAL F 00032670
    DATA ISMAX/100/ 00032680
    CALL CQUAD(A, B, RESULT, K, EPSIL, NPTS, ICHECK, F, MEV) 00032690
    CQSUBA = RESULT(K) 00032700
    RELERR = (0.0,0.0) 00032710
    IF(REAL(CQSUBA).NE.0.0.AND.AIMAG(CQSUBA).NE.0.0) RELERR= 00032720
    * CMPLX(ABS(REAL(RESULT(K)-RESULT(K-1)))/REAL(CQSUBA), 00032730
    * ABS(AIMAG(RESULT(K)-RESULT(K-1)))/AIMAG(CQSUBA)) 00032740
C CHECK IF SUBDIVISION IS NEEDED 00032750
    IF (ICHECK.EQ.0) RETURN 00032760
C SUBDIVIDE 00032770
    ESTIM=CQSUBA*EPSIL 00032780
    ESTIM=CMPLX(ABS(REAL(ESTIM)),ABS(AIMAG(ESTIM))) 00032790
    RELERR = (0.0,0.0) 00032800
    CQSUBA = (0.0,0.0) 00032810
    IS = 1 00032820
    IC = 1 00032830
    SUB1 = A 00032840
    SUB3 = B 00032850
10 SUB2 = (SUB1+SUB3)*0.5 00032860
    CALL CQUAD(SUB1, SUB2, RESULT, K, EPSIL, NF, ICHECK, F, MEV) 00032870
    NPTS = NPTS + NF 00032880
    IF(NPTS.GE.MEV) GO TO 50 00032890
    COMP = (RESULT(K)-RESULT(K-1)) 00032900
    COMP=CMPLX(ABS(REAL(COMP)),ABS(AIMAG(COMP))) 00032910
    IF (ICHECK.EQ.0) GO TO 30 00032920
    IF(REAL(COMP).LE.REAL(ESTIM).AND, 00032930

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      $ AIMAG(COMP),LE,AIMAG(ESTIM)) GO TO 70          00032940
      IF (IS,GE,ISMAX) GO TO 20                      00032950
C STACK SUBINTERVAL (SUB1,SUB2) FOR FUTURE EXAMINATION 00032960
      STACK(IS) = SUB1                              00032970
      IS = IS + 1                                    00032980
      STACK(IS) = SUB2                              00032990
      IS = IS + 1                                    00033000
      GO TO 40                                       00033010
20 IC = -IABS(IC)                                    00033020
30 CQSUBA = CQSUBA + RESULT(K)                      00033030
      RELERR = RELERR + COMP                        00033040
40 CALL CQUAD(SUB2, SUB3, RESULT, K, EPSIL, NF, ICHECK, F,MEV) 00033050
      NPTS = NPTS + NF                             00033060
      IF(NPTS,GE,MEV) GO TO 50                     00033070
      COMP = (RESULT(K)-RESULT(K-1))                00033080
      COMP=CMPLX(ABS(REAL(COMP)),ABS(AIMAG(COMP)))    00033090
      IF (ICHECK,EQ,0) GO TO 50                     00033100
      IF(REAL(COMP),LE,REAL(ESTIM),AND,             00033110
      $ AIMAG(COMP),LE,AIMAG(ESTIM)) GO TO 80        00033120
C SUBDIVIDE INTERVAL (SUB2,SUB3)                    00033130
      SUB1 = SUB2                                    00033140
      GO TO 10                                       00033150
50 CQSUBA = CQSUBA + RESULT(K)                      00033160
      RELERR = RELERR + COMP                        00033170
      IF(NPTS,GE,MEV) RETURN                        00033180
      IF (IS,EQ,1) GO TO 60                         00033190
C SUBDIVIDE THE DELINQUENT INTERVAL LAST STACKED    00033200
      IS = IS - 1                                    00033210
      SUB3 = STACK(IS)                              00033220
      IS = IS - 1                                    00033230
      SUB1 = STACK(IS)                              00033240
      GO TO 10                                       00033250
C SUBDIVISION RESULT                                00033260
60 ICHECK = IC                                       00033270
      RELERR=CMPLX(REAL(RELERR)/ABS(REAL(CQSUBA)),    00033280
      $ AIMAG(RELERR)/ABS(AIMAG(CQSUBA)))            00033290
      RETURN                                         00033300
C RELAXED CONVERGENCE                               00033310
70 IC = ISIGN(2,IC)                                 00033320
      GO TO 30                                       00033330
80 IC = ISIGN(2,IC)                                 00033340
      GO TO 50                                       00033350
      END                                           00033360

      SUBROUTINE IMSLMQ(SUBZ,SUBEND)                 00033370
C--IMSLMQ-- DERIVATIVE-FREE 'IMSL' MARQUARDT INVERSION--5/4/79 00033380
C FOR SOLVING GENERAL NONLINEAR LEAST SQUARES PROBLEMS. USER NEED ONLY 00033390
C WRITE SUBROUTINES 'FCODE', SUBZ, AND SUBEND' EXACTLY AS USED 00033400
C IN PROGRAM 'MARQRT'. ALSO, THE SAME PARAMETER FILE05 AND DATA 00033410
C FILE10 MAY BE USED BY 'IMSLMQ' AS IN 'MARQRT'.    00033420
C                                                    00033430
C--NOTE: 'FCODE' CANNOT BE PASSED AS EXTERNAL DUE TO THE 00033440

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C 'BLACK-BOX' NATURE OF IMSL ROUTINE 'ZXSSQ' (SEE IMSL DOC.), 00033450
C THUS, ONE SHOULD RENAME ACTUAL NAME TO 'FCODE' FOR USE HERE. 00033460
C (I.E., SEE CALL FCODE IN 'FPXSSQ'--EXTERNAL FUNCTION FOR ZXSSQ), 00033470
C 00033480
C--THE USER MUST DECLARE THE CALLING PARAMETERS 00033490
C SUBZ,SUBEND (ANY DESIRED NAMES MAY BE USED) AS EXTERNAL IN 00033500
C MAIN CALLING PROGRAM; E.G., 00033510
C 00033520
C     EXTERNAL SUBZ,SUBEND 00033530
C     CALL IMSLMQ(SUBZ,SUBEND) 00033540
C     STOP 00033550
C     END 00033560
C 00033570
C--THIS INTERFACE BETWEEN 'MARQRT' AND 'IMSLMQ' WAS WRITTEN BY 00033580
C W.L.ANDERSON, U.S. GEOLOGICAL SURVEY, DENVER, COLORADO. 00033590
C 00033600
C--SEE DOCUMENTATION OF 'MARQLOOPS', USGS OPEN-FILE REPT 79-240 (1979), 00033610
C FOR DETAILS ON CODING THE REQUIRED SUBROUTINES FCODE,SUBZ, AND 00033620
C SUBEND. ALSO SEE IMSL DOCUMENTATION FOR 'ZXSSQ'. 00033630
C 00033640
C--THE INPUT ORDER ON FILE05 (PARAMETER FILE) IS: 00033650
C 00033660
C 1. TITLE (MAX. 80-CHARACTER TITLE--ALWAYS REQUIRED). 00033670
C 2. $PARMS (SAME PARMS DEFINITIONS FOR PGM MARQRT FOR PARAMETERS: 00033680
C     N,K,IP,M,IALT,ISTOP,IWT,NITER,E,SCALEP,B(),IPRT, AND IB()), 00033690
C     PLUS, ADDITIONAL PARMS FOR 'ZXSSQ' (SEE IMSL DOC): 00033700
C     IOPT,NSIG,MAXFN,EPS,DELTA,PARM(4). 00033710
C 3. (OBJECT-TIME FORMAT STATEMENT) FOR READING THE DATA MATRIX 00033720
C     (Y(I),X(I,J),J=1,M*) ON FILE IALT (DEFAULT 10), WHERE M*=M+IWT. 00033730
C (3A. INSERT DATA MATRIX HERE ONLY IF IALT=5) 00033740
C 4. $INIT OPTIONAL NAMELIST FOR READING ADDITIONAL PARMS IN 00033750
C     SUBROUTINE SUBZ (WHICH MAY BE A DUMMY SUBROUTINE). 00033760
C 5. OPTIONALLY, REPEAT STEPS 1-4, IF ISTOP=0 WAS USED IN STEP 2. 00033770
C 00033780
C--OUTPUT IS GIVEN ON FILE06 (ON-LINE USUALLY), AND 00033790
C ON FILE16 (CONTAINS ALL PRINTABLE OUTPUT); FILE06 CONTAINS ONLY 00033800
C OUTPUT VIA PARM IPRT (0--ABBREVIATED, 1 OR -2 --DETAIL). 00033810
C 00033820
C----- 00033830
C--THE USER SHOULD ADD >IML>IMSL TO THE SEARCH RULES ON MULTICS. 00033840
C (IMSL ROUTINES USED: ZXSSQ,LEQT1P,LUDECF,LUELMP,UERTST,LINV1P) 00033850
C----- 00033860
C 00033870
C     DIMENSION B(20),GRAD(20),TITLE(16),H(270),COV(20,20),SE(20) 00033880
C     DIMENSION SQWT(200),IB(20),PRNT(5),C(20),INDEX(20), 00033890
C     & XJAC(200,20),XJTJ(210),WORK(710),PARM(4),F(200) 00033900
C     INTEGER SP,SCALEP,SY,SCALEY 00033910
C--THE FOLLOWING CHARACTER STATEMENTS ONLY FOR HONEYWELL MULTICS: 00033920
C CHARACTER*4 FMT(18) 00033930
C CHARACTER*5 TITLE 00033940
C COMMON/FIXDAT/Y(200),X(200,5),BFIX(20),YMAX,IIB(20),IIF,NDBS,K 00033950
C COMMON/PRT/IPRT 00033960

