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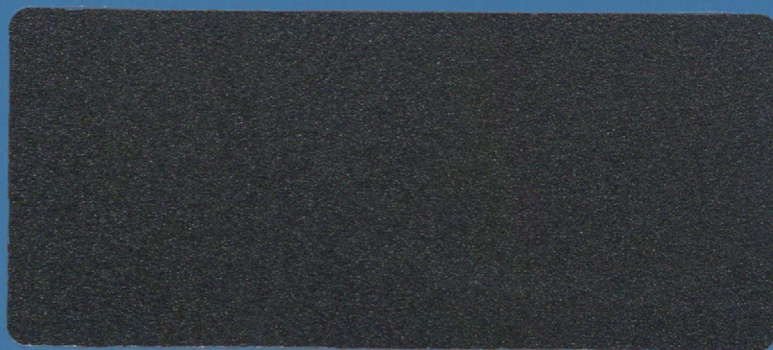
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IN ILLINOIS STREAMS

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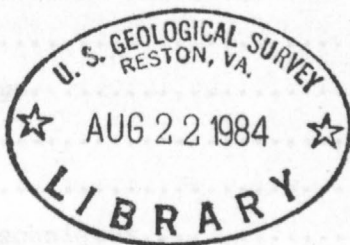
TRAVELTIME AND LONGITUDINAL DISPERSION  
IN ILLINOIS STREAMS

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By Julia B. Graf

U.S. GEOLOGICAL SURVEY

Open-File Report 84-468



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## CONVERSION FACTORS

For use of readers who prefer to use International System of Units (SI), conversion factors for terms used in this report are listed below:

<u>Multiply inch-pound units</u>	<u>By</u>	<u>To obtain SI units</u>
mile (mi)	1.609	kilometer (km)
square mile (mi <sup>2</sup> )	2.590	square kilometer (km <sup>2</sup> )
mile per hour (mi/h)	1.609	kilometer per hour (km/h)
foot per mile (ft/mi)	0.1894	meter per kilometer (m/km)
pound (lb)	0.4536	kilogram (kg)
cubic foot per second (ft <sup>3</sup> /s)	0.02832	cubic meter per second (m <sup>3</sup> /s)
cubic foot (ft <sup>3</sup> )	28.32	liter (L)

## GLOSSARY

Average reach velocity (V). The mean rate of flow of water through a stream reach, in miles per hour.

Measured average reach velocity. The average reach velocity measured by the rate of movement of the center of mass of the dye cloud through a stream reach, in miles per hour.

Computed average reach velocity. The average reach velocity computed from hydraulic geometry relations, in miles per hour.

Backwater. Water retarded in its course as compared to the normal or natural condition of flow.

Daily mean discharge. The arithmetic mean of all instantaneous discharges available at a gaging station for a given day. At the gaging stations used in this study, gage height is recorded at 15-minute intervals, and daily mean discharge is computed from the discharges that correspond to those 96 gage-height values.



Discharge. The volume of water that passes a given point in a given period of time, in cubic feet per second.

Time-weighted average discharge. The average discharge for a given period of time computed by multiplying discharge by the time interval during which that discharge prevailed, summing the resulting numbers for the entire period of time, and dividing the sum by the total number of time intervals in the period.

Dispersion. The mixing of water during flow by velocity gradients, by turbulent diffusion, and by molecular diffusion.

Dispersion efficiency. The rate of mixing of water during flow, measured in this study as the rate of decrease in unit-peak concentration of a solute with traveltime and the rate of increase in passage time of a solute past a site with traveltime.

Flow-duration curve. A curve that shows the cumulative frequency distribution of discharge at a particular site over a specified period of time.

Flow-duration frequency ( $F$ ). The fraction of time a given discharge at a gaging station is equaled or exceeded, determined from a flow-duration curve for that station, expressed in this report as a decimal fraction, dimensionless.

Gaging station. A particular site on a body of water where systematic observations of gage height and discharge are obtained.

Hydraulic geometry. The relation of hydraulic characteristics such as width, depth, channel slope, and roughness to discharge, expressed as a simple power function.

Index gage. A gaging station, in or near the reaches measured in this study, that provided flow frequency data used in analysis of traveltime and dispersion data.

Injection. The introduction of the dye tracer into the stream water.

Passage time ( $P$ ). The time for a solute to pass a site on a stream, measured as the time between the arrival of the solute at the site and the time corresponding to a solute concentration of 1 percent of the peak concentration on the receding limb of the time-concentration curve, in hours.

Sampling point. The location in a cross section at a sampling site where dye samples were collected.

Sampling site. A location along a stream where the cloud resulting from injection of dye was sampled.

Solute. A substance dissolved in a fluid.

Steady flow. A flow condition in which the discharge past a given point on a stream channel does not change with time.

Stream order ( $U$ ). A classification of streams in a drainage basin based on the pattern of confluences within the basin, dimensionless.

Transverse mixing. Mixing of water in a direction normal to the mean direction of flow in a stream.

Traveltime of peak ( $T$ ). The time for the peak concentration of a solute to move through a given reach of a stream, in hours.

Unit-peak concentration ( $C_u$ ). The peak concentration of a solute adjusted to remove the effects of discharge differences at sites along a stream and of different amounts of solute introduced into the stream, in micrograms per liter per pound times cubic feet per second.

Water year. A period beginning on October 1, ending on September 30, and designated by the calendar year in which the period ends.

#### LIST OF SYMBOLS

- $A$  Cross sectional area of flow at a site on a stream reach, in square feet.
- $c$  Constant which is a measure of the influence of channel geometry and degree of mixing on the transverse mixing coefficient, dimensionless.
- $C$  Concentration of dye at a given site on a stream at a given time, in micrograms per liter.
- $C_u$  Unit-peak concentration of dye at a site on a stream, in micrograms per liter per pound times cubic feet per second.
- $d$  Mean depth of flow in a stream reach, in feet.
- $D$  Area of the drainage basin of a stream, in square miles.
- $E_z$  Transverse mixing coefficient, equal to  $cd_u$ , in square feet per second.
- $F$  Flow-duration frequency, expressed as a decimal, dimensionless.
- $L$  Transverse mixing length, or the distance along a stream required for transverse mixing, in miles.
- $P$  Passage time of dye cloud past a site on the stream, in hours.



- $Q$  Discharge at a given site on a stream, in cubic feet per second.
- $R$  Recovery ratio, or the fraction of injected dye which passes a site on the stream downstream of injection, dimensionless.
- $T$  Cumulative traveltime of the peak dye concentration through a stream reach, in hours.
- $T_L$  Cumulative traveltime of the leading edge of the dye cloud through a stream reach, in hours.
- $t$  Time, in hours.
- $t_{0.01}$  Time on the receding limb of the time-concentration curve at which the dye concentration has decreased to 1 percent of its peak concentration, in hours.
- $\bar{t}$  Mean time, or centroid, of the time-concentration curve, in hours.
- $u_*$  Mean shear velocity of flow in a reach, in feet per second.
- $U$  Stream order, dimensionless.
- $V$  Mean velocity of flow through a stream reach, in miles per hour.
- $w$  Weight of dye observed at a sampling site, in micrograms.
- $W$  Average width of flow in a stream reach, in feet.
- $X$  Distance of a site downstream of the point of injection of dye, in miles.

## INTRODUCTION

Traveltime and mixing of water within a stream reach are basic streamflow characteristics needed by water-resources managers and planners to predict the rate of movement and dilution of contaminants which may be introduced into streams. They also are necessary for most water-quality models used in water-resources planning. A study designed to measure traveltime and longitudinal mixing in selected reaches of Illinois streams under a range of steady flow conditions was carried out from 1975 through 1982 in cooperation with the Illinois Environmental Protection Agency.





By Julia B. Graf

## ABSTRACT

Twenty-seven measurements of traveltime and longitudinal dispersion in 10 Illinois streams made from 1975 to 1982 provide data needed for estimating traveltime of peak concentration of a conservative solute, traveltime of the leading edge of a solute cloud, peak concentration resulting from injection of a given quantity of solute, and passage time of solute past a given point on a stream. These four variables can be estimated graphically for each stream from distance of travel and either discharge at the downstream end of the reach or flow-duration frequency. The traveltime and dispersion characteristics also can be estimated for other unregulated streams in Illinois with drainage areas less than about 1,500 square miles from equations developed from field measurements. For unmeasured streams, traveltime of peak concentration and of the leading edge of the cloud are related to discharge at the downstream end of the reach and distance of travel. For both measured and unmeasured streams, peak concentration and passage time are best estimated from the relation of each to traveltime. In measured streams, dispersion efficiency is greater than that predicted by Fickian diffusion theory. The rate of decrease in peak concentration with traveltime is about equal to the rate of increase in passage time. Average velocity in a stream reach, given by the velocity of the center of solute mass in that reach, can be estimated from an equation developed from measured values. The equation relates average reach velocity to discharge at the downstream end of the reach. Average reach velocity computed for 9 of the 10 streams from available equations based on hydraulic geometry relations are high relative to measured values. The estimating equation developed from measured velocities provides estimates of average reach velocity that are closer to measured velocities than are those computed with equations developed from hydraulic-geometry relations.

## INTRODUCTION

Traveltime and mixing of water within a stream reach are basic streamflow characteristics needed by water-resources managers and planners to predict the rate of movement and dilution of contaminants which may be introduced into streams. They also are necessary for most water-quality models used in water-resources planning. A study designed to measure traveltime and longitudinal mixing in selected reaches of Illinois streams under a range of steady flow conditions was carried out from 1975 through 1982 in cooperation with the Illinois Environmental Protection Agency.

## Purpose and Scope

The purpose of this report is to summarize the results of measurements that were used to develop relations for estimating traveltime and mixing characteristics for unregulated streams in Illinois, and to present the estimating techniques.

Ten streams were selected for measurement of traveltime and mixing characteristics (fig. 1). They include a range in drainage area and conditions expected to govern velocity and mixing. Length of measured reaches ranges from 5.2 to 40.3 miles, average channel slopes from 0.98 to 7.97 ft/mi, and drainage areas above sampling sites from 12.4 to 1,516 mi<sup>2</sup>. Most of the studied streams, like the majority of streams in Illinois, have sand beds with sand and gravel riffles. Beds of the Apple and Vermilion Rivers are coarser than the others and are composed primarily of gravel and bedrock. Although nine of the streams have predominantly naturally-formed meandering channels, the Kaskaskia River has a straightened, dredged channel in the reach measured. Flow is unregulated in all reaches measured, but some artificial structures or modifications are present. Riffle-pool sequences are apparent on the streambed at low flow and these cause local variations in channel geometry, velocity, and slope. Stream gages are located on each stream (fig. 1 and table 1), and the gaging records provided the data base used to relate measured variables to the long-term streamflow regime.

Details of the measurements and graphical relations for estimation of traveltime and mixing characteristics are presented for each measured stream. Equations for estimating traveltime and mixing for unmeasured streams are derived, and examples of the application of techniques to both measured and unmeasured streams are presented. An estimating equation for average reach velocity, developed from measurements of velocity of the center of mass of the dye cloud, is presented. Measured reach velocities are compared to velocities computed from the hydraulic-geometry relations (Stall and Fok, 1968, p. 20) available for 9 of the 10 measured streams. Velocity and mixing characteristics of Illinois streams are discussed in the final section.

## Previous Studies

Although techniques for estimating velocity are available, conditions in natural stream channels are often very different from those for which the techniques have been derived, and the applicability of these relations to realistic situations is limited. Relations such as the Manning equation and hydraulic-geometry equations (Leopold and Maddock, 1953, p. 25) that relate reach velocity to channel geometry, slope, or roughness can be used to estimate velocity in some situations. However, the nonuniformity of natural channels and the difficulty in defining values of roughness parameters for reaches prevent these equations from being useful for a large range of conditions. Equations for velocity of peak concentration of a conservative solute, which is close to the average reach velocity in many cases, developed from measurements on 300 streams throughout the United States (Boning, 1974) have standard

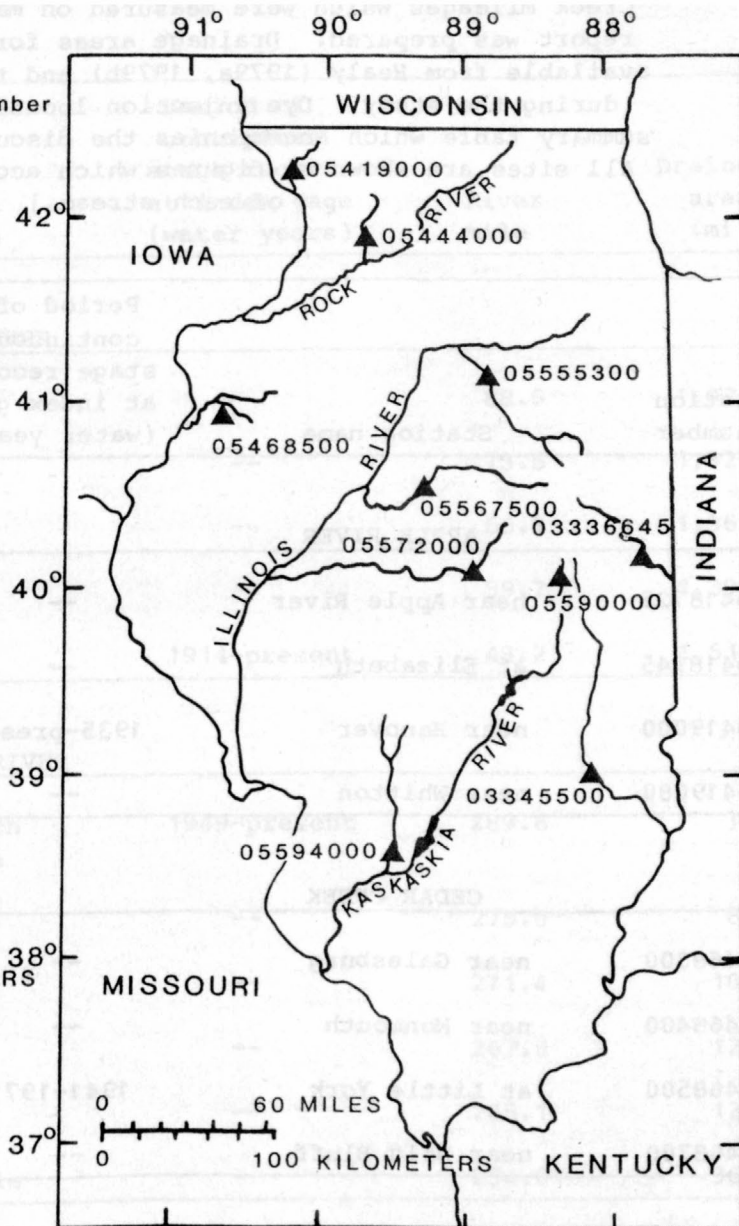


# EXPLANATION

▲ 05419000 Gaging station and number



0 400 MILES  
0 800 KILOMETERS



Base from U.S. Geological Survey State Map, 1972

Figure 1.--Location of Illinois streams measured and index gages used in the study.

Table 1.--Sampling sites and index gages for traveltime measurements

[River miles obtained from Healy (1979a, 1979b), except for Cedar Creek mileages which were measured on maps revised since that report was prepared. Drainage areas for some locations were available from Healy (1979a, 1979b) and the others were measured during the study. Dye injection locations are given in the summary table which accompanies the discussion of each stream. All sites are shown on figures which accompany the discussion of each stream.]

Station number	Station name	Period of continuous stage record at index gage (water years)	River mile	Drainage area (mi <sup>2</sup> )
APPLE RIVER				
05418725	near Apple River	--	45.0	36.1
05418945	at Elizabeth	--	23.9	188
05419000	near Hanover	1935-present	13.9	247
05419080	near Whitton	--	9.9	249
CEDAR CREEK				
05468300	near Galesburg	--	35.5	33.2
05468400	near Monmouth	--	19.2	76.7
05468500	at Little York	1941-1971	5.5	130
05468700	near Bald Bluff	--	0.0	165
ELKHORN CREEK				
05443560	near Haldane	--	45.6	20.9
05443650	near Milledgeville	--	33.6	69.2
05444000	near Penrose	1940-present	17.5	146
05444025	near Emerson	--	6.3	215



Table 1.--Sampling sites and index gages for  
traveltime measurements--Continued

Station number	Station name	Period of continuous stage record at index gage (water years)	River mile	Drainage area (mi <sup>2</sup> )
EMBARRAS RIVER				
03344200	near Greenup	--	88.5	1,022
03344600	near Rose Hill	--	73.6	1,327
03344680	near Falmouth	--	66.8	1,365
03345000	at Newton	--	59.7	1,392
03345500	at Ste. Marie	1914-present	48.2	1,516
KASKASKIA RIVER				
05590000	Kaskaskia Ditch at Bondville	1949-present	289.6	12.4
05590280	near Grange	--	275.0	67.2
05590400	near Pesotum	--	271.4	109
05590460	near Hayes	--	267.8	120
05590480	above Ficklin	--	265.1	125
05590950	at Chesterville	--	254.0	360
MACKINAW RIVER				
05567500	near Congerville <sup>1</sup>	1945-present	58.7	767
05567600	near Mackinaw	--	39.9	855
05567650	near Tremont	--	34.7	911
05568005	below Green Valley	--	10.1	1,092

<sup>1</sup> The index gage near Congerville is above the measured reach and is not a sampling site.

Table 1.--Sampling sites and index gages for  
traveltime measurements--Continued

Station number	Station name	Period of continuous stage record at index gage (water years)	River mile	Drainage area (mi <sup>2</sup> )
MIDDLE FORK VERMILION RIVER				
03336280	near Armstrong	--	60.2	279
03336645	above Oakwood	1979-present	31.7	432
SANGAMON RIVER				
05571000	at Mahomet	--	185.7	362
05571100	near Mahomet	--	184.4	364
05572000	at Monticello	1914-present	162.2	550
05572125	at Allerton Park near Monticello	--	158.0	573
05572300	near Cisco	--	150.0	625
SHOAL CREEK				
05593880	near Old Ripley	--	55.0	464
05593950	at Jamestown	--	38.2	700
05593975	at Frogtown	--	26.4	727
05594000	near Breese	1946-present	21.3	735
VERMILION RIVER				
05555300	near Leonore	1931-present	17.2	1,251
05555500	at Lowell	--	10.5	1,278
05555600	at Oglesby	--	2.7	1,329



errors of 30 to 50 percent. Other studies (Eikenberry and Davis, 1976) have shown that the standard error can be reduced significantly when a more geographically limited data base is used for development of the estimating equations.

Traveltimes have been computed for many Illinois streams (Stall and Hiestand, 1969) from velocities computed from hydraulic-geometry relations at gaged sites (Stall and Fok, 1968, p. 20). Stall and Hiestand (1969, p. 6) believed that actual velocities would be close to computed velocities for relatively high flows but could be much lower than computed for low flows. Prior to the present study, very few measurements were available to determine the accuracy of these computed velocities.

Longitudinal mixing in open channels is commonly described as a one-dimensional Fickian-type diffusion process (Fischer, 1973, eq. 11, p. 63). Dye injected into a stream at steady flow will move with the mean flow of the stream and mix with surrounding water, forming a cloud of increasing size. This mixing, called dispersion, is caused by molecular diffusion, by turbulent diffusion, and by velocity gradients (Fischer, 1973, p. 59). For turbulent flows in natural channels, molecular diffusion is generally neglected, and velocity gradients are assumed to be the primary cause of dispersion (Fischer, 1973, p. 59).

The one-dimensional approach is used to describe the spreading of the dye cloud and change in dye concentration after the dye has become mixed, or nearly mixed, throughout the width and depth of flow. According to the theory, dye concentrations are normally distributed, and the variance of the concentration distribution increases linearly with travel distance and time (Nordin and Sabol, 1974, p. 6-7). A number of studies have shown that the mixing process is not adequately described by the one-dimensional Fickian approach. Godfrey and Frederick (1970, p. k9) measured diffusion coefficients 4 to 35 times those predicted by the theory. Day (1975, p. 913) found that dye-cloud variance did not increase linearly with distance in mountain streams in New Zealand. Nordin and Sabol (1974, p. 55) and Day (1975, p. 916) observed that measured dye-concentration curves are often skewed rather than symmetrical as predicted by theory. More complex models have been proposed to account for characteristics in streams which may be causing these deviations from the one-dimensional theory (for example, Nordin and Troutman, 1980), but as yet no technique has been developed which can reliably estimate concentrations of a dispersing substance or the size of the cloud which it forms.

## TECHNIQUES

### Data Collection

For this study, a known quantity of fluorescent dye was traced through 5- to 40-mile-long reaches of 10 streams at two or three flow conditions each. Water samples collected at two to four sites in each reach were analyzed for dye concentration. Criteria for sampling-site selection were (1) the feasibility of measuring discharge over a range of flow conditions, (2) accessibility,

and (3) security for unattended automatic sampling equipment. All sampling sites were located at bridge crossings where these requirements could be met (table 1). When possible, the same sampling sites were used for all measurements on a given stream. Time constraints, equipment malfunction, and other problems caused some sampling sites to be changed.

Flow-duration curves provide a common base for comparison of streams with different size drainage areas. Flow-duration curves developed from daily mean discharge over the period of record at the index gages (table 1) were used to select the discharges at each index gage corresponding to certain flow-duration frequencies. For the measured streams, flows that occur at low flow-duration frequencies are relatively high discharges that occur during floods, whereas flows that occur with high flow-duration frequencies are low discharges that approach steady, base-flow conditions. In this report, flow-duration frequency ( $F$ ) is expressed as a decimal fraction. Discharges corresponding to flow-duration frequencies of 0.20, 0.50, and 0.80 were initially selected, but because of the unpredictable nature of streamflow, measurements at discharges other than the preselected discharges were sometimes made. Measurements were made at discharges corresponding to flow-duration frequencies ranging from 0.04 to 0.90. Although measurements were planned for steady flows, some change in discharge with time was observed during most traveltime measurements. The greatest rate of change in discharge occurred during the traveltime measurement at the highest flow rate (lowest flow-duration frequency) for a given stream, because many of these measurements were made as discharge was decreasing from a peak. Measurements were begun after the initial rapid recession had ceased, but when the change in discharge with time was still significant.

Rhodamine WT, a red fluorescent dye developed for tracer work, was used in this study. This dye is detectable at very low concentrations, mixes readily with the stream water, and is relatively inexpensive. Although some dye is lost during a measurement due to sorption by aquatic plants or sediment and by chemical and photochemical decay, recovery is high compared to other available substances (Smart and Laidlaw, 1977).

The amount of dye needed was estimated before each injection from an empirical relation between volume of dye and discharge, reach length, reach velocity and dye concentration (Hubbard and others, 1982, p. 18-19).

An analytical expression for transverse mixing of a dye slug injected into the center of flow presented by Yotsukura and Cobb (1972, p. C17) and Fischer and others (1979, p. 114) was used to estimate transverse mixing lengths for reaches below injection points at the measured flow conditions. The relation is

$$L = \frac{0.1 V W^2}{E_z} \quad (1)$$

where  $V$  is mean reach velocity,  $W$  is stream width, and  $E_z$  is a transverse mixing coefficient, equal to a constant times the product of depth,  $d$ , and shear velocity,  $u_*$ . (Symbols are defined in a list of symbols and glossary at

the front of the report.) For complete mixing in straight rectangular channels, the value of the constant,  $c$ , is about 0.2, whereas the value is higher (0.4 to 0.6) (Fischer and others, 1979, p. 109-112) in channels with curves and irregular banks. In this study, a value of 0.2 was used for  $c$ , as recommended by Hubbard and others (1982). This lower value yields estimated transverse-mixing lengths that are long compared with those which may be expected in many natural channels.

Mean flow width and depth in the reach and mean reach velocity were estimated from field observations for the initial mixing-length estimates. Channel slope in the reach, determined from topographic maps, was used to approximate water-surface slope. Transverse mixing lengths,  $L$ , were estimated again with equation 1 after measurements were completed, using reach velocities measured by the dye movement rather than estimated velocity. Comparison of these estimated mixing lengths with distances between injection and the first sampling site for measured flows (table 2) shows that mixing should have been approximately complete at the first sampling site for most of the measurements. Estimated mixing lengths are greater than the distance between the point of injection and the first sampling site for some flows in the Vermilion, Mackinaw, and Embarras Rivers.

For each traveltime measurement, the dye was measured into buckets, diluted with stream water to aid in mixing, and poured into the stream from a bridge or, conditions permitting, from a point in the stream. Dye was injected as a single slug near the center of flow in most cases. Dye was injected in a line across the central two-thirds of flow or as two slugs separated by about one-third the channel width where mixing lengths were estimated to be close to the distance between injection and the first sampling site. These injection methods will decrease the downstream distance required for transverse mixing (Hubbard and others, 1982).

At each sampling site, samples were collected periodically by hand in a small glass bottle or with a battery-operated automatic sampler. The automatic sampler was designed specifically for dye tracing work and is described by Kilpatrick (1972). Both methods sample only water near the surface. Sampling interval varied with passage time of the dye cloud and ranged from 1 to 2 minutes to 1 to 2 hours. Samples of stream water were collected before arrival of the dye for measurement of background fluorescence. The dye cloud was sampled from its first appearance at each site to at least a time when the concentration had decreased to 10 percent of its peak concentration. At most sampling sites, samples were collected at one point in the cross section. For a few measurements, samples were collected at two or three points at the first sampling site to assess the degree of transverse mixing. The results are discussed in the sections for the rivers to which they apply.

Relative dye concentrations were measured at the site with a filter fluorometer to determine arrival time of the dye, approximate peak concentration and time at which an approximate concentration of 10 percent of the peak was reached. Samples were reanalyzed in the laboratory for accurate concentrations using methods described by Wilson (1968). For the final measurements, the fluorometer was calibrated with solutions of known concentration of dye of the same dye lot used for the measurement. Samples and standard solutions were allowed to equilibrate to the laboratory temperature for measurement.



Discharge at index gage (ft <sup>3</sup> /s)	Measured average reach velocity, <i>V</i> (ft/s)	Estimated average values for reach			Estimated mixing distance, <i>L</i> (mi)	Distance from dye injection to site 1 (mi)
		Flow width, <i>W</i> (ft)	Flow depth, <i>d</i> (ft)	Shear velocity, <i>u</i> <sub>*</sub> (ft/s)		
Apple River						
663	1.00	30	1.5	0.314	0.2	1.2
111	.45	30	.7	.215	.3	1.2
Cedar Creek						
141	0.70	25	1.9	0.208	0.1	2.9
44.8	.40	25	.7	.126	.3	2.9
20.8	.40	25	.7	.126	.3	2.9
Elkhorn Creek						
102	1.00	18	0.9	0.146	0.2	1.6
53.9	.70	18	.5	.109	.4	1.6
Embarras River						
1,170	2.00	125	4.0	0.189	3.9	1.5
346	1.35	115	1.8	.127	7.4	1.5
81.9	.40	70	.9	.090	2.3	1.5

471	1.40	110	1.75	0.185	5.0	1.2
374	1.15	110	1.75	.185	4.1	1.2
31.5	.16	45	1.40	.165	.1	1.2
Middle Fork Vermilion River						
263	1.35	70	3.0	0.273	0.8	3.0
51.3	.47	30	1.0	.157	.3	3.0
Sangamon River						
372,	1.00	100	2.0	0.382	1.2	1.9
185	.90	100	1.8	.362	1.3	3.2
27.3	.15	80	1.2	.296	.3	3.2
Shoal Creek						
257	1.35	60	2.6	0.173	1.0	1.7
72.0	.67	60	1.25	.120	1.5	1.7
49.5	.63	45	1.15	.115	.9	1.7
Vermilion River						
1,540	3.00	160	3.6	0.268	7.5	2.2
495	1.30	120	2.5	.223	3.2	2.2
97.0	.45	70	2.0	.200	.5	2.2

Discharge,  $Q$ , was measured at least once at each site during dye cloud passage. Additional measurements were made if changes in stage indicated significant discharge changes during dye passage. Discharge was measured at the index gaging station to determine if adjustments to the existing stage-discharge relation were needed for the period of the traveltime measurements.

Photographs were taken, and visual observations made, of the character of bed materials and of the channel configuration during each measurement at locations along the stream where access was possible. These observations aided in description of measured reaches and qualitative evaluation of traveltime results. Because access was limited to bridge crossings, stream descriptions given in following sections apply only to a small fraction of the measured reach.

### Data Analysis

Once accurate concentrations for each sample had been measured in the laboratory, background concentration of stream water was subtracted from each sample concentration to give dye concentration. Curves of elapsed time versus dye concentration,  $C$ , (time-concentration curves) were plotted from these data. Although some of the dye clouds were sampled until concentrations had decreased to background concentration, for many traveltime measurements, especially those at sites near the end of a reach, sampling was terminated before background concentrations had been reached. Curves were either truncated at, or extrapolated to, a time corresponding to concentration of 1 percent of the peak concentration, and that time was taken as the trailing edge of the dye cloud. For extrapolation, a linear decrease of the logarithm of dye concentration with time was assumed.

The fraction of injected dye that was recovered at each sampling site (the recovery ratio,  $R$ ,) was computed by dividing the weight of dye observed at a cross section by the weight of dye injected. The weight of dye observed was found from

$$w = 1.02 \times 10^5 Q \int_0^{t_{0.01}} C dt \quad (2)$$

where  $w$  is weight of dye in micrograms,  $Q$  is discharge through the cross section in cubic feet per second,  $C$  is dye concentration in micrograms per liter ( $\mu\text{g/L}$ ),  $t$  is time in hours,  $t_{0.01}$  is the time on the time-concentration curve at which the dye concentration has decreased to 1 percent of its peak value, and  $1.02 \times 10^5$  is a constant used to convert cubic feet per second to liters per hour. Weight of injected dye was computed using a dye concentration of stock solution of  $2.38 \times 10^8 \mu\text{g/L}$ , computed for a 20 percent solution with a specific gravity of 1.19 (Hubbard and others, 1982, p. 33). The quantity

$$\int_0^{t_{0.01}} C dt$$

is the area under the time-concentration curve and was computed by numerical integration using the trapezoid method. It is assumed that the mass of dye recovered at the sampled points is representative of the entire cross section



(that the dye is mixed across the section) and that the discharge did not change during passage of the dye cloud past the sampling site. Some of the computed recovery ratios are unrealistic (greater than one, or greater at downstream sites than at upstream sites) and these values are probably caused by failure to meet these assumptions. Although some error is involved in measuring dye concentration and in determining the area under the time-concentration curve, these errors are usually small compared to errors caused by discharge changes or incomplete mixing.

