Appendix 13. Model Archival Summary for Hardness Concentration at U.S. Geological Survey Site 06887500, Kansas River at Wamego, Kansas, during July 2012 through September 2019

This model archival summary summarizes the hardness as calcium carbonate ($CaCO_3$; U.S. Geological Survey [USGS] parameter code 00900) concentration model developed to compute 15-minute $CaCO_3$ concentrations from July 2012 onward. This model supersedes all previous models.

Any use of trade, firm, or product names is for descriptive purposes only and does not imply endorsement by the U.S. Government.

Site and Model Information

Site number: 06887500
Site name: Kansas River at Wamego, Kansas
Location: Lat 39°11'54", long 96°18'19" referenced to North American Datum of 1927, in SW 1/4 NW 1/4 SE 1/4 sec.9, T.10 S., R.10 E., Pottawatomie County, Kans., hydrologic unit 10270102.

Equipment: A YSI 6600 water-quality monitor equipped with sensors for water temperature, specific conductance (SC), dissolved oxygen, pH, and turbidity was installed from August 2012 through June 2014. A Xylem YSI EXO2 water-quality monitor equipped with sensors for water temperature, SC, dissolved oxygen, pH, turbidity, and chlorophyll and phycocyanin fluorescence was installed during June 2014 through September 2019. The monitor was housed in a 4-inch-diameter galvanized steel pipe. Readings from the water-quality monitor were recorded every 15 minutes and transmitted by way of satellite, hourly.

Date model was created: March 26, 2020

Model calibration data period: July 19, 2012, through September 23, 2019

Model application date: July 19, 2012, onward

Model-Calibration Dataset

All data were collected using USGS protocols (Wagner and others, 2006; U.S. Geological Survey, variously dated) and are stored in the National Water Information System (U.S. Geological Survey, 2020) database and available to the public. Ordinary least squares analysis was used to develop regression models using R programming language (R Core Team, 2020). Potential explanatory variables that were evaluated individually and in combination included streamflow, water temperature, SC, dissolved oxygen, pH, turbidity, and chlorophyll and phycocyanin fluorescence. The maximum time span between two continuous data points used for interpolation was 2 hours (in order to preserve the sample dataset, field monitor averages obtained during sample collection were used for model development data if no continuous data were available or if gaps larger than 1 hour in the continuous data record resulted in missing interpolated data). Seasonal components (sine and cosine variables) were also evaluated as potential explanatory variables.

The final selected regression model was based on 101 concurrent measurements of $CaCO_3$ concentration and sensor-measured SC during July 19, 2012, through September 23, 2019. Samples were collected throughout the range of continuously observed hydrologic conditions. No samples had concentrations below laboratory detection limits. Summary statistics and the complete model-calibration dataset are provided below. Potential outliers were identified using the methods described in Rasmussen and others (2009). Additionally, studentized residuals from the final model were inspected for values greater than three or less than negative three. Values outside of that range were considered potential outliers and were investigated. One of the sensor-measured SC samples, from July 28, 2014, was deemed an outlier and removed from the model calibration dataset. The removed sensor-measured SC value was significantly lower than the field monitor and laboratory result during this sample. All other potential outliers were not found to have errors associated with collection, processing, or analysis and were therefore considered valid.

This model is specific to the Kansas River at Wamego, Kans., during this study period and cannot be applied to data collected from other sites on the Kansas River or data collected from other waterbodies.

Hardness Sampling Details

Cross-section samples typically were collected either from the downstream side of the bridge or instream within 100 feet of the bridge. The equal-width-increment collection method was used (although multiple vertical, single vertical, and grab samples were occasionally collected), and samples typically were composited for analysis (U.S. Geological Survey, variously dated). During July 2012 through June 2017, cross-section samples were collected every 2 weeks during March through October, once a month during November through February, and during selected reservoir release and runoff events. During July 2017 through September 2019,

cross-section samples were collected on a monthly to bimonthly basis, depending on flow conditions. A FISP US DH–81, DH–95, D–95, D–96a, or D–96 depth integrating sampler was used. Additional detail on sample collection is available in Foster and Graham (2016) and Graham and others (2018). Samples were analyzed for $CaCO_3$ concentration at the USGS National Water Quality Laboratory in Lakewood, Colorado.

Model Development

Ordinary least squares regression analysis was done using R programming language (R Core Team, 2020) to relate discretely collected $CaCO_3$ concentration to sensor-measured SC. The distribution of residuals was examined for normality, and the plots of residuals (the difference between the measured and computed values) were examined for homoscedasticity (departures from zero did not change substantially over the range of computed values). Previously published explanatory variables were also strongly considered for continuity.

SC was selected as a good surrogate for $CaCO_3$ based on residual plots, coefficient of determination (R^2), and model standard percentage error. Values for all the aforementioned statistics were computed and are included below along with all relevant sample data and additional statistical information.