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EXTERNAL FPXSSQ,LNXSSQ                                00033970
EQUIVALENCE (SQWT(1),X(1,5)),(SP,SCALEP),(N,NBBS),    00033980
& (M,NVARS),(NITER,LIMIT),(SY,SCALEY),(E,EPS),(SS,SSQ), 00033990
& (IB(1),IIB(1)),(IP,IIP),(B(1),BFIX(1))              00034000
NAMELIST/PARMS/N,K,IP,M,IALT,NITER,IB,E,B,IWT,ISTOP,SP,SY, 00034010
& SCALEP,SCALEY, IDER,IPRT,INON,FF,T,TAU,XL,MODLAM,GAMCR, 00034020
& DEL,ZETA,IOUT,IOPT,NSIG,MAXFN,EPS,DELTA,PARM        00034030
C-- NOTE NAMELIST PARMS INCLUDED (BUT IGNORED) FOR COMPATIBILITY 00034040
C ARE: IDER,INON,FF,T,TAU,XL,MODLAM,GAMCR,DEL,ZETA,IOUT. 00034050
C ALSO, SP=SCALEP WILL BE CONSIDERED MODE=1 (ALOG OPTION) ONLY 00034060
C WHEN SP=2 OR 1 (AND MODE=0 LINEAR WHEN SP=0). SY=SCALEY IS 00034070
C IGNORED FOR THIS VERSION OF 'IMSLMQ'.                00034080
C                                                        00034090
C--READ IMSLMQ TITLE LINE                               00034100
      READ(5,4) TITLE                                  00034110
4      FORMAT(16A5)                                     00034120
C--PRESET DEFAULTS                                     00034130
      N=0                                                00034140
      K=0                                                00034150
      M=0                                                00034160
      IP=0                                               00034170
      IPRT=0                                             00034180
      ISTOP=1                                           00034190
      IWT=0                                              00034200
      IALT=10                                           00034210
      NITER=10                                          00034220
      SP=0                                               00034230
      MODE=0                                             00034240
      FMIN=0.0                                          00034250
      IOPT=1                                             00034260
      NSIG=3                                             00034270
      MAXFN=0                                           00034280
      EPS=0.0                                           00034290
      DELTA=0.0                                         00034300
      PARM(1)=.01                                       00034310
      PARM(2)=2.                                        00034320
      PARM(3)=120.                                      00034330
      PARM(4)=.1                                        00034340
      DO 5 I=1,20                                       00034350
      IB(I)=0                                           00034360
      B(I)=0.0                                          00034370
5      GRAD(I)=0.0                                       00034380
C--READ $PARMS                                         00034390
6      READ(5,PARMS)                                    00034400
C--TEST $PARMS BEFORE PROCEEDING                      00034410
      IF(N.GT.200.OR.K.GT.20.OR.M.GT.4.OR.IWT.GT.1.OR.IP.GT.19.OR. 00034420
& N.LT.1.OR.K.LT.1.OR.M.LT.1.OR.IWT.LT.0.OR.IP.LT.0.OR. 00034430
& N.LT.K-IP.OR.IALT.EQ.6.OR.IALT.EQ.16)              00034440
&CALL ERRMSG('SOME $PARMS OUT OF RANGE.',5,6,16)     00034450
      DO 7 I=1,K                                       00034460
      IF(B(I).EQ.0.0)CALL ERRMSG('SOME B(I)=0.0 ',3,6,16) 00034470
7      CONTINUE                                         00034480

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      IF(MAXFN.EQ.0) MAXFN=2*K*NITER                                00034490
      IF(IP.LE.0) GO TO 9                                           00034500
      DO 8 I=1,IP                                                    00034510
      IF(IB(I).GT.0) GO TO 8                                         00034520
      CALL ERRMSG('IP.GT.1 BUT SOME IB(I).LE.0      ',6,6,16)      00034530
8      CONTINUE                                                    00034540
9      IF(SP.NE.0) MODE=1                                           00034550
      IF(IPRT.EQ.1) IPRT=-2                                         00034560
C--READ OBJECT FORMAT FOR DATA MATRIX ON FILE IALT.              00034570
      READ(5,10) (FMT(I),I=1,18)                                    00034580
10     FORMAT(18A4)                                                 00034590
      M1=M+IWT                                                       00034600
      YMAX=0.0                                                       00034610
      DO 11 I=1,N                                                    00034620
      READ(IALT,FMT) Y(I),(X(I,J),J=1,M1)                          00034630
      SQWT(I)=1.0                                                    00034640
      IF(IWT.EQ.1.AND.X(I,M1).NE.0.0) SQWT(I)=1.0/X(I,M1)         00034650
      IF(ABS(Y(I)).GT.YMAX) YMAX=ABS(Y(I))                         00034660
11     CONTINUE                                                    00034670
      IF(IALT.NE.5) REWIND IALT                                     00034680
C--INITIALIZATION VIA CALL SUBZ (READ $INIT, TEST B,X,Y, ETC)     00034690
      CALL SUBZ(Y,X,B,PRNT,NDUM,N,TITLE,1)                         00034700
C--WRITE $PARMS ON UNIT 6 AND 16                                   00034710
      WRITE(6,60) TITLE,N,K,IP,M,E,IALT,ISTOP,IWT,NITER,SP,IPRT,  00034720
      & IOPT,NSIG,MAXFN,EPS,DELTA,PARM                              00034730
60     FORMAT('1I M S L M Q  --      ',16A5// ' N=',I5,9X,' K=',I4,10X,' IP=' 00034740
      & ',I4,9X,' M=',I3,11X,' E=',E10.3/' IALT=',I3,8X,' ISTOP=',I2,8X,  00034750
      & ' IWT=',I2,10X,' NITER=',I6,4X,' SCALEP=',I2/' IPRT=',I3,      00034760
      & 8X,' IOPT=',I2,9X,' NSIG=',I3,8X,' MAXFN=',I6,4X,' EPS=',E10.3/  00034770
      & ' DELTA=',E10.3/' PARM=',4E10.3)                          00034780
      WRITE(16,60) TITLE,N,K,IP,M,E,IALT,ISTOP,IWT,NITER,SP,IPRT,  00034790
      & IOPT,NSIG,MAXFN,EPS,DELTA,PARM                              00034800
      IF(IP.EQ.0) GO TO 661                                           00034810
      WRITE(6,660) (IB(I),I=1,IP)                                    00034820
660     FORMAT('/' IB=',19I3)                                         00034830
      WRITE(16,660) (IB(I),I=1,IP)                                   00034840
661     WRITE(6,662) FMT                                             00034850
662     FORMAT('/' FMT=',18A4/)                                       00034860
      WRITE(16,662) FMT                                              00034870
      WRITE(6,6000) (B(I),I=1,K)                                     00034880
6000    FORMAT('/' INITIAL PARAMETERS'//(5E16.8))                  00034890
      WRITE(16,6000) (B(I),I=1,K)                                    00034900
C--INTERFACE WITH ZXSSQ USING MARQRT FCODE                        00034910
      DO 1 I=1,20                                                    00034920
1      INDEX(I)=I                                                  00034930
      KIP=K-IP                                                       00034940
      IF(IP.EQ.0) GO TO 400                                           00034950
C--REORDER B TO C WHEN IP>0                                       00034960
      IM=0                                                           00034970
      DO 202 I=1,K                                                   00034980
      DO 201 J=1,IP                                                  00034990
      IF(I.EQ.IB(J)) GO TO 202                                       00035000