Dye concentrations that would have been observed if no dye had been lost during the measurement (conservative concentrations) were computed by dividing measured concentration by the recovery ratio. Conservative-peak concentrations reflect variations in discharge along the reach and differences in the amount of dye injected. To reduce the effect of these factors, each conservative-peak concentration was divided by the weight of dye injected and multiplied by the discharge at the sampling site. The result is a quantity,  $C_u$ , known as unit-peak concentration (Hubbard and others, 1982, p. 34) that reflects only variations in dispersion.

The times of the leading edge, the peak concentration, and the trailing edge of the dye cloud at each site were found from the time-concentration curves. Passage time,  $P$ , was computed as the time of the leading edge minus the time of the trailing edge. The time corresponding to the center of mass of dye concentration, the mean time or centroid of the time-concentration curve, was found from the equation

$$\bar{t} = \frac{\int_0^{t_{0.01}} C t dt}{\int_0^{t_{0.01}} C dt} , \quad (3)$$

and integrals were computed numerically using the trapezoid method.

In this report, traveltime is expressed as both the traveltime of the leading edge of the dye cloud and traveltime of the peak concentration, and dispersion as changes in unit-peak concentration and passage time. Data are presented in both tabular and graph form. For each stream, the time from injection to the arrival of the peak at a specific sampling site, the cumulative traveltime of the peak concentration,  $T$ , is plotted against discharge,  $Q$ , at the sampling site on a double logarithmic scale (for example, see fig. 6). Each point on these plots represents a measurement at one sampling site at one flow condition (flow-duration frequency,  $F$ ). Traveltimes for equal distances of travel,  $X$ , plot along nearly straight lines, for example, line M62 - M15 on figure 6. These lines can be extrapolated to show the relation between traveltime and discharge at that site for all flow conditions. Traveltimes measured at the same flow-duration frequency,  $F$ , also plot along nearly straight lines, line G15 - B15, figure 6. These flow-duration frequency lines cross the equal-distance lines at a high angle and illustrate the relation between traveltime and discharge at the site for the same flow condition for all distances of

travel. To aid in use of these plots for estimation of traveltime at flow conditions and distances other than those measured, lines of equal distance of travel and of equal flow-duration frequency have been drawn on each plot. Positions of lines were determined by solution of equations computed by least squares linear regression using logarithms of the measured variables. The equations used differ for each stream and are presented on their respective plots.

Traveltime of the leading edge of the dye cloud relates to flow-duration frequency, discharge at the sampling site and distance of travel in much the same way as does traveltime of the peak concentration. For each stream, equations for estimating traveltime of the leading edge from flow-duration frequency and distance of travel and from discharge at the sampling site and distance of travel are presented.

Unit-peak concentration and passage time data for each stream are each plotted against cumulative traveltime from injection, also on double logarithmic scale. For some streams, the points define a single straight line, and unit-peak concentration or passage time can be estimated directly from the plot of that line or from its equation. Equations were computed using simple linear regression techniques with the logarithm of cumulative-peak traveltime as the independent variable and the logarithm of unit-peak concentration or the logarithm of passage time as the dependent variable. For other streams, a variation in unit-peak concentration, passage time, or both, with flow-duration frequency is shown on these plots. For those streams, flow-duration frequency was added as an independent variable in the regression, and the resulting multiple regression equations used to plot lines of equal flow-duration frequency. The slope of lines computed by the regression equations or of lines drawn through the data points on these graphs is a measure of dispersion efficiency of the stream. Steeper slopes indicate more efficient dispersion, or more rapid reduction of peak concentration and increase in dye-cloud length with time. Standard errors for these equations are given in table 13 and discussed in the section on limits of application.

Data from all streams were used to develop equations for estimating traveltime of peak concentration, traveltime of the leading edge, unit-peak concentration, and passage time for unmeasured streams with channel and watershed characteristics similar to measured streams. Step-backward regression was used to find the most significant set of independent variables from among drainage area, channel slope, discharge at the index gage, average discharge at the index gage, discharge at the sampling site, and flow-duration frequency. Logarithmic transformations of the variables were examined as well as untransformed values. In the backward-elimination procedure, a variable was retained in the regression model if the coefficient for that term was significantly different from zero when tested at the 95 percent confidence level.

## RESULTS FOR MEASURED STREAMS

### Apple River

The Apple River (figs. 1 and 2) drains an area of northwestern Illinois that is partially forested and serves as pasture for dairy cattle. Gravel and bedrock make up the riverbed at most observed locations, and in places the meandering channel flows along rock cliffs. Bed materials consist of silty sand at the sampling site near Whitton. Channel slope is high compared to most Illinois streams and averages 7.97 ft/mi from the injection site near Apple River to the gaging station near Hanover (table 1, fig. 2). Channel slope decreases from 10.85 ft/mi near Apple River to 2.93 ft/mi in the vicinity of the gaging station near Hanover. At the Whitton site (fig. 2), flow was much more sluggish than at upstream sites, and backwater from the Mississippi River occasionally affects stream velocity. A dam 8 to 10 feet high extends across the river above the index gage near Hanover.

Traveltime measurements were made in the Apple River at discharges at the index gage of 663 and 111 ft<sup>3</sup>/s, corresponding to 0.04 and 0.34 flow-duration frequencies, respectively (table 3). Riffles and pools were observed along the channel at both flow conditions. However, the difference in depth and velocity of flow between the riffles and pools was not great. Eddies at bends were larger at the lower discharge, but were observed during both measurements. Gravel bars, many grass-covered, exposed at the lower flow were submerged at the higher flow.

Both measurements were made as discharge at the index gage (at the lower end of the reach) was decreasing. The higher flow measurement was begun after a discharge peak had passed the gage; discharge at the gage decreased 33 percent during the measurement. The lower flow measurement was made during a slower recession, with discharge at the index gage decreasing 16 percent.

Estimated lengths for transverse mixing (table 2) are all well within the 1.2-mile distance from injection to the first sampling site.

Six data points from the two traveltime measurements served as the basis for development of figure 3, which shows the relation of traveltime of peak concentration to discharge at the sampling site, flow-duration frequency, and distance of travel. The lines of equal flow-duration frequency and distance of travel, computed with the equations shown in the figure, permit estimation of traveltime of peak for flow-duration frequencies from 0.02 to 0.40 and for travel distances up to 40 miles. Traveltime is estimated equally well by the two equations (table 13). The longer than expected traveltime observed at the Whitton site may be caused by backwater from the Mississippi River or by the reduced channel slope in that reach.



Equations developed for traveltime of the leading edge are

$$T_L = 12.2 X^{1.33} Q^{-0.60} \quad (4)$$

and

$$T_L = 3.48 X^{1.02} F^{0.44} \quad (5)$$

where  $X$  is distance of travel, in miles;  $Q$  is discharge, in cubic feet per second; and  $F$  is flow-duration frequency. As for traveltime of the peak concentration, the two equations have about equal standard errors of estimate (table 13). As expected, these equations are very similar to those computed for traveltime of the peak (fig. 3).

The relation of unit-peak concentration to traveltime of peak is shown in figure 4A; some indication that the relation between these variables varies with flow condition can be seen in the figure. Values measured at the higher flow appear to lie on a line that is approximately parallel to, but above, a line through the values measured at the lower flow. However, flow-duration frequency was not retained in the regression relation because the dependence was judged to be too weak to justify its inclusion. The computed equation and the regression line are shown in figure 4A.

Flow-duration frequency, within the range studied, does not appear to be significant in determining passage time, and simple linear regression of the logarithm of passage time against the logarithm of traveltime gives a line which best fits the data. The line or its equation (fig. 4B) can be used to estimate passage time for any flow-duration frequency less than about 0.40.

Examples of the use of these graphs to estimate traveltime, peak concentration and passage time will be given in a succeeding section.

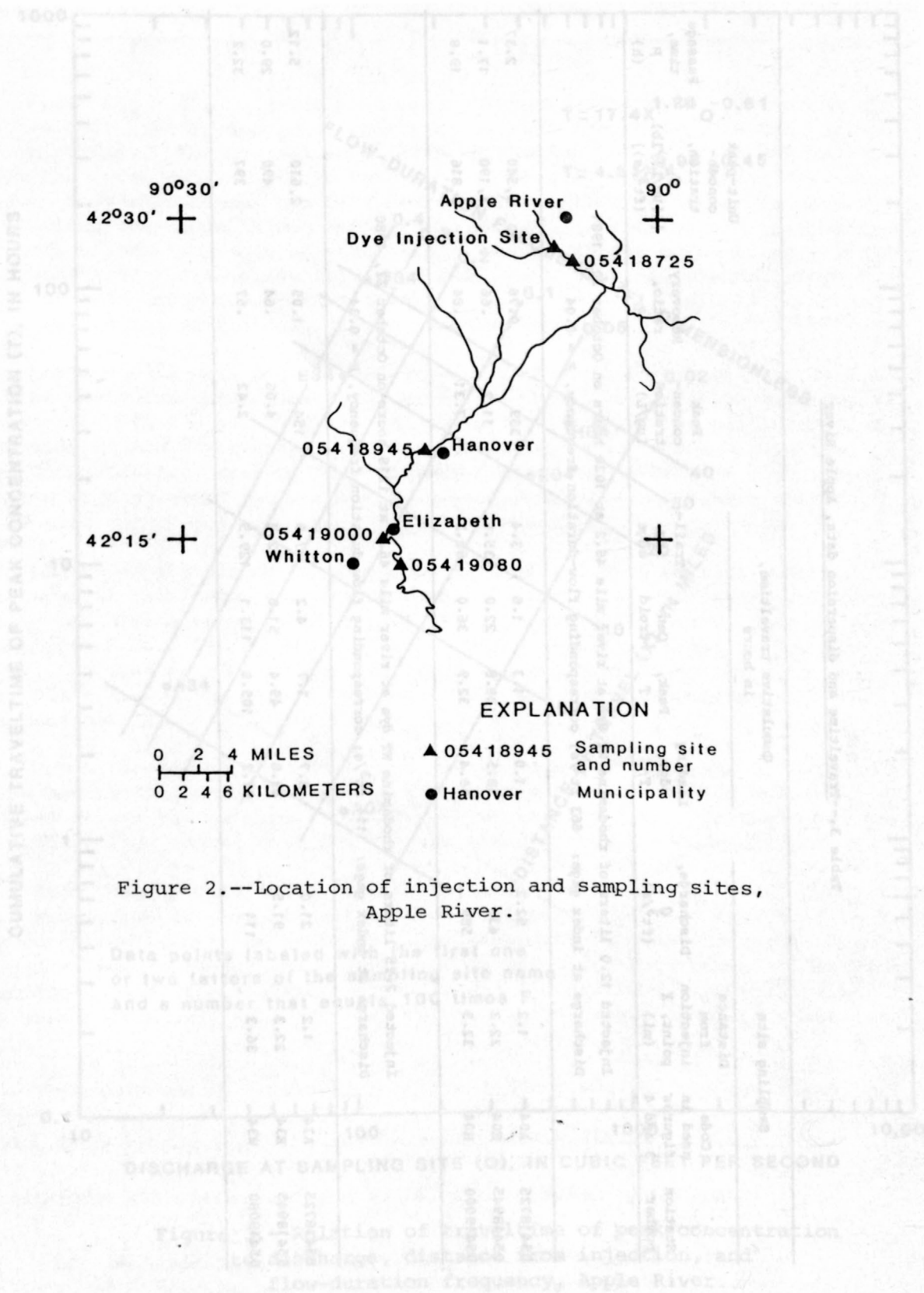


Table 3.--Traveltime and dispersion data, Apple River

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ ] ( $\text{ft}^3/\text{s}$ )]	Passage time, $P$ (h)
Station number	Code used in figures 3 and 4	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 12.0 liters of rhodamine WT dye at river mile 46.2 at 1020 hours on October 20, 1981											
Discharge at index gage: 663 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.04$											
05418725	A04	1.2	92.2	1.0	1.3	1.6	3.4	339	0.76	6,540	2.37
05418945	E04	22.3	439	18.5	20.8	22.0	35.6	11.2	.66	1,190	17.1
05419000	H04	32.3	589	30.4	32.9	36.0	50.2	7.31	.84	816	19.8
Injected 2.25 liters of rhodamine WT dye at river mile 46.2 at 1218 hours on October 27, 1980											
Discharge at index gage: 111 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.34$											
05418725	A34	1.2	21.0	2.7	3.7	4.2	7.8	154	1.05	2,610	5.12
05418945	E34	22.3	91.5	43.8	49.4	51.8	72.8	4.06	.64	490	29.0
05419080	W34	36.3	111	97.2	105.8	113.1	129.5	2.42	.57	397	32.2



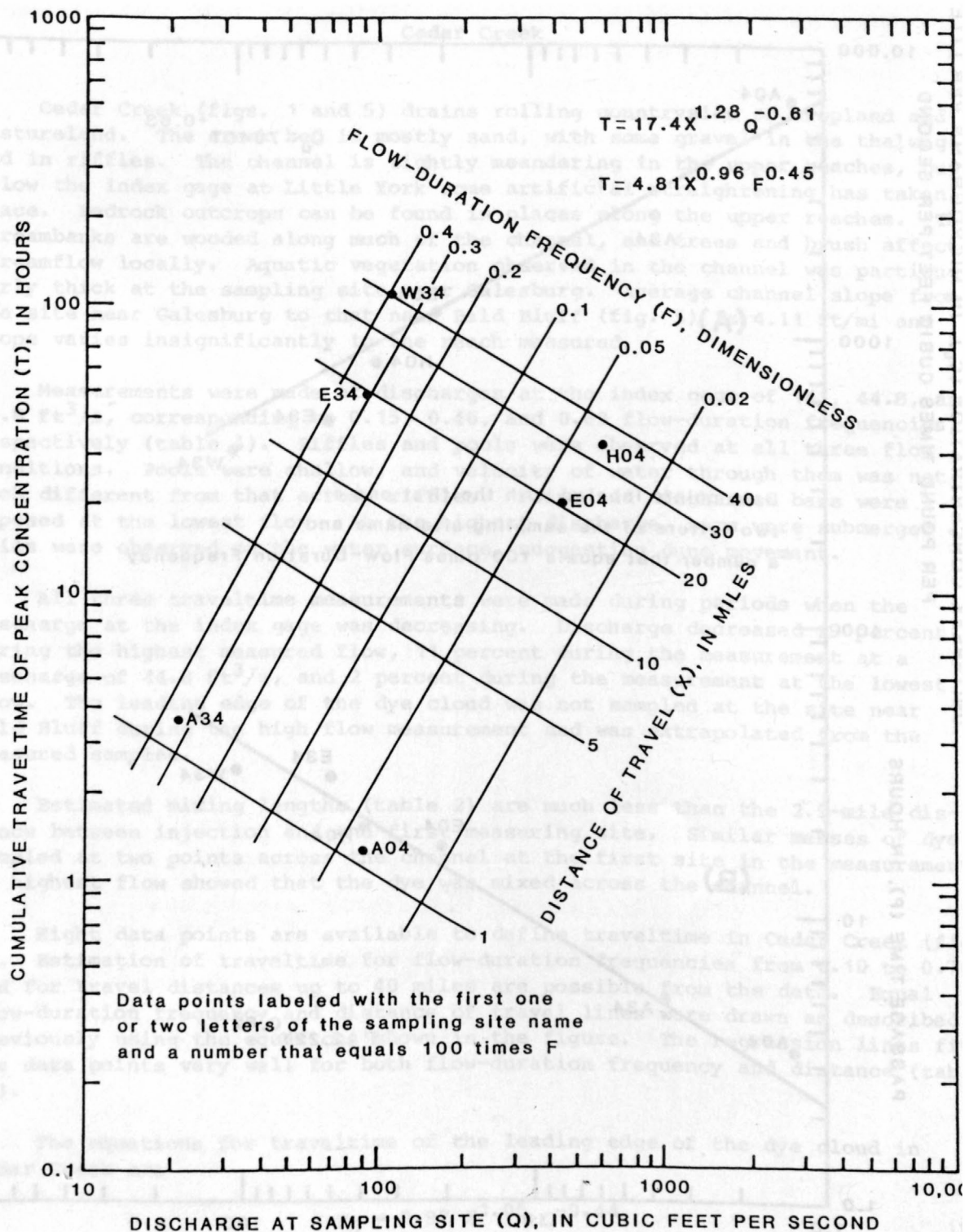


Figure 3.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Apple River.

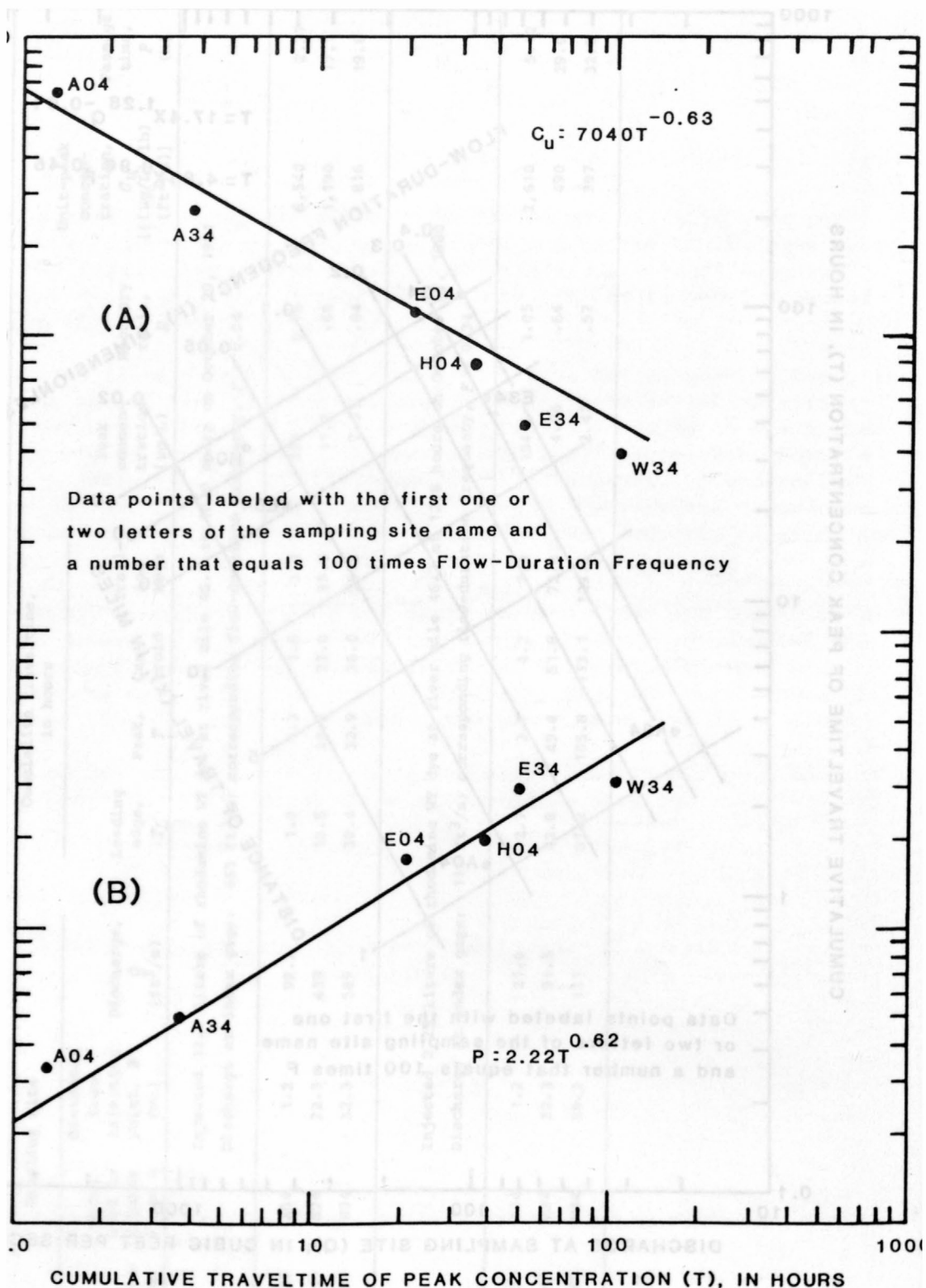


Figure 4.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration, Apple River.

## Cedar Creek

Cedar Creek (figs. 1 and 5) drains rolling countryside of cropland and pastureland. The creek bed is mostly sand, with some gravel in the thalweg and in riffles. The channel is tightly meandering in the upper reaches, but below the index gage at Little York some artificial straightening has taken place. Bedrock outcrops can be found in places along the upper reaches. The streambanks are wooded along much of the channel, and trees and brush affect streamflow locally. Aquatic vegetation observed in the channel was particularly thick at the sampling site near Galesburg. Average channel slope from the site near Galesburg to that near Bald Bluff (fig. 5) is 4.11 ft/mi and slope varies insignificantly in the reach measured.

Measurements were made at discharges at the index gage of 141, 44.8, and 20.8 ft<sup>3</sup>/s, corresponding to 0.15, 0.46, and 0.62 flow-duration frequencies, respectively (table 4). Riffles and pools were observed at all three flow conditions. Pools were shallow, and velocity of water through them was not much different from that across riffles. Point and midchannel bars were exposed at the lowest flow. At the highest discharge, bars were submerged and boils were observed on the water surface, suggesting dune movement.

All three traveltime measurements were made during periods when the discharge at the index gage was decreasing. Discharge decreased 29 percent during the highest measured flow, 11 percent during the measurement at a discharge of 44.8 ft<sup>3</sup>/s, and 2 percent during the measurement at the lowest flow. The leading edge of the dye cloud was not sampled at the site near Bald Bluff during the high flow measurement and was extrapolated from the measured samples.

Estimated mixing lengths (table 2) are much less than the 2.9-mile distance between injection and the first measuring site. Similar masses of dye sampled at two points across the channel at the first site in the measurement at highest flow showed that the dye was mixed across the channel.

Eight data points are available to define traveltime in Cedar Creek (fig. 6). Estimation of traveltime for flow-duration frequencies from 0.10 to 0.70 and for travel distances up to 40 miles are possible from the data. Equal flow-duration frequency and distance of travel lines were drawn as described previously using the equations shown in the figure. The regression lines fit the data points very well for both flow-duration frequency and distance (table 13).

The equations for traveltime of the leading edge of the dye cloud in Cedar Creek are

$$T_L = 9.97 X^{1.05} Q^{-0.44} \quad (6)$$

and

$$T_L = 4.70 X^{0.89} F^{0.46} \quad (7)$$

Standard errors of estimate are about equal for the two equations (table 13).



Unit-peak concentrations and passage time appear not to vary systematically with flow-duration frequency (fig. 7) and each can be estimated from its relation to traveltime.

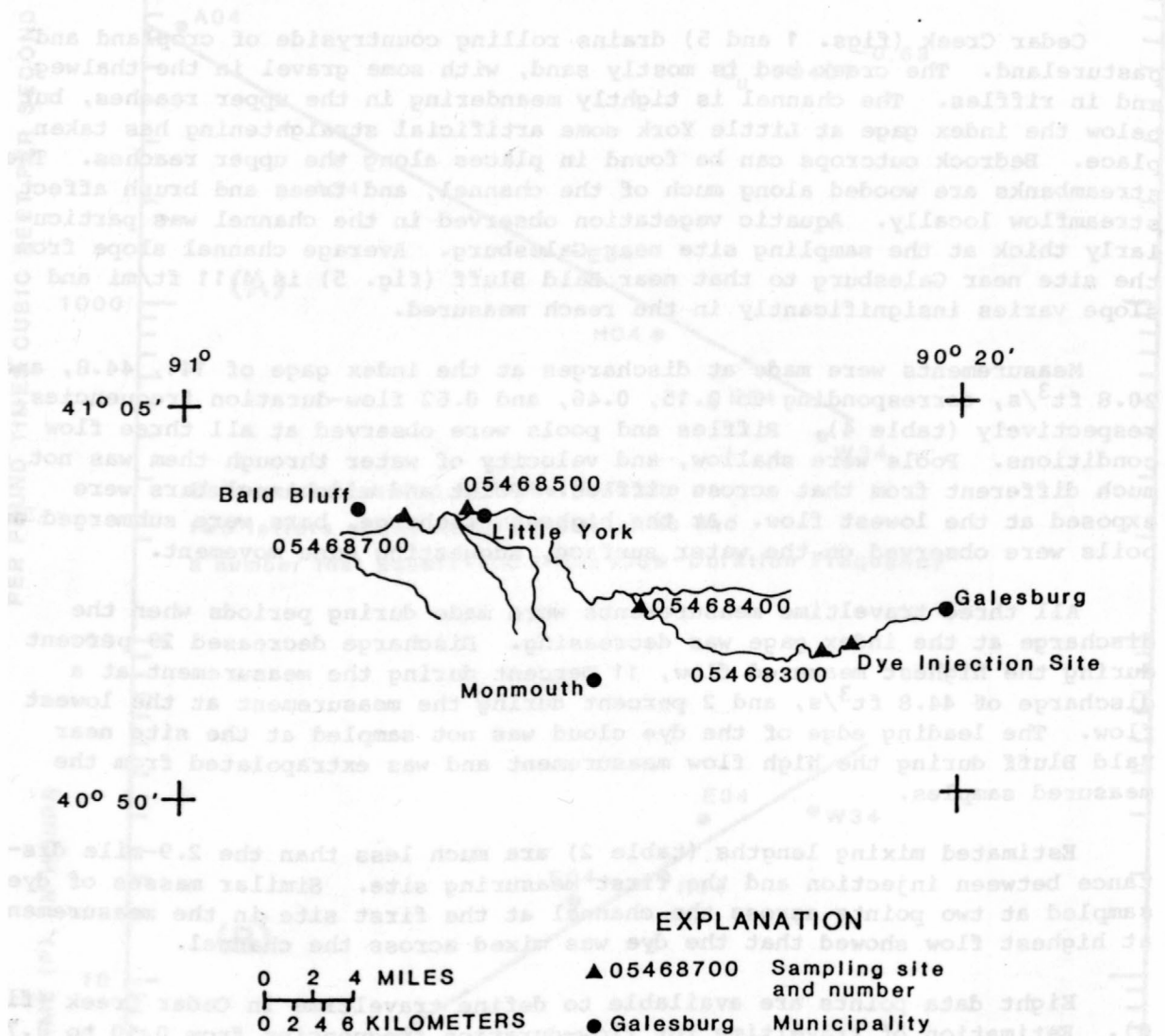


Figure 5.--Location of injection and sampling sites, Cedar Creek.

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ ] ( $\text{ft}^3/\text{s}$ )]	Passage time, $P$ (h)
Station number	Code used in figures 6 and 7	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 2.0 liters of rhodamine WT dye at river mile 38.4 at 1100 hours on June 17, 1980											
Discharge at index gage: 141 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.15$											
05468300	G15	2.9	54.4	5.3	5.90	6.0	7.8	114	1.05	5,650	2.50
05468400	M15	19.2	109	28.1	30.0	30.9	45.1	16.7	.90	1,930	17.0
05468700	B15	38.4	130	48.1	50.3	52.7	72.8	6.10	.74	1,030	24.7
Injected 2.0 liters of rhodamine WT dye at river mile 38.4 at 1050 hours on July 22, 1981											
Discharge at index gage: 44.8 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.46$											
05468300	G46	2.9	19.4	8.8	10.2	10.5	13.6	87.7	0.58	2,800	4.77
05468400	M46	19.2	35.6	46.8	50.6	51.9	67.8	16.9	.55	1,040	20.9
05468500	Y46	32.9	44.6	72.6	78.3	81.1	107.4	5.56	.42	565	34.9
Injected 0.75 liters of rhodamine WT dye at river mile 38.4 at 1140 hours on August 25, 1980											
Discharge at index gage: 20.8 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.62$											
05468300	G62	2.9	12.3	8.8	10.1	10.4	14.0	45.6	0.50	2,830	5.20
05468400	M62	19.2	22.3	57.6	62.1	65.5	93.2	7.29	.61	680	35.6

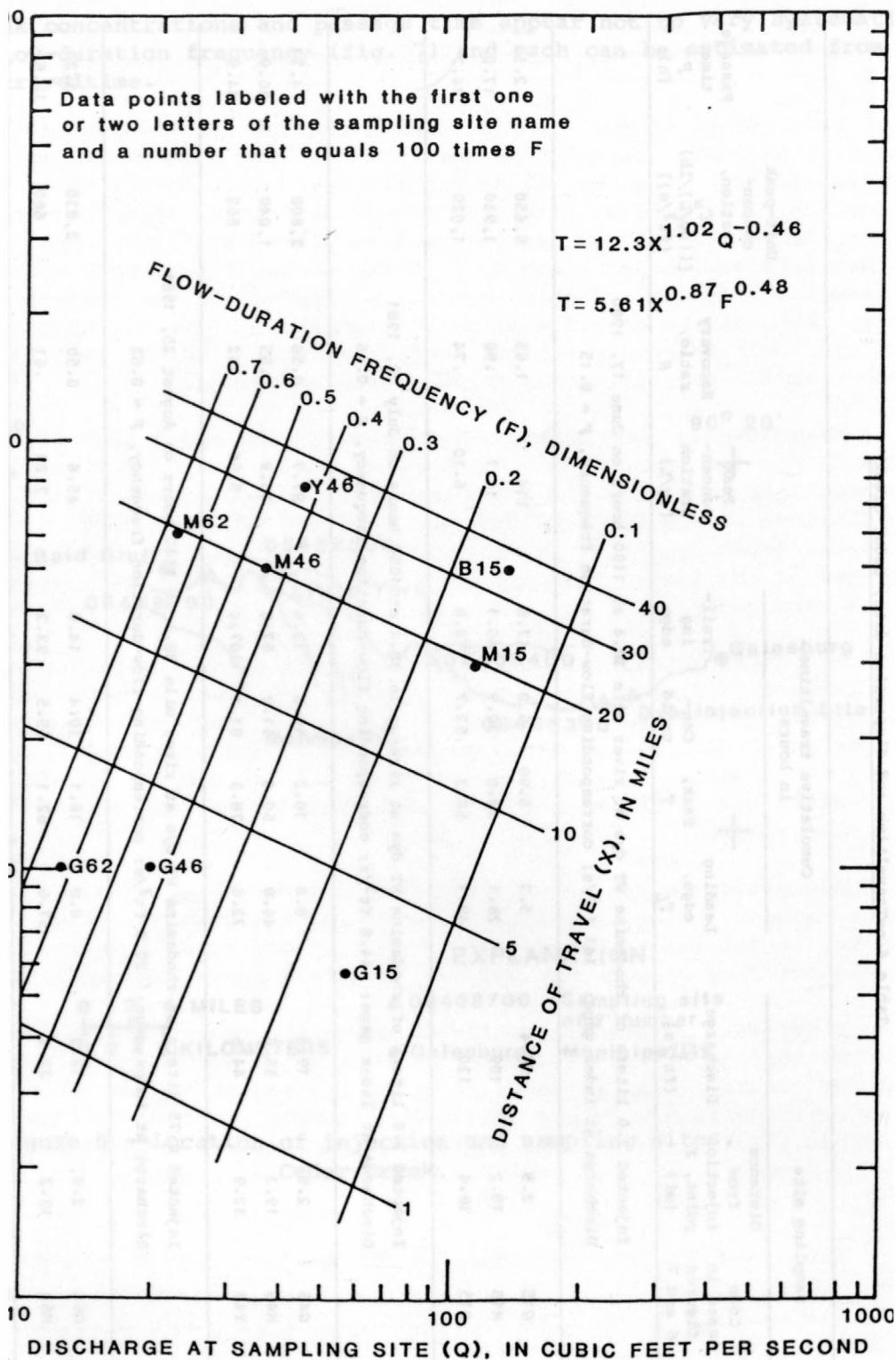


Figure 6.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Cedar Creek.