Model Summary

The following is a summary of final regression analysis for $CaCO_3$ concentration at USGS site 06887500:

$CaCO_3$ concentration-based model:

$$\log CaCO_3 = 0.723 \times \log SC + 0.314$$

where

log = logarithm base 10;

$CaCO_3$ = hardness as calcium carbonate concentration, in milligrams per liter; and

SC = specific conductance, in microsiemens per centimeter at 25 degrees Celsius.

SC makes physical and statistical sense as an explanatory variable for $CaCO_3$ because of its positive correlation with charged ionic species (Hem, 1992).

The logarithmically (log) transformed model may be retransformed to the original units so that $CaCO_3$ can be calculated directly. The retransformation introduces a bias in the calculated constituent. This bias may be corrected using Duan's bias correction factor (BCF; Duan, 1983). For this model, the calculated BCF is 1.00. The retransformed model, accounting for BCF is as follows:

$$CaCO_3 = 1 \times (SC^{0.723} \times 10^{0.314})$$

Previous Models

There are no previously published models for hardness as calcium carbonate at this site.

Model Statistics, Data, and Plots

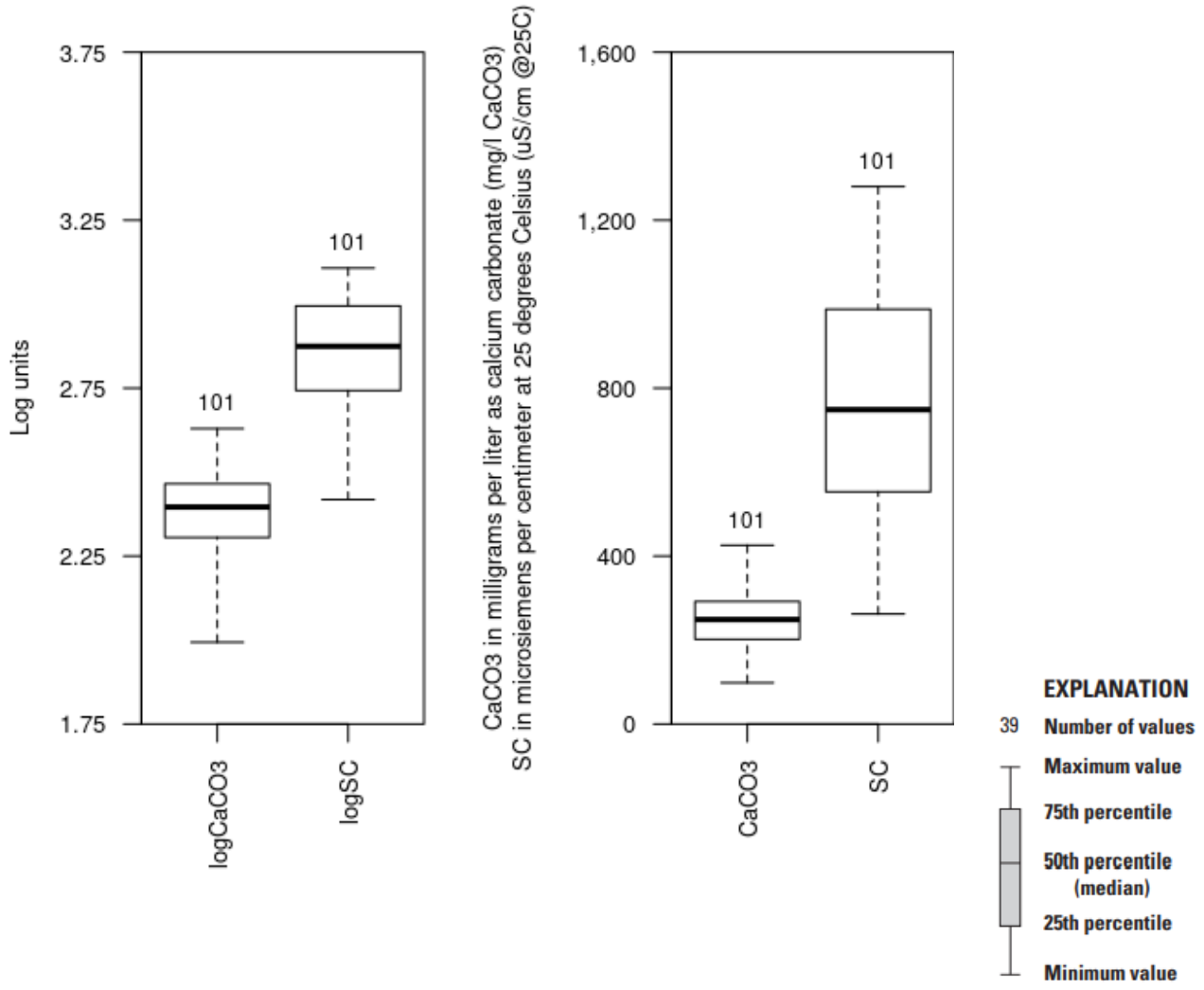
Model

logCaCO3 = + 0.723 * logSC + 0.314

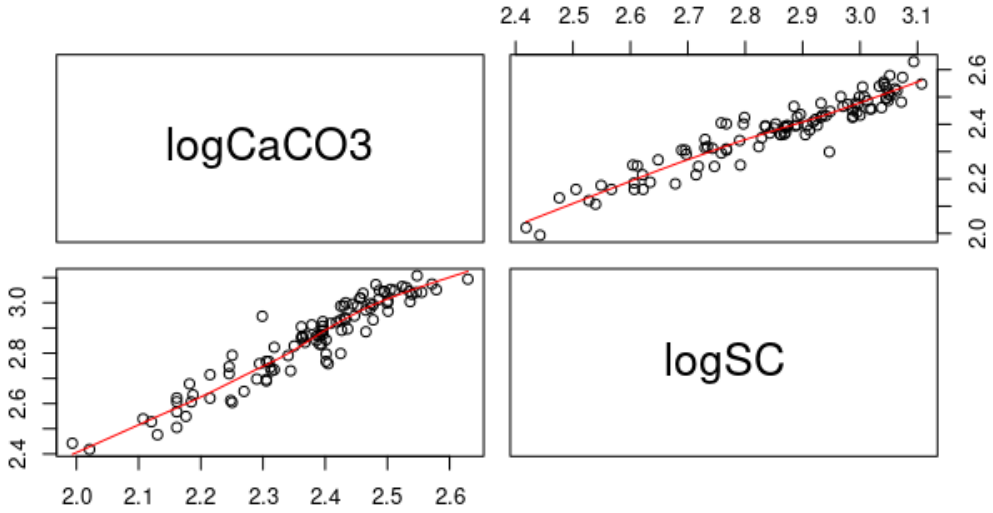
Variable Summary Statistics

	logCaCO3	CaCO3	logSC	SC
Minimum	1.99	98.5	2.42	262
1st Quartile	2.31	202.0	2.74	553
Median	2.40	249.0	2.87	749
Mean	2.38	247.0	2.85	762
3rd Quartile	2.47	292.0	2.99	988
Maximum	2.63	426.0	3.11	1280

Box Plots



Exploratory Plots



Red line shows the locally weighted scatterplot smoothing (LOWESS).

The x- and y-axis labels for a given bivariate plot are defined by the intersecting row and column labels.

Basic Model Statistics

Number of Observations	101
Standard error (RMSE)	0.0406
Average Model standard percentage error (MSPE)	9.37
Coefficient of determination (R^2)	0.9
Adjusted Coefficient of Determination (Adj. R^2)	0.899
Bias Correction Factor (BCF)	1

Explanatory Variables

	Coefficients	Standard Error	t value	Pr(>|t|)
(Intercept)	0.314	0.0692	4.54	1.60e-05
logSC	0.723	0.0242	29.80	2.66e-51

Correlation Matrix

	Intercept	E.vars
Intercept	1.000	-0.998
E.vars	-0.998	1.000

Outlier Test Criteria

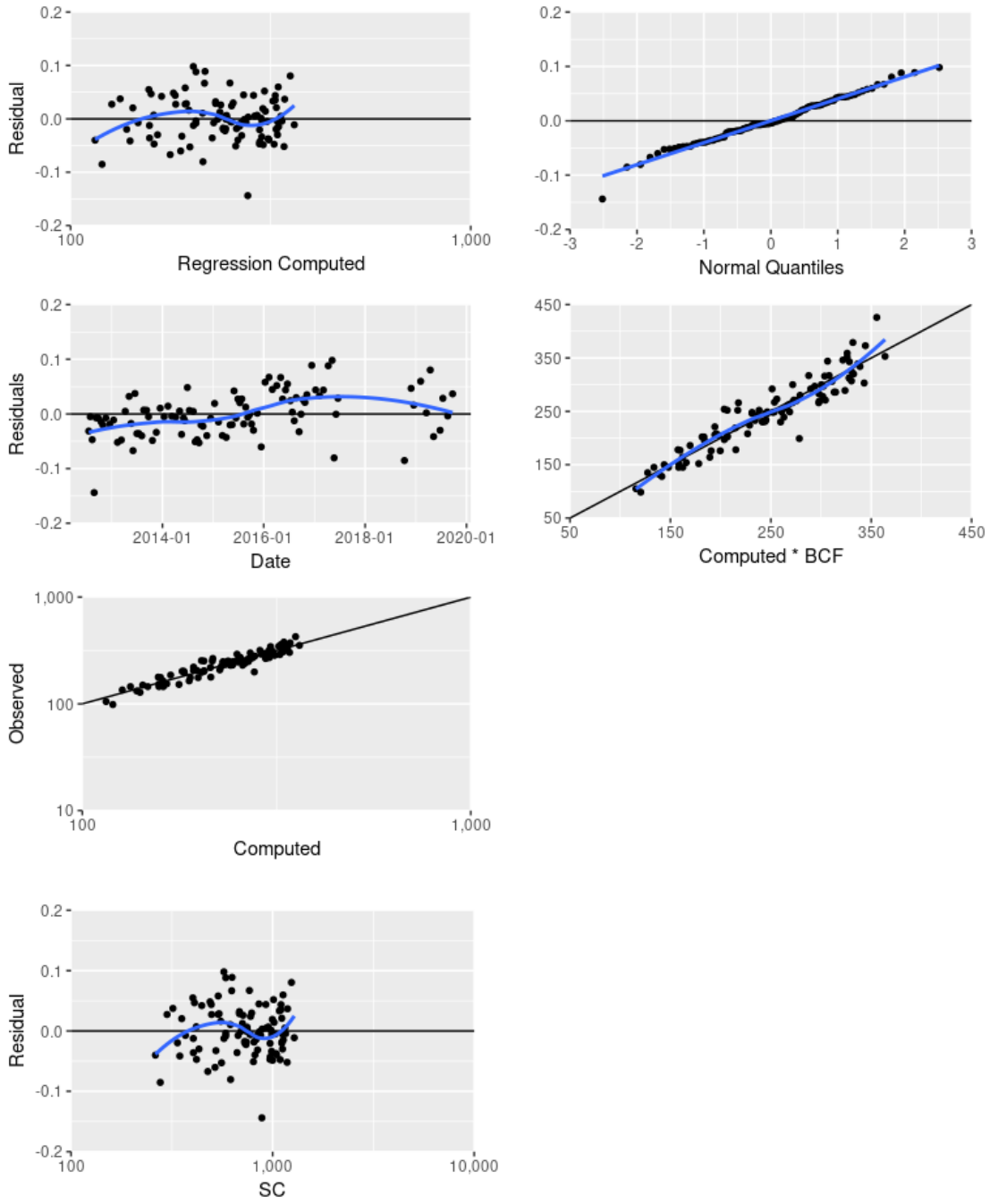
Leverage	Cook's D	DFFITS
0.0594	0.1944	0.2814