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201	CONTINUE	00035010
	IM=IM+1	00035020
	C(IM)=B(I)	00035030
	INDEX(IM)=I	00035040
202	CONTINUE	00035050
	WRITE(6,203) (I,I=1,K)	00035060
203	FORMAT(/' PARAMETER INDEX:',20I3)	00035070
	WRITE(16,203) (I,I=1,K)	00035080
	WRITE(6,204) (INDEX(I),I=1,KIP)	00035090
204	FORMAT(' REORDERED AS...:',20I3)	00035100
	WRITE(16,204) (INDEX(I),I=1,KIP)	00035110
	WRITE(6,206) (C(I),I=1,KIP)	00035120
206	FORMAT(/' REORDERED PARAMETERS'/(5E16.8))	00035130
	WRITE(16,206) (C(I),I=1,KIP)	00035140
	GO TO 500	00035150
400	DO 401 I=1,K	00035160
401	C(I)=B(I)	00035170
500	CONTINUE	00035180
	IF(MODE.EQ.0) GO TO 12	00035190
	C--LOG PARAMETERS CHOSEN (MODE=1 OR SP.NE.0)	00035200
	DO 111 I=1,KIP	00035210
	IF(C(I).LE.0.0)CALL ERRMSG('SP.NE.0 & SOME B(I).LE.0.',5,6,16)	00035220
111	C(I)=ALOG(C(I))	00035230
	CALL ZXSSQ(LNXSSQ,N,KIP,NSIG,EPS,DELTA,MAXFN,IOPT,PARM,	00035240
	& C,SSQ,F,XJAC,200,XJTJ,WORK,INFER,IER)	00035250
	DO 1111 I=1,KIP	00035260
1111	C(I)=EXP(C(I))	00035270
	GO TO 21	00035280
	C--LINEAR PARAMETERS CHOSEN (MODE=0 OR SP=0)	00035290
12	CALL ZXSSQ(FPXSSQ,N,KIP,NSIG,EPS,DELTA,MAXFN,IOPT,PARM,	00035300
	& C,SSQ,F,XJAC,200,XJTJ,WORK,INFER,IER)	00035310
	C--ZXSSQ ERRMSG CODE HANDLERS	00035320
21	IF(IER.EQ.0) GO TO 100	00035330
	IF(IER.EQ.129)	00035340
	&CALL ERRMSG('SINGULARITY DETECTED IN JACOBIAN & RECOVERY FAILED',	00035350
	& 10,6,16)	00035360
	IF(IER.EQ.130)	00035370
	&CALL ERRMSG('N,K-IP,IOPT,PARM(1) OR PARM(2) INCORRECT',8,6,16)	00035380
	IF(IER.EQ.131)	00035390
	&CALL WARN('MARQUARDT PARAMETER EXCEEDED PARM(3) ',8,6,16,\$100)	00035400
	IF(IER.EQ.132) CALL ERRMSG(	00035410
	&'AFTER RECOVERY FROM SINGULAR JACOBIAN, B CYCLED BACK AGAIN..',	00035420
	& 12,6,16)	00035430
	IF(IER.EQ.133)CALL WARN('MAXFN EXCEEDED.',3,6,16,\$100)	00035440
	IF(IER.EQ.38)CALL WARN('JACOBIAN=0. SOLUTION IS STATIONARY POINT',	00035450
	& 8,6,16,\$100)	00035460
100	WRITE(6,603) (WORK(I),I=1,5),INFER,IER,SSQ,(C(I),I=1,KIP)	00035470
	WRITE(16,603) (WORK(I),I=1,5),INFER,IER,SSQ,(C(I),I=1,KIP)	00035480
603	FORMAT(/' \$\$\$ IMSLMQ CONVERGENCE INFORMATION:'//	00035490
	& ' NORM OF GRADIENT',T32,E16.8/' FUNCTION EVALUATIONS',T32,E16.8/	00035500
	& ' EST. SIGN. DIGITS',T32,E16.8/' MARQUARDT PARAMETER',T32,	00035510
	& E16.8/' NO. ITERATIONS',T32,E16.8/' TYPE CONVERGENCE (INFER)',	00035520

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& T32,I3// ERROR CODE (IER)',T32,I5/ 00035530
& ' RESIDUAL SUM-OF-SQUARES (SSQ)=' ,E16.8// 00035540
& ' **** FINAL UNSCALED PARAMETERS'// 00035550
& (5E16.8)) 00035560
99 KK=MAX0((KIP+1)*KIP/2,5) 00035570
DO 80 I=1,KIP 00035580
80 GRAD(I)=2.*WORK(KK+I) 00035590
WRITE(6,82) (GRAD(I),I=1,KIP) 00035600
82 FORMAT(/' SCALED GRADIENT'// (5E16.8)) 00035610
WRITE(16,82) (GRAD(I),I=1,KIP) 00035620
IF(IPRT.EQ.-2) WRITE(6,699) 00035630
699 FORMAT(/3X,'I',4X,'OBS.Y(I)',6X,'CAL',11X,'RES',8X,'X(I,1)',8X, 00035640
& 'WT(I)') 00035650
WRITE(16,1699) 00035660
1699 FORMAT(/3X,'I',4X,'OBS.Y(I)',6X,'CAL',11X,'RES',8X,'X(I,1)',8X, 00035670
& 'X(I,2)',8X,'X(I,3)',8X,'X(I,4)',8X,'WT(I)') 00035680
SUMF2=0.0 00035690
DO 110 I=1,NOBS 00035700
RES=F(I)/SQWT(I) 00035710
YCAL=Y(I)-RES 00035720
WT=SQWT(I)*SQWT(I) 00035730
SUMF2=SUMF2+F(I)*F(I) 00035740
IF(IPRT.EQ.-2) WRITE(6,210) I,Y(I),YCAL,RES,X(I,1),WT 00035750
210 FORMAT(1X,I3,2E14.6,E11.3,2E14.6) 00035760
WRITE(16,211) I,Y(I),YCAL,RES,(X(I,J),J=1,4),WT 00035770
211 FORMAT(1X,I3,2E14.6,E11.3,5E14.6) 00035780
110 CONTINUE 00035790
IF(N.EQ.KIP) RMSERR=0.0 00035800
IF(N.GT.KIP) RMSERR=SQRT(SUMF2/(N-KIP)) 00035810
WRITE(6,604) RMSERR 00035820
604 FORMAT(/' **** RMSERR=' ,E16.8) 00035830
WRITE(16,604) RMSERR 00035840
C--PRINT ON FILE16 (ONLY) THE FINAL SCALED PARTIALS (JACOBIAN) 00035850
WRITE(16,605) 00035860
605 FORMAT(/' FINAL SCALED PARTIALS (JACOBIAN)') 00035870
DO 112 I=1,NOBS 00035880
WRITE(16,606) I,(XJAC(I,J),J=1,KIP) 00035890
606 FORMAT(1X,I3,5E16.8/(4X,5E16.8)) 00035900
112 CONTINUE 00035910
C--GET INVERSE JACOBIAN TRANSPOSE*JACOBIAN (FROM XJTJ SYMMETRIC MATRIX) 00035920
CALL LINV1P(XJTJ,KIP,H,5,D1,D2,IER) 00035930
IF(IER.GT.128) CALL ERRMSG('IN LINV1P CALL.',3,6,16) 00035940
C--FINAL STATISTICS 00035950
DO 301 I=1,KIP 00035960
DO 301 J=1,KIP 00035970
301 COV(I,J)=H(LOC(I,J)) 00035980
IF(IPRT.EQ.-2) WRITE(6,120) 00035990
120 FORMAT(/' SCALED COVARIANCE MATRIX (INVERSE OF XJTJ)') 00036000
WRITE(16,120) 00036010
DO 122 I=1,KIP 00036020
SE(I)=SQRT(ABS(COV(I,I))) 00036030
IF(IPRT.EQ.-2) WRITE(6,300) INDEX(I),(COV(I,J),J=1,KIP) 00036040

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300	FORMAT(1X,I2,10E12.4/(3X,10E12.4))	00036050
	WRITE(16,300) INDEX(I),(COV(I,J),J=1,KIP)	00036060
122	CONTINUE	00036070
	IF(IPRT.EQ.-2) WRITE(6,304)	00036080
304	FORMAT('/ CORRELATION MATRIX')	00036090
	WRITE(16,304)	00036100
	DO 131 I=1,KIP	00036110
	IF(SE(I).EQ.0.0) GO TO 132	00036120
	DO 129 J=1,KIP	00036130
	IF(SE(J).EQ.0.0) GO TO 129	00036140
	COV(I,J)=COV(I,J)/(SE(I)*SE(J))	00036150
129	CONTINUE	00036160
133	IF(IPRT.EQ.-2) WRITE(6,300) INDEX(I),(COV(I,J),J=1,KIP)	00036170
	WRITE(16,300) INDEX(I),(COV(I,J),J=1,KIP)	00036180
	GO TO 131	00036190
132	COV(I,I)=1.0	00036200
	GO TO 133	00036210
131	CONTINUE	00036220
125	WRITE(6,303)	00036230
303	FORMAT(/15H ** PARAMETER,3X,9HSTD ERROR,3X,	00036240
	& 31HSTD ERROR/PARAMETER (UNSCALED))	00036250
	WRITE(16,303)	00036260
	DO 126 I=1,KIP	00036270
	SE(I)=RMSERR*SE(I)	00036280
	IF(SP.GT.0) SE(I)=C(I)*SE(I)	00036290
	SEC=SE(I)/C(I)	00036300
	WRITE(6,300) INDEX(I),C(I),SE(I),SEC	00036310
	WRITE(16,300) INDEX(I),C(I),SE(I),SEC	00036320
126	CONTINUE	00036330
	DO 600 I=1,KIP	00036340
600	H(I)=C(I)	00036350
	IF(IP.EQ.0) GO TO 601	00036360
	C--PUT SOL C AND BFIX TOGETHER FOR SUBEND USE.	00036370
	IM=0	00036380
	DO 127 I=1,K	00036390
	H(I)=B(I)	00036400
	DO 128 J=1,IP	00036410
	IF(I.EQ.IB(J)) GO TO 127	00036420
128	CONTINUE	00036430
	IM=IM+1	00036440
	H(I)=C(IM)	00036450
127	CONTINUE	00036460
601	CALL SUBEND(Y,X,H,K,N,TITLE,1)	00036470
	IF(ISTOP.EQ.1) GO TO 999	00036480
	READ(5,4) TITLE	00036490
	DO 1000 I=1,20	00036500
1000	B(I)=0.0	00036510
	GO TO 6	00036520
	C--FOLLOWING CALL ONLY FOR HONEYWELL MULTICS SYSTEM:	00036530
999	CALL CLOSE_FILE('-ALL')	00036540
C	STOP	00036550
	RETURN	00036560