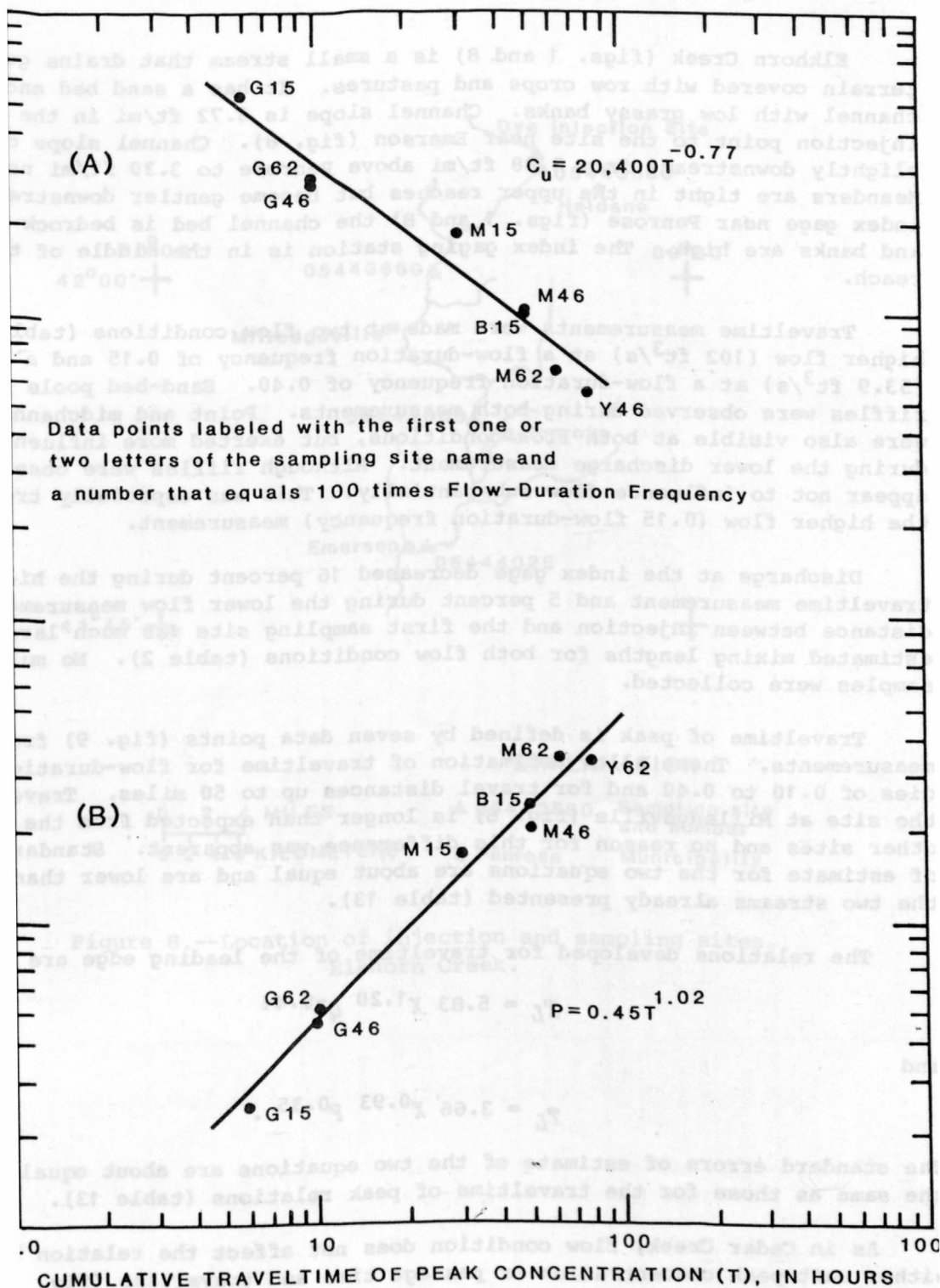


Figure 7.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration, Cedar Creek.

## Elkhorn Creek

Elkhorn Creek (figs. 1 and 8) is a small stream that drains gently rolling terrain covered with row crops and pastures. It has a sand bed and meandering channel with low grassy banks. Channel slope is 3.72 ft/mi in the reach from injection point to the site near Emerson (fig. 8). Channel slope decreases slightly downstream, from 3.88 ft/mi above Penrose to 3.30 ft/mi near Emerson. Meanders are tight in the upper reaches but become gentler downstream. At the index gage near Penrose (figs. 1 and 8) the channel bed is bedrock and gravel, and banks are high. The index gaging station is in the middle of the measured reach.

Traveltime measurements were made at two flow conditions (table 5), the higher flow (102 ft<sup>3</sup>/s) at a flow-duration frequency of 0.15 and a lower flow (53.9 ft<sup>3</sup>/s) at a flow-duration frequency of 0.40. Sand-bed pools and gravel riffles were observed during both measurements. Point and midchannel bars were also visible at both flow conditions, but exerted more influence on flow during the lower discharge measurement. Although riffles were observed, they appear not to influence flow substantially. This was especially true during the higher flow (0.15 flow-duration frequency) measurement.

Discharge at the index gage decreased 16 percent during the higher flow traveltime measurement and 5 percent during the lower flow measurement. The distance between injection and the first sampling site was much larger than estimated mixing lengths for both flow conditions (table 2). No multiple samples were collected.

Traveltime of peak is defined by seven data points (fig. 9) from the two measurements. These allow estimation of traveltime for flow-duration frequencies of 0.10 to 0.40 and for travel distances up to 50 miles. Traveltime to the site at Milledgeville (fig. 8) is longer than expected from the values for other sites and no reason for this difference was apparent. Standard errors of estimate for the two equations are about equal and are lower than those for the two streams already presented (table 13).

The relations developed for traveltime of the leading edge are

$$T_L = 5.83 X^{1.20} Q^{-0.44} \quad (8)$$

and

$$T_L = 3.66 X^{0.93} F^{0.35} \quad (9)$$

The standard errors of estimate of the two equations are about equal and about the same as those for the traveltime of peak relations (table 13).

As in Cedar Creek, flow condition does not affect the relation between either unit-peak concentration or passage time and traveltime (fig. 10). A single line computed from the regression of the logarithms of the variables can be used to estimate both unit-peak concentration and passage time.

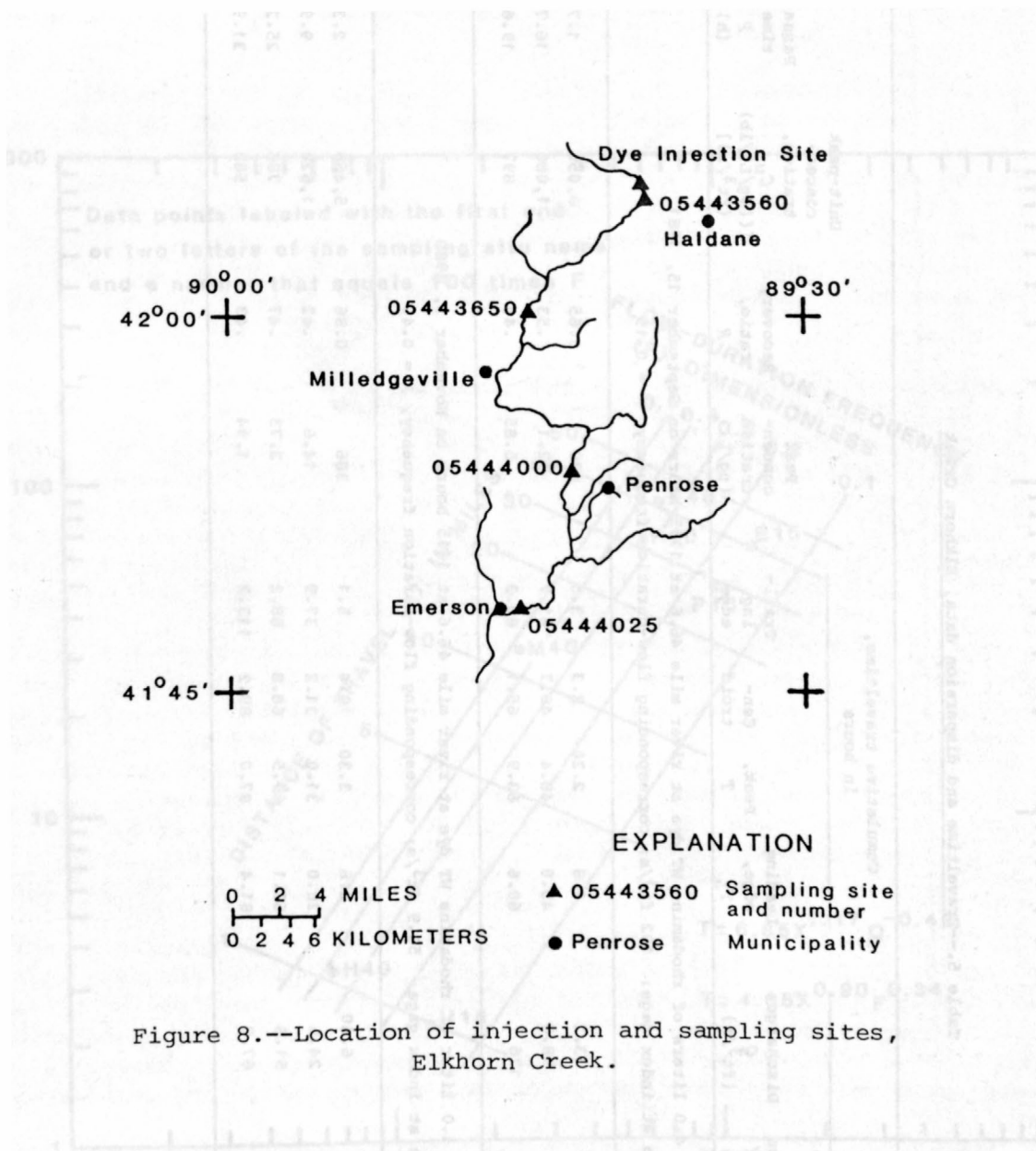


Figure 8.--Location of injection and sampling sites, Elkhorn Creek.



Table 5.--Traveltime and dispersion data, Elkhorn Creek

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/\text{lb}$ ] ( $\text{ft}^3/\text{s}$ )]	Passage time, $P$ (h)
Station number	Code used in figures 9 and 10	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Cen- troid	Trail- ing edge				
Injected 4.0 liters of rhodamine WT dye at river mile 46.6 at 1115 hours on September 15, 1981											
Discharge at index gage: 102 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.15$											
05443560	H15	1.0	13.2	1.8	2.20	2.3	3.5	830	0.65	8,050	1.72
05444000	P15	29.1	98.8	45.0	48.4	49.7	61.7	12.1	.53	1,080	16.7
05444025	E15	40.3	126	60.6	63.9	65.1	80.3	6.85	.46	897	19.6
Injected 1.0 liter of rhodamine WT dye at river mile 46.6 at 1115 hours on November 3, 1980											
Discharge at index gage: 53.9 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.40$											
05443560	H40	1.0	6.40	2.8	3.30	3.4	5.1	386	0.86	5,460	2.33
05443650	M40	13.0	24.6	28.0	31.0	31.2	37.9	14.6	.42	1,620	9.9
05444000	P40	29.1	51.8	63.1	67.5	68.8	88.2	3.73	.47	786	25.2
05444025	E40	40.3	67.8	81.4	87.0	89.2	113.2	1.94	.43	582	31.9

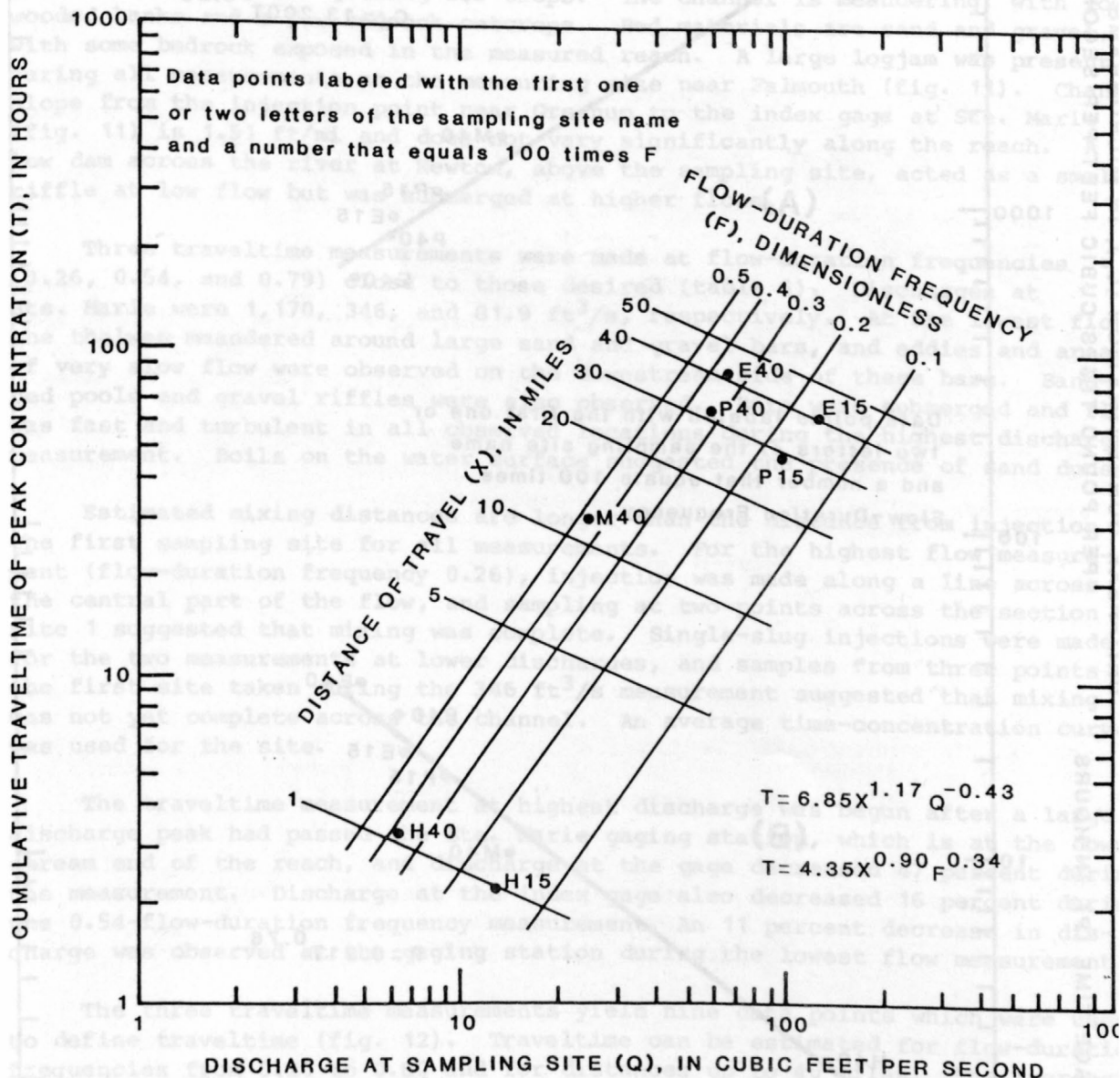


Figure 9.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Elkhorn Creek.

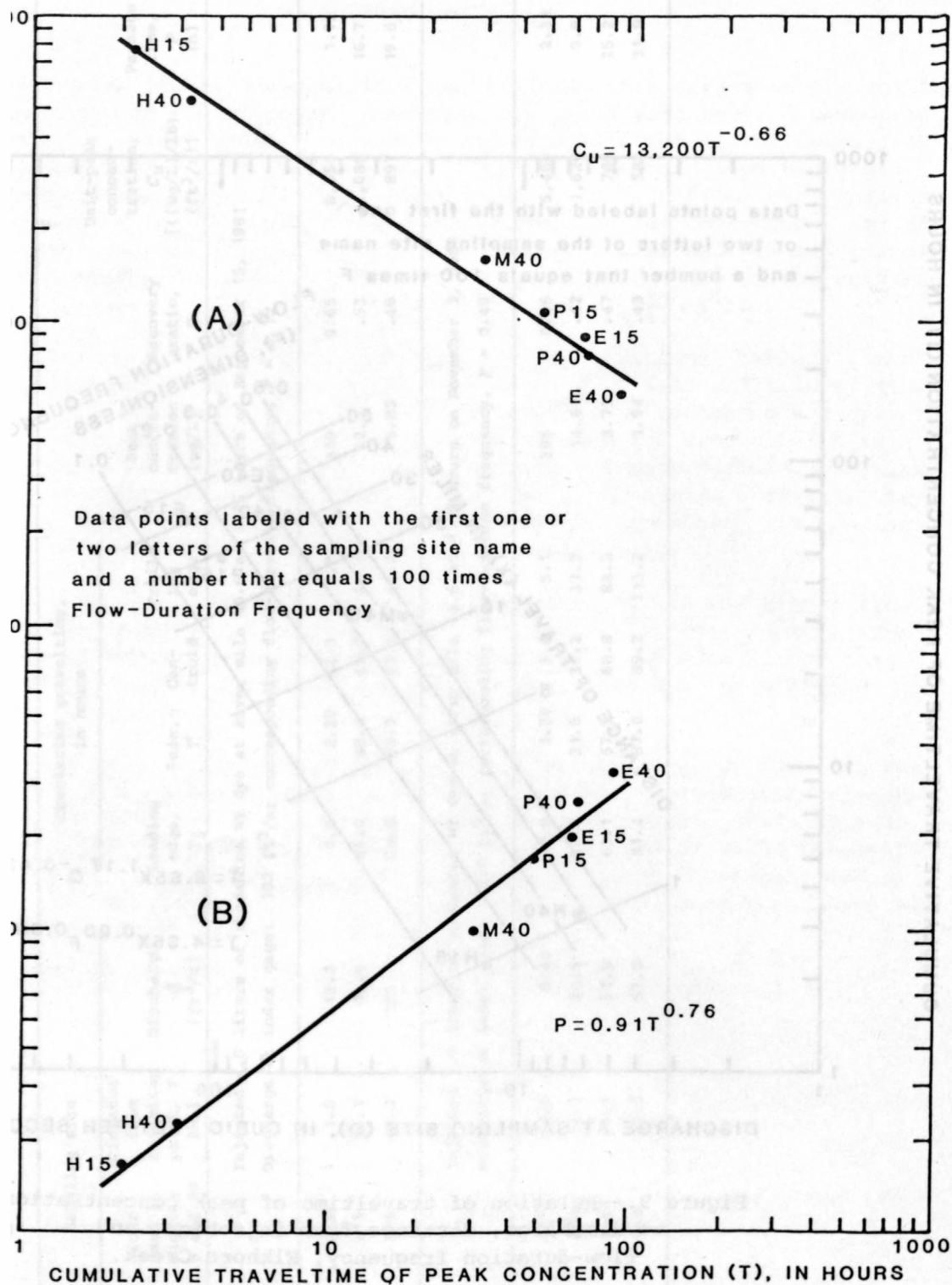


Figure 10.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration, Elkhorn Creek.



## Embarras River

The Embarras River (figs. 1 and 11) drains slightly undulating countryside used largely for growing row crops. The channel is meandering, with low wooded banks and a few bedrock outcrops. Bed materials are sand and gravel, with some bedrock exposed in the measured reach. A large logjam was present during all measurements at the measuring site near Falmouth (fig. 11). Channel slope from the injection point near Greenup to the index gage at Ste. Marie (fig. 11) is 1.51 ft/mi and does not vary significantly along the reach. A low dam across the river at Newton, above the sampling site, acted as a small riffle at low flow but was submerged at higher flows.

Three traveltime measurements were made at flow-duration frequencies (0.26, 0.54, and 0.79) close to those desired (table 6). Discharges at Ste. Marie were 1,170, 346, and 81.9 ft<sup>3</sup>/s, respectively. At the lowest flow, the thalweg meandered around large sand and gravel bars, and eddies and areas of very slow flow were observed on the downstream side of these bars. Sand-bed pools and gravel riffles were also observed. Bars were submerged and flow was fast and turbulent in all observed locations during the highest discharge measurement. Boils on the water surface suggested the presence of sand dunes.

Estimated mixing distances are longer than the distance from injection to the first sampling site for all measurements. For the highest flow measurement (flow-duration frequency 0.26), injection was made along a line across the central part of the flow, and sampling at two points across the section at site 1 suggested that mixing was complete. Single-slug injections were made for the two measurements at lower discharges, and samples from three points at the first site taken during the 346 ft<sup>3</sup>/s measurement suggested that mixing was not yet complete across the channel. An average time-concentration curve was used for the site.

The traveltime measurement at highest discharge was begun after a large discharge peak had passed the Ste. Marie gaging station, which is at the downstream end of the reach, and discharge at the gage decreased 47 percent during the measurement. Discharge at the index gage also decreased 16 percent during the 0.54-flow-duration frequency measurement. An 11 percent decrease in discharge was observed at the gaging station during the lowest flow measurement.

The three traveltime measurements yield nine data points which were used to define traveltime (fig. 12). Traveltime can be estimated for flow-duration frequencies from 0.20 to 0.80 and for distances up to 40 miles. The regression relation used to compute the lines of equal flow-duration frequency does not fit these data points as well as streams discussed previously (table 13). Lines of equal distance computed from the regression relations fit the data well, except for the measurement at Ste. Marie.

Traveltime of the leading edge can be estimated from either

$$T_L = 17.8 X^{1.14} Q^{-0.53} \quad (10)$$

or

$$T_L = 2.62 X^{1.12} F^{1.34} \quad (11)$$

However, equation 11 has a significantly higher standard error of estimate (table 13). As in the case of traveltime of the peak concentration, the equation using discharge at the sampling site would probably provide better estimates than that using flow-duration frequency. A possible source of error in both cases is in the assignment of a single flow-duration frequency to flows that changed with time.

Plots of unit-peak concentration and passage time as a function of travel time of peak (fig. 13) show that, for the Embarras River, flow-duration frequency is a significant factor. Multiple linear regression was used to relate unit-peak concentration to traveltime, and the resulting equation was used to compute lines of equal flow-duration frequency (fig. 13A). The relation to flow-duration frequency is less well defined for passage time (fig. 13B), but is significant. Flow-duration frequency was included in the regression for passage time as well as for unit-peak concentration.

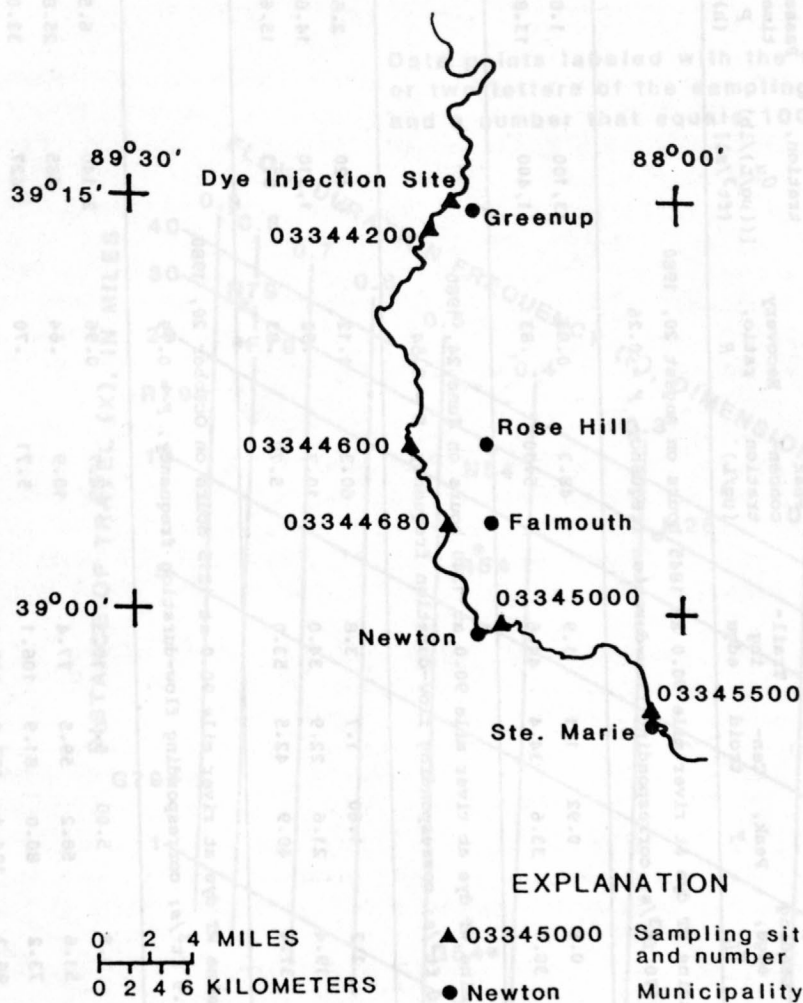


Figure 11.--Location of injection and sampling sites, Embarras River.

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ $(\text{ft}^3/\text{s})$ ]]	Passage time, $P$ (h)
Station number	Code used in figures 12 and 13	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 8.0 liters of rhodamine WT dye at river mile 90.0 at 1845 hours on August 20, 1980 Discharge at index gage: 1,170 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.26$											
03344200	G26	1.5	972	0.8	0.92	1.1	1.9	48.3	0.85	13,100	1.07
03345500	M26	41.8	980	30.7	33.6	34.4	44.6	5.00	.83	1,400	13.8
Injected 5.0 liters of rhodamine WT dye at river mile 90.0 at 1240 hours on June 24, 1980 Discharge at index gage: 346 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.54$											
03344200	G54	1.5	314	1.2	1.60	1.7	3.8	60.3	1.12	6,420	2.65
03344600	R54	16.4	306	19.4	21.6	22.9	34.0	10.3	.92	1,310	14.6
03345000	N54	30.3	332	37.4	40.9	42.5	53.0	5.70	.83	873	15.6
Injected 2.5 liters of rhodamine WT dye at river mile 90.0 at 1215 hours on October 20, 1980 Discharge at index gage: 81.9 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.79$											
03344200	G79	1.5	41.5	3.8	5.00	5.7	10.3	64.7	0.96	2,140	6.50
03344600	R79	16.4	52.7	51.6	58.2	59.5	77.4	10.9	.64	685	25.8
03344680	F79	23.2	68.6	73.2	80.0	81.9	106.1	5.71	.70	427	33.0
03345000	N79	30.3	68.7	96.3	104.4	107.0	127.1	4.29	.57	394	30.8



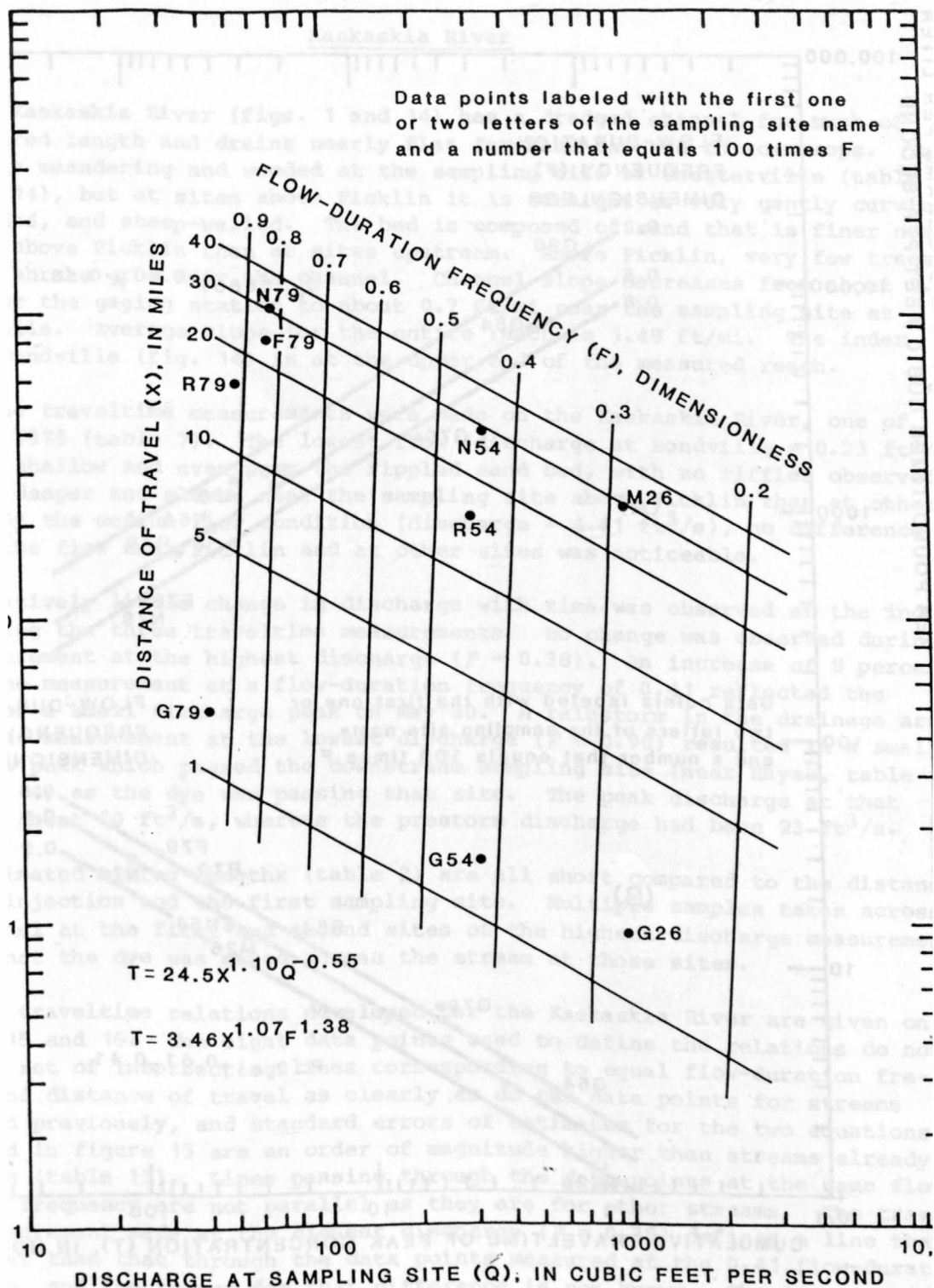


Figure 12.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Embarras River.