Flagged Observations

	logCaCO3	Estimate	Residual	Standard Residual	Studentized Residual	Leverage	Cook's D	DFFITS
201208271120	2.30	2.44	-0.1440	-3.570	-3.800	0.0130	0.0838	-0.436
201308050730	2.02	2.06	-0.0400	-1.020	-1.030	0.0768	0.0437	-0.296
201506290820	2.13	2.10	0.0273	0.693	0.692	0.0602	0.0154	0.175
201705080920	2.40	2.31	0.0981	2.430	2.490	0.0131	0.0391	0.287

201810110940	1.99	2.08	-0.0852	-2.170	-2.220	0.0696	0.1770	-0.606	
201904150950	2.63	2.55	0.0804	2.010	2.040	0.0304	0.0634	0.362	

Statistical Plots



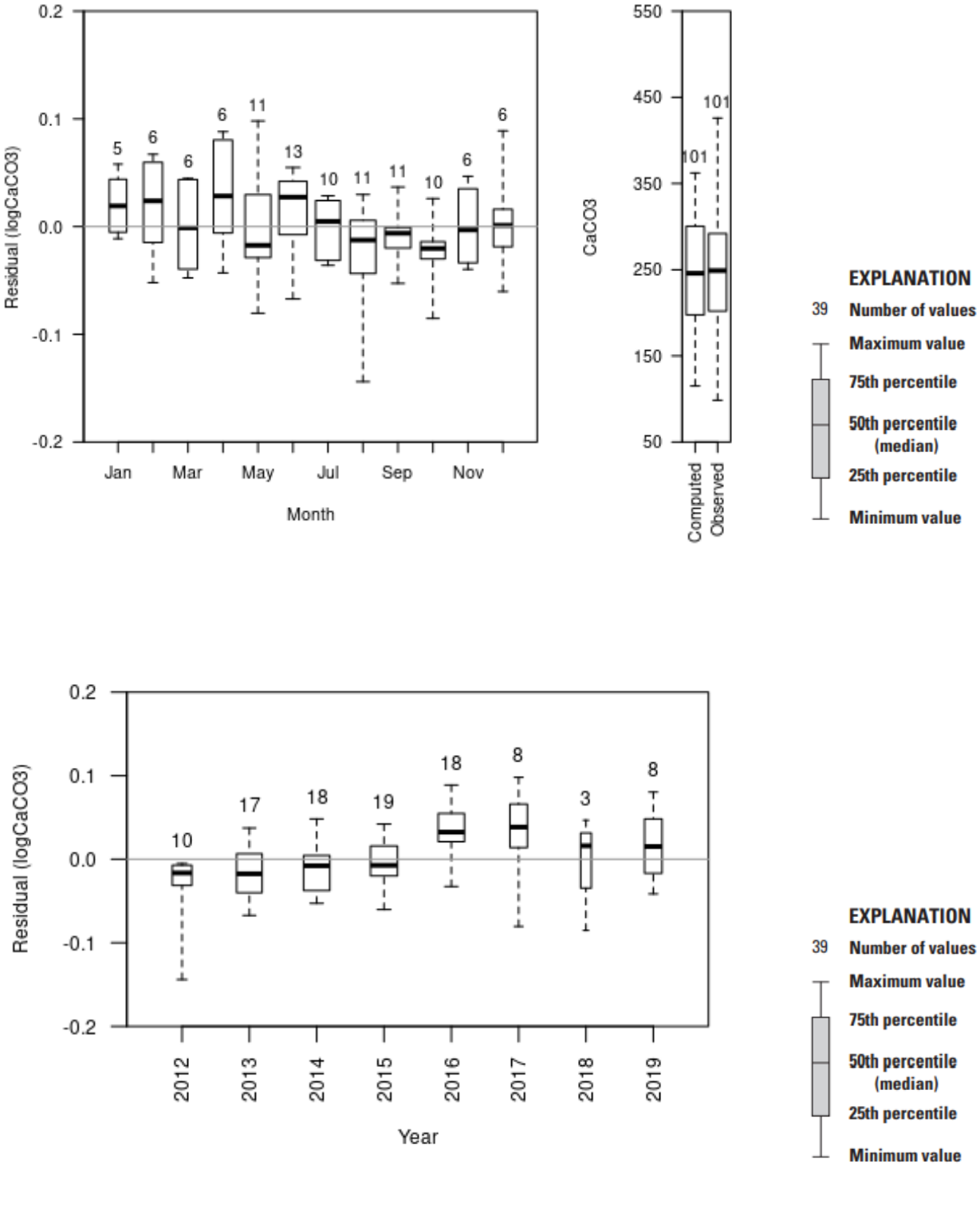
First row (left): Residual CaCO3 related to regression computed CaCO3 with local polynomial regression fitting, or locally estimated scatterplot smoothing (LOESS), indicated by the blue line.

