

# Appendix 15. Model Archival Summary for Nitrate plus Nitrite Concentration at U.S. Geological Survey Site 06887500, Kansas River at Wamego, Kansas, during June 2014 through September 2019

This model archival summary summarizes the nitrate plus nitrite (NO<sub>x</sub>; U.S. Geological Survey [USGS] parameter code 00631) concentration model developed to compute 15-minute NO<sub>x</sub> concentrations from June 2014 onward. This model supersedes all previous models.

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## Site and Model Information

Site number: 06887500

Site name: Kansas River at Wamego, Kansas

Location: Lat 39°11'54", long 96°18'19" referenced to North American Datum of 1927, in SW 1/4 NW 1/4 SE 1/4 sec.9, T.10 S., R.10 E., Pottawatomie County, Kans., hydrologic unit 10270102.

Equipment: A YSI 6600 water-quality monitor equipped with sensors for water temperature, specific conductance (SC), dissolved oxygen, pH, and turbidity was installed from August 2012 through June 2014. A Xylem YSI EXO2 water-quality monitor equipped with sensors for water temperature, SC, dissolved oxygen, pH, turbidity, and chlorophyll (fCHL) and phycocyanin fluorescence was installed during June 2014 through September 2019. The monitor was housed in a 4-inch-diameter galvanized steel pipe. Readings from the water-quality monitor were recorded every 15 minutes and transmitted by way of satellite, hourly.

Date model was created: March 31, 2020

Model calibration data period: June 11, 2014, through September