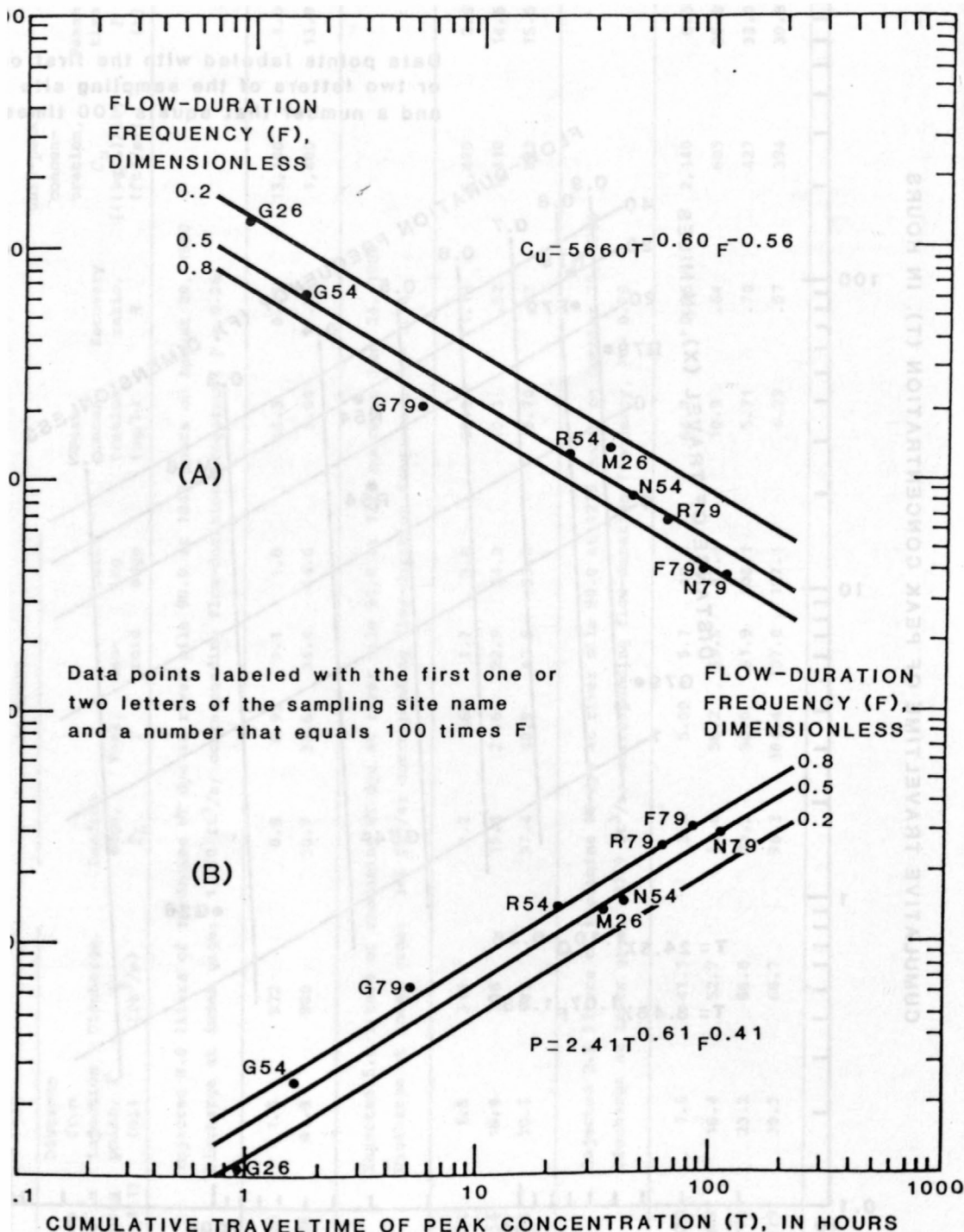


Figure 13.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration and flow-duration frequency, Embarras River.

## Kaskaskia River

The Kaskaskia River (figs. 1 and 14) has a dredged channel for much of the measured length and drains nearly flat farmland devoted to row crops. The channel is meandering and wooded at the sampling site at Chesterville (table 1 and fig. 14), but at sites above Ficklin it is straight or very gently curving, flat-bedded, and steep-walled. The bed is composed of sand that is finer near the site above Ficklin than at sites upstream. Above Ficklin, very few trees or large shrubs grow near the channel. Channel slope decreases from about 2.3 ft/mi near the gaging station to about 0.7 ft/mi near the sampling site at Chesterville. Average slope for the entire reach is 1.48 ft/mi. The index gage at Bondville (fig. 14) is at the upper end of the measured reach.

Three traveltime measurements were made on the Kaskaskia River, one of these in 1975 (table 7). The lowest flow (discharge at Bondville =  $0.23 \text{ ft}^3/\text{s}$ ) was very shallow and even over the rippled sand bed, with no riffles observed. Flow was deeper and slower near the sampling site above Ficklin than at other sites. At the medium flow condition (discharge =  $4.41 \text{ ft}^3/\text{s}$ ), no difference between the flow near Ficklin and at other sites was noticeable.

Relatively little change in discharge with time was observed at the index gage during the three traveltime measurements. No change was observed during the measurement at the highest discharge ( $P = 0.38$ ). An increase of 8 percent during the measurement at a flow-duration frequency of 0.41 reflected the passage of a small discharge peak on May 30. A rainstorm in the drainage area during the measurement at the lowest discharge ( $P = 0.90$ ) resulted in a small discharge peak which passed the downstream sampling site (near Hayes, table 1 and fig. 14) as the dye was passing that site. The peak discharge at that site was about  $50 \text{ ft}^3/\text{s}$ , whereas the prestorm discharge had been  $23 \text{ ft}^3/\text{s}$ .

Estimated mixing lengths (table 2) are all short compared to the distances between injection and the first sampling site. Multiple samples taken across the channel at the first and second sites of the highest discharge measurement showed that the dye was mixed across the stream at those sites.

The traveltime relations developed for the Kaskaskia River are given on figures 15 and 16. The eight data points used to define the relations do not define a set of intersecting lines corresponding to equal flow-duration frequency and distance of travel as clearly as do the data points for streams discussed previously, and standard errors of estimates for the two equations presented in figure 15 are an order of magnitude higher than streams already presented (table 13). Lines passing through the data points at the same flow-duration frequency are not parallel as they are for other streams. The traveltime measurement made at the highest discharge ( $P = 0.38$ ) defines a line that is steeper than that through the data points measured at the 0.41 flow-duration frequency, and the reason for that difference is not known. The increase in discharge downstream for the 0.41-flow-duration frequency measurement is greater than that for the 0.38-flow-duration frequency measurement; this may be an indication that discharge increases caused by the rainstorm influenced both discharge and traveltime in the lower reaches. The steeper slope of the line representing the traveltime measurement at lowest flow may be caused by discharge changes during the measurement.

The equations for traveltime of the leading edge are

$$T_L = 3.14 X^{1.38} Q^{-0.44} \quad (12)$$

and

$$T_L = 5.43 X^{0.84} F^{0.95} \quad (13)$$

The standard error of estimate for equation 12 is close to those of the equations for traveltime of the peak, but that for equation 13 is lower (table 13)

Some variation with flow condition can be seen on the graphs of unit-peak concentration and passage time versus traveltime (fig. 16), but here, too, the variation with flow-duration frequency is not systematic. For this reason, flow-duration frequency was found not to be statistically significant and the relation between each of those two variables and traveltime is represented by a single straight line (fig. 16).



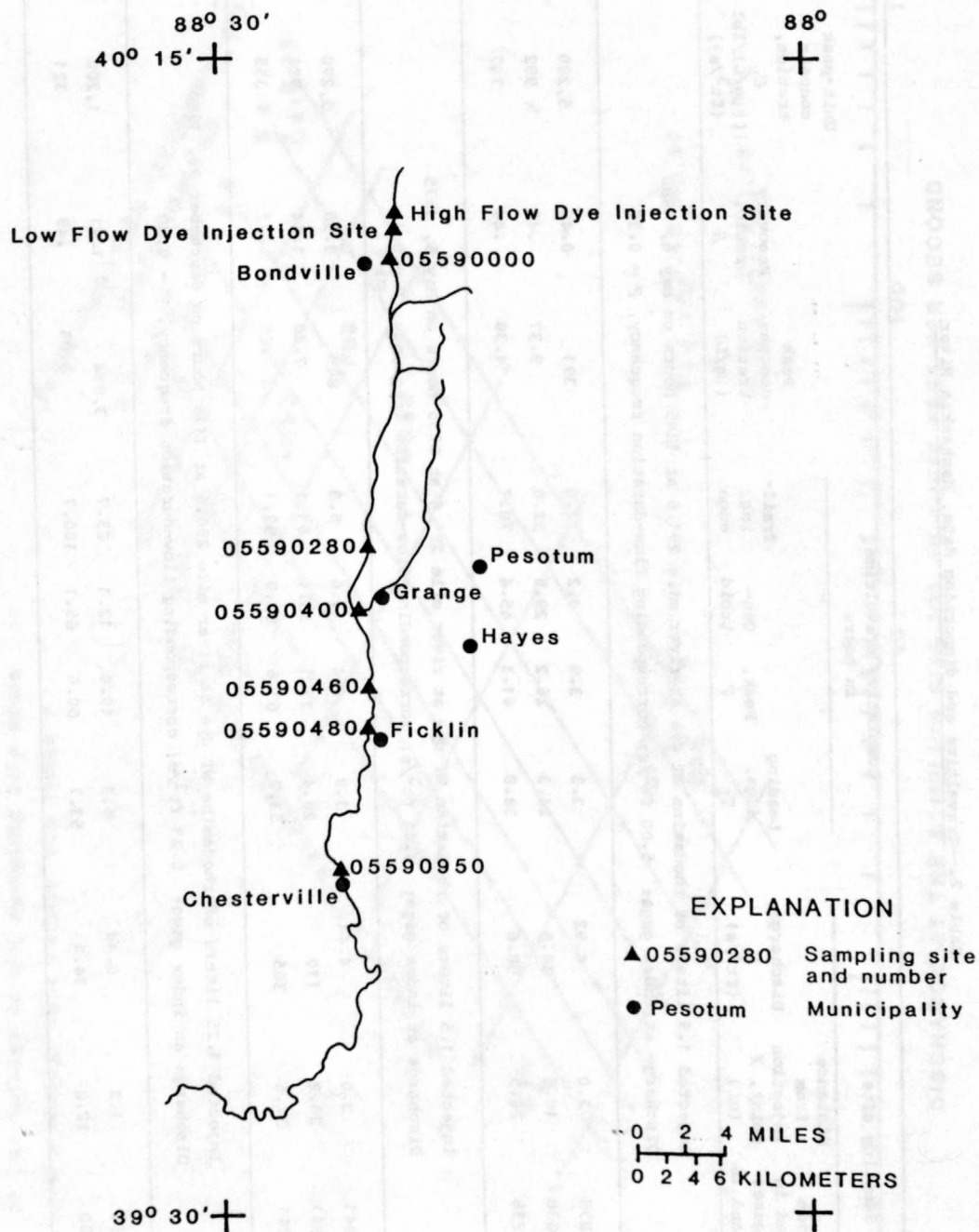
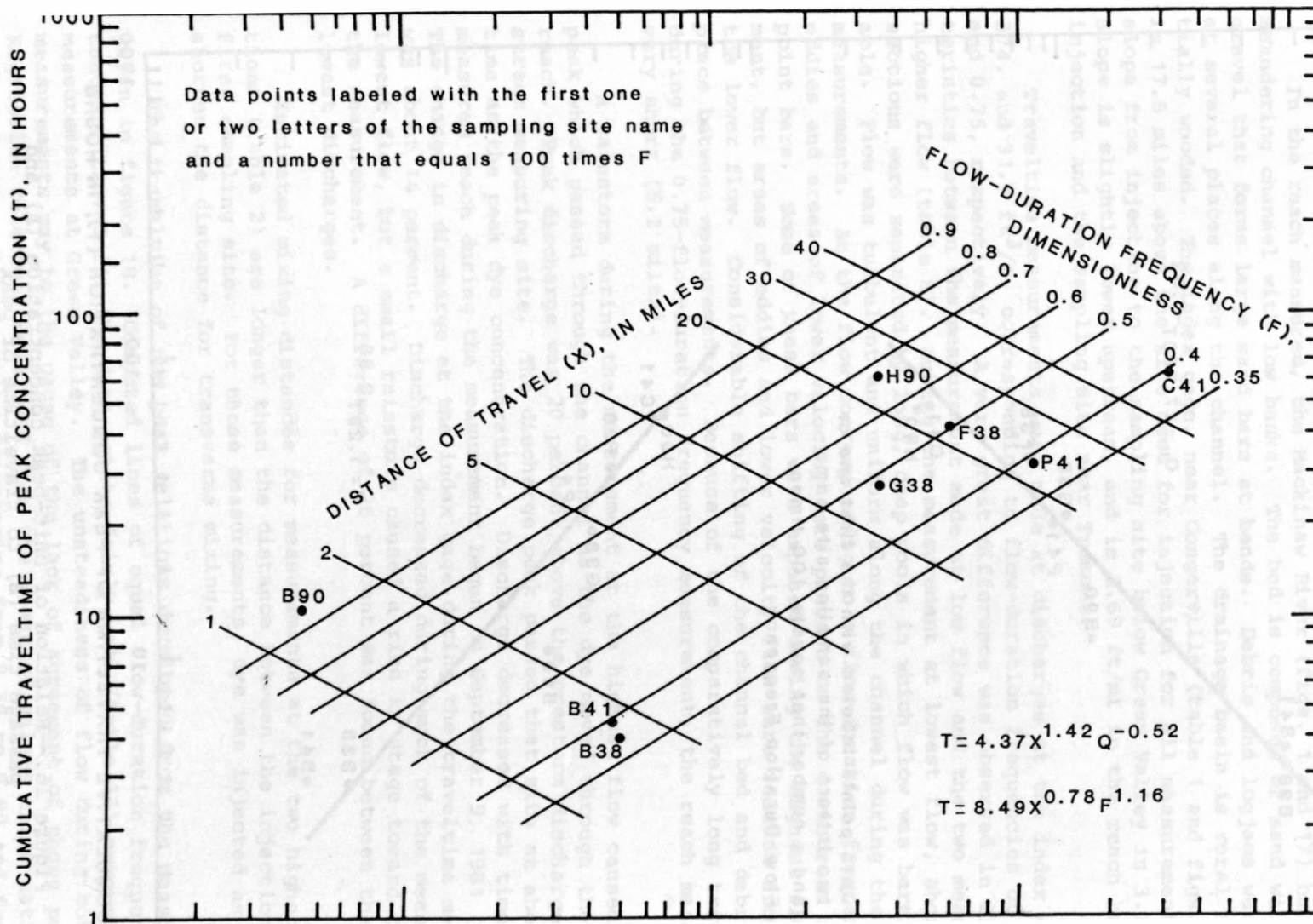


Figure 14.--Location of injection and sampling sites, Kaskaskia River.

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ $(\text{ft}^3/\text{s})$ ]]	Passage time, $P$ (h)
Station number	Code used in figures 15 and 16	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 1.5 liters of rhodamine WT dye at river mile 291.6 at 1245 hours on May 6, 1980 Discharge at index gage: 5.00 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.38$											
05590000	B38	2.0	4.92	3.3	3.9	4.2	7.6	391	0.46	5,280	4.33
05590280	G38	16.6	34.6	24.3	26.2	29.5	52.0	9.37	.42	992	27.7
05590480	F38	26.5	58.6	38.8	41.3	45.4	70.7	4.38	.44	747	31.9
Injected 1.5 liters of rhodamine WT dye at river mile 291.6 at 0955 hours on May 5, 1975 Discharge at index gage: 4.41 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.41$											
05590000	B41	2.0	4.41	3.8	4.4	4.6	6.8	849	0.90	5,270	3.03
05590400	P41	20.2	110	28.4	31.1	33.4	51.1	7.40	1.14	906	22.8
05590950	C41	37.6	305	53.2	61.6	63.9	97.1	.65	.71	355	44.0
Injected 1.25 liters of rhodamine WT dye at river mile 290.6 at 1115 hours on September 29, 1980 Discharge at index gage: 0.23 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.90$											
05590000	B90	1.0	0.44	6.1	10.4	12.1	25.7	3,054	1.71	1,200	19.6
05590460	H90	22.8	34.1	53.7	60.6	65.1	100.7	3.01	.49	321	47.0



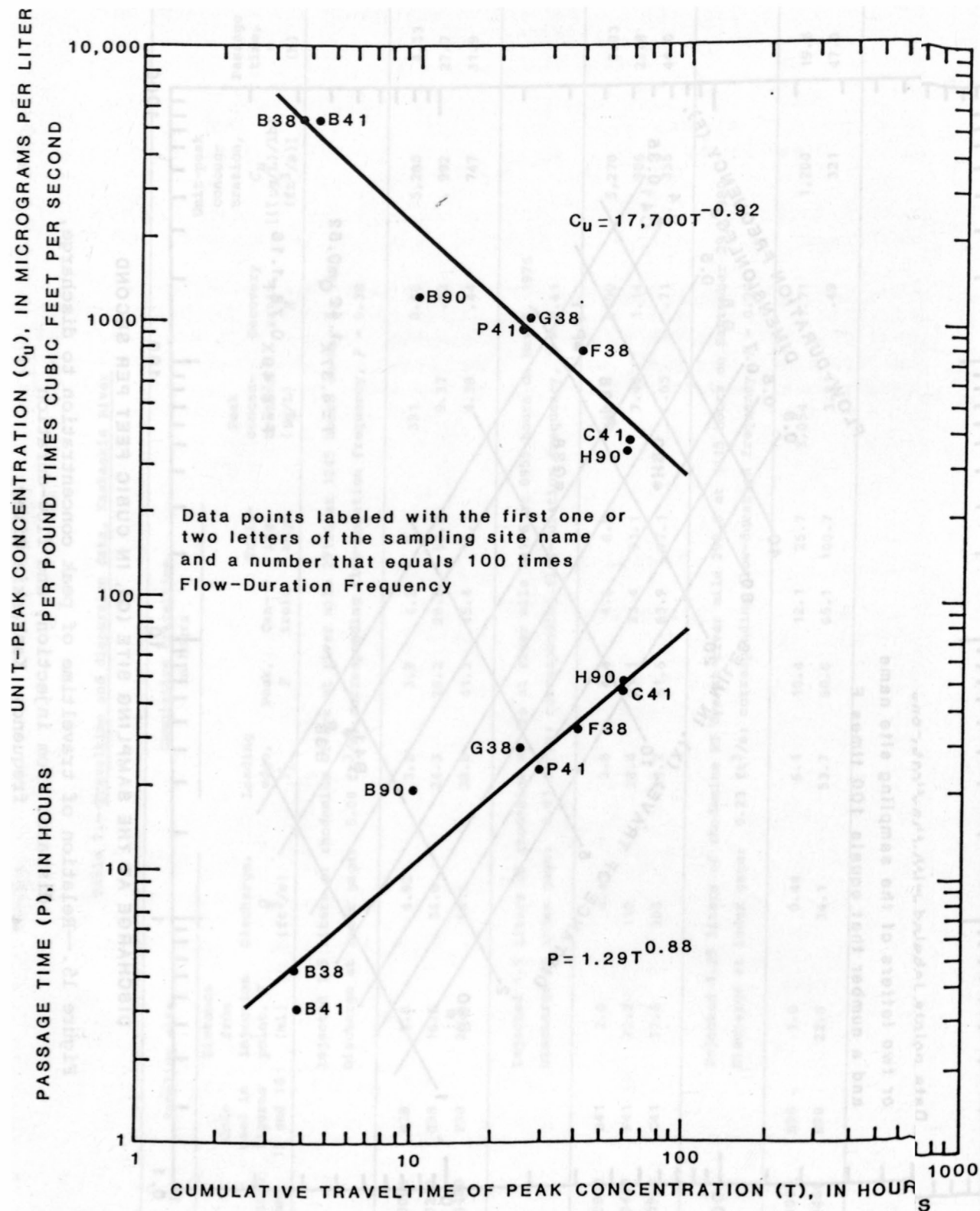


Figure 16.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration, Kaskaskia River.



## Mackinaw River

In the reach measured, the Mackinaw River (figs. 1 and 17) has a wide meandering channel with low banks. The bed is composed of sand with some gravel that forms large sand bars at bends. Debris and logjams were observed at several places along the channel. The drainage basin is rural and partially wooded. The index gage, near Congerville (table 1 and figs. 1 and 17), is 17.6 miles above the site used for injection for all measurements. Channel slope from injection to the sampling site below Green Valley is 3.22 ft/mi. Slope is slightly lower upstream, and is 2.69 ft/mi in the reach between injection and the sampling site near Tremont.

Traveltime measurements were made at discharges at the index gage of 471, 374, and 31.5 ft<sup>3</sup>/s, corresponding to flow-duration frequencies of 0.29, 0.34, and 0.75, respectively. A very great difference was observed in flow characteristics between the measurement made at low flow and the two measurements at higher flow (table 8). During the measurement at lowest flow, short riffle sections were separated by long, deep pools in which flow was barely detectable. Flow was turbulent and uniform along the channel during the other two measurements. At the flow corresponding to a flow-duration frequency of 0.34, eddies and areas of lower velocity were present on the downstream sides of point bars. Some of these bars were exposed during the highest flow measurement, but areas of eddies and lower velocity flow were reduced from those at the lower flow. Considerable shifting of the channel bed and debris jams took place between measurements. Because of the comparatively long traveltime during the 0.75-flow-duration frequency measurement, the reach measured is very short (5.2 miles).

A rainstorm during the measurement at the highest flow caused a discharge peak which passed through the channel as the dye moved through the measured reach. Peak discharge was 20 percent above the prestorm discharge at the downstream measuring site. The discharge peak passed that site at about the same time as the peak dye concentration. Discharge decreased with time in the measured reach during the measurement begun on September 9, 1981 (table 8). The change in discharge at the index gage during the traveltime measurement was about 14 percent. Discharge decreased during much of the measurement at lowest flow, but a small rainstorm caused a rise in stage toward the end of the measurement. A difference of 26 percent was found between the highest and lowest discharges.

Estimated mixing distances for measurements at the two higher flow conditions (table 2) are longer than the distance between the injection and the first sampling site. For those measurements, dye was injected as two slugs to shorten the distance for transverse mixing.

The traveltime of the peak relations developed from the measurements are given in figure 18. Computed lines of equal flow-duration frequency and distance of travel fit the data points fairly well (table 13) except for the measurements at Green Valley. The unsteadiness of flow during both those measurements may be the cause of the lack of agreement of those points. Regression relations developed from the measured values allow estimation of traveltime for flow-duration frequencies from 0.30 to 0.80 and for distances up to 30 miles.

The equations developed for traveltime of the leading edge are

$$T_L = 36.7 X^{1.06} Q^{-0.62} \quad (14)$$

and

$$T_L = 7.03 X^{1.00} P^{1.85} \quad (15)$$

For both traveltime of the peak and traveltime of the leading edge, the equations that use flow-duration frequency have lower standard errors than those that use discharge at the sampling site (table 13).

Both unit-peak concentration and passage time are strongly dependent on flow condition in the Mackinaw River (fig. 19). Because of that dependence, regression relations that include flow-duration frequency were developed, and equations used to compute the lines of equal flow-duration frequency shown in figure 19.

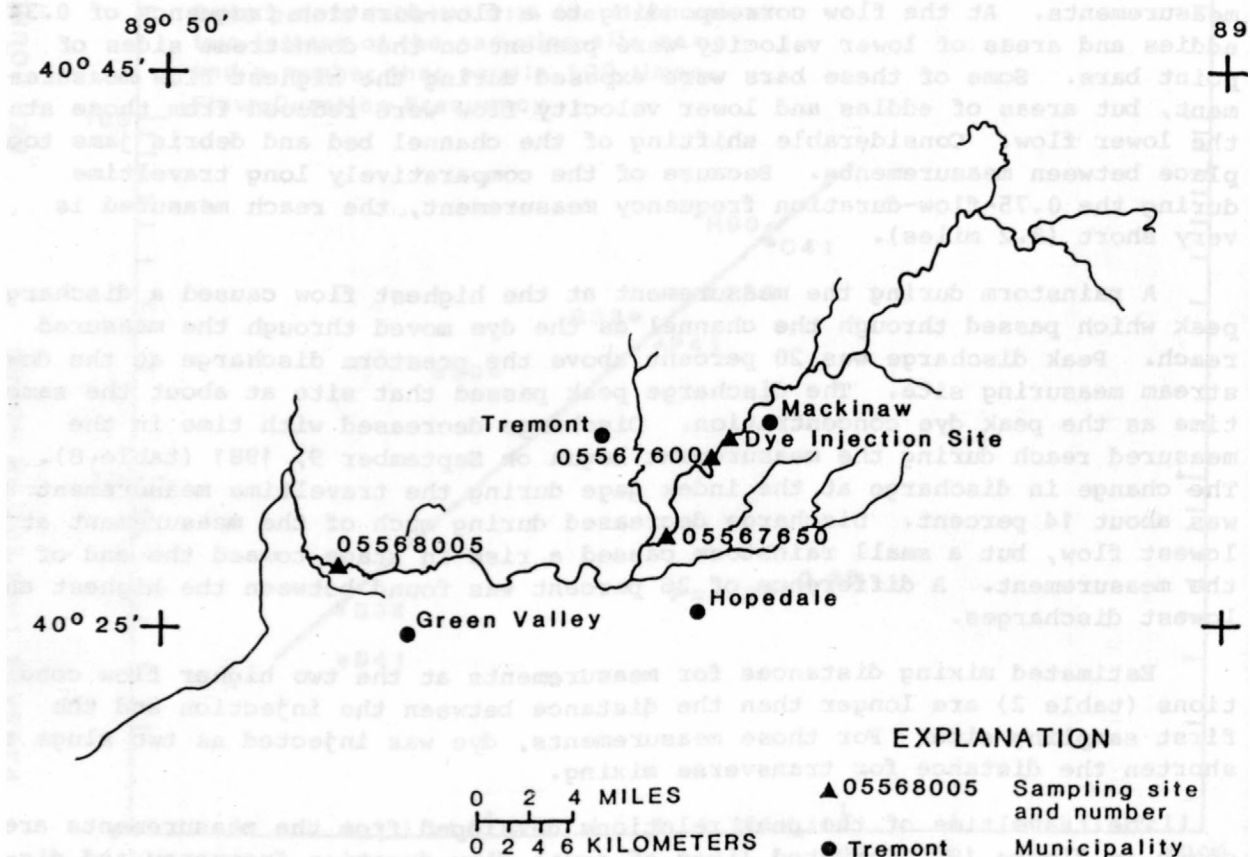


Figure 17.--Location of injection and sampling sites, Mackinaw River.

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ ] ( $\text{ft}^3/\text{s}$ )]	Passage time, $P$ (h)
Station number	Code used in figures 18 and 19	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 12.0 liters of rhodamine WT dye at river mile 41.1 at 1420 hours on June 8, 1981											
Discharge at index gage: 471 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.29$											
05567600	M29	1.2	571	0.9	1.1	1.3	2.3	132	1.12	10,600	1.37
05568005	G29	31.0	1,150	22.2	23.7	24.1	27.8	9.20	.69	2,430	5.62
Injected 9.0 liters of rhodamine WT dye at river mile 41.1 at 1020 hours on September 9, 1981											
Discharge at index gage: 374 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.34$											
05567600	M34	1.2	391	1.0	1.4	1.5	2.9	70.9	0.81	7,290	1.93
05568005	G34	31.0	378	28.8	32.7	33.2	40.9	6.66	.50	1,060	12.1
Injected 2.5 liters of rhodamine WT dye at river mile 41.1 at 1135 hours on August 11, 1980											
Discharge at index gage: 31.5 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.75$											
05567600	M75	1.2	36.5	5.4	7.8	11.0	25.8	24.3	0.80	847	20.3
05567650	T75	6.4	46.1	24.4	29.0	31.3	56.2	7.73	.59	459	31.7

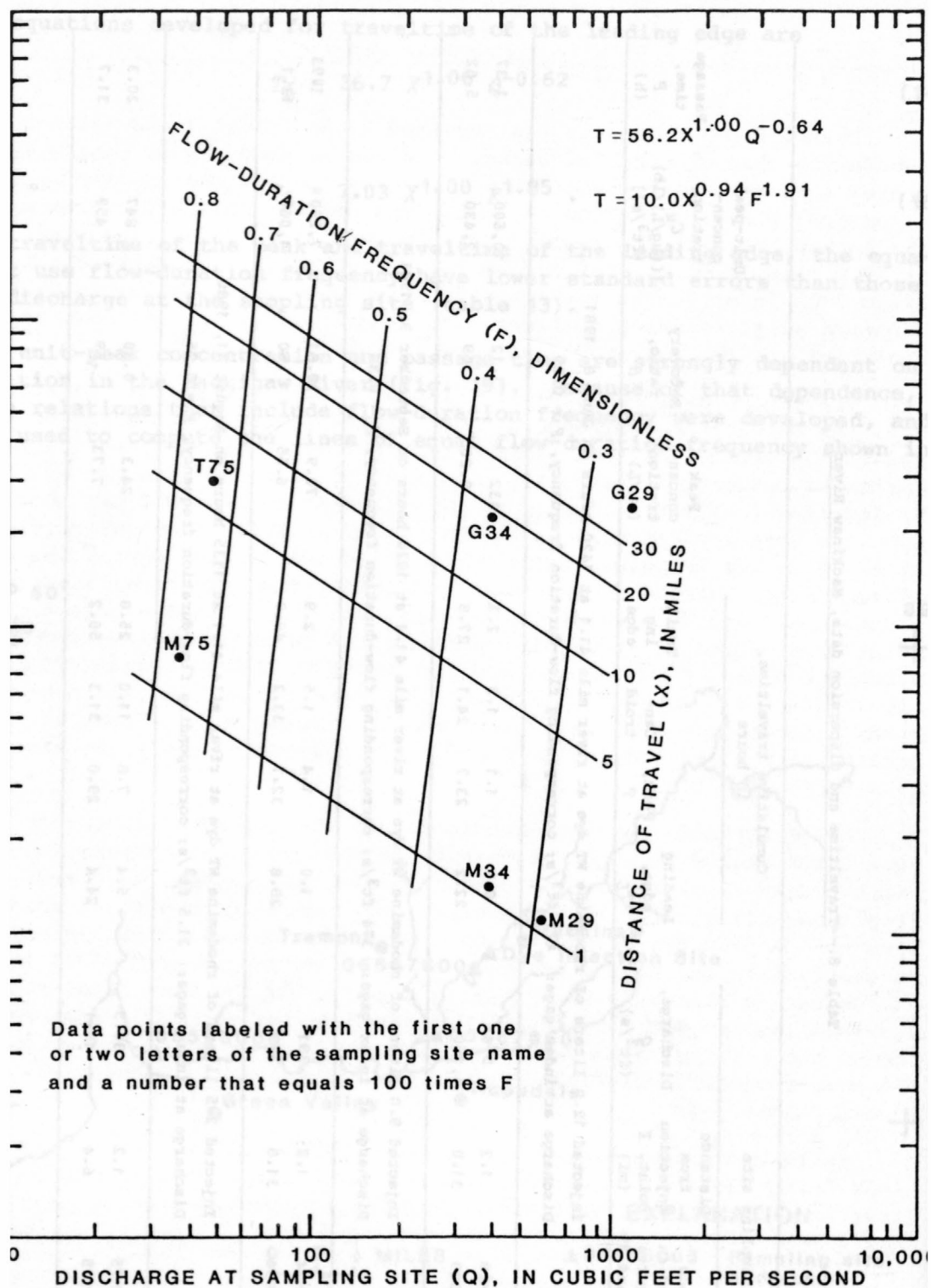


Figure 18.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Mackinaw River.