First row (right): Residual CaCO3 related to the corresponding normal quantile of the residual with simple linear regression, indicated by the blue line.

Second row: Residual CaCO3 related to date (left) and regression computed CaCO3 multiplied by the BCF (right) with LOESS, indicated by the blue line.

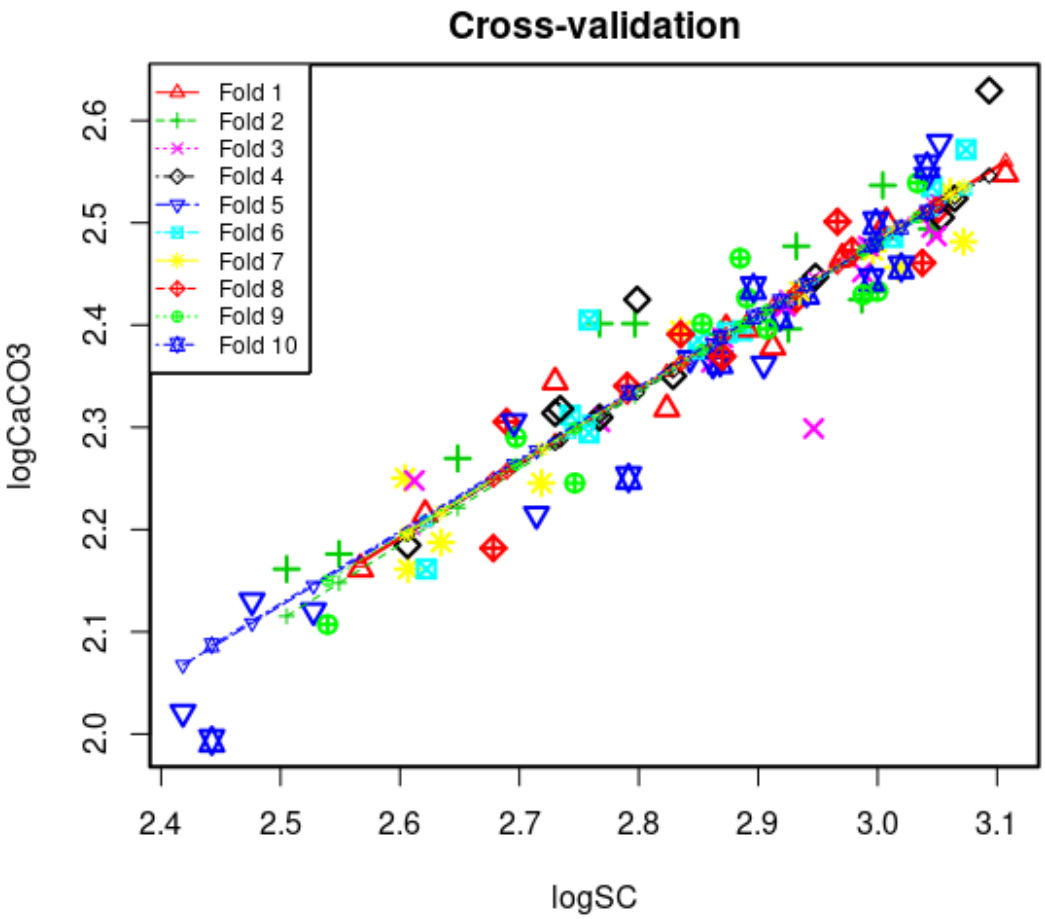
Third row: Observed CaCO3 related to regression computed CaCO3.