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C--GENERAL UTILITY TO MODIFY COMMON/SAVE/ AS FOLLOWS      00037060
C CALL SAVER(I,J) WILL REPLACE FSAVE() ARRAY WITH        00037070
C FSAVE(K)=GSAVE(K)**I * FSAVE(K)**J                     00037080
C FOR K=1,NSAVE,                                          00037090
C                                                         00037100
C INPUT PARAMETERS (I,J) MAY BE NEGATIVE,ZERO, OR POSITIVE INTEGERS. 00037110
C                                                         00037120
C--SUBROUTINE SAVER MAY BE USED IN CONJUNCTION WITH SUBPROGRAM ZHANKS 00037130
C TO MODIFY SAVED KERNELS WHEN USING NEW=0 OPTION (SEE ZHANKS).    00037140
C                                                         00037150
C     COMPLEX FSAVE                                         00037160
C     COMMON/SAVE/FSAVE(283),GSAVE(283),NSAVE              00037170
C     DO 1 K=1,NSAVE                                         00037180
C     FSAVE(K)=CMPLX(GSAVE(K)**I,0.0)*(FSAVE(K)**J)        00037190
1  CONTINUE                                                00037200
    RETURN                                                  00037210
    END                                                    00037220

    COMPLEX FUNCTION ZHANKS(N,B,FUN,TOL,NF,NEW)              00037230
C=====00037240
C COMPLEX HANKEL TRANSFORMS OF ORDER 0 OR 1 FOR RELATED (SAVED) KERNELS00037250
C AND FIXED TRANSFORM ARGUMENT B.GT.0.                    00037260
C                                                         00037270
C--REF: ANDERSON, W.L., 1979, GEOPHYSICS, VOL. 44, NO. 7, P. 1287-1305. 00037280
C                                                         00037290
C--SUBPROGRAM ZHANKS EVALUATES THE INTEGRAL FROM 0 TO INFINITY OF      00037300
C FUN(G)*JN(G*B)*DG, DEFINED AS THE COMPLEX HANKEL TRANSFORM OF      00037310
C ORDER N (=0 OR 1) AND TRANSFORM ARGUMENT B.GT.0. THE METHOD IS BY    00037320
C ADAPTIVE DIGITAL FILTERING OF THE COMPLEX KERNEL FUNCTION FUN,      00037330
C USING DIRECT AND/OR PREVIOUSLY SAVED KERNEL FUNCTION VALUES.      00037340
C                                                         00037350
C--PARAMETERS (ALL INPUT, EXCEPT NF)                          00037360
C                                                         00037370
C     N      = ORDER (=0 OR 1) OF THE HANKEL TRANSFORM TO BE EVALUATED. 00037380
C     B      = REAL TRANSFORM ARGUMENT B.GT.0.0 OF THE HANKEL TRANSFORM. 00037390
C              IF NEW=0, B IS ASSUMED EQUAL TO THE LAST B USED WHEN NEW=100037400
C              (SEE PARAMETER NEW AND SUBPROGRAM USAGE BELOW).         00037410
C     FUN(G)= EXTERNAL DECLARED COMPLEX FUNCTION NAME (USER SUPPLIED) 00037420
C              OF A REAL ARGUMENT G.GT.0. THIS REFERENCE MUST BE SUPPLIED00037430
C              EVEN WHEN NEW=0, SINCE THE ADAPTIVE CONVOLUTION          00037440
C              MAY NEED SOME DIRECT FUNCTION CALLS (E.G. IF TOL REDUCED).00037450
C              IF PARAMETERS OTHER THAN G ARE REQUIRED IN FUN, USE COMMON00037460
C              IN THE CALLING PROGRAM AND IN SUBPROGRAM FUN. BOTH      00037470
C              REAL AND IMAGINARY PARTS OF THE COMPLEX FUNCTION FUN(G) 00037480
C              MUST BE CONTINUOUS BOUNDED FUNCTIONS FOR G.GT.0.0. FOR A 00037490
C              REAL FUNCTION F1(G), FUN=CMPLX(F1(G),0.0) MAY BE USED.   00037500
C              TWO INDEPENDENT REAL-FUNCTIONS F1(G),F2(G) MAY BE      00037510
C              INTEGRATED IN PARALLEL BY WRITING FUN=CMPLX(F1(G),F2(G)). 00037520
C     TOL    = REQUESTED REAL TRUNCATION TOLERANCE ACCEPTED AT THE FILTER00037530
C              TAILS FOR ADAPTIVE FILTERING. A TRUNCATION CRITERION IS 00037540
C              DEFINED DURING CONVOLUTION IN A FIXED ABSCISSA RANGE AS 00037550
C              THE MAX. ABSOLUTE CONVOLVED PRODUCT TIMES TOL. TYPICALLY,00037560

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C      TOL.LE.0.00001 WOULD GIVE ABOUT .01 PER CENT ACCURACY      00037570
C      FOR WELL-BEHAVED KERNELS AND MODERATE VALUES OF B.  FOR  00037580
C      VERY LARGE OR SMALL B, A VERY SMALL TOL SHOULD BE USED.  00037590
C      IN GENERAL, DECREASING THE TOLERANCE WOULD PRODUCE HIGHER 00037600
C      ACCURACY IN THE CONVOLUTION SINCE MORE FILTER WEIGHTS ARE 00037610
C      USED (UNLESS EXPONENT UNDERFLOWS OCCUR IN THE KERNEL      00037620
C      EVALUATION -- SEE NOTE (1) BELOW).                          00037630
C      FOR MAXIMUM ACCURACY POSSIBLE, TOL=0.0 MAY BE USED.        00037640
C      NF      = TOTAL NUMBER OF DIRECT FUN CALLS USED DURING CONVOLUTION 00037650
C      FOR ANY VALUE OF NEW (NF IS AN OUTPUT PARAMETER).          00037660
C      NF IS IN THE RANGE 21.LE.NF.LE.283 WHEN NEW=1.  USUALLY,   00037670
C      NF IS MUCH LESS THAN 283 (OR 0) WHEN NEW=0.                00037680
C      NEW      =1 IS REQUIRED FOR THE VERY FIRST CALL TO ZHANKS, OR IF 00037690
C      FORCING DIRECT FUNCTION FUN(G) CALLS, E.G., IF USING      00037700
C      ZHANKS FOR UNRELATED KERNELS.                             00037710
C      NEW=1 INITIALIZES COMMON/SAVE/FSAVE(283),GSAVE(283),NSAVE 00037720
C      FOR NSAVE COMPLEX KERNEL VALUES IN FSAVE AND CORRESPONDING 00037730
C      REAL ARGUMENTS IN GSAVE FOR THE GIVEN PARAMETER B.         00037740
C      NEW      =0 TO USE RELATED KERNELS (MODIFIED BY USER) CURRENTLY STORED 00037750
C      IN COMMON/SAVE/. FUN IS CALLED ONLY IF REQUIRED             00037760
C      DURING THE CONVOLUTION.  ADDITIONAL FUNCTION VALUES WHEN 00037770
C      NEEDED ARE AUTOMATICALLY ADDED TO THE COMMON/SAVE/ BLOCK.  00037780
C      00037790
C      ***** NOTE THAT IT IS THE USERS RESPONSIBILITY TO MODIFY THE 00037800
C      COMMON FSAVE() VALUES FOR NEW=0 CALLS, EXTERNALLY IN      00037810
C      THE USERS CALLING PROGRAM (SEE SUBPROGRAM USAGE BELOW).    00037820
C      00037830
C=====00037840
C--SUBPROGRAM USAGE-- ZHANKS IS CALLED AS FOLLOWS                00037850
C      ...                                                         00037860
C      COMPLEX Z1,Z2,ZHANKS,FSAVE                                  00037870
C      COMMON/SAVE/FSAVE(283),GSAVE(283),NSAVE                    00037880
C      EXTERNAL ZF1,ZF2                                           00037890
C      ...                                                         00037900
C      Z1=ZHANKS(N1,B,ZF1,TOL,NF1,1)                               00037910
C      DO 1 I=1,NSAVE                                              00037920
C      C--MODIFY FSAVE IN COMMON/SAVE/ TO OBTAIN RELATED ZF2 FROM ZF1. 00037930
C      C--E.G. FSAVE(I)=GSAVE(I)*FSAVE(I) -- FOR RELATION ZF2(G)=G*ZF1(G) 00037940
C      1 CONTINUE                                                 00037950
C      Z2=ZHANKS(N2,B,ZF2,TOL,NF2,0)                               00037960
C      ...                                                         00037970
C      END                                                         00037980
C      COMPLEX FUNCTION ZF1(G)                                     00037990
C      ...USER SUPPLIED CODE FOR DIRECT EVALUATION OF ZF1(G), G.GT.0. 00038000
C      END                                                         00038010
C      COMPLEX FUNCTION ZF2(G)                                     00038020
C      ...USER SUPPLIED CODE FOR DIRECT EVALUATION OF ZF2(G), G.GT.0. 00038030
C      END                                                         00038040
C=====00038050
C--NOTES                                                         00038060
C      (1).  EXP-UNDERFLOW MAY OCCUR IN EXECUTING THIS SUBPROGRAM.  00038070
C      THIS IS OK PROVIDED THE MACHINE SYSTEM CONDITIONALLY SETS 00038080