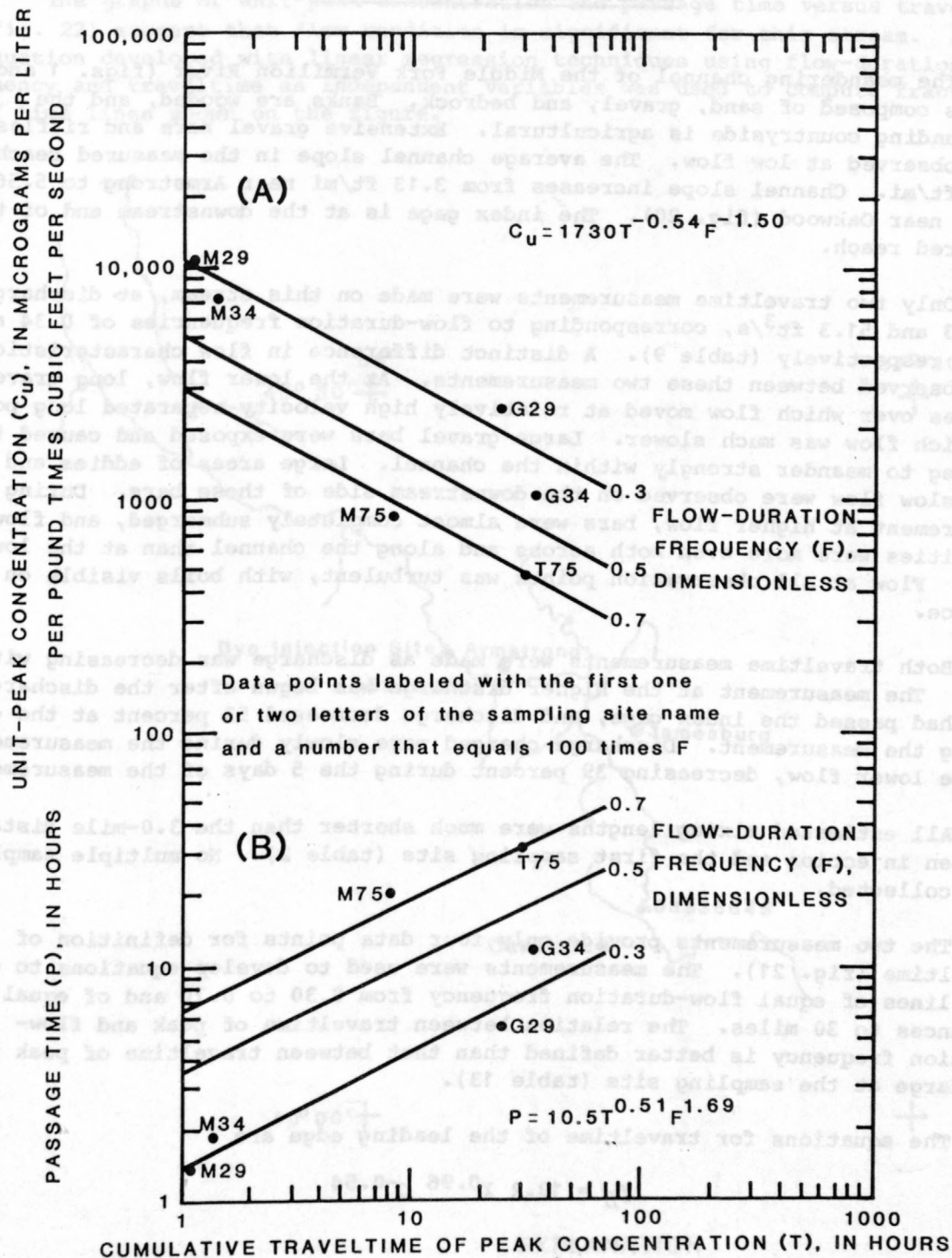


Figure 19.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration and flow-duration frequency, Mackinaw River.

## Middle Fork Vermilion River

The meandering channel of the Middle Fork Vermilion River (figs. 1 and 20) is composed of sand, gravel, and bedrock. Banks are wooded, and the surrounding countryside is agricultural. Extensive gravel bars and riffles were observed at low flow. The average channel slope in the measured reach is 4.07 ft/mi. Channel slope increases from 3.13 ft/mi near Armstrong to 5.56 ft/mi near Oakwood (fig. 20). The index gage is at the downstream end of the measured reach.

Only two traveltime measurements were made on this stream, at discharges of 263 and 51.3 ft<sup>3</sup>/s, corresponding to flow-duration frequencies of 0.34 and 0.65, respectively (table 9). A distinct difference in flow characteristics was observed between these two measurements. At the lower flow, long gravel riffles over which flow moved at relatively high velocity separated long pools in which flow was much slower. Large gravel bars were exposed and caused the thalweg to meander strongly within the channel. Large areas of eddies and very slow flow were observed on the downstream side of these bars. During the measurement at higher flow, bars were almost completely submerged, and flow velocities were more even both across and along the channel than at the lower flow. Flow at all observation points was turbulent, with boils visible on the surface.

Both traveltime measurements were made as discharge was decreasing with time. The measurement at the higher discharge was begun after the discharge peak had passed the index gage, and discharge decreased 53 percent at the gage during the measurement. Discharge changed more slowly during the measurement at the lower flow, decreasing 39 percent during the 5 days of the measurement.

All estimated mixing lengths were much shorter than the 3.0-mile distance between injection and the first sampling site (table 2). No multiple samples were collected.

The two measurements provide only four data points for definition of traveltime (fig. 21). The measurements were used to develop equations to compute lines of equal flow-duration frequency from 0.30 to 0.70 and of equal distances to 30 miles. The relation between traveltime of peak and flow-duration frequency is better defined than that between traveltime of peak and discharge at the sampling site (table 13).

The equations for traveltime of the leading edge are

$$T_L = 19.2 X^{0.96} Q^{-0.54} \quad (16)$$

and

$$T_L = 4.03 X^{1.00} F^{1.39} \quad (17)$$

The standard errors of estimate of these two equations are nearly equal and relatively low (table 13).

The graphs of unit-peak concentration and passage time versus traveltime (fig. 22) suggest that flow condition is significant for this stream. An equation developed with linear regression techniques using flow-duration frequency and traveltime as independent variables was used to compute fractions of time lines shown on the figure.

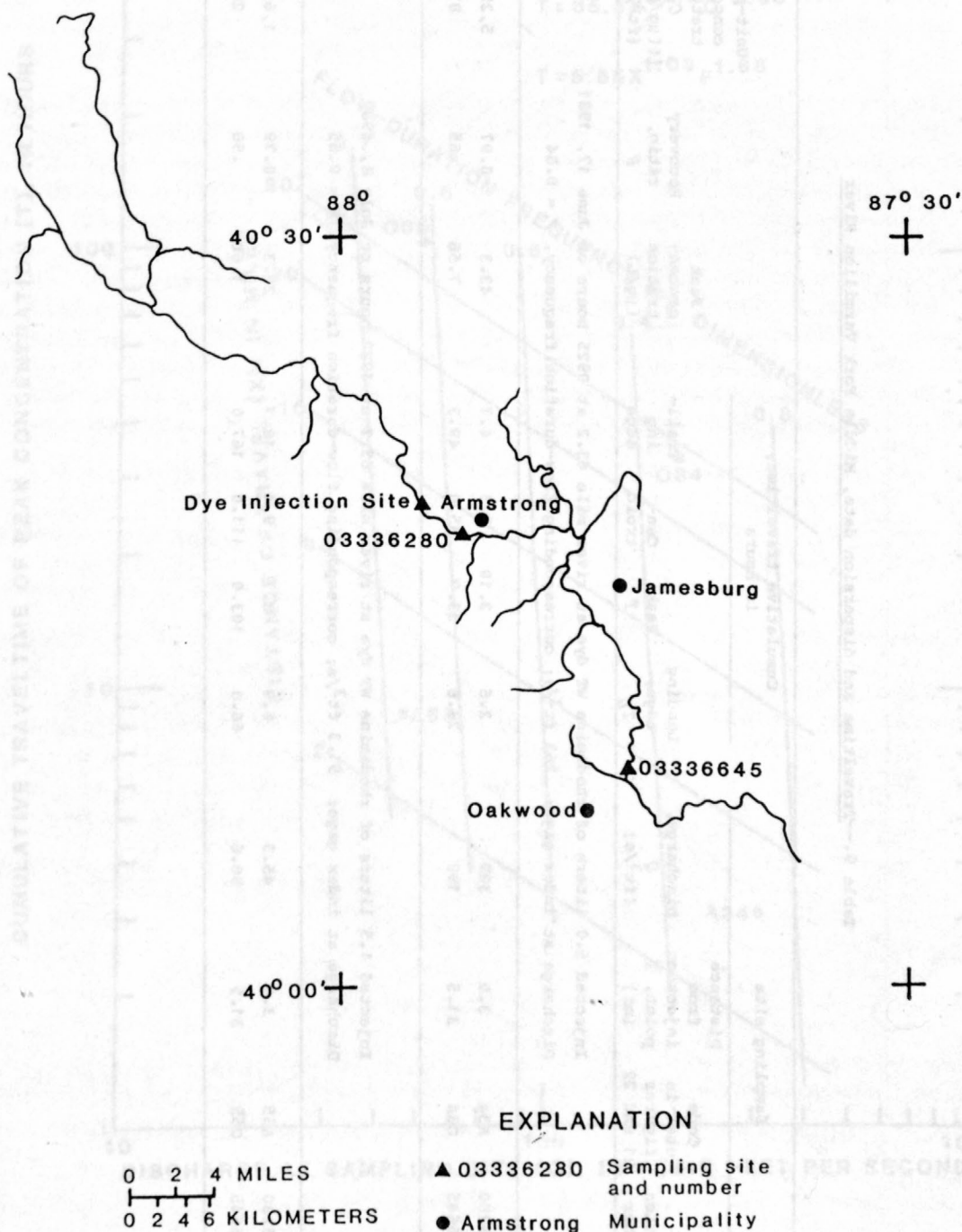


Figure 20.--Location of injection and sampling sites, Middle Fork Vermilion River.

Table 9.--Traveltime and dispersion data, Middle Fork Vermilion River

Sampling site			Cumulative traveltime, in hours					Peak concen- tration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concen- tration, $C_u$ [[ $(\mu\text{g/L})/\text{lb}$ ] $(\text{ft}^3/\text{s})$ ]	Passag time, $P$ (h)
Station number	Code used in figures 21 and 22	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Cen- troid	Trail- ing edge				
Injected 5.0 liters of rhodamine WT dye at river mile 63.2 at 0925 hours on June 17, 1981											
Discharge at index gage: 263 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.34$											
03336280	A34	3.0	309	2.6	3.10	3.3	4.7	43.3	0.97	5,250	2.12
03336645	O34	31.5	198	29.6	33.9	35.0	49.3	7.56	.65	874	19.7
Injected 1.5 liters of rhodamine WT dye at river mile 63.2 at 1020 hours on July 8, 1980											
Discharge at index gage: 51.3 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.65$											
03336280	A65	3.0	45.3	6.9	8.7	9.4	18.7	22.3	0.79	1,630	11.8
03336645	O65	31.5	50.6	66.8	103.0	111.0	167.0	1.60	.50	205	100.2



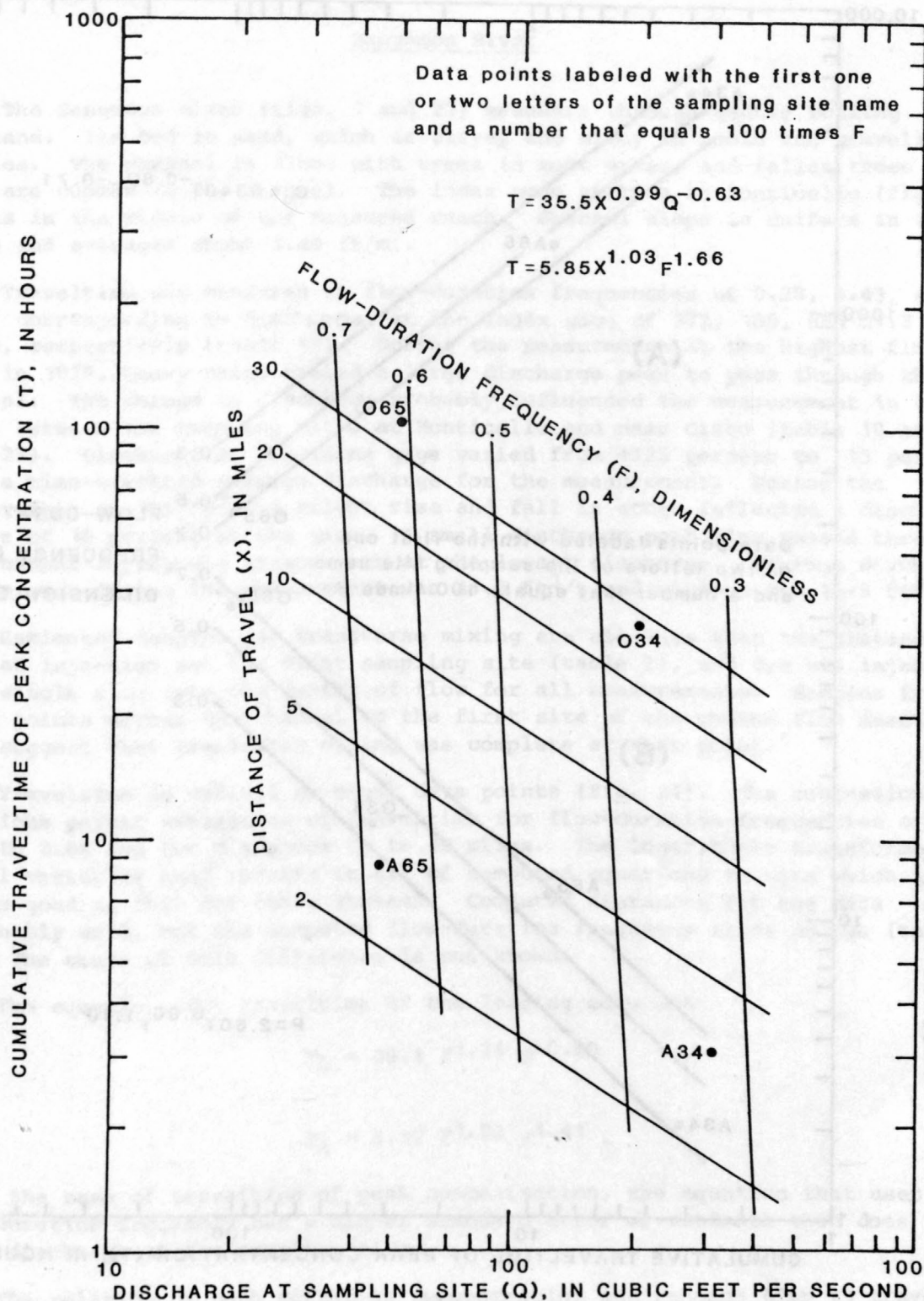


Figure 21.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Middle Fork Vermilion River.

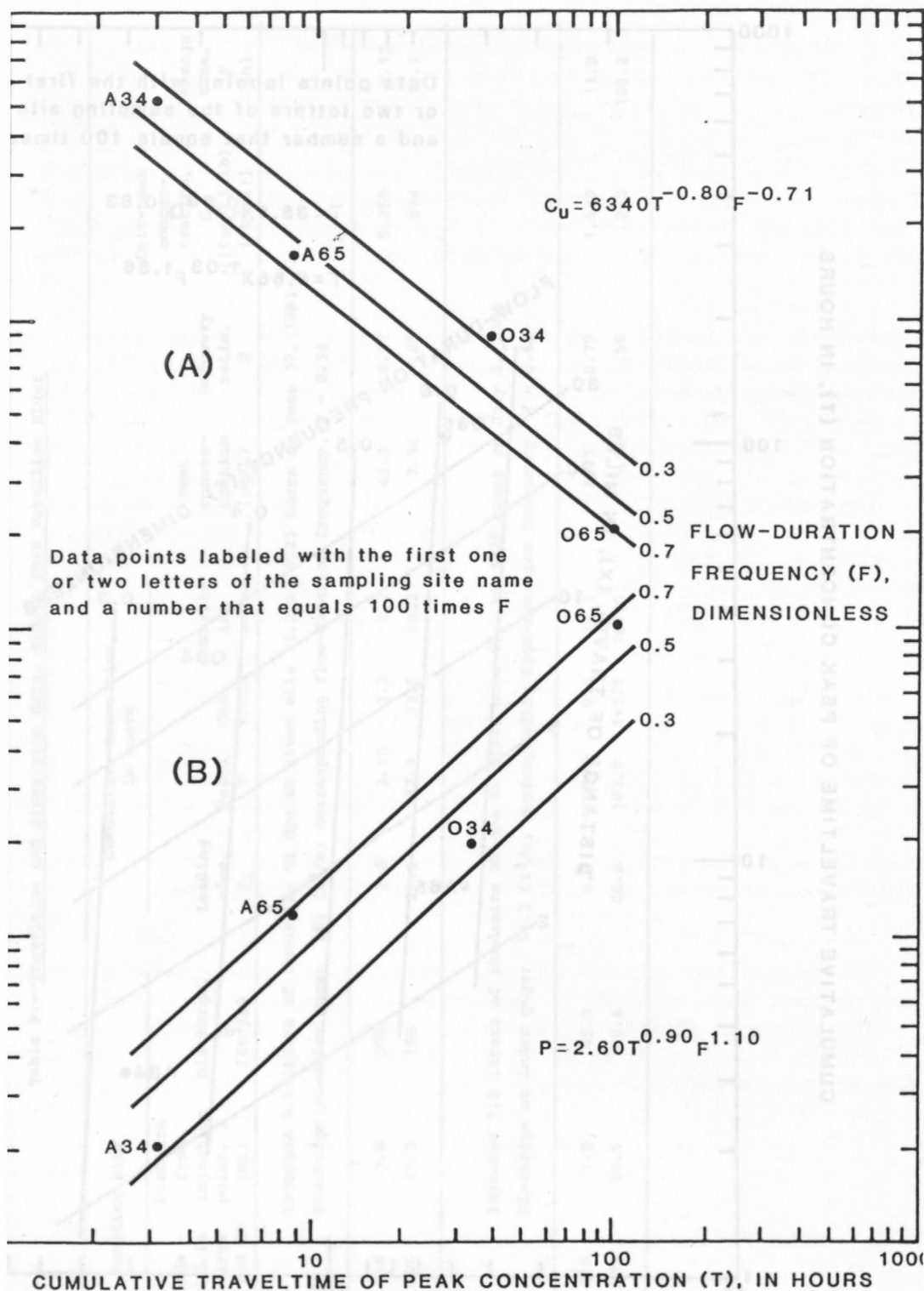


Figure 22.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration and flow-duration frequency, Middle Fork Vermilion River.

## Sangamon River

The Sangamon River (figs. 1 and 23) meanders through gently rolling farmland. Its bed is sand, which is clayey and silty in pools and gravelly at riffles. The channel is lined with trees in most areas, and fallen trees and logs are common in the channel. The index gage station at Monticello (fig. 23) is in the middle of the measured reach. Channel slope is uniform in the reach and averages about 1.40 ft/mi.

Traveltime was measured at flow-duration frequencies of 0.28, 0.43, and 0.76, corresponding to discharges at the index gage of 372, 185, and 27.3 ft<sup>3</sup>/s, respectively (table 10). During the measurement at the highest flow, made in 1975, heavy rains caused a large discharge peak to pass through the channel. The change in discharge probably influenced the measurement in the reach between the sampling sites at Monticello and near Cisco (table 10 and fig. 23). Discharge at the index gage varied from +125 percent to -43 percent of the time-weighted average discharge for the measurement. During the measurement at 185 ft<sup>3</sup>/s a slight rise and fall in stage reflected a discharge change of 16 percent at the gage. A small discharge peak also passed through the channel during the measurement at the lowest discharge. Maximum discharge at the gage during the measurement was 41.5 ft<sup>3</sup>/s and minimum was 16.5 ft<sup>3</sup>/s.

Estimated lengths for transverse mixing are all less than the distance between injection and the first sampling site (table 2), and dye was injected as a single slug into the center of flow for all measurements. Samples from three points across the channel at the first site of the medium flow measurement suggest that transverse mixing was complete at that point.

Traveltime is defined by eight data points (fig. 24). The regression equations permit estimation of traveltime for flow-duration frequencies of 0.30 to 0.80 and for distances up to 40 miles. The logarithmic transformation of all variables used results in fit of computed equations to data which is not as good as that for other streams. Computed distances fit the data reasonably well, but the computed flow-duration frequency lines do not (table 13). The cause of this difference is not known.

The equations for traveltime of the leading edge are

$$T_L = 30.1 X^{1.24} Q^{-0.69} \quad (18)$$

and

$$T_L = 6.37 X^{1.03} F^{1.41} \quad (19)$$

As in the case of traveltime of peak concentration, the equation that uses flow-duration frequency has a higher standard error of estimate than does that using discharge at the sampling site.

The relation of both unit-peak concentration and passage time to traveltime for the Sangamon River (fig. 25) is strongly dependent on flow condition, and lines of equal flow-duration frequency are shown in the figure to aid in interpolation.

Dashed lines labeled "example in test" are used in the "Applications" section to illustrate the use of the graphs presented.

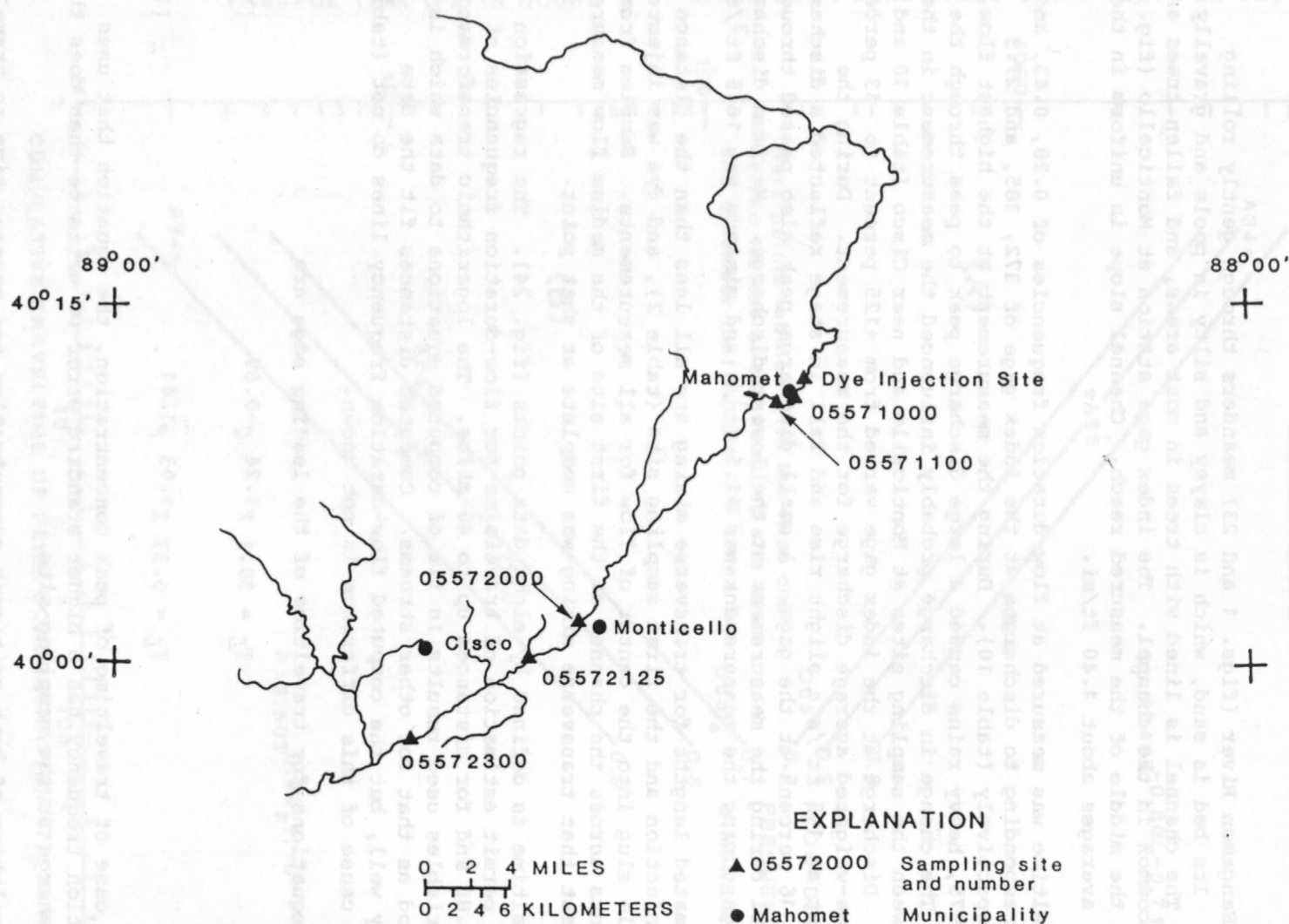


Figure 23.--Location of injection and sampling sites, Sangamon River.



Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ ] ( $\text{ft}^3/\text{s}$ )]]	Passage time, $P$ (h)
Station number	Code used in figures 24 and 25	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 2.5 liters of rhodamine WT dye at river mile 187.6 at 0930 hours on June 23, 1975											
Discharge at index gage: 372 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.28$											
05571000	M28	1.9	122	2.2	2.6	2.8	4.6	44.0	0.80	5,090	2.40
05572000	MO28	25.4	275	36.4	39.3	39.7	45.9	3.20	.59	1,150	9.48
05572300	C28	37.6	293	55.1	58.2	58.4	63.3	1.50	.28	1,210	8.23
Injected 8.0 liters of rhodamine WT dye at river mile 187.6 at 1305 hours on May 13, 1980											
Discharge at index gage: 185 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.43$											
05571100	MA43	3.2	126	3.9	5.1	5.4	8.2	62.2	0.57	3,290	4.32
05572000	MO43	25.4	200	44.4	49.0	52.6	67.4	7.84	.46	810	23.0
05572300	C43	37.6	236	68.8	74.4	74.7	88.1	5.09	.40	710	19.2
Injected 2.0 liters of rhodamine WT dye at river mile 187.6 at 1145 hours on September 15, 1980											
Discharge at index gage: 27.3 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.76$											
05571100	MA76	3.2	19.4	21.6	27.1	28.4	44.7	52.9	1.81	540	23.2
05572125	A76	29.6	32.6	139.0	150.0	157.0	193.9	3.18	.41	240	54.9

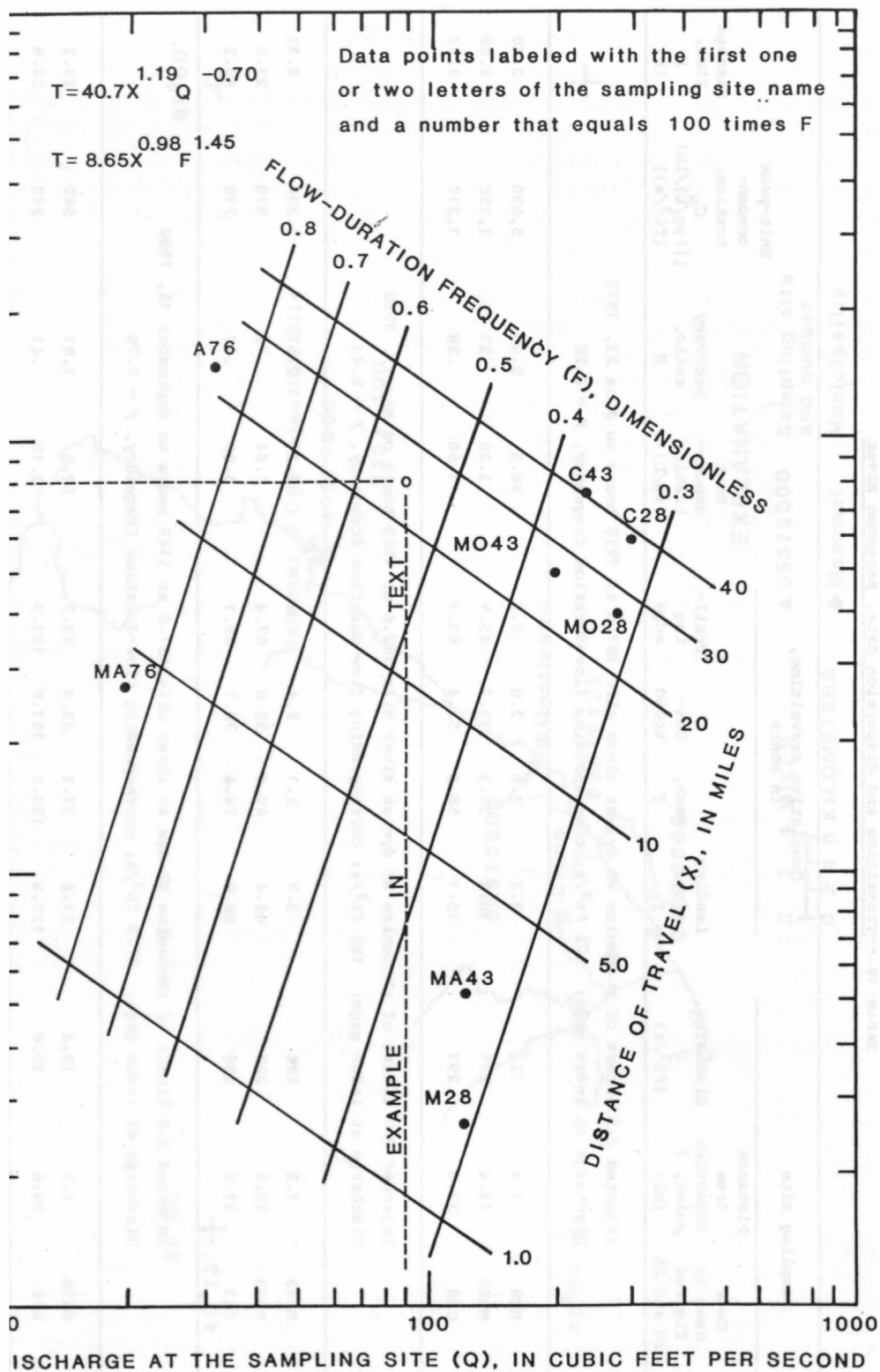


Figure 24.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Sangamon River.