Fourth row: Residual CaCO3 related to SC with LOESS, indicated by the blue line.


0.2
0.1
0.0
-0.1
-0.2
Residual (logCaCO3)
5
6
6
6
11
13
10
11
11
10
6
6
Jan
Mar
May
Jul
Sep
Nov
Month
550
450
350
250
150
50
CaCO3
101
101
Computed
Observed
EXPLANATION
39
Number of values
Maximum value
75th percentile
50th percentile
(median)
25th percentile
Minimum value

0.2
0.1
0.0
-0.1
-0.2
Residual (logCaCO3)
10
17
18
19
18
8
3
8
2012
2013
2014
2015
2016
2017
2018
2019
Year
EXPLANATION
39
Number of values
Maximum value
75th percentile
50th percentile
(median)
25th percentile
Minimum value

Cross-Validation

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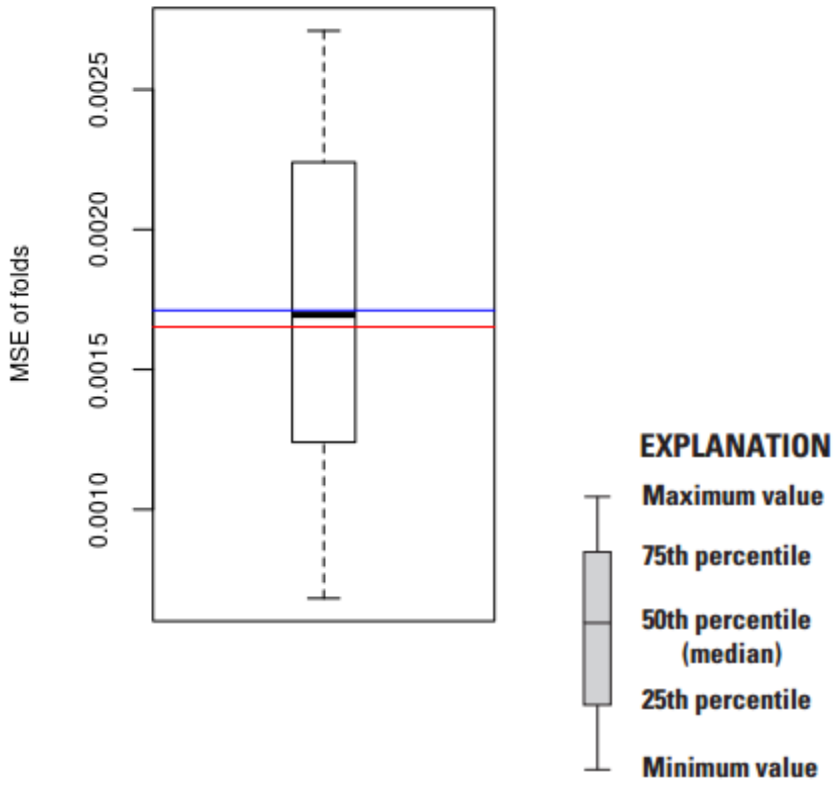
Fold - equal partition of the data (10 percent of the data).

Large symbols – observed value of a data point removed in a fold.

Small symbols – recomputed value of a data point removed in a fold.

Recomputed regression lines – adjusted regression line with one fold removed.