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C      EXP-UNDERFLOW TO 0.0.                                00038090
C      (2).  ANSI FORTRAN (AMERICAN STANDARD X3.9-1966) IS USED, EXCEPT 00038100
C      DATA STATEMENTS MAY NEED TO BE CHANGED FOR SOME COMPILERS. 00038110
C      TO CONVERT ZHANKS TO THE NEW AMERICAN STANDARD FORTRAN 00038120
C      (X3.9-1978), ADD THE FOLLOWING DECLARATION TO THIS ROUTINE 00038130
C      SAVE Y1,ISAVE                                          00038140
C      (3).  THE FILTER ABSCISSA CORRESPONDING TO EACH FILTER WEIGHT 00038150
C      IS GENERATED IN DOUBLE-PRECISION (TO REDUCE ROUND-OFF), 00038160
C      BUT IS USED IN SINGLE-PRECISION IN FUNCTION FUN. 00038170
C      (4).  NO CHECKS ARE MADE ON CALLING PARAMETERS (TO SAVE TIME), 00038180
C      HENCE UNPREDICTABLE RESULTS COULD OCCUR IF ZHANKS 00038190
C      IS CALLED INCORRECTLY (OR IF FUN OR COMMON IS IN ERROR). 00038200
C=====00038210
C      00038220
C      COMPLEX FUN,C,CMAX,FSAVE                                00038230
C      COMMON/SAVE/FSAVE(283),GSAVE(283),NSAVE                00038240
C      DOUBLE PRECISION E,ER,Y1,Y                             00038250
C      DIMENSION T(2),TMAX(2)                                  00038260
C      DIMENSION WTO(283),WAO(76),WBO(76),WCO(76),WDO(55),    00038270
C      * WT1(283),WA1(76),WB1(76),WC1(76),WD1(55)             00038280
C      EQUIVALENCE (WTO(1),WAO(1)),(WTO(77),WBO(1)),(WTO(153),WCO(1)), 00038290
C      * (WTO(229),WDO(1)),(WT1(1),WA1(1)),(WT1(77),WB1(1)), 00038300
C      * (WT1(153),WC1(1)),(WT1(229),WD1(1))                   00038310
C      EQUIVALENCE (C,T(1)),(CMAX,TMAX(1))                     00038320
C-----E=DEXP(.2D0), ER=1.0D0/E                               00038330
C      DATA E/1.221402758160169834 D0/,ER/.818730753077981859 D0/ 00038340
C--JO--TRANSFORM FILTER WEIGHT ARRAYS (EQUIVALENT TO WTO ARRAY) 00038350
C      DATA WAO/                                              00038360
C      * 2.1969101E-11, 4.1201161E-09,-6.1322980E-09, 7.2479291E-09, 00038370
C      *-7.9821627E-09, 8.5778983E-09,-9.1157294E-09, 9.6615250E-09, 00038380
C      *-1.0207546E-08, 1.0796633E-08,-1.1393033E-08, 1.2049873E-08, 00038390
C      *-1.2708789E-08, 1.3446466E-08,-1.4174300E-08, 1.5005577E-08, 00038400
C      *-1.5807160E-08, 1.6747136E-08,-1.7625961E-08, 1.8693427E-08, 00038410
C      *-1.9650840E-08, 2.0869789E-08,-2.1903555E-08, 2.3305308E-08, 00038420
C      *-2.4407377E-08, 2.6033678E-08,-2.7186773E-08, 2.9094334E-08, 00038430
C      *-3.0266804E-08, 3.2534013E-08,-3.3672072E-08, 3.6408936E-08, 00038440
C      *-3.7425022E-08, 4.0787921E-08,-4.1543242E-08, 4.5756842E-08, 00038450
C      *-4.6035233E-08, 5.1425075E-08,-5.0893896E-08, 5.7934897E-08, 00038460
C      *-5.6086570E-08, 6.5475248E-08,-6.1539913E-08, 7.4301996E-08, 00038470
C      *-6.7117043E-08, 8.4767837E-08,-7.2583120E-08, 9.7366568E-08, 00038480
C      *-7.7553611E-08, 1.1279873E-07,-8.1416723E-08, 1.3206914E-07, 00038490
C      *-8.3217217E-08, 1.5663185E-07,-8.1482581E-08, 1.8860593E-07, 00038500
C      *-7.3963141E-08, 2.3109673E-07,-5.7243707E-08, 2.8867452E-07, 00038510
C      *-2.6163525E-08, 3.6808773E-07, 2.7049871E-08, 4.7932617E-07, 00038520
C      * 1.1407365E-07, 6.3720626E-07, 2.5241961E-07, 8.6373487E-07, 00038530
C      * 4.6831433E-07, 1.1916346E-06, 8.0099716E-07, 1.6696015E-06, 00038540
C      * 1.3091334E-06, 2.3701475E-06, 2.0803829E-06, 3.4012978E-06/ 00038550
C      DATA WBO/                                              00038560
C      * 3.2456774E-06, 4.9240402E-06, 5.0005198E-06, 7.1783540E-06, 00038570
C      * 7.6367633E-06, 1.0522038E-05, 1.1590021E-05, 1.5488635E-05, 00038580
C      * 1.7510398E-05, 2.2873836E-05, 2.6368006E-05, 3.3864387E-05, 00038590
C      * 3.9610390E-05, 5.0230379E-05, 5.9397373E-05, 7.4612122E-05, 00038600

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* 8.8951409E-05, 1.1094809E-04, 1.3308026E-04, 1.6511335E-04, 00038610
* 1.9895671E-04, 2.4587195E-04, 2.9728181E-04, 3.6629770E-04, 00038620
* 4.4402013E-04, 5.4589361E-04, 6.6298832E-04, 8.1375348E-04, 00038630
* 9.8971624E-04, 1.2132772E-03, 1.4772052E-03, 1.8092022E-03, 00038640
* 2.2045122E-03, 2.6980811E-03, 3.2895354E-03, 4.0238764E-03, 00038650
* 4.9080203E-03, 6.0010999E-03, 7.3216878E-03, 8.9489225E-03, 00038660
* 1.0919448E-02, 1.3340696E-02, 1.6276399E-02, 1.9873311E-02, 00038670
* 2.4233627E-02, 2.9555699E-02, 3.5990069E-02, 4.3791529E-02, 00038680
* 5.3150319E-02, 6.4341372E-02, 7.7506720E-02, 9.2749987E-02, 00038690
* 1.0980561E-01, 1.2791555E-01, 1.4525830E-01, 1.5820085E-01, 00038700
* 1.6058576E-01, 1.4196085E-01, 8.9781222E-02, -1.0238278E-02, 00038710
* -1.5083434E-01, -2.9059573E-01, -2.9105437E-01, -3.7973244E-02, 00038720
* 3.8273717E-01, 2.2014118E-01, -4.7342635E-01, 1.9331133E-01, 00038730
* 5.3839527E-02, -1.1909845E-01, 9.9317051E-02, -6.6152628E-02, 00038740
* 4.0703241E-02, -2.4358316E-02, 1.4476533E-02, -8.6198067E-03/ 00038750
DATA WCO/ 00038760
* 5.1597053E-03, -3.1074602E-03, 1.8822342E-03, -1.1456545E-03, 00038770
* 7.0004347E-04, -4.2904226E-04, 2.6354444E-04, -1.6215439E-04, 00038780
* 9.9891279E-05, -6.1589037E-05, 3.7996921E-05, -2.3452250E-05, 00038790
* 1.4479572E-05, -8.9417427E-06, 5.5227518E-06, -3.4114252E-06, 00038800
* 2.1074101E-06, -1.3019229E-06, 8.0433617E-07, -4.9693681E-07, 00038810
* 3.0702417E-07, -1.8969219E-07, 1.1720069E-07, -7.2412496E-08, 00038820
* 4.4740283E-08, -2.7643004E-08, 1.7079403E-08, -1.0552634E-08, 00038830
* 6.5200311E-09, -4.0284597E-09, 2.4890232E-09, -1.5378695E-09, 00038840
* 9.5019040E-10, -5.8708696E-10, 3.6273937E-10, -2.2412348E-10, 00038850
* 1.3847792E-10, -8.5560821E-11, 5.2865474E-11, -3.2664392E-11, 00038860
* 2.0182948E-11, -1.2470979E-11, 7.7057678E-12, -4.7611713E-12, 00038870
* 2.9415274E-12, -1.8170081E-12, 1.1221034E-12, -6.9271067E-13, 00038880
* 4.2739744E-13, -2.6344388E-13, 1.6197105E-13, -9.9147443E-14, 00038890
* 6.0487998E-14, -3.6973097E-14, 2.2817964E-14, -1.4315547E-14, 00038900
* 9.1574735E-15, -5.9567236E-15, 3.9209969E-15, -2.5911739E-15, 00038910
* 1.6406939E-15, -8.8248590E-16, 3.0195409E-16, 2.2622634E-17, 00038920
* -8.0942556E-17, -3.7172363E-17, 1.9299542E-16, -3.3388160E-16, 00038930
* 4.6174116E-16, -5.8627358E-16, 7.2227767E-16, -8.7972941E-16, 00038940
* 1.0211793E-15, -1.0940039E-15, 1.0789555E-15, -9.7089714E-16/ 00038950
DATA WDO/ 00038960
* 7.4110927E-16, -4.1700094E-16, 8.5977184E-17, 1.3396469E-16, 00038970
* -1.7838410E-16, 4.8975421E-17, 1.9398153E-16, -5.0046989E-16, 00038980
* 8.3280985E-16, -1.1544640E-15, 1.4401527E-15, -1.6637066E-15, 00038990
* 1.7777129E-15, -1.7322187E-15, 1.5247247E-15, -1.1771155E-15, 00039000
* 6.9747910E-16, -1.2088956E-16, -4.8382957E-16, 1.0408292E-15, 00039010
* -1.5220450E-15, 1.9541597E-15, -2.4107448E-15, 2.9241438E-15, 00039020
* -3.5176475E-15, 4.2276125E-15, -5.0977851E-15, 6.1428456E-15, 00039030
* -7.3949962E-15, 8.8597601E-15, -1.0515959E-14, 1.2264584E-14, 00039040
* -1.3949870E-14, 1.5332490E-14, -1.6146782E-14, 1.6084121E-14, 00039050
* -1.4962523E-14, 1.2794804E-14, -9.9286701E-15, 6.8825809E-15, 00039060
* -4.0056107E-15, 1.5965079E-15, -7.2732961E-18, -4.0433218E-16, 00039070
* -6.5679655E-16, 3.3011866E-15, -7.3545910E-15, 1.2394851E-14, 00039080
* -1.7947697E-14, 2.3774303E-14, -3.0279168E-14, 3.9252831E-14, 00039090
* -5.5510504E-14, 9.0505371E-14, -1.7064873E-13/ 00039100
C---END OF JO FILTER WEIGHTS 00039110
C 00039120