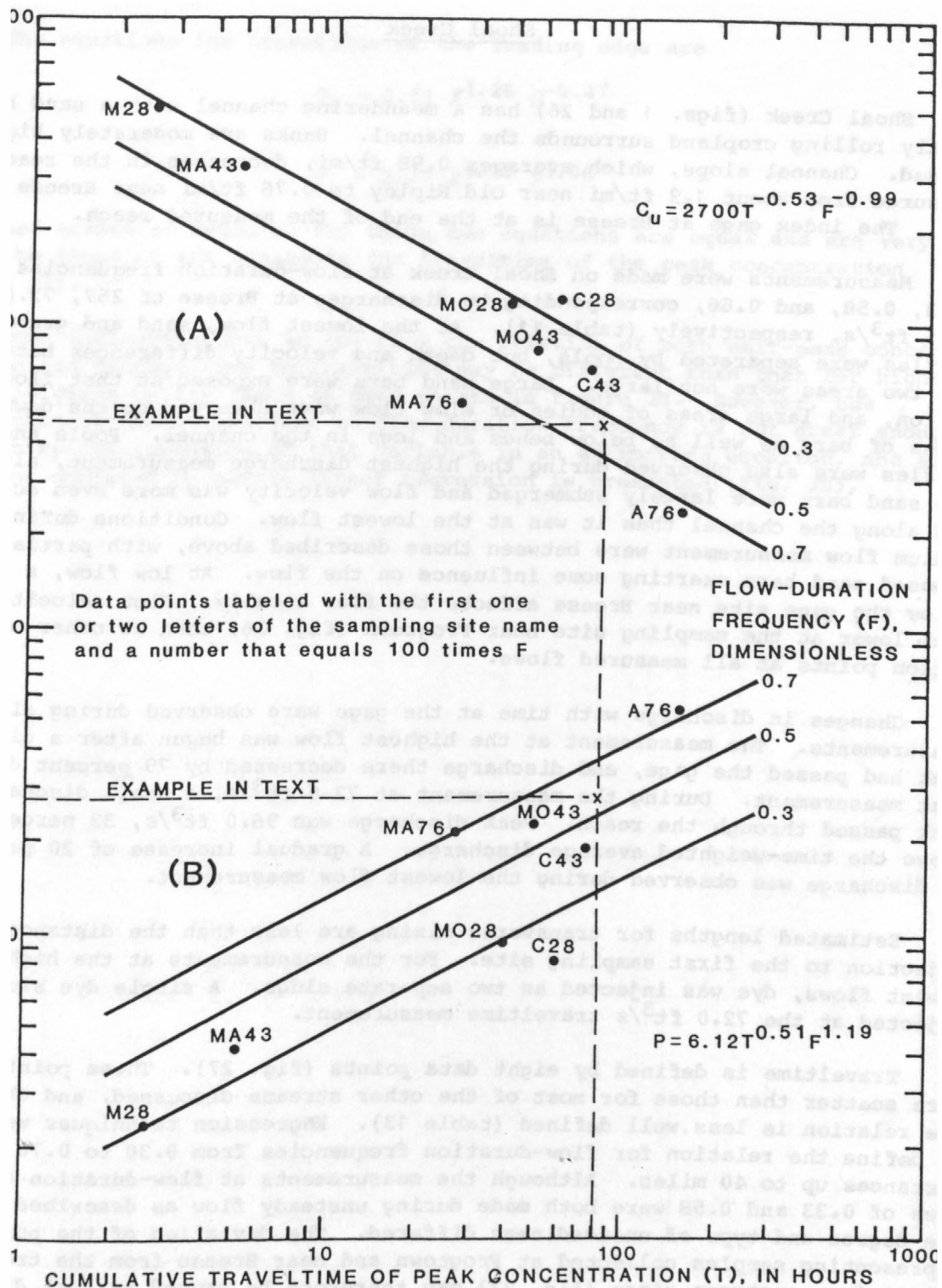


Figure 25.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration and flow-duration frequency, Sangamon River.

## Shoal Creek

Shoal Creek (figs. 1 and 26) has a meandering channel with a sand bed. Gently rolling cropland surrounds the channel. Banks are moderately high and wooded. Channel slope, which averages 0.98 ft/mi, decreases in the reach measured from about 1.9 ft/mi near Old Ripley to 0.76 ft/mi near Breese (fig. 26). The index gage at Breese is at the end of the measured reach.

Measurements were made on Shoal Creek at flow-duration frequencies of 0.33, 0.58, and 0.66, corresponding to discharges at Breese of 257, 72.0, and 49.5 ft<sup>3</sup>/s, respectively (table 11). At the lowest flow, sand and gravel riffles were separated by pools, but depth and velocity differences between the two areas were not large. Large sand bars were exposed at that flow condition, and large areas of eddies or slow flow were observed on the downstream sides of bars as well as below bends and logs in the channel. Pools and riffles were also observed during the highest discharge measurement, although the sand bars were largely submerged and flow velocity was more even across and along the channel than it was at the lowest flow. Conditions during the medium flow measurement were between those described above, with partially exposed sand bars exerting some influence on the flow. At low flow, a riffle below the gage site near Breese affects the flow locally. Flow velocity was much lower at the sampling site near Frogtown (fig. 26) than at other observation points at all measured flows.

Changes in discharge with time at the gage were observed during all three measurements. The measurement at the highest flow was begun after a discharge peak had passed the gage, and discharge there decreased by 79 percent during that measurement. During the measurement at 72.0 ft<sup>3</sup>/s, a small discharge peak passed through the reach. Peak discharge was 96.0 ft<sup>3</sup>/s, 33 percent above the time-weighted average discharge. A gradual increase of 20 percent in discharge was observed during the lowest flow measurement.

Estimated lengths for transverse mixing are less than the distance from injection to the first sampling site. For the measurements at the highest and lowest flows, dye was injected as two separate slugs. A single dye slug was injected at the 72.0 ft<sup>3</sup>/s traveltime measurement.

Traveltime is defined by eight data points (fig. 27). These points show more scatter than those for most of the other streams discussed, and therefore the relation is less well defined (table 13). Regression techniques were used to define the relation for flow-duration frequencies from 0.30 to 0.70 and for distances up to 40 miles. Although the measurements at flow-duration frequencies of 0.33 and 0.58 were both made during unsteady flow as described above, the degree and type of unsteadiness differed. The deviation of the points representing samples collected at Frogtown and near Breese from the trends of points from upstream sites (fig. 27) may therefore be caused by real differences in the character of flow in those reaches and not by unsteady flow.



The equations for traveltime of the leading edge are

$$T_L = 8.11 X^{1.26} Q^{-0.47} \quad (20)$$

and

$$T_L = 2.47 X^{1.20} F^{1.06} . \quad (21)$$

Standard errors of estimate for these two equations are equal and are very close to those of the equations for traveltime of the peak concentration (table 13).

Some indication that at low flow the relation of both unit-peak concentration and passage time to traveltime may be different than that for higher flows is given by the trend of data points in figure 28. However, the dependence of those relations on flow-duration frequency is not great enough to justify the inclusion of that variable in an estimating equation, and an equation computed by simple linear regression is presented (fig. 28).

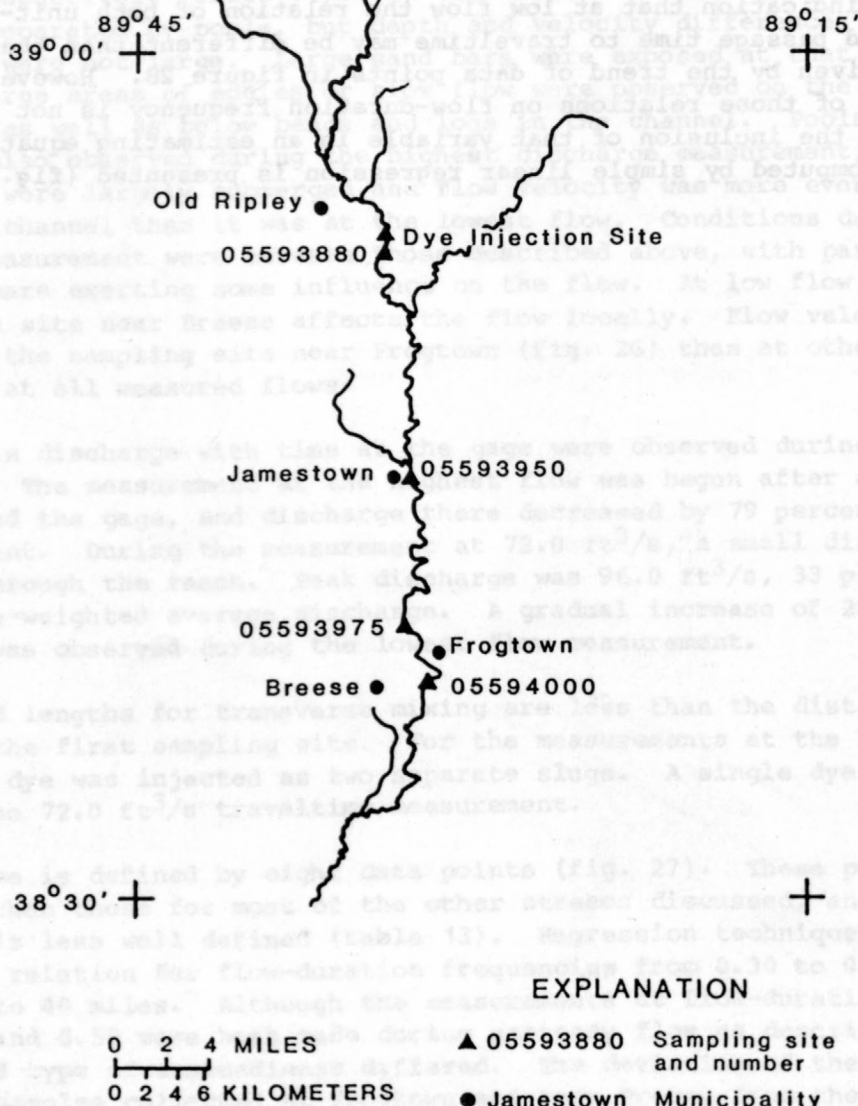


Figure 26.--Location of injection and sampling sites, Shoal Creek.

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/\text{lb}$ ] ( $\text{ft}^3/\text{s}$ )]]	Passage time, $P$ (h)
Station number	Code used in figures 27 and 28	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Cen- troid	Trail- ing edge				
Injected 8.0 liters of rhodamine WT dye at river mile 56.7 at 1008 hours on August 18, 1981											
Discharge at index gage: 257 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.33$											
05593880	R33	1.7	196	1.5	1.6	1.9	2.7	185	0.84	10,300	1.27
05593950	J33	18.5	209	24.2	26.6	27.2	32.2	27.4	.83	1,650	8.05
05594000	B33	35.4	133	59.1	63.8	66.1	80.1	13.1	.66	626	21.0
Injected 3.0 liters of rhodamine WT dye at river mile 56.7 at 1300 hours on April 14, 1981											
Discharge at index gage: 72.0 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.58$											
05593880	R58	1.7	42.3	2.2	2.7	2.9	4.4	169	0.79	5,780	2.25
05593950	J58	18.5	89.5	40.8	44.3	44.9	51.6	12.1	.60	1,150	10.9
05593975	F58	30.3	74.1	73.1	79.0	81.4	101.7	7.37	.64	542	28.6
Injected 2.0 liters of rhodamine WT dye at river mile 56.7 at 1025 hours on November 17, 1981											
Discharge at index gage: 49.5 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.66$											
05593880	R66	1.7	25.1	3.4	4.6	4.0	8.5	95.7	0.84	2,720	5.07
05593950	J66	18.5	44.4	67.6	73.9	77.5	103.0	8.07	.71	478	35.3

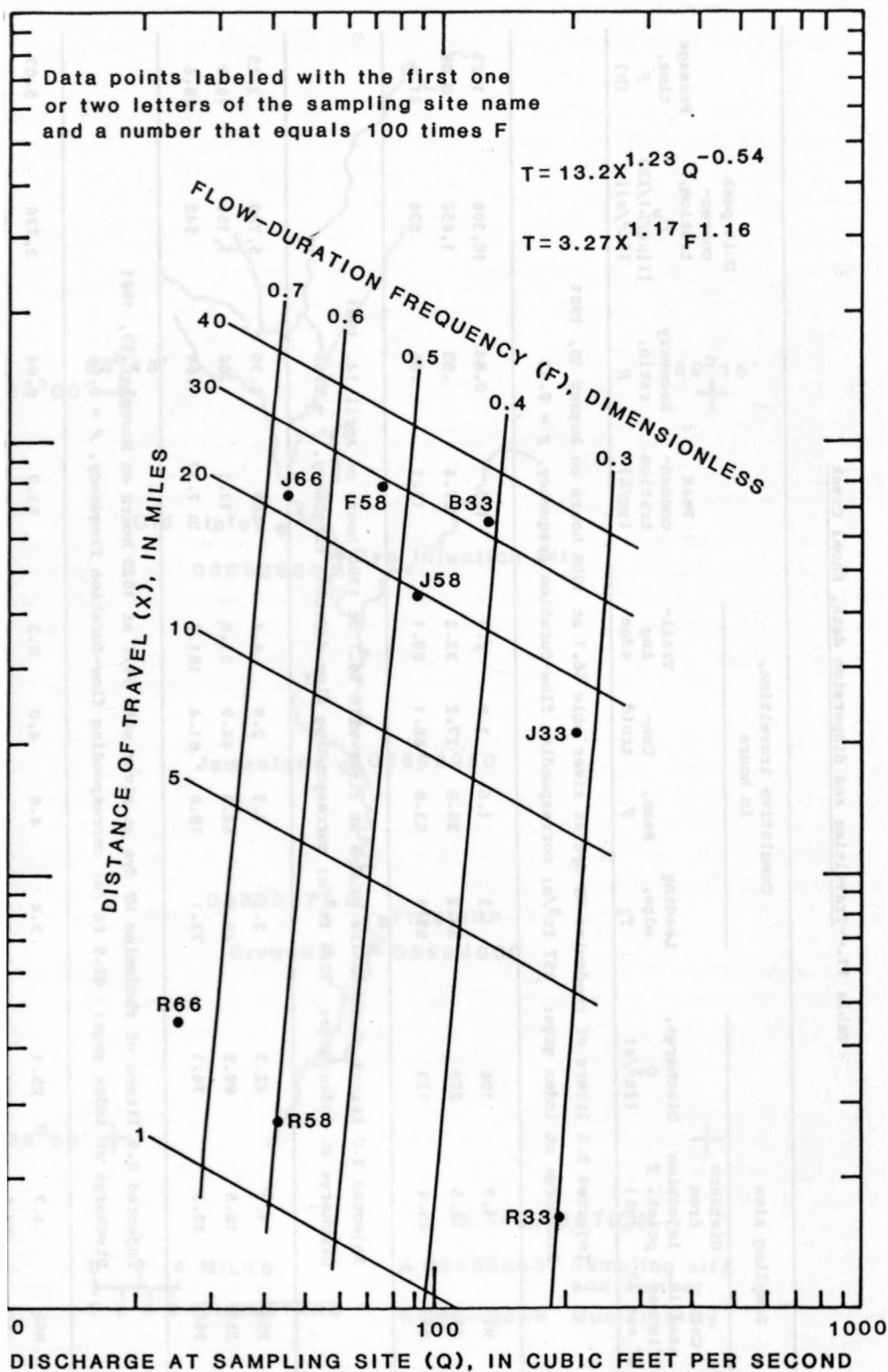


Figure 27.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Shoal Creek.



UNIT-PEAK CONCENTRATION ( $C_u$ ), IN MICROGRAMS PER  
LITER PER POUND TIMES CUBIC FEET PER SECOND

PASSAGE TIME (P), IN HOURS

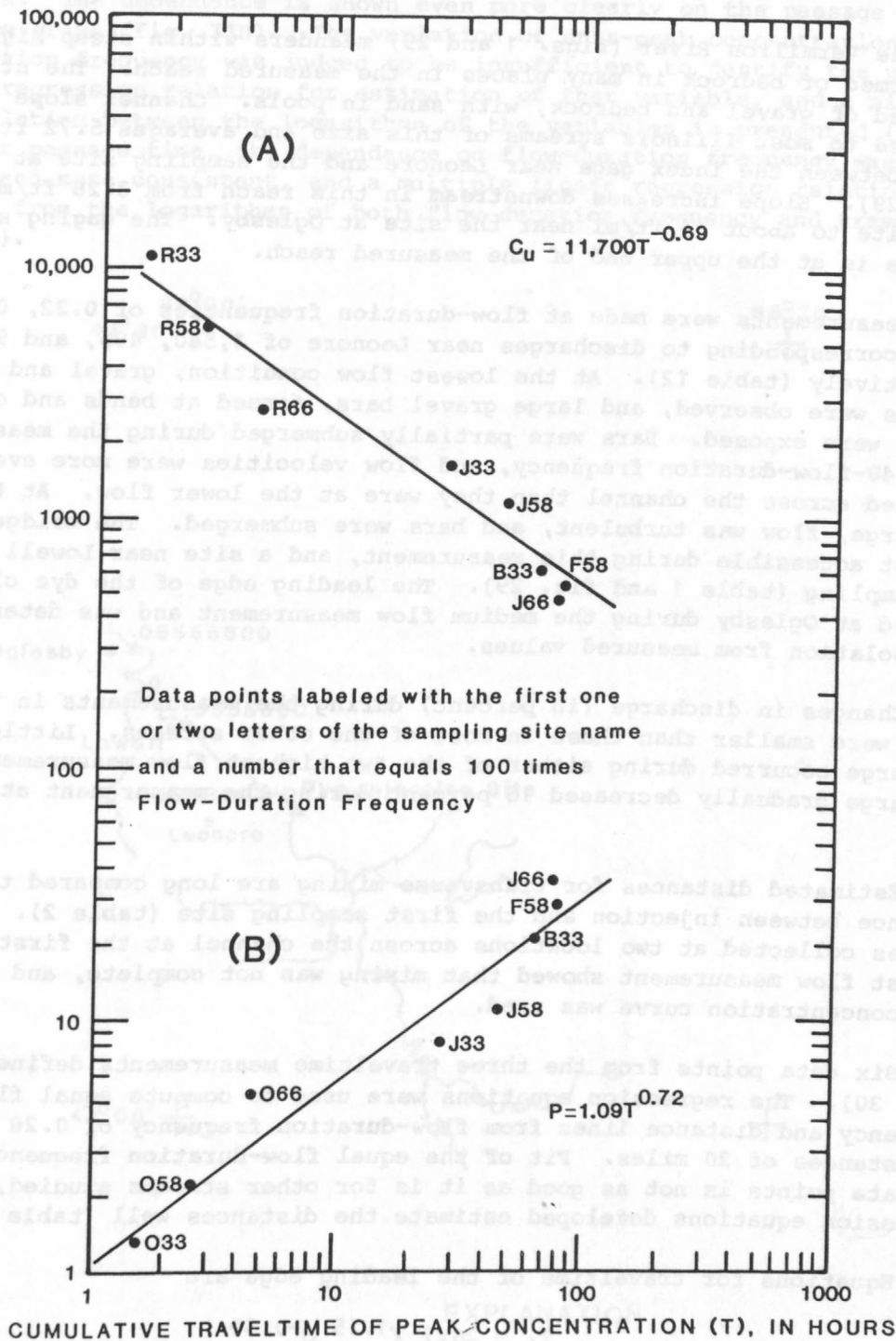


Figure 28.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration, Shoal Creek.

## Vermilion River

The Vermilion River (figs. 1 and 29) meanders within steep high banks that are formed of bedrock in many places in the measured reach. The streambed is composed of gravel and bedrock, with sand in pools. Channel slope is steep compared to most Illinois streams of this size and averages 5.72 ft/mi in the reach between the index gage near Leonore and the sampling site at Oglesby (fig. 29). Slope increases downstream in this reach from 3.28 ft/mi at the gage site to about 11 ft/mi near the site at Oglesby. The gaging station near Leonore is at the upper end of the measured reach.

Measurements were made at flow-duration frequencies of 0.22, 0.48, and 0.76, corresponding to discharges near Leonore of 1,540, 495, and 97.0 ft<sup>3</sup>/s, respectively (table 12). At the lowest flow condition, gravel and bedrock riffles were observed, and large gravel bars, formed at bends and obstructions, were exposed. Bars were partially submerged during the measurement at the 0.48-flow-duration frequency, and flow velocities were more evenly distributed across the channel than they were at the lower flow. At the highest discharge, flow was turbulent, and bars were submerged. The bridge at Oglesby was not accessible during this measurement, and a site near Lowell was used for sampling (table 1 and fig. 29). The leading edge of the dye cloud was not sampled at Oglesby during the medium flow measurement and was determined by extrapolation from measured values.

Changes in discharge (in percent) during the measurements in the Vermilion River were smaller than those in most of the other streams. Little change in discharge occurred during either of the two highest flow measurements. Discharge gradually decreased 16 percent during the measurement at the lowest flow.

Estimated distances for transverse mixing are long compared to the distance between injection and the first sampling site (table 2). Analyses of samples collected at two locations across the channel at the first site of the highest flow measurement showed that mixing was not complete, and an average time-concentration curve was used.

Six data points from the three traveltime measurements define traveltime (fig. 30). The regression equations were used to compute equal flow-duration frequency and distance lines from flow-duration frequency of 0.20 to 0.80 and to distances of 20 miles. Fit of the equal flow-duration frequency lines to the data points is not as good as it is for other streams studied, but the regression equations developed estimate the distances well (table 13).

Equations for traveltime of the leading edge are

$$T_L = 28.7 X^{1.15} Q^{-0.59} \quad (22)$$

and

$$T_L = 2.39 X^{1.15} F^{1.29} \quad (23)$$

The standard error of estimate for equation 22 is low, but that for equation 23 is relatively high (table 13).

Some dependence of unit-peak concentration on flow condition is shown in figure 31A. The dependence is shown even more clearly on the passage time-traveltime graph (fig. 31B). The variation of unit-peak concentration with flow-duration frequency was judged to be insufficient to justify the use of a multiple regression relation for estimation of that variable, and a simple linear relation between the logarithms of the variables is presented (fig. 31A). For passage time, the dependence on flow-duration frequency was stronger and more consistent, and a multiple linear regression relation was developed from the logarithms of both flow-duration frequency and traveltime (fig. 31B).

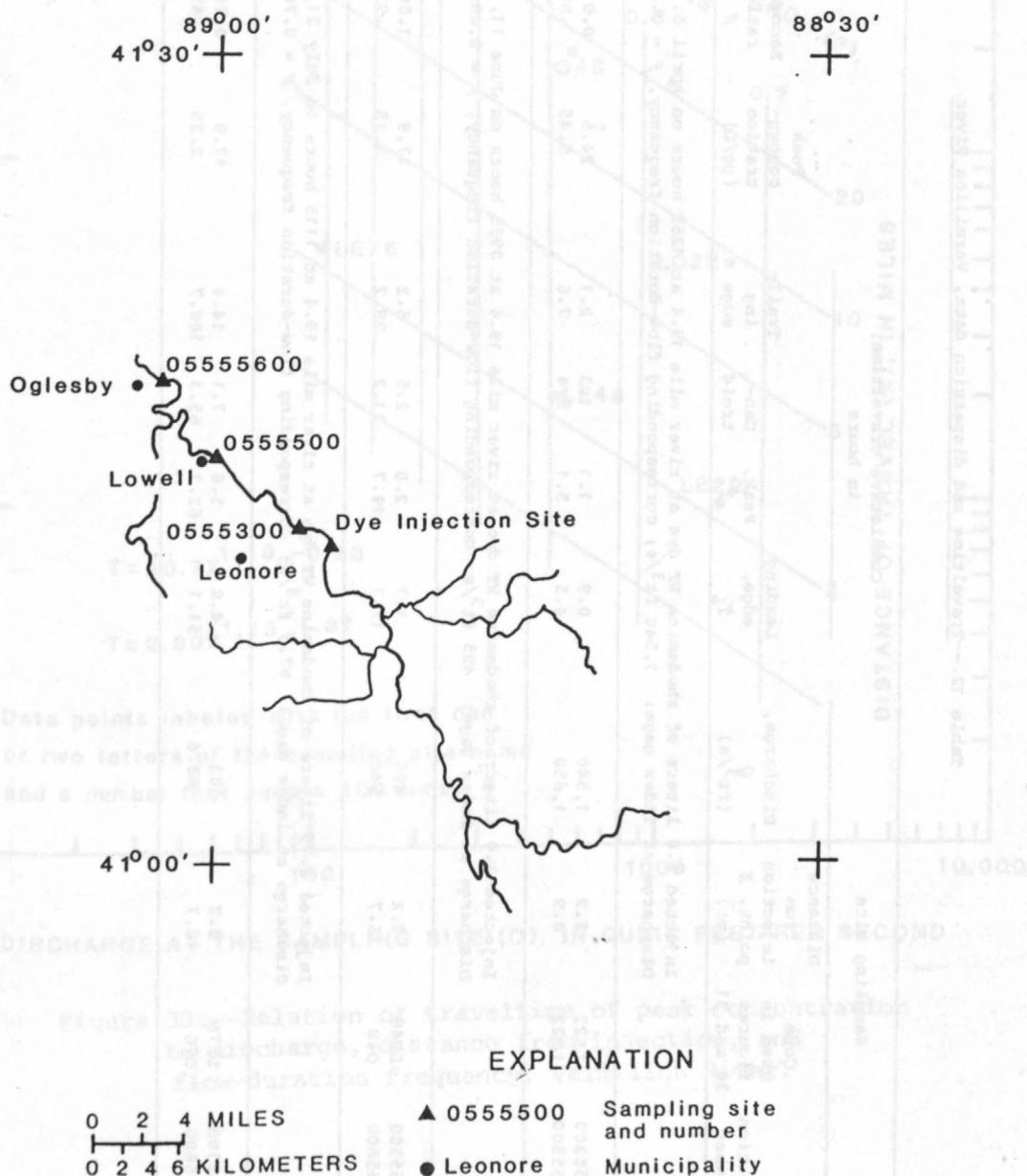


Figure 29.--Location of injection and sampling sites, Vermilion River.