              Minimum MSE of folds:  0.000682
                 Mean MSE of folds:  0.001710
               Median MSE of folds:  0.001700
              Maximum MSE of folds:  0.002710
 (Mean MSE of folds) / (Model MSE):  1.040000
```



Red line - Model MSE

Blue line - Mean MSE of folds

Model-Calibration Dataset

	Date	logCaCO3	logSC	CaCO3	SC	Computed logCaCO3	Computed CaCO3	Residual	Normal Quantiles	Censored Values
1	2012-07-19	2.4	2.93	249	842	2.43	269	-0.0313	-0.761	--
2	2012-07-30	2.39	2.89	248	770	2.4	252	-0.00505	-0.0248	--
3	2012-08-13	2.42	2.99	266	970	2.47	298	-0.0471	-1.2	--
4	2012-08-27	2.3	2.95	199	884	2.44	278	-0.144	-2.52	--
5	2012-09-10	2.42	2.93	266	854	2.43	272	-0.00711	-0.149	--
6	2012-09-24	2.43	2.94	270	872	2.44	276	-0.00717	-0.174	--
7	2012-10-15	2.41	2.92	256	828	2.42	266	-0.014	-0.381	--
8	2012-10-29	2.45	2.99	283	971	2.47	298	-0.0205	-0.635	--
9	2012-11-19	2.42	2.92	262	837	2.43	268	-0.00738	-0.225	--
10	2012-12-17	2.5	3.05	313	1110	2.51	328	-0.0187	-0.518	--
11	2013-01-14	2.55	3.11	353	1280	2.56	364	-0.0112	-0.302	--
12	2013-02-11	2.48	3.07	303	1180	2.53	343	-0.052	-1.51	--
13	2013-03-11	2.46	3.04	289	1090	2.51	324	-0.0477	-1.31	--
14	2013-04-08	2.53	3.06	339	1150	2.53	337	0.00483	0.225	--
15	2013-05-06	2.39	2.84	248	684	2.36	231	0.0321	0.795	--
16	2013-05-20	2.36	2.86	231	726	2.38	241	-0.0174	-0.434	--
17	2013-06-03	2.18	2.68	152	477	2.25	178	-0.0672	-1.8	--
18	2013-06-17	2.16	2.51	145	320	2.12	134	0.0374	0.939	--
19	2013-07-01	2.16	2.61	145	404	2.2	158	-0.036	-0.901	--
20	2013-07-15	2.32	2.82	208	666	2.35	227	-0.0359	-0.864	--

21	2013-08-05	2.02	2.42	105	262	2.06	116	-0.04	-1.06	--
22	2013-08-19	2.21	2.62	164	418	2.21	162	0.00705	0.328	--
23	2013-09-09	2.47	2.98	297	952	2.47	294	0.00668	0.302	--
24	2013-09-23	2.49	3.01	306	1030	2.49	311	-0.00507	-0.0496	--
25	2013-10-21	2.43	3	271	1000	2.48	304	-0.0485	-1.37	--
26	2013-11-18	2.44	2.99	278	988	2.48	302	-0.0337	-0.829	--
27	2013-12-16	2.34	2.79	219	617	2.33	215	0.0105	0.354	--
28	2014-01-13	2.51	3.05	325	1120	2.52	330	-0.00519	-0.0744	--
29	2014-02-10	2.5	3.01	317	1020	2.49	308	0.0143	0.407	--
30	2014-03-10	2.52	3.06	334	1160	2.53	339	-0.00434	0	--
31	2014-04-07	2.47	3	297	991	2.48	302	-0.00592	-0.0992	--
32	2014-05-05	2.47	2.97	292	934	2.46	290	0.0053	0.25	--
33	2014-05-19	2.46	3.02	286	1040	2.49	313	-0.0375	-0.939	--
34	2014-06-02	2.35	2.83	224	674	2.36	229	-0.00746	-0.25	--
35	2014-06-11	2.18	2.61	153	404	2.2	158	-0.0124	-0.328	--
36	2014-06-30	2.31	2.69	202	489	2.26	182	0.0483	1.25	--
37	2014-07-14	2.4	2.87	249	747	2.39	246	0.00636	0.276	--
38	2014-08-11	2.39	2.87	246	738	2.39	244	0.00461	0.199	--
39	2014-08-25	2.36	2.9	230	803	2.41	260	-0.0509	-1.44	--
40	2014-09-08	2.16	2.62	145	419	2.21	162	-0.0472	-1.25	--
41	2014-09-22	2.25	2.75	176	558	2.3	200	-0.0527	-1.6	--
42	2014-10-06	2.49	3.05	312	1110	2.51	328	-0.0201	-0.575	--
43	2014-10-20	2.36	2.87	231	738	2.39	244	-0.0226	-0.665	--
44	2014-11-17	2.38	2.91	239	817	2.42	263	-0.0397	-1.02	--
45	2014-12-15	2.31	2.77	202	585	2.31	207	-0.0081	-0.276	--
46	2015-01-12	2.5	3	316	997	2.48	304	0.0192	0.462	--
47	2015-02-09	2.51	3.05	320	1130	2.52	332	-0.0147	-0.407	--
48	2015-03-09	2.46	3.02	286	1050	2.5	315	-0.0395	-0.978	--
49	2015-04-06	2.43	2.99	269	972	2.47	298	-0.0429	-1.15	--
50	2015-05-04	2.36	2.86	230	728	2.38	242	-0.0202	-0.605	--
51	2015-05-18	2.12	2.53	132	337	2.14	139	-0.0196	-0.546	--
52	2015-06-01	2.27	2.65	186	445	2.23	170	0.0421	0.978	--
53	2015-06-15	2.16	2.57	145	369	2.17	148	-0.0073	-0.199	--
54	2015-06-29	2.13	2.48	135	299	2.1	127	0.0273	0.635	--
55	2015-07-13	2.18	2.55	150	354	2.16	144	0.0204	0.489	--
56	2015-07-27	2.31	2.73	206	537	2.29	194	0.0275	0.665	--