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C--J1-TRANSFORM FILTER WEIGHT ARRAYS (EQUIVALENT TO WT1 ARRAY)      00039130
  DATA WA1/                                                            00039140
    *-4.2129715E-16, 5.3667031E-15,-7.1183962E-15, 8.9478500E-15,    00039150
    *-1.0767891E-14, 1.2362265E-14,-1.3371129E-14, 1.3284178E-14,    00039160
    *-1.1714302E-14, 8.4134738E-15,-3.7726725E-15,-1.4263879E-15,    00039170
    * 6.1279163E-15,-9.1102765E-15, 9.9696405E-15,-9.3649955E-15,    00039180
    * 8.6009018E-15,-8.9749846E-15, 1.1153987E-14,-1.4914821E-14,    00039190
    * 1.9314024E-14,-2.3172388E-14, 2.5605477E-14,-2.6217555E-14,    00039200
    * 2.5057768E-14,-2.2485539E-14, 1.9022752E-14,-1.5198084E-14,    00039210
    * 1.1422464E-14,-7.9323958E-15, 4.8421406E-15,-2.1875032E-15,    00039220
    *-3.2177842E-17, 1.8637565E-15,-3.3683643E-15, 4.6132219E-15,    00039230
    *-5.6209538E-15, 6.4192841E-15,-6.8959928E-15, 6.9895792E-15,    00039240
    *-6.5355935E-15, 5.6125163E-15,-4.1453931E-15, 2.6358827E-15,    00039250
    *-9.5104370E-16, 1.4600474E-16, 5.6166519E-16, 8.2899246E-17,    00039260
    * 5.0032100E-16, 4.3752205E-16, 2.1052293E-15,-9.5451973E-16,    00039270
    * 6.4004437E-15,-2.1926177E-15, 1.1651003E-14, 5.8415433E-16,    00039280
    * 1.8044664E-14, 1.0755745E-14, 3.0159022E-14, 3.3506138E-14,    00039290
    * 5.8709354E-14, 8.1475200E-14, 1.2530006E-13, 1.8519112E-13,    00039300
    * 2.7641786E-13, 4.1330823E-13, 6.1506209E-13, 9.1921659E-13,    00039310
    * 1.3698462E-12, 2.0447427E-12, 3.0494477E-12, 4.5501001E-12,    00039320
    * 6.7870250E-12, 1.0126237E-11, 1.5104976E-11, 2.2536053E-11/    00039330
  DATA WB1/                                                            00039340
    * 3.3617368E-11, 5.0153839E-11, 7.4818173E-11, 1.1161804E-10,    00039350
    * 1.6651222E-10, 2.4840923E-10, 3.7058109E-10, 5.5284353E-10,    00039360
    * 8.2474468E-10, 1.2303750E-09, 1.8355034E-09, 2.7382502E-09,    00039370
    * 4.0849867E-09, 6.0940898E-09, 9.0913020E-09, 1.3562651E-08,    00039380
    * 2.0233058E-08, 3.0184244E-08, 4.5029477E-08, 6.7176304E-08,    00039390
    * 1.0021488E-07, 1.4950371E-07, 2.2303208E-07, 3.3272689E-07,    00039400
    * 4.9636623E-07, 7.4049804E-07, 1.1046805E-06, 1.6480103E-06,    00039410
    * 2.4585014E-06, 3.6677163E-06, 5.4714550E-06, 8.1626422E-06,    00039420
    * 1.2176782E-05, 1.8166179E-05, 2.7099223E-05, 4.0428804E-05,    00039430
    * 6.0307294E-05, 8.9971508E-05, 1.3420195E-04, 2.0021123E-04,    00039440
    * 2.9860417E-04, 4.4545291E-04, 6.6423156E-04, 9.9073275E-04,    00039450
    * 1.4767050E-03, 2.2016806E-03, 3.2788147E-03, 4.8837292E-03,    00039460
    * 7.2596811E-03, 1.0788355E-02, 1.5973323E-02, 2.3612041E-02,    00039470
    * 3.4655327E-02, 5.0608141E-02, 7.2827752E-02, 1.0337889E-01,    00039480
    * 1.4207357E-01, 1.8821315E-01, 2.2996815E-01, 2.5088500E-01,    00039490
    * 2.0334626E-01, 6.0665451E-02,-2.0275683E-01,-3.5772336E-01,    00039500
    *-1.8280529E-01, 4.7014634E-01, 7.2991233E-03,-3.0614594E-01,    00039510
    * 2.4781735E-01,-1.1149185E-01, 2.5985386E-02, 1.0850279E-02,    00039520
    *-2.2830217E-02, 2.4644647E-02,-2.2895284E-02, 2.0197032E-02/    00039530
  DATA WC1/                                                            00039540
    *-1.7488968E-02, 1.5057670E-02,-1.2953923E-02, 1.1153254E-02,    00039550
    *-9.6138436E-03, 8.2952090E-03,-7.1628361E-03, 6.1882910E-03,    00039560
    *-5.3482055E-03, 4.6232056E-03,-3.9970542E-03, 3.4560118E-03,    00039570
    *-2.9883670E-03, 2.5840861E-03,-2.2345428E-03, 1.9323046E-03,    00039580
    *-1.6709583E-03, 1.4449655E-03,-1.2495408E-03, 1.0805480E-03,    00039590
    *-9.3441130E-04, 8.0803899E-04,-6.9875784E-04, 6.0425624E-04,    00039600
    *-5.2253532E-04, 4.5186652E-04,-3.9075515E-04, 3.3790861E-04,    00039610
    *-2.9220916E-04, 2.5269019E-04,-2.1851585E-04, 1.8896332E-04,    00039620
    *-1.6340753E-04, 1.4130796E-04,-1.2219719E-04, 1.0567099E-04,    00039630
    *-9.1379828E-05, 7.9021432E-05,-6.8334412E-05, 5.9092726E-05,    00039640