Sampling site			Cumulative traveltime, in hours					Peak concentration ( $\mu\text{g/L}$ )	Recovery ratio, $R$	Unit-peak concentration, $C_u$ [[ $(\mu\text{g/L})/(\text{lb})$ $(\text{ft}^3/\text{s})$ ]]	Passage time, $P$ (h)
Station number	Code used in figures 30 and 31	Distance from injection point, $X$ (mi)	Discharge, $Q$ ( $\text{ft}^3/\text{s}$ )	Leading edge, $T_L$	Peak, $T$	Centroid	Trailing edge				
Injected 6.0 liters of rhodamine WT dye at river mile 19.4 at 1250 hours on April 6, 1982 Discharge at index gage: 1,540 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.22$											
05555300	LE22	2.2	1,540	0.9	1.1	1.3	2.1	24.5	0.91	13,200	1.22
05555500	LO22	8.9	1,650	4.5	5.1	5.4	7.6	5.45	.87	3,280	3.12
Injected 3.0 liters of rhodamine WT dye at river mile 19.4 at 0935 hours on June 11, 1981 Discharge at index gage: 495 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.48$											
05555300	LE48	2.2	495	1.7	2.0	2.5	5.2	17.9	1.06	5,320	3.48
05555600	O48	16.7	548	17.7	19.7	21.2	28.7	3.15	.97	1,130	11.0
Injected 2.75 liters of rhodamine WT dye at river mile 19.4 at 1115 hours on July 21, 1980 Discharge at index gage: 97.0 $\text{ft}^3/\text{s}$ ; corresponding flow-duration frequency, $F = 0.76$											
05555300	LE76	2.2	103	4.8	5.6	7.1	14.4	17.9	0.76	1,680	9.62
05555600	O76	16.7	83.6	51.1	62.3	65.3	100.7	2.35	.49	277	49.6



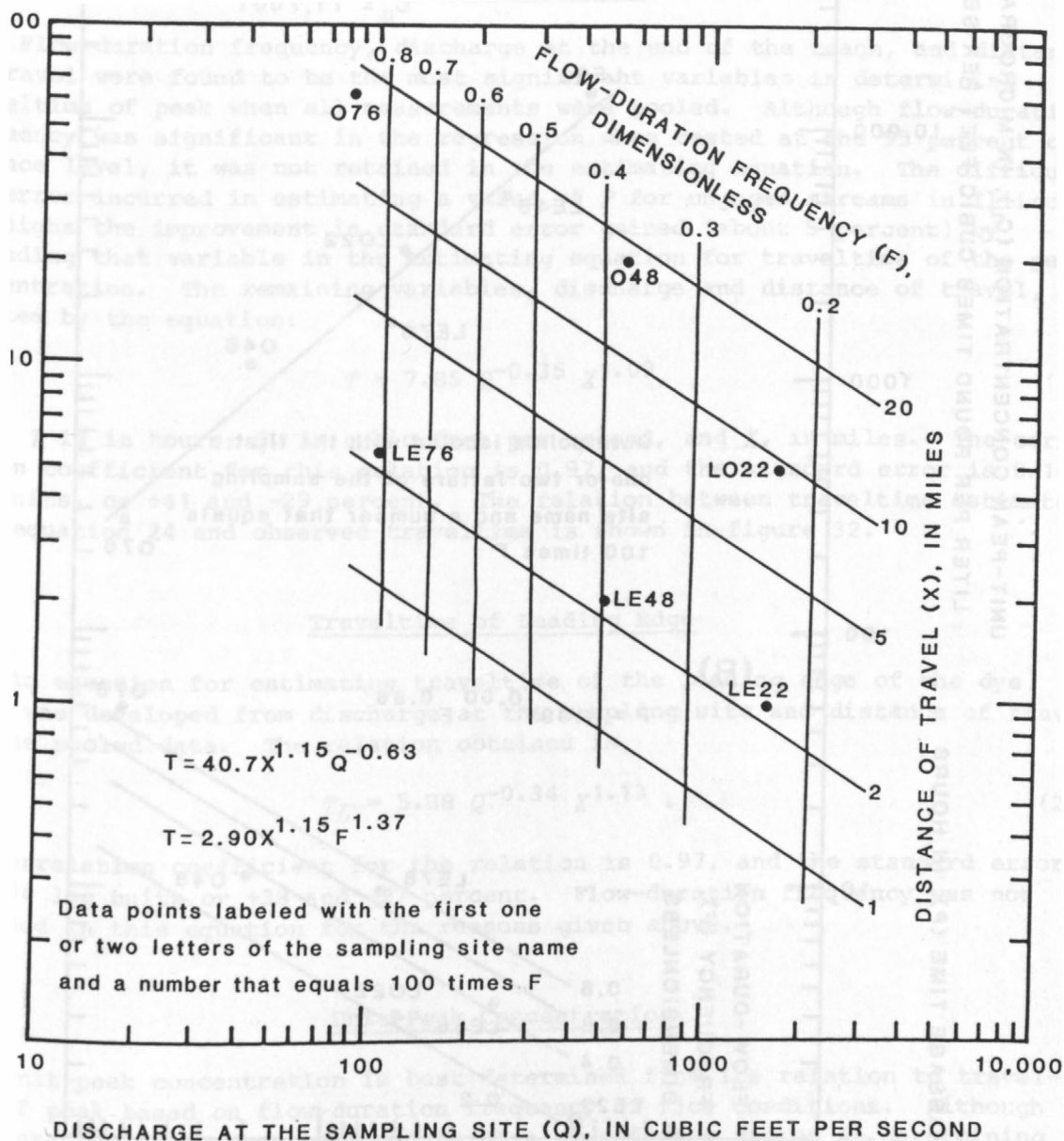


Figure 30.--Relation of traveltime of peak concentration to discharge, distance from injection, and flow-duration frequency, Vermilion River.

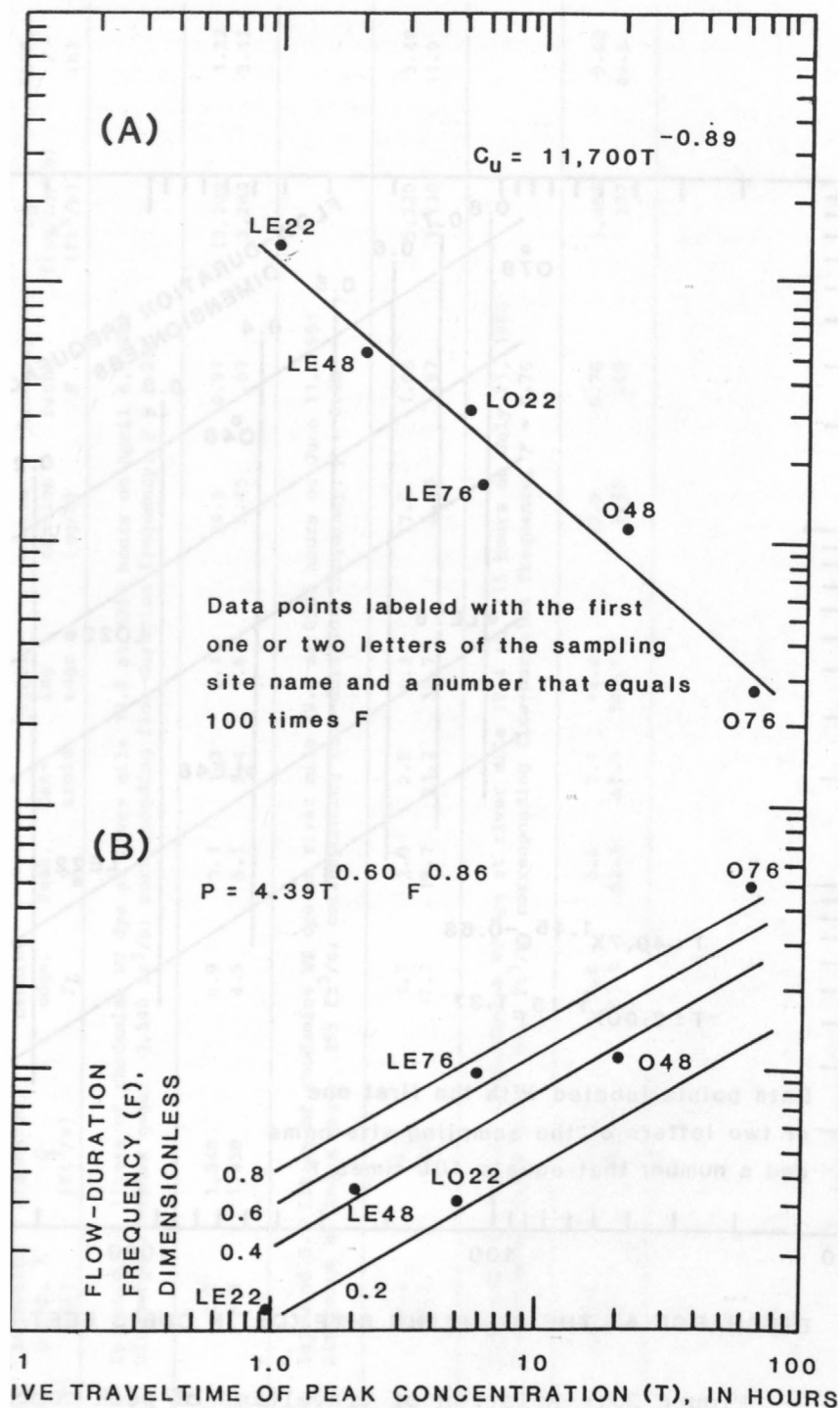


Fig. 31.---Relation of unit-peak concentration (A) and flow-duration frequency (B) to traveltime of peak concentration and flow-duration frequency, Vermilion River.

Traveltime of Peak

Flow-duration frequency, discharge at the end of the reach, and distance of travel were found to be the most significant variables in determining traveltime of peak when all measurements were pooled. Although flow-duration frequency was significant in the regression when tested at the 95 percent confidence level, it was not retained in the estimating equation. The difficulty and error incurred in estimating a value of  $F$  for ungaged streams in Illinois outweighs the improvement in standard error gained (about 5 percent) by including that variable in the estimating equation for traveltime of the peak concentration. The remaining variables, discharge and distance of travel, are related by the equation:

$$T = 7.85 Q^{-0.35} X^{1.09}, \quad (24)$$

where  $T$  is in hours;  $Q$ , in cubic feet per second, and  $X$ , in miles. The correlation coefficient for this relation is 0.97, and the standard error is 0.15 log units, or +41 and -29 percent. The relation between traveltime estimated with equation 24 and observed traveltime is shown in figure 32.

Traveltime of Leading Edge

An equation for estimating traveltime of the leading edge of the dye cloud was developed from discharge at the sampling site and distance of travel for the pooled data. The relation obtained is

$$T_L = 5.88 Q^{-0.34} X^{1.13}. \quad (25)$$

The correlation coefficient for the relation is 0.97, and the standard error is 0.14 log units or +38 and -27 percent. Flow-duration frequency was not included in this equation for the reasons given above.

Unit-Peak Concentration

Unit-peak concentration is best determined from its relation to traveltime of peak based on flow-duration frequency of flow conditions. Although flow-duration frequency was found to be a significant factor in determining unit-peak concentration for 5 of the 10 streams described above, it was not significant in the regression model developed from the pooled data. The equation for unit-peak concentration computed by linear regression from all data is

$$C_u = 10,200 T^{-0.69}. \quad (26)$$

The correlation coefficient of the relation is 0.93, and the standard error of estimate is 0.17 log units or +48 and -32 percent.

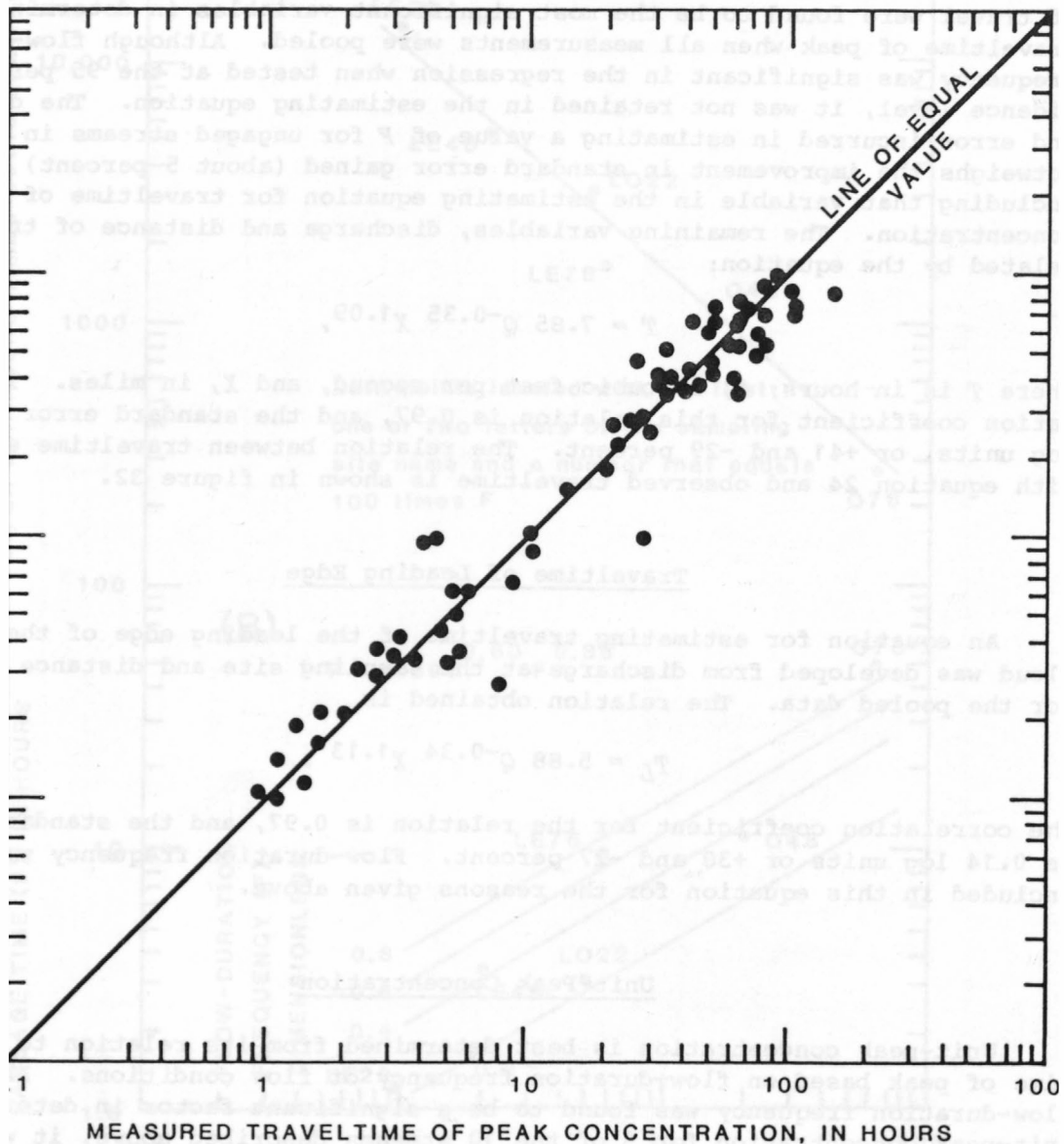


Figure 32.--Relation between measured and estimated traveltime of peak concentration.



A plot of all unit-peak concentration data versus traveltime of peak (fig. 33) illustrates the strong linear relation between the logarithms of the two variables, but also reveals that data points from most low-flow measurements (high flow-duration frequencies) are clustered to one side of the group. A flow-duration frequency of 0.6 was found by trial and error to best separate the two groups of points, and a separate regression equation was developed for each group (fig. 33A). The two regression lines were found to be significantly different at the 95 percent confidence level using an F-test. Application of the F-test to the regression coefficients revealed that the slopes of the two lines were not significantly different, at that same confidence level. The equation developed for low flows ( $F$  greater than 0.6) is

$$C_u = 5,680 T^{-0.63} . \quad (27)$$

The correlation coefficient of the equation is 0.90, and the standard error is 0.16 log units or +46 and -31 percent. For medium and high flows ( $F$  less than or equal to 0.6), the following equation best explained data:

$$C_u = 10,900 T^{-0.66} . \quad (28)$$

The correlation coefficient of this relation is 0.96, and the standard error is 0.12 log units or +33 and -25 percent.

The standard errors given above do not include the error incurred when estimated traveltimes are used in equations 27 and 28. To quantify that error, traveltime of the peak was estimated with equation 24 for all measured conditions and estimated traveltime used to solve equations 27 and 28 for  $C_u$ . Unit-peak concentrations estimated in this way were then compared to observed unit-peak concentrations using regression analysis on untransformed values. The standard error of this regression is +44 and -44 percent.

#### Passage Time

Passage time shows a distribution similar to unit-peak concentration when plotted against traveltime of the peak (fig. 33B). Estimating equations for passage time were developed in the same way as those for unit-peak concentration. The relation obtained from the entire data set is

$$P = 1.41 T^{0.72} . \quad (29)$$

That relation has a correlation coefficient of 0.92 and a standard error of estimate of 0.20 log units or +59 and -37 percent. For low flows ( $F$  greater than 0.6),

$$P = 2.93 T^{0.61} \quad (30)$$

best describes the data. For medium and high flows ( $F$  less than or equal to 0.6) the equation computed is

$$P = 1.29 T^{0.70} . \quad (31)$$

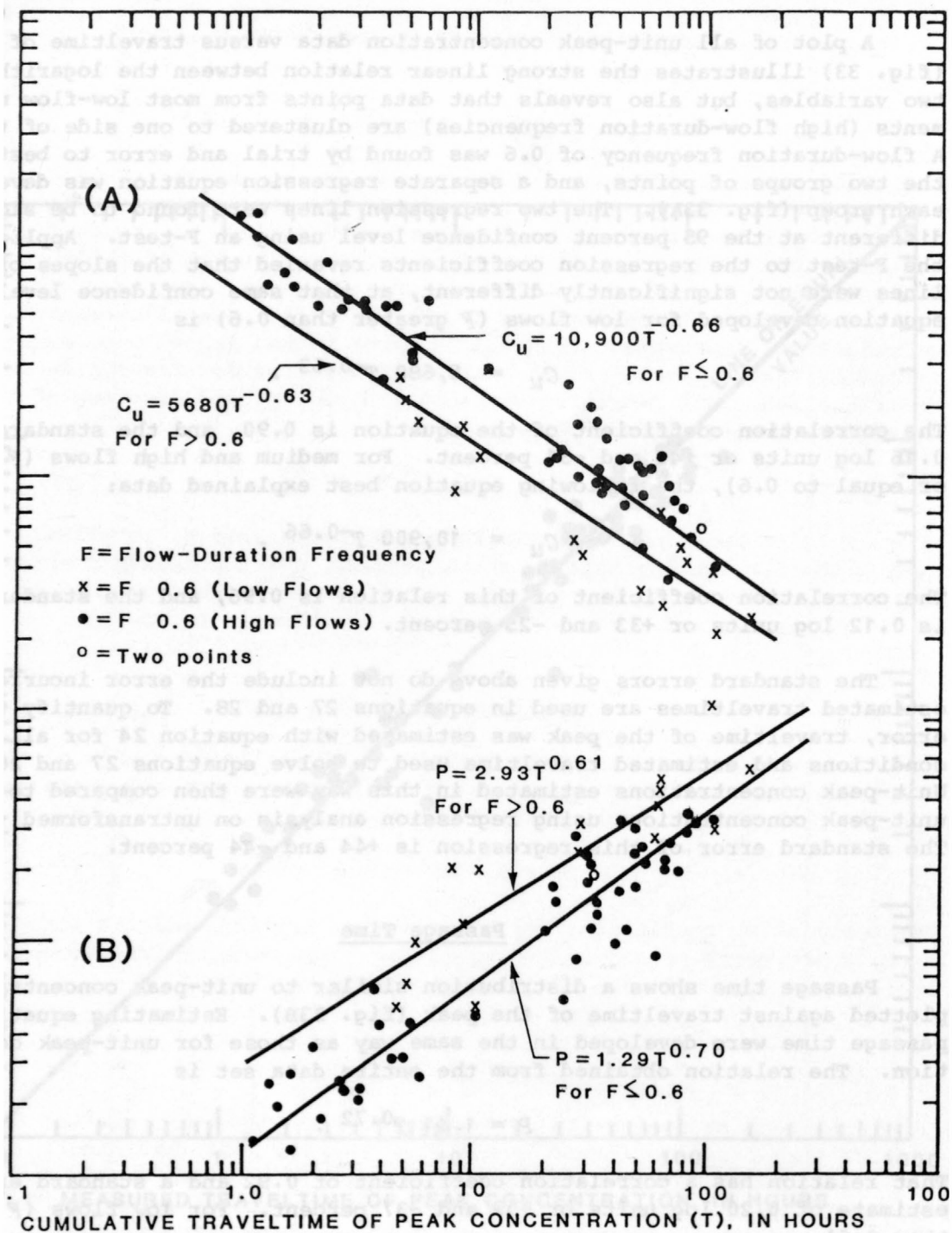


Figure 33.--Relation of unit-peak concentration (A) and passage time (B) to traveltime of peak concentration and flow-duration frequency, for all measured streams.

The correlation coefficients of the last two relations are 0.88 and 0.94, respectively, and the standard error for equation 30 is 0.18 log units or +53 and -34 percent and for equation 31 is 0.16 log units or +45 and -31 percent. For passage time, intercepts of the two regression lines also were found to be significantly different whereas slopes were not (fig. 33B).

The standard error of estimate of passage time, using estimated travel-times to solve equations 30 and 31, was determined in the same way as that for unit-peak concentration and is +40 and -40 percent.

Guidelines for use of these equations are given in the following section.

## APPLICATION OF ESTIMATING TECHNIQUES

### Examples

Application of the estimating techniques is illustrated below with hypothetical situations for both measured and unmeasured streams.

Example 1.--Consider that approximately 100 pounds of toxic material are spilled into the Sangamon River at the Interstate 74 bridge. Estimates of traveltime to Monticello, a community 24.1 miles downstream (Healy, 1979b), and of peak concentration and passage time at that site are needed to plan response tactics. River stage at Monticello is found by reading the gage at Monticello, and discharge is found to be 90 ft<sup>3</sup>/s from the existing stage-discharge relation at the gaging station. This discharge is equaled or exceeded 55 percent of the time ( $F = 0.55$ ), as found from the flow-duration curve developed for the gaging station. With figure 24, traveltime is estimated graphically for a discharge of 90 ft<sup>3</sup>/s and a travel distance of 24.1 miles to be about 80 hours. The same value of traveltime is estimated graphically from figure 24 for a flow-duration frequency of 0.55 and a distance of 24.1 miles.

If traveltime is estimated using the regression equations presented in figure 24, slightly different results will be obtained from the two equations. For example, the traveltime estimated in terms of travel distance and discharge is

$$\begin{aligned} T &= 40.7 X^{1.19} Q^{-0.70} \\ &= 40.7 (24.1)^{1.19} (90)^{-0.70} \\ &= 77 \text{ hours} \end{aligned}$$

and in terms of travel distance and flow-duration frequency is

$$\begin{aligned} T &= 8.65 X^{0.98} F^{1.45} \\ &= 8.65 (24.1)^{0.98} (0.55)^{1.45} \\ &= 82 \text{ hours.} \end{aligned}$$

The difference is within the error of the estimate.

The equations for traveltime of the leading edge are used to estimate the time to first arrival of the contaminant at the site. Using equation 18:

$$\begin{aligned} T_L &= 30.1 X^{1.24} Q^{-0.69} \\ &= 30.1 (24.1)^{1.24} (90)^{-0.69} \\ &= 70 \text{ hours;} \end{aligned}$$

and with equation 19:

$$\begin{aligned} T_L &= 6.37 X^{1.03} F^{1.41} \\ &= 6.37 (24.1)^{1.03} (0.55)^{1.41} \\ &= 73 \text{ hours.} \end{aligned}$$

Unit-peak concentration estimated graphically from figure 25A using a traveltime of 80 hours is about 480  $[(\mu\text{g/L})/\text{lb}](\text{ft}^3/\text{s})$ . The equation on that figure gives an estimated unit-peak concentration of

$$\begin{aligned} C_u &= 2,700 T^{-0.53} F^{-0.99} \\ &= 2,700 (80)^{-0.53} (0.55)^{-0.99} \\ &= 478 [(\mu\text{g/L})/\text{lb}](\text{ft}^3/\text{s}). \end{aligned}$$

The estimated peak concentration for a conservative solute is computed by multiplying the estimated unit-peak concentration by the pounds of substance spilled (100) and dividing by the discharge at the site of interest (90  $\text{ft}^3/\text{s}$ ). In this case, using a  $C_u$  of 478  $[(\mu\text{g/L})/\text{lb}](\text{ft}^3/\text{s})$ , peak concentration is estimated to be about 530  $\mu\text{g/L}$ .

Passage time past the gage at Monticello is estimated graphically from figure 25B to be 28 hours and from the equation given in the figure to be

$$\begin{aligned} P &= 6.12 T^{0.51} F^{1.19} \\ &= 6.12 (80)^{0.51} (0.55)^{1.19} \\ &= 28 \text{ hours.} \end{aligned}$$

**Example 2.**--For planning purposes, it is of interest to know the traveltime and mixing characteristics of a reach of the La Moine River between Stat Highway 101 and the gaging station near Ripley, a distance of 30.5 miles, at both low and high flow conditions. At a flow-duration frequency of 0.75, the discharge near Ripley is 67  $\text{ft}^3/\text{s}$ , and at a flow-duration frequency of 0.25 is 720  $\text{ft}^3/\text{s}$ . For the lower flow condition, traveltime is estimated with equation 24 to be:

$$\begin{aligned} T &= 7.85 Q^{-0.35} X^{1.09} \\ &= 7.85 (67)^{-0.35} (30.5)^{1.09} \\ &= 75 \text{ hours;} \end{aligned}$$



and for the higher flow to be:

$$\begin{aligned}T &= 7.85 Q^{-0.35} X^{1.09} \\&= 7.85 (720)^{-0.35} (30.5)^{1.09} \\&= 33 \text{ hours.}\end{aligned}$$

Traveltime of the leading edge at the lower flow is estimated with equation 25 to be:

$$\begin{aligned}T_L &= 5.88 Q^{-0.34} X^{1.13} \\&= 5.88 (67)^{-0.34} (30.5)^{1.13} \\&= 67 \text{ hours;}\end{aligned}$$

and for the higher flow to be:

$$\begin{aligned}T_L &= 5.88 Q^{-0.34} X^{1.13} \\&= 5.88 (720)^{-0.34} (30.5)^{1.13} \\&= 30 \text{ hours.}\end{aligned}$$

Equation 27 is used to estimate unit-peak concentrations for the lower flow condition,

$$\begin{aligned}C_u &= 5,680 T^{-0.63} \\&= 5,680 (75)^{-0.63} \\&= 374 [(\mu\text{g/L})/\text{lb}](\text{ft}^3/\text{s});\end{aligned}$$

and equation 28 for the higher flow condition,

$$\begin{aligned}C_u &= 10,900 T^{-0.66} \\&= 10,900 (33)^{-0.66} \\&= 1,180 [(\mu\text{g/L})/\text{lb}](\text{ft}^3/\text{s}).\end{aligned}$$

For passage time at Ripley, equation 30 is used for the lower flow condition

$$\begin{aligned}P &= 2.93 T^{0.61} \\&= 2.93 (75)^{0.61} \\&= 41 \text{ hours;}\end{aligned}$$

and equation 31 for the higher flow condition

$$\begin{aligned}P &= 1.29 T^{0.70} \\&= 1.29 (33)^{0.70} \\&= 15 \text{ hours.}\end{aligned}$$

### Limits of Application

Traveltime and mixing relations presented in this report apply only to substances dissolved in stream water. The movement of a substance such as oil, which floats on the water surface, or a particulate substance, which may settle, cannot be estimated with these relations. Unit-peak-concentration relations give the change in concentration caused only by mixing. If other processes, such as chemical reactions or biological processes, are acting to change concentration, the relations presented in this report will not be sufficient to estimate concentration.

Data used to develop the estimating equations for unmeasured streams (equations 24 through 31) were collected in reaches ranging from 5.2 to 40.3 miles in length and from 0.7 to 11 ft/mi in slope. Flow-duration frequency ranged from 0.04 to 0.90. Drainage area at sampling points ranged from 12.4 to 1,516 mi<sup>2</sup>. Flow in all measured reaches was unregulated, but represented a range in conditions from strongly-developed riffles and pools to even, turbulent flow. Configurations ranged from nearly straight dredged channels to tightly meandering natural configurations. The equations presented, therefore, are applicable to a wide range of unregulated streams in Illinois with drainage areas less than about 1,500 mi<sup>2</sup>.

The relations presented for measured streams are strictly applicable only to the reaches measured. They probably can be used successfully for other reaches of the same stream which are similar in character to the measured reach. If the reach of interest is very different from the measured reach in channel geometry or other characteristics which control flow, the equations developed for unmeasured streams should be used for estimation of flow rate and dispersion. Relations for individual streams are applicable only to flows within the range of conditions measured.

All estimating equations developed in this study were computed using simple or multiple linear regression techniques. Equations derived from pooled data (equations 24-31) were examined for violation of assumptions underlying the application of the regression technique, and all these equations do agree with the assumptions. For equations presented for individual streams (equations 4-23 and those shown in figs. 3, 4, 6, 7, 9, 10, 12, 13, 15, 16, 18, 19, 21, 22, 24, 25, 27, 28, 30, and 31), data points are too few to allow evaluation of the ability of the equations to meet the assumptions. Also, each data point used in the regressions exerts a strong influence on the result. Linear regression was used in these cases to provide a consistent, systematic method for interpolation between measured values, and the limitations of applying this technique to a very small number of data points should be recognized when the resulting equations are applied to a given situation.

Standard errors of estimate for each equation presented for the individual streams are given in table 13. Because these equations are computed from very few data points (four to nine), and most of them have two independent variables, the degrees of freedom are very small. The standard errors of estimate shown in table 13 should therefore be used only in conjunction with examination of the data presented in the figures as a guide to relative fit of the equations to the data.