57	2015-08-10	2.37	2.87	234	741	2.39	245	-0.0184	-0.462	--
58	2015-08-24	2.39	2.85	243	708	2.37	237	0.0125	0.381	--
59	2015-09-08	2.4	2.89	249	777	2.4	254	-0.00614	-0.124	--
60	2015-09-21	2.43	2.93	271	860	2.43	273	-0.00122	0.0496	--
61	2015-10-05	2.4	2.91	249	808	2.41	261	-0.0184	-0.489	--
62	2015-10-19	2.49	3.05	307	1120	2.52	330	-0.0299	-0.728	--
63	2015-11-16	2.48	2.99	300	982	2.48	300	0.00131	0.124	--
64	2015-12-14	2.21	2.71	164	518	2.28	189	-0.0603	-1.69	--
65	2016-01-11	2.34	2.73	221	537	2.29	194	0.058	1.44	--
66	2016-02-08	2.47	2.88	292	767	2.4	251	0.0671	1.69	--
67	2016-03-03	2.48	2.93	300	855	2.43	272	0.0448	1.15	--
68	2016-04-04	2.54	3	344	1010	2.48	307	0.0519	1.31	--
69	2016-05-02	2.4	2.8	252	626	2.33	217	0.0667	1.6	--
70	2016-05-16	2.29	2.7	195	498	2.26	184	0.0273	0.605	--
71	2016-06-06	2.31	2.7	202	496	2.26	183	0.0439	1.06	--
72	2016-06-20	2.25	2.6	178	402	2.2	158	0.0549	1.37	--
73	2016-07-11	2.43	2.89	267	777	2.4	254	0.0242	0.546	--
74	2016-07-25	2.45	2.95	280	887	2.44	279	0.00327	0.174	--
75	2016-08-08	2.29	2.76	197	573	2.31	204	-0.0125	-0.354	--

76	2016-08-22	2.44	2.9	273	787	2.41	256	0.0298	0.761	--
77	2016-09-12	2.25	2.72	176	523	2.28	191	-0.0326	-0.795	--
78	2016-09-26	2.39	2.87	244	742	2.39	245	-0.000485	0.0992	--
79	2016-10-11	2.4	2.85	252	713	2.38	238	0.026	0.575	--
80	2016-10-24	2.54	3.05	343	1110	2.51	328	0.021	0.518	--
81	2016-11-07	2.55	3.04	352	1100	2.51	326	0.0351	0.864	--
82	2016-12-12	2.42	2.8	266	629	2.34	218	0.0889	2.15	--
83	2017-01-09	2.5	2.97	317	925	2.46	288	0.0439	1.11	--
84	2017-02-06	2.54	3.03	346	1080	2.51	322	0.0334	0.829	--
85	2017-03-06	2.56	3.04	359	1100	2.51	326	0.0437	1.02	--
86	2017-04-10	2.4	2.77	252	585	2.31	207	0.0881	1.95	--
87	2017-05-08	2.4	2.76	254	573	2.31	204	0.0981	2.52	--
88	2017-05-22	2.25	2.79	178	619	2.33	215	-0.0804	-1.95	--
89	2017-06-05	2.37	2.84	233	696	2.37	234	-0.000586	0.0744	--
90	2017-06-19	2.39	2.84	246	684	2.36	231	0.0286	0.728	--
91	2018-10-11	1.99	2.44	98.5	277	2.08	120	-0.0852	-2.15	--
92	2018-11-28	2.25	2.61	177	409	2.2	160	0.0468	1.2	--
93	2018-12-17	2.31	2.74	205	553	2.3	198	0.0161	0.434	--
94	2019-02-05	2.58	3.05	379	1130	2.52	332	0.0597	1.51	--
95	2019-03-18	2.39	2.87	247	749	2.39	247	0.00202	0.149	--
96	2019-04-15	2.63	3.09	426	1240	2.55	356	0.0804	1.8	--
97	2019-05-09	2.11	2.54	128	346	2.15	141	-0.0415	-1.11	--
98	2019-06-25	2.19	2.63	154	431	2.22	166	-0.0299	-0.696	--
99	2019-07-15	2.32	2.73	208	542	2.29	196	0.0286	0.696	--
100	2019-08-19	2.31	2.77	204	585	2.31	207	-0.00364	0.0248	--
101	2019-09-23	2.57	3.07	373	1190	2.53	344	0.0368	0.901	--

Definitions

CaCO3: Total hardness, in milligrams per liter as calcium carbonate (00900).

Cook's D: Cook's distance (Helsel and others, 2020).

DFFITS: Difference in fits statistic (Helsel and others, 2020).

E.vars: Explanatory variables.

Leverage: An outlier's measure in the x direction (Helsel and others, 2020).

LOESS: Local polynomial regression fitting, or locally estimated scatterplot smoothing (Helsel and others, 2020).

LOWESS: Locally weighted scatterplot smoothing (Cleveland, 1979; Helsel and others, 2020).

MSE: Model standard error (Helsel and others, 2020).

MSPE: Model standard percentage error (Helsel and others, 2020).

Probability(>|t|): The probability that the independent variable has no effect on the dependent variable (Helsel and others, 2020).

RMSE: Root mean square error (Helsel and others, 2020).

SC: Specific conductance, in microsiemens per centimeter at 25 degrees Celsius (00095).

t value: Student's t value; the coefficient divided by its associated standard error (Helsel and others, 2020).

References Cited

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