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*-5.1100905E-05, 4.4189914E-05,-3.8213580E-05, 3.3045496E-05, 00039650
*-2.8576356E-05, 2.4711631E-05,-2.1369580E-05, 1.8479514E-05, 00039660
*-1.5980307E-05, 1.3819097E-05,-1.1950174E-05, 1.0334008E-05, 00039670
*-8.9364160E-06, 7.7278366E-06,-6.6827083E-06, 5.7789251E-06, 00039680
*-4.9973715E-06, 4.3215167E-06,-3.7370660E-06, 3.2316575E-06, 00039690
*-2.7946015E-06, 2.4166539E-06,-2.0898207E-06, 1.8071890E-06, 00039700
*-1.5627811E-06, 1.3514274E-06,-1.1686576E-06, 1.0106059E-06, 00039710
*-8.7392952E-07, 7.5573750E-07,-6.5353002E-07, 5.6514528E-07, 00039720
*-4.8871388E-07, 4.2261921E-07,-3.6546333E-07, 3.1603732E-07/ 00039730
  DATA WD1/ 00039740
*-2.7329579E-07, 2.3633470E-07,-2.0437231E-07, 1.7673258E-07, 00039750
*-1.5283091E-07, 1.3216174E-07,-1.1428792E-07, 9.8831386E-08, 00039760
*-8.5465227E-08, 7.3906734E-08,-6.3911437E-08, 5.5267923E-08, 00039770
*-4.7793376E-08, 4.1329702E-08,-3.5740189E-08, 3.0906612E-08, 00039780
*-2.6726739E-08, 2.3112160E-08,-1.9986424E-08, 1.7283419E-08, 00039790
*-1.4945974E-08, 1.2924650E-08,-1.1176694E-08, 9.6651347E-09, 00039800
*-8.3580023E-09, 7.2276490E-09,-6.2501673E-09, 5.4048822E-09, 00039810
*-4.6739154E-09, 4.0418061E-09,-3.4951847E-09, 3.0224895E-09, 00039820
*-2.6137226E-09, 2.2602382E-09,-1.9545596E-09, 1.6902214E-09, 00039830
*-1.4616324E-09, 1.2639577E-09,-1.0930164E-09, 9.4519327E-10, 00039840
*-8.1736202E-10, 7.0681930E-10,-6.1122713E-10, 5.2856342E-10, 00039850
*-4.5707937E-10, 3.9526267E-10,-3.4180569E-10, 2.9557785E-10, 00039860
*-2.5560176E-10, 2.2103233E-10,-1.9113891E-10, 1.6528994E-10, 00039870
*-1.4294012E-10, 1.2361991E-10,-8.2740936E-11/ 00039880
C---END OF J1 FILTER WEIGHTS 00039890
C 00039900
  NONE=0 00039910
  IF(NEW.EQ.0) GO TO 100 00039920
  NSAVE=0 00039930
C-----INITIALIZE KERNEL ABSCISSA GENERATION FOR GIVEN B 00039940
  Y1=0.7358852661479794460D0/DBLE(B) 00039950
100 ZHANKS=(0.0,0.0) 00039960
  CMAX=(0.0,0.0) 00039970
  NF=0 00039980
  Y=Y1 00039990
C-----BEGIN RIGHT-SIDE CONVOLUTION AT WEIGHT 131 (EITHER NEW=1 OR 0) 00040000
  ASSIGN 110 TO M 00040010
  I=131 00040020
  Y=Y*E 00040030
  GO TO 200 00040040
110 TMAX(1)=AMAX1(ABS(T(1)),TMAX(1)) 00040050
  TMAX(2)=AMAX1(ABS(T(2)),TMAX(2)) 00040060
  I=I+1 00040070
  Y=Y*E 00040080
  IF(I.LE.149) GO TO 200 00040090
  IF(TMAX(1).EQ.0.0.AND.TMAX(2).EQ.0.0) NONE=1 00040100
C-----ESTABLISH TRUNCATION CRITERION (CMAX=CMPLX(TMAX(1),TMAX(2)) 00040110
  CMAX=TOL*CMAX 00040120
  ASSIGN 120 TO M 00040130
  GO TO 200 00040140
C-----CHECK FOR FILTER TRUNCATION AT RIGHT END 00040150
120 IF(ABS(T(1)).LE.TMAX(1).AND.ABS(T(2)).LE.TMAX(2)) GO TO 130 00040160

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I=I+1	00040170
Y=Y*E	00040180
IF(I,LE,283) GO TO 200	00040190
130 Y=Y1	00040200
C-----CONTINUE WITH LEFT-SIDE CONVOLUTION AT WEIGHT 130	00040210
ASSIGN 140 TO M	00040220
I=130	00040230
GO TO 200	00040240
C-----CHECK FOR FILTER TRUNCATION AT LEFT END	00040250
140 IF(ABS(T(1)),LE,TMAX(1),AND,ABS(T(2)),LE,TMAX(2),AND,	00040260
* NONE,EQ,0) GO TO 190	00040270
I=I-1	00040280
Y=Y*ER	00040290
IF(I,GT,0) GO TO 200	00040300
C-----RETURN WITH ISAVE=1 PRESET FOR POSSIBLE NEW=0 USE.	00040310
190 ISAVE=1	00040320
C-----NORMALIZE BY B TO ACCOUNT FOR INTEGRATION RANGE CHANGE	00040330
ZHANKS=ZHANKS/B	00040340
RETURN	00040350
C-----SAVE/RETRIEVE PSEUDO-SUBROUTINE (CALL FUN ONLY WHEN NECESSARY)	00040360
200 G=SNGL(Y)	00040370
IF(NEW) 300,210,300	00040380
210 IF(ISAVE,GT,NSAVE) GO TO 300	00040390
ISAVE0=ISAVE	00040400
220 IF(G,EQ,GSAVE(ISAVE)) GO TO 240	00040410
ISAVE=ISAVE+1	00040420
IF(ISAVE,LE,NSAVE) GO TO 220	00040430
ISAVE=ISAVE0	00040440
C-----G NOT IN COMMON/SAVE/----- EVALUATE FUN.	00040450
GO TO 300	00040460
C-----G FOUND IN COMMON/SAVE/----- USE FSAVE AS GIVEN.	00040470
240 C=FSAVE(ISAVE)	00040480
ISAVE=ISAVE+1	00040490
C-----SWITCH ON ORDER N	00040500
250 IF(N) 270,260,270	00040510
260 C=C*WT0(I)	00040520
GO TO 280	00040530
270 C=C*WT1(I)	00040540
280 ZHANKS=ZHANKS+C	00040550
GO TO M,(110,120,140)	00040560
C-----DIRECT FUN EVALUATION (AND ADD TO END OF COMMON/SAVE/)	00040570
300 NSAVE=NSAVE+1	00040580
C=FUN(G)	00040590
NF=NF+1	00040600
FSAVE(NSAVE)=C	00040610
GSAVE(NSAVE)=G	00040620
GO TO 250	00040630
END	00040640
SUBROUTINE ERRMSG(MSG,M5,I6,I9)	00040650
C--ERROR MESSAGE WRITE ROUTINE AND STOP, WHERE--	00040660
C	00040670

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C      MSG=      ANY MULTIPLE OF 5 CHARACTERS--MAX. OF 120      00040680
C      (USE NH----- FORM FOR ANSI COMPATABILITY)      00040690
C      M5=      NO.CHARS IN MSG/5 (REMAINDER MUST BE 0) 1.LE.M5.LE.24      00040700
C      I6=      1ST UNIT FOR WRITE(I6, ) MSG -- USUALLY I6=6 FOR LPT.      00040710
C      IF I6.LE.0 UNIT I6 IGNORED.      00040720
C      I9=      2ND UNIT FIR WRITE(I9, ) MSG --      00040730
C      IF I9.LE.0, UNIT I9 IGNORED.      00040740
C--MESSAGE WRITTEN IN FORM--      00040750
C      /ERROR--MSG HERE      00040760
C      00040770
C      DIMENSION MSG(30)      00040780
C      J=5*M5      00040790
C      K=J/4+MOD(J,4)      00040800
C      IF(I6.GT.0) WRITE(I6,10) (MSG(I),I=1,K)      00040810
10  FORMAT(/8H ERROR--,30A4)      00040820
C      IF(I9.GT.0) WRITE(I9,10) (MSG(I),I=1,K)      00040830
C      CALL CLOSE_FILE('ALL')      00040840
C      00040850
C      STOP      00040860
C      END      00040870

      SUBROUTINE WARN(MSG,M5,I6,I9,*)      00040880
C--WARNING MESSAGE WRITE ROUTINE WHERE:      00040890
C      00040900
C      MSG=      'ANY MULTIPLE OF 5 CHARACTERS--MAX. OF 120      '      00040910
C      M5=      NO.CHAR'S IN MSG/5 (REMAINDER MUST BE 0) 1<=M5<=24      00040920
C      I6=      1ST UNIT NO. FOR WRITE(I6, )MSG--USUALLY I6=6 FOR LPT.      00040930
C      IF I6<=0 UNIT I6 IGNORED.      00040940
C      I9=      2ND UNIT NO. FOR WRITE(I9, )MSG--IF I9<=0, I9 IGNORED      00040950
C      *=      $LABEL NO. TO RETURN AFTER ERROR CALLED ($NO. MUST BE      00040960
C      GIVEN      00040970
C      00040980
C      DIMENSION MSG(30)      00040990
C      J=5*M5      00041000
C      K=J/4+MOD(J,4)      00041010
C      IF(I6.GT.0) WRITE(I6,6) (MSG(I),I=1,K)      00041020
6  FORMAT('WARNING--',30A4)      00041030
C      IF(I9.GT.0) WRITE(I9,6) (MSG(I),I=1,K)      00041040
C      RETURN (1)      00041050
C      END      00041060

```

Appendix 2.-- Conversion to other systems

1. All lower-case letters used for parameters and Fortran names in this report should be changed to upper-case letters for most other systems.
2. Any of the following Multics statements and/or calls should be deleted or replaced if converting to another system:

character*n	(replace with logical*n or delete)
call open_	(delete)
call close_	(delete)
exp_	(replace with exp)
dexp_	(replace with dexp)
cexp_	(replace with cexp)
call initref	(delete)

3. All Multics exponent underflow messages are suppressed and the result set to 0.0. An equivalent method should be used for other systems.
4. Subprograms ERRMSG and WARN should be changed according to the number of characters per word of the target machine (note that 4 char/word uses format A4 on the Honeywell Multics system; however, 5 char/word is assumed in the input parameter array MSG). Similar changes should be made, if necessary, to other character arrays and format statements (e.g., see subroutine IMSLMQ, arrays TITLE and FMT).
5. Multics names greater than 6-characters (e.g. MQLVTHXYZ\_SUBZ, MQLVTHXYZ\_SUBEND, etc) should be renamed to 6 or less characters for most other systems.
6. To replace the IMSL interface routines (IMSLMQ, FFXSSQ, LNXSSQ, and all calls to the IMSL Library) with the nonlinear least squares subprogram MARQRT (available in Anderson, 1979c), replace the main program (lines 00000010-00000140) with the following code:

```
C--NON-IMSL MAIN PROGRAM USING MARQRT (ANDERSON, 1979)
  EXTERNAL FCODE,DUMMY_FCODE,ITHXYZ,ETHXYZ
  CALL MARQRT(FCODE,DUMMY_FCODE,ITHXYZ,ETHXYZ)
  STOP
  END
```

Note: Subprogram DUMMY\_FCODE is referenced as the second external parameter in the CALL MARQRT, but DUMMY\_FCODE will never be called since \$parms ilder=1 should be used (because analytic derivatives are not used in IMSLMQ, the fcode subprogram was not needed). For systems requiring all



external references to be available (even if not called),  
the following subprogram could be used:

```
SUBROUTINE DUMMY_FCODE(A,B,C,D,E,I,J,K)
PRINT 'USE IDER=1' STOP
END
```

If converting to subprogram MARQRT, all parameters  
prefixed by an "\*" apply; however, parameters  
ioft,parm(),nsis,eps,delta, and maxfn cannot be used in  
this case. In addition to subprogram MARQRT, the following  
subprograms from Anderson (1979c) are also called: GJR,  
UNSCAL, ASINH, and ERRMSG.

Appendix 3.-- Test problem input/output listing

The following input file (file05) was used to run a test problem on a Honeywell Multics system. Note that file10 is not required because \$parms ialt=5. The output listing (file16) follows beginning on the next page.

file05

```
malvthxyz test problem2, model parms b0=1,1,1,1,.1,150
$parms n=15,ip=1,ib=1,sp=1,sg=1,m=2,iwt=1,iert=-2,ialt=5,k=6,
b=1,1,1,1,.1,250$
(2e14.5,f13.0,e14.5)
  0.23010e-07  0.50000e-02  2.          0.23    e-07
  0.46094e-07  0.19905e-01  2.          0.469    e-07
  0.86019e-07  0.79245e-01  2.          0.86     e-07
  0.81049e-07  0.79245e+00  2.          0.81     e-07
  0.80052e-07  0.19905e+01  2.          0.8       e-07
  0.30237e-08  0.79245e-02  3.          0.3       e-08
  0.15069e-07  0.31548e-01  3.          0.15     e-07
  0.71822e-07  0.19905e+00  3.          0.72     e-07
  0.79080e-07  0.79245e+00  3.          0.79     e-07
  0.79539e-07  0.31548e+01  3.          0.8       e-07
  0.10003e+01  0.158    e+02  4.
  0.10601e+01  0.1       e+03  4.
  0.155    e+01  0.252    e+03  4.          0.155    e+01
  0.311    e+01  0.63     e+03  4.          0.31     e+01
  0.426    e+01  0.1       e+04  4.          0.43     e+01
$init  nf=5,mm=2,x=0,y=1000,ister=1,iob=4$
```

1T H X Y Z-- malvthxyz test Problem2, model parms b0=1,1,1,1,1,250

data set parms are

ister= 1 x= 0.0000E+00 y= 0.1000E+04 r= 0.1000E+04 current= 0.1000E+01  
source length= 0.1000E+01 l= 1  
ifltx= 0 iflty= 0 ifltz= 0

control parms are

tol= 0.1000E-03 nf = 5 iob = 4  
method= 2

1i m s l m a -- malvthxyz test Problem2, model parms b0=1,1,1,1,1,250

n= 15 k= 6 ip= 1 m= 2 e= 0.000E+00  
ialt= 5 istop= 1 iwt= 1 niter= 10 scaler= 1  
iprt= -2 iopt= 1 nsis= 3 maxfn= 120 eps= 0.000E+00  
delta= 0.000E+00  
parm= 0.100E-01 0.200E+01 0.120E+03 0.100E+00

ib= 1

fmt=(2e14.5,f13.0,e14.5)

initial parameters

0.10000000E+01 0.10000000E+01 0.10000000E+01 0.10000000E+01 0.10000000E+00  
0.25000000E+03

parameter index: 1 2 3 4 5 6  
reordered as...: 2 3 4 5 6

reordered parameters

0.10000000E+01 0.10000000E+01 0.10000000E+01 0.10000000E+00 0.25000000E+03  
Warning--marquardt parameter exceeded parm(3).

---

\$\$\$ imslma convergence information:

norm of gradient 0.16253650E-02  
function evaluations 0.46000000E+02  
est. sign. digits 0.45923176E+01  
marquardt parameter 0.26165364E+03  
no. iterations 0.70000000E+01  
type convergence (infer) 0  
error code (ier) 131  
residual sum-of-squares (ssq)= 0.41113755E-03

\*\*\*\* final unscaled parameters

0.10042551E+01 0.99890090E+00 0.99777942E+00 0.98586691E-01 0.15074997E+03

scaled gradient

-0.26512254E-04 -0.25798774E-03 0.16032409E-02 0.27969514E-04 0.58197892E-04

i	obs.y(i)	cal	res	x(i,1)	x(i,2)	x(i,3)	x(i,4)	wt(i)
1	0.230100E-07	0.226074E-07	0.403E-09	0.500000E-02	0.200000E+01	0.230000E-07	0.000000E+00	0.189036E+16
2	0.460940E-07	0.463114E-07	-0.217E-09	0.199050E-01	0.200000E+01	0.469000E-07	0.000000E+00	0.454626E+15
3	0.860190E-07	0.863804E-07	-0.361E-09	0.792450E-01	0.200000E+01	0.860000E-07	0.000000E+00	0.135208E+15
4	0.810490E-07	0.813849E-07	-0.336E-09	0.792450E+00	0.200000E+01	0.810000E-07	0.000000E+00	0.152416E+15
5	0.800520E-07	0.803887E-07	-0.337E-09	0.199050E+01	0.200000E+01	0.800000E-07	0.000000E+00	0.156250E+15
6	0.302370E-08	0.303244E-08	-0.874E-11	0.792450E-02	0.300000E+01	0.300000E-08	0.000000E+00	0.111111E+18
7	0.150690E-07	0.150673E-07	0.165E-11	0.315480E-01	0.300000E+01	0.150000E-07	0.000000E+00	0.444444E+16
8	0.718220E-07	0.717602E-07	0.618E-10	0.199050E+00	0.300000E+01	0.720000E-07	0.000000E+00	0.192901E+15
9	0.790800E-07	0.789986E-07	0.814E-10	0.792450E+00	0.300000E+01	0.790000E-07	0.000000E+00	0.160231E+15
10	0.795390E-07	0.794522E-07	0.868E-10	0.315480E+01	0.300000E+01	0.800000E-07	0.000000E+00	0.156250E+15
11	0.100030E+01	0.100249E+01	-0.219E-02	0.158000E+02	0.400000E+01	0.000000E+00	0.000000E+00	0.100000E+01
12	0.106010E+01	0.106171E+01	-0.161E-02	0.100000E+03	0.400000E+01	0.000000E+00	0.000000E+00	0.100000E+01
13	0.155000E+01	0.154799E+01	0.201E-02	0.252000E+03	0.400000E+01	0.155000E+01	0.000000E+00	0.416233E+00
14	0.311000E+01	0.310224E+01	0.776E-02	0.630000E+03	0.400000E+01	0.310000E+01	0.000000E+00	0.104058E+00
15	0.426000E+01	0.426851E+01	-0.851E-02	0.100000E+04	0.400000E+01	0.430000E+01	0.000000E+00	0.540833E-01

\*\*\*\* rmser= 0.64120007E-02

final scaled partials (Jacobian)

1	-0.98300802E+00	0.00000000E+00	0.45169752E+00	-0.21029400E-03	0.32285083E-02
2	-0.98752421E+00	0.00000000E+00	0.54289651E+00	0.18732516E-01	0.20704610E+00
3	-0.10040869E+01	0.00000000E+00	0.15933372E+00	0.84025984E-02	0.10631049E+00
4	-0.10045505E+01	0.00000000E+00	-0.14146162E-01	-0.98771935E-02	-0.11320418E-01
5	-0.10046485E+01	0.00000000E+00	-0.43594473E-02	-0.41669784E-02	-0.25581703E-02
6	0.00000000E+00	-0.10110864E+01	0.56004203E+00	0.11198296E-03	0.26295337E-01
7	0.00000000E+00	-0.10040268E+01	0.12456908E+01	0.10079574E+00	0.68332703E+00
8	0.00000000E+00	-0.99655251E+00	0.16540021E+00	0.38473478E-01	0.13312211E+00
9	0.00000000E+00	-0.10003372E+01	0.81988631E-02	0.50908907E-02	0.62373467E-02
10	0.00000000E+00	-0.99281596E+00	0.24915792E-02	0.48387353E-03	0.22351111E-03
11	0.00000000E+00	0.00000000E+00	0.10014908E+01	0.10824785E-03	0.81669775E-03
12	0.00000000E+00	0.00000000E+00	0.98560736E+00	0.14433047E-01	0.16270619E+00
13	0.00000000E+00	0.00000000E+00	0.55119987E+00	0.93325926E-01	0.68588632E+00
14	0.00000000E+00	0.00000000E+00	0.80360779E-01	0.24391849E+00	0.73421075E+00
15	0.00000000E+00	0.00000000E+00	-0.10809307E+00	0.34162687E+00	0.63704752E+00

primary field factors: 0.10000000E+01 0.10042551E+01 0.99890090E+00

```

final unscaled parameters--
                                resistivity 1yr          depth
1      0.99777942E+00  0.10022255E+01
2      0.98586691E-01  0.10143357E+02
3      0.15074997E+03                                1      0.15074997E+03

```