Table 13.--Standard error of estimate for equations for traveltime of the peak concentration and leading edge of the dye cloud, unit-peak concentration, and passage time for individual streams

[ $X$  is distance of travel, in miles;  $Q$  is discharge at the sampling site, in cubic feet per second;  $F$  is flow-duration frequency, dimensionless; and  $T$  is traveltime of the peak concentration, in hours]

River	Equation	Standard error of estimate		
		Log units	Percent	
Traveltime of peak concentration				
Apple	$T = 17.4 X^{1.28} Q^{-0.61}$	0.06	+15	-13
	$T = 4.81 X^{0.96} F^{0.45}$	.06	+15	-13
Cedar	$T = 12.3 X^{1.02} Q^{-0.46}$	.04	+10	-8.8
	$T = 5.61 X^{0.87} F^{0.48}$	.03	+7.2	-6.7
Elkhorn	$T = 6.85 X^{1.17} Q^{-0.43}$	.03	+7.2	-6.7
	$T = 4.35 X^{0.90} F^{0.34}$	.02	+4.7	-4.5
Embarras	$T = 24.5 X^{1.10} Q^{-0.55}$	.02	+4.7	-4.5
	$T = 3.46 X^{1.07} F^{1.38}$	.12	+32	-24
Kaskaskia	$T = 4.37 X^{1.42} Q^{-0.52}$	.17	+48	-32
	$T = 8.49 X^{0.78} F^{1.16}$	.12	+32	-24
Mackinaw	$T = 56.2 X^{1.00} Q^{-0.64}$	.08	+20	-17
	$T = 10.0 X^{0.94} F^{1.91}$	.05	+12	-11
Middle Fork Vermilion	$T = 35.5 X^{0.99} Q^{-0.63}$	.09	+23	-19
	$T = 5.85 X^{1.03} F^{1.66}$	.02	+4.7	-4.5
Sangamon	$T = 40.7 X^{1.19} Q^{-0.70}$	.09	+23	-19
	$T = 8.65 X^{0.98} F^{1.65}$	.14	+38	-28
Shoal	$T = 13.2 X^{1.23} Q^{-0.54}$	.07	+17	-15
	$T = 3.27 X^{1.17} F^{1.16}$	.08	+20	-17
Vermilion	$T = 40.7 X^{1.15} Q^{-0.63}$	.02	+4.7	-4.5
	$T = 2.90 X^{1.15} F^{1.37}$	.13	+35	-26

Table 13.--Standard error of estimate for equations for traveltime of the peak concentration and leading edge of the dye cloud, unit-peak concentration, and passage time for individual streams--Continued

River	Equation	Standard error of estimate		
		Log units	Percent	
Traveltime of leading edge				
Apple	$T_L = 12.2 X^{1.33} Q^{-0.60}$	0.06	+15	-13
	$T_L = 3.48 X^{1.02} F^{0.44}$	.06	+15	-13
Cedar	$T_L = 9.97 X^{1.05} Q^{-0.41}$	.04	+9.6	-8.8
	$T_L = 4.70 X^{0.89} F^{0.46}$	.03	+4.7	-4.5
Elkhorn	$T_L = 5.83 X^{1.20} Q^{-0.44}$	.03	+7.2	-6.7
	$T_L = 3.66 X^{0.93} F^{0.35}$	.02	+4.7	-4.5
Embarras	$T_L = 17.8 X^{1.14} Q^{-0.53}$	.03	+7.2	-6.7
	$T_L = 2.62 X^{1.12} F^{1.34}$	.13	+35	-26
Kaskaskia	$T_L = 3.14 X^{1.38} Q^{-0.44}$	.12	+32	-24
	$T_L = 5.43 X^{0.84} F^{0.95}$	.08	+20	-17
Mackinaw	$T_L = 36.7 X^{1.06} Q^{-0.62}$	.09	+23	-19
	$T_L = 7.03 X^{1.00} F^{1.85}$	.05	+12	-11
Middle Fork Vermilion	$T_L = 19.2 X^{0.96} Q^{-0.54}$	.03	+7.2	-6.7
	$T_L = 4.03 X^{1.00} F^{1.39}$	.04	+10	-8.8
Sangamon	$T_L = 30.1 X^{1.24} Q^{-0.69}$	.08	+20	-17
	$T_L = 6.37 X^{1.03} F^{1.41}$	.15	+41	-29
Shoal	$T_L = 8.11 X^{1.26} Q^{-0.47}$	.08	+20	-17
	$T_L = 2.47 X^{1.20} F^{1.06}$	.08	+20	-17
Vermilion	$T_L = 28.7 X^{1.15} Q^{-0.59}$	.02	+4.7	-4.5
	$T_L = 2.39 X^{1.15} F^{1.29}$	.12	+32	-24



Table 13.--Standard error of estimate for equations for traveltime of the peak concentration and leading edge of the dye cloud, unit-peak concentration, and passage time for individual streams--Continued

River	Equation	Standard error of estimate		
		Log units	Percent	
Unit-peak concentration				
Apple	$C_u = 7,040 T^{-0.63}$	0.07	+17	-15
Cedar	$C_u = 20,400 T^{-0.77}$	.09	+23	-19
Elkhorn	$C_u = 13,200 T^{-0.66}$	.05	+12	-11
Embarras	$C_u = 5,660 T^{-0.60} F^{-0.56}$	.05	+12	-11
Kaskaskia	$C_u = 17,700 T^{-0.92}$	.13	+35	-26
Mackinaw	$C_u = 1,730 T^{-0.54} F^{-1.50}$	.08	+20	-17
Middle Fork Vermilion	$C_u = 6,340 T^{-0.80} F^{-0.71}$	.05	+12	-11
Sangamon	$C_u = 2,700 T^{-0.53} F^{-0.99}$	.07	+17	-15
Shoal	$C_u = 11,700 T^{-0.69}$	.12	+32	-24
Vermilion	$C_u = 11,700 T^{-0.89}$	.13	+35	-26

Table 13.--Standard error of estimate for equations for traveltime of the peak concentration and leading edge of the dye cloud, unit-peak concentration, and passage time for individual streams--Continued

River	Equation	Standard error of estimate	
		Log units	Percent
Passage time			
Apple	$P = 2.22 T^{0.62}$	0.07	+17 -15
Cedar	$P = 0.45 T^{1.02}$	.06	+15 -13
Elkhorn	$P = 0.91 T^{0.76}$	.06	+15 -13
Embarras	$P = 2.41 T^{0.61} F^{0.41}$	.07	+17 -15
Kaskaskia	$P = 1.29 T^{0.88}$	.15	+41 -29
Mackinaw	$P = 10.5 T^{0.51} F^{1.69}$	.07	+17 -15
Middle Fork Vermilion	$P = 2.60 T^{0.90} F^{1.10}$	.03	+7.2 -6.
Sangamon	$P = 6.12 T^{0.51} F^{1.19}$	.09	+23 -19
Shoal	$P = 1.09 T^{0.72}$	.15	+41 -29
Vermilion	$P = 4.39 T^{0.60} F^{0.86}$	.08	+20 -17

For traveltime of the peak concentration and traveltime of the leading edge, standard errors for both equations using discharge at the sampling site and equations using flow-duration frequency are presented. For most streams, the standard error for equations with distance and discharge as independent variables is nearly equal to that for equations with distance and flow-duration frequency. However, the equation using discharge would give better estimates of traveltime of the peak for the Embarras, Sangamon, and Vermilion Rivers than that using flow-duration frequency. The equation using flow-duration frequency yields better estimates for the Middle Fork Vermilion River. For traveltime of the leading edge, the equations using discharge give better estimates than those using flow-duration frequency for the Embarras, Sangamon, and Vermilion Rivers.

In development of the equations for passage time and unit-peak concentration for unmeasured streams, flow-duration frequency was found not to be statistically significant in the relations. However, when the data set was split into two groups on the basis of flow-duration frequency, equations computed from the two groups were found to be significantly different. Flow-duration frequency is used in this analysis because it is one quantitative way of accounting for factors that vary with flow condition and that cannot be easily quantified directly. The fact that the passage time-traveltime and unit-peak concentration-traveltime relations are influenced by flow-duration frequency suggests that factors controlling longitudinal dispersion change with flow condition. For the measured streams, the changes appear to take place over a narrow range of flow conditions near a flow-duration frequency of 0.6. Changes could be the emergence of bars that cause the thalweg to meander strongly and that create eddies or stagnant zones, or the transition to nonuniform flow caused by riffles. The value 0.6 found in this study probably depends strongly on the streams chosen for measurement and on the flows measured.

Some knowledge of the character of the stream channel and flow conditions is required to successfully use the separate equations for low and high flows for an unmeasured stream. If the channel is characterized by strongly-developed riffles and pools, if the thalweg meanders strongly around bars or obstructions, if there are large areas of eddies or stagnant-appearing water, then the equations for low flows (equations 27 and 30) probably would give better estimates of unit-peak concentration and passage time than the equations computed from the entire pooled data set, even though the flow-duration frequency is less than 0.6. If little or nothing is known about the stream for which estimates are needed, then the equations developed from the pooled data (equation 26 for unit-peak concentration and equation 29 for passage time) should be used even though an estimate of flow-duration frequency is available.

Although traveltime is a useful variable for the type of application given in the examples, reach velocity is also of interest and may be needed for other applications, such as calibration of streamflow models. In a straight uniform channel downstream of the transverse mixing distance, the velocity of the centroid, or center of mass, of the dye cloud through a reach is a measure of the average velocity of flow through that reach. Using centroid velocity measured in these streams, an estimating equation for average reach velocity was developed from the data for all measurements in the same way as the equation presented above for traveltime.

As expected from the results of the traveltime analysis, flow-duration frequency and discharge at the downstream end of the reach (discharge at the sampling site) were found to be the most significant variables for estimating reach velocity. However, in the case of reach velocity, untransformed values of the variables were found to be most suitable for the regression. Residuals from the regression on untransformed variables were found to be normally distributed about the regression line, as required for application of the linear regression model, whereas residuals from the regression on logarithms of values had a distinctly non-normal distribution about the regression line. Because residuals of regression of logarithms of traveltime on logarithms of the independent variables were normally distributed, the transformation was used in that regression (equation 24). Flow-duration frequency was not retained in the equation for the reasons given in the traveltime of peak section. The estimating equation obtained for reach velocity is

$$V = 0.38 + 0.000883 Q, \quad (32)$$

where velocity is in miles per hour and discharge in cubic feet per second. The correlation coefficient for this relation is 0.87, and the standard error is +29 percent. Figure 34 shows the relation between observed velocity and velocity estimated with equation 32. The two points which lie above the main cluster of values represent measurements in the Apple River at the most downstream sites for the medium and high measurements. Velocities at one of these sites, near Whitton, could have been influenced by backwater from the Mississippi River during the measurement, whereas velocities at the site at Hanover may have been significantly affected by a pool upstream of the sampling site. Although these factors did not greatly influence the traveltime-discharge graphs for the Apple River (fig. 4), they appear to influence velocity significantly.

Equations for average velocity through stream reaches in 18 drainage basins in Illinois were developed from hydraulic-geometry relations by Stall and Fok (1968). They used records of discharge measurements at all gaging stations in each basin to develop a relation between discharge and velocity at a cross section. Flow-duration curves developed for each gaging station were used to express velocity ( $V$ ) in terms of flow-duration frequency ( $F$ ), rather than discharge. From data for all gages within a basin, Stall and Fok developed relations of the form  $\ln V = a + bF + cU$ , where  $a$ ,  $b$ , and  $c$  are constants for a basin, and  $U$  is stream order. Because drainage area is more



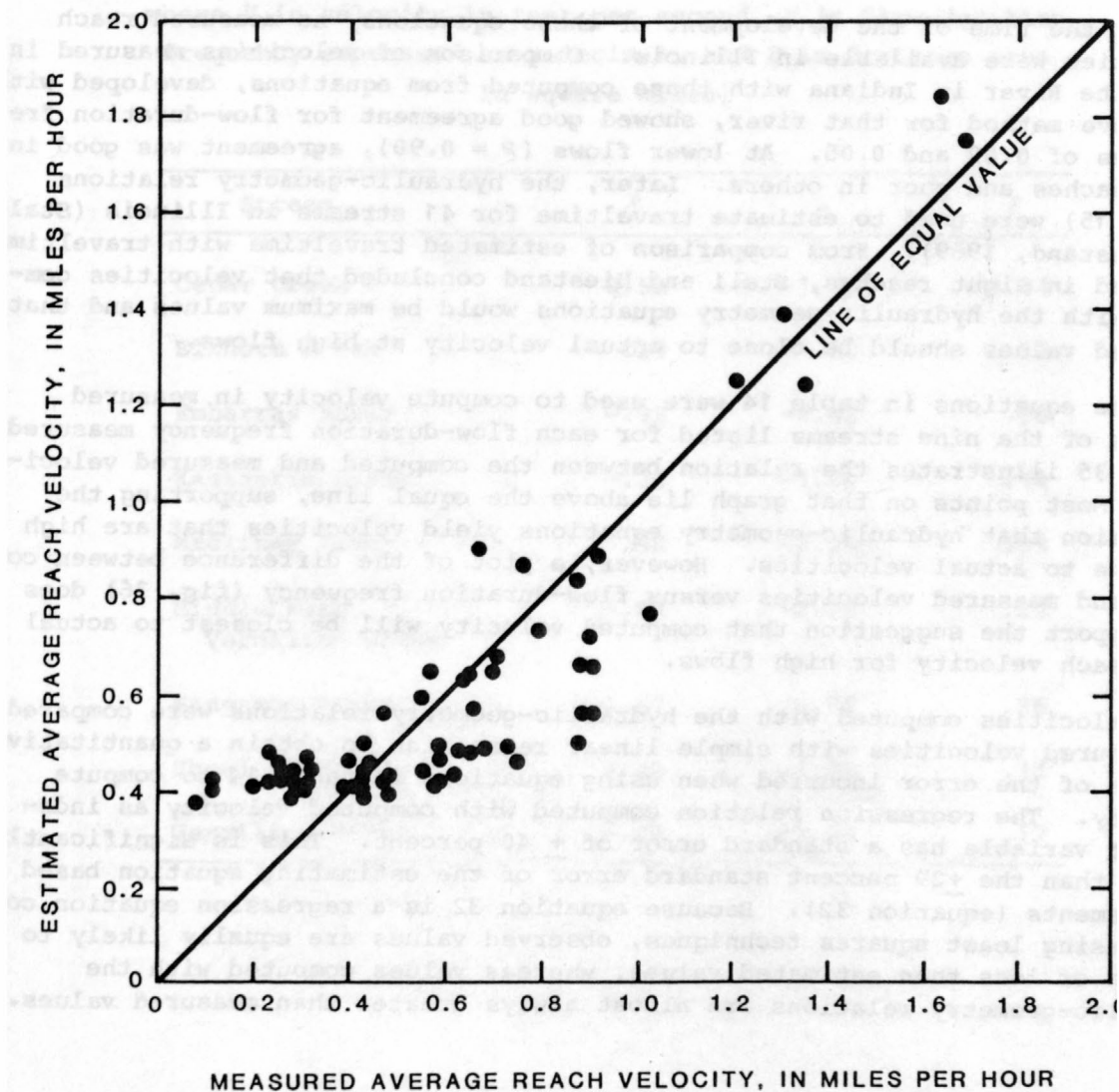


Figure 34.--Relation between measured and estimated average reach velocity for measured streams.

easily obtained than stream order, Stall and Fok converted the equations to the form  $\ln V = d + eF + f \ln D$  using the relation of stream order to drainage area ( $D$ ) developed for each basin. The coefficients represented by  $d$ ,  $e$ , and  $f$  are constants for a basin. Nine of the 10 streams for which velocity was measured as a part of the present study are within basins for which velocity equations were developed. The equations are given in table 14.

At the time of the development of these equations, no measured reach velocities were available in Illinois. Comparison of velocities measured in the White River in Indiana with those computed from equations, developed with the above method for that river, showed good agreement for flow-duration frequencies of 0.02 and 0.05. At lower flows ( $F = 0.90$ ), agreement was good in some reaches and poor in others. Later, the hydraulic-geometry relations (table 15) were used to estimate traveltime for 41 streams in Illinois (Stall and Hiestand, 1969). From comparison of estimated traveltime with traveltime measured in eight reaches, Stall and Hiestand concluded that velocities computed with the hydraulic-geometry equations would be maximum values and that computed values should be close to actual velocity at high flows.

The equations in table 14 were used to compute velocity in measured reaches of the nine streams listed for each flow-duration frequency measured. Figure 35 illustrates the relation between the computed and measured velocities. Most points on that graph lie above the equal line, supporting the conclusion that hydraulic-geometry equations yield velocities that are high relative to actual velocities. However, a plot of the difference between computed and measured velocities versus flow-duration frequency (fig. 36) does not support the suggestion that computed velocity will be closest to actual mean reach velocity for high flows.

Velocities computed with the hydraulic-geometry relations were compared to measured velocities with simple linear regression to obtain a quantitative measure of the error incurred when using equations in table 14 to compute velocity. The regression relation computed with computed velocity as independent variable has a standard error of  $\pm 40$  percent. This is significantly larger than the  $\pm 29$  percent standard error of the estimating equation based on measurements (equation 32). Because equation 32 is a regression equation computed using least squares techniques, observed values are equally likely to be greater or less than estimated values, whereas values computed with the hydraulic-geometry relations are almost always greater than measured values.

#### DISCUSSION OF DISPERSION CHARACTERISTICS IN MEASURED STREAMS

Graphs for individual streams which show the change in unit-peak concentration and passage time with traveltime reveal that measured streams define two types of dispersion relations. One group of streams (Apple River, Cedar Creek, Elkhorn Creek, Kaskaskia River, and Shoal Creek) shows little or no systematic variation in dispersion with flow-duration frequency. For those streams, the change in passage time and unit-peak concentration with traveltime can be adequately described by a simple linear regression model using logarithmically transformed data. On the other hand, the relations between traveltime and dispersion in the Embarras, Mackinaw, Middle Fork Vermilion, Sangamon, and Vermilion Rivers vary systematically with flow-duration frequency.

Table 14.--Hydraulic-geometry relations used to compute reach velocity  
for nine streams

[Equations, developed by Stall and Fok (1968), are of the form

$$\ln V = d + eF + f \ln D,$$

where  $V$  is velocity in feet per second,  $F$  is flow-duration frequency expressed as a decimal, and  $D$  is drainage area in square miles]

Stream	$d$	$e$	$f$
Cedar Creek	0.58	-1.76	0.01
Elkhorn Creek	.20	-1.50	.13
Embarras River	-.92	-1.62	.26
Kaskaskia River	-.26	-1.28	.14
Mackinaw River	.38	-2.26	.09
Middle Fork Vermilion River	-.81	-2.20	.29
Sangamon River	-1.01	-.95	.26
Shoal Creek	-.26	-1.28	.14
Vermilion River	-.20	-2.19	.17

Figure 35.--Relation between measured average reach velocity and reach velocity computed with hydraulic geometry relations.

Table 15.--Dispersion efficiency of measured streams

Stream	Rate of change of indicated variable with traveltime of peak concentration	
	Unit-peak concentration,	Passage time,
	$C_u$	$P$
Apple River	-0.63	0.62
Cedar Creek	-.77	1.02
Elkhorn Creek	-.66	.76
Embarras River	-.60	.61
Kaskaskia River	-.92	.88
Mackinaw River	-.54	.51
Middle Fork Vermilion River	-.80	.90
Sangamon River	-.53	.51
Shoal Creek	-.69	.72
Vermilion River	-.89	.60

## DISCUSSION OF DISPERSION CHARACTERISTICS IN MEASURED STREAMS

Graphs for individual streams which show the change in unit-peak concentration and passage time with traveltime reveal that measured streams define types of dispersion relations. One group of streams (Apple River, Cedar Creek, Elkhorn Creek, Kaskaskia River, and Shoal Creek) shows little or no systematic variation in dispersion with flow-duration frequency. For these streams, the change in passage time and unit-peak concentration with traveltime can be adequately described by a simple linear regression model using arithmetically transformed data. On the other hand, the relations between traveltime and dispersion in the Embarras, Mackinaw, Middle Fork Vermilion, Sangamon, and Vermilion Rivers vary systematically with flow-duration frequency.



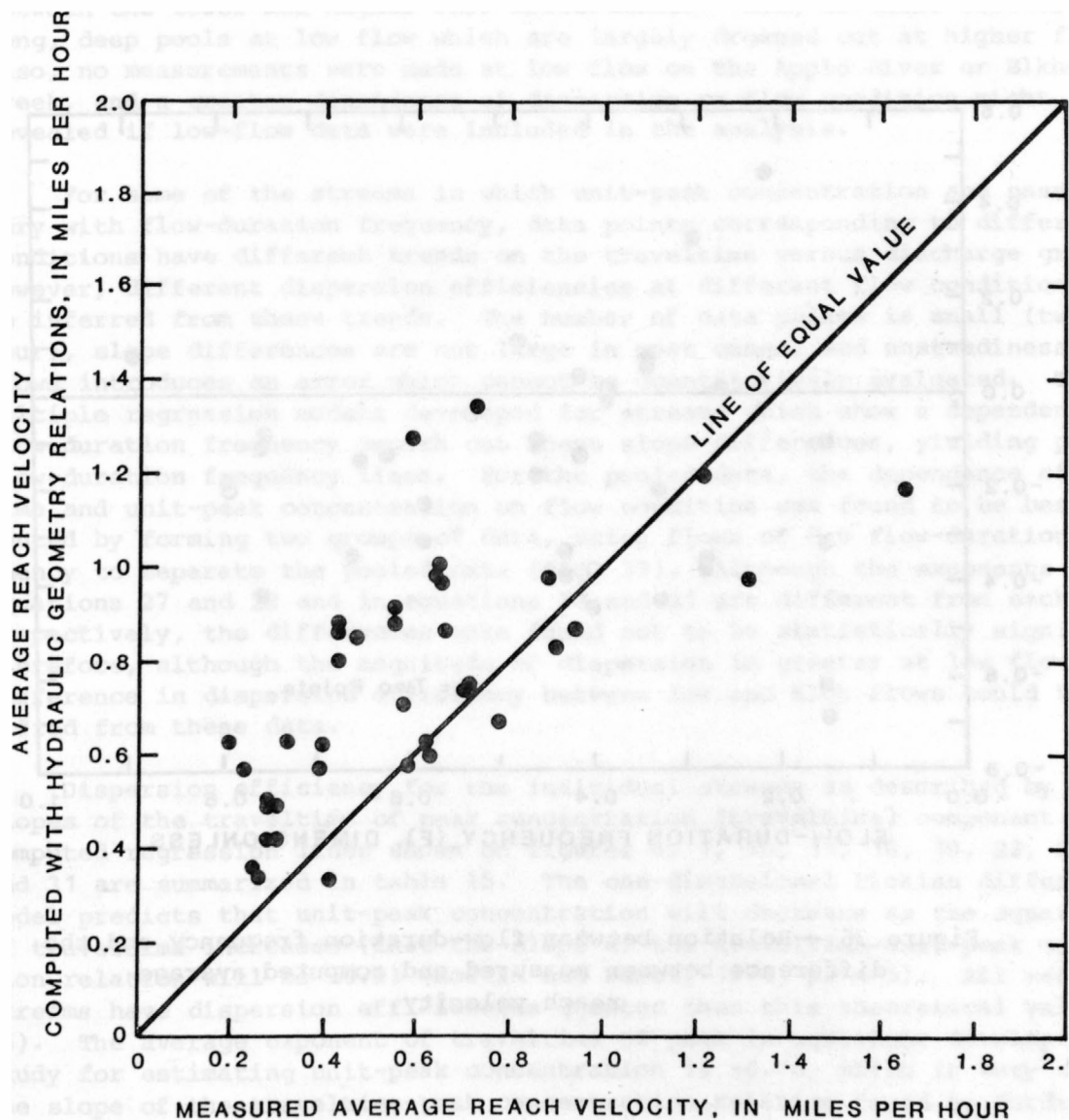


Figure 35.--Relation between measured average reach velocity and reach velocity computed with hydraulic geometry relations.

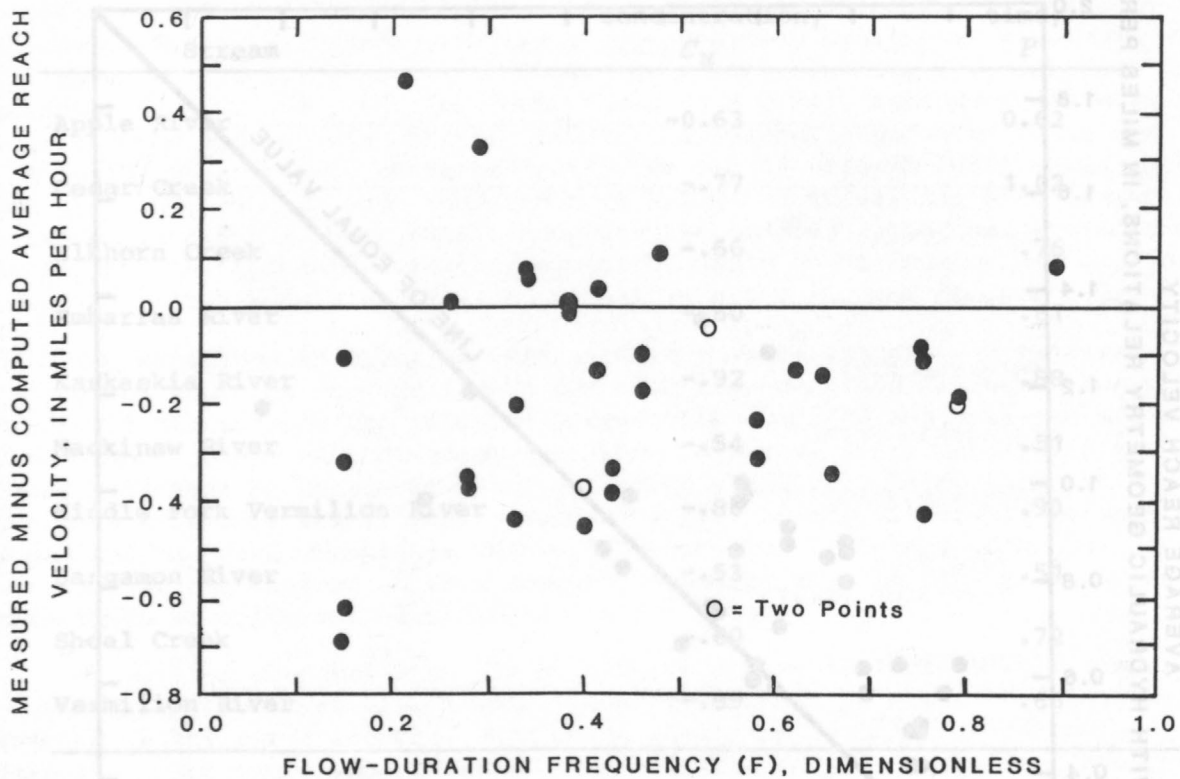


Figure 36.--Relation between flow-duration frequency and the difference between measured and computed average reach velocity.

Although no quantitative explanation for the presence of these two types of behavior can be presented, it should be noted that the Mackinaw and Sangamon Rivers, which show the greatest dependence of dispersion on flow-duration frequency, also underwent the greatest change in flow characteristics between the lower and higher flow measurements. Both of these streams develop long, deep pools at low flow which are largely drowned out at higher flows. Also, no measurements were made at low flow on the Apple River or Elkhorn Creek, and a greater dependence of dispersion on flow condition might be revealed if low-flow data were included in the analysis.

For some of the streams in which unit-peak concentration and passage time vary with flow-duration frequency, data points corresponding to different flow conditions have different trends on the traveltime versus discharge graphs. However, different dispersion efficiencies at different flow conditions cannot be inferred from these trends. The number of data points is small (two to four), slope differences are not large in most cases, and unsteadiness of flows introduces an error which cannot be quantitatively evaluated. The multiple regression models developed for streams which show a dependence upon flow-duration frequency smooth out these slope differences, yielding parallel flow-duration frequency lines. For the pooled data, the dependence of passage time and unit-peak concentration on flow condition was found to be best represented by forming two groups of data, using flows of 0.6 flow-duration frequency to separate the pooled data (fig. 33). Although the exponents in equations 27 and 28 and in equations 30 and 31 are different from each other, respectively, the differences were found not to be statistically significant. Therefore, although the magnitude of dispersion is greater at low flow, no difference in dispersion efficiency between low and high flows could be identified from these data.

Dispersion efficiency for the individual streams as described by the slopes of the traveltime of peak concentration (traveltime) component of the computed regression lines shown on figures 4, 7, 10, 13, 16, 19, 22, 25, 28, and 31 are summarized in table 15. The one-dimensional Fickian diffusion model predicts that unit-peak concentration will decrease as the square root of traveltime increases (that the slope of the traveltime-unit-peak concentration relation will be  $-0.5$ ) (Nordin and Sabol, 1974, p. 4-5). All measured streams have dispersion efficiencies greater than this theoretical value (table 15). The average exponent of traveltime of peak in equations developed in this study for estimating unit-peak concentration is  $-0.70$ , which is very close to the slope of the traveltime-peak concentration relation found by Nordin and Sabol (1974, p. 56) in their analysis of 51 sets of dispersion data from streams nationwide. In the present study, the rate of increase of passage time with traveltime of peak concentration was found to be about the same as the rate of decrease in unit-peak concentration. The average exponent of traveltime in the passage time estimating equations is  $0.71$ .

The Mackinaw and Sangamon Rivers are closest to the theoretical dispersion efficiency, the Apple and Embarras Rivers and Elkhorn and Shoal Creeks disperse more efficiently, and Cedar Creek and the Kaskaskia, Middle Fork Vermilion, and Vermilion Rivers are most efficient. Although data are not available to quantitatively relate these dispersion efficiencies to channel and flow characteristics, some qualitative observations can be made. The

Mackinaw and Sangamon Rivers are both large, deep streams which form very large pools at low flow. Water velocity through pools is extremely low and riffle sections are short. The streams with greater dispersion efficiencies tend to be shallower and to have coarser bed materials. Greater efficiencies also appear to be associated with large slack-water zones downstream of channel bars which are present over a range of flow conditions, and a thalweg that is sinuous within the channel because of development of bars. The relatively large dispersion efficiency of the Kaskaskia River is difficult to explain. The channel is quite straight, and the sand bed is flat and even over much of the measured reach. The stream does not undergo great changes in flow characteristics with changing flow condition.

## CONCLUSIONS

Traveltime and longitudinal dispersion characteristics for many unregulated streams in Illinois can be estimated with the techniques presented in this report. The techniques were developed from an extensive set of data obtained by measurement of these characteristics on 10 streams over a range of flow conditions. Prior to this study, no measured data were available to estimate these characteristics for Illinois streams. The measured values, and the techniques developed for them, provide a means for estimating values that reflect the actual behavior of these streams better than those obtained from previously available techniques.

For measured streams, traveltime of the peak concentration and leading edge of the solute cloud are estimated from distance of travel and either flow-duration frequency or discharge at the site of interest. Estimating techniques based on both flow-duration frequency and discharge are presented in order to make the techniques more flexible. For unmeasured streams, although flow-duration frequency and discharge were found to explain a significant amount of the variation in the data, flow-duration frequency was not retained in the estimating equations because a sufficiently accurate value is not readily available for unmeasured streams.

Passage time and unit-peak concentration, measures of longitudinal dispersion, are estimated from traveltime of the peak concentration for both measured and unmeasured streams. For 5 of the 10 measured streams, the amount of longitudinal dispersion varies with flow-duration frequency. To account for this variation, the technique presented for estimating passage time and unit-peak concentration consists of an equation for low flows and one for medium and high flows. The data suggest that the rate of change of longitudinal dispersion with traveltime (dispersion efficiency) does not vary significantly with flow condition. Dispersion efficiency determined from measurements is greater than predicted by the one-dimensional Fickian diffusion model.

Most of the measured average reach velocities are less than velocities estimated from the hydraulic-geometry equations developed by Stall and Fok (1968). An estimating equation developed from measured values relates average reach velocity to discharge.



Techniques of measurement and analysis used in this study are based on the assumption of steady or gradually-varying flow. Discharge changed with time during almost all measurements, and changes at the index gage were greater than 20 percent for 11 of the 27 measurements. Discharge decreased during most measurements, either because the measurement was made during flow recession following storm runoff, or because base-flow recession was taking place. Although the changes in discharge are larger than desirable for consideration as steady or gradually-varying flow, they are probably representative of those that occur at the measured flows.

Channel slope was considered in the analysis but was found not to contribute significantly to the regression equations developed for traveltime or average reach velocity (equations 24 and 30). This differs from the results of both Boning (1974) and Eikenberry and Davis (1976), who found slope to be a significant variable even for pool-riffle reaches. The data suggest, however, that slope may be significant in determining traveltime in some streams (for example, the Vermilion River), but that measurements in which slope is significant are too few to influence the regression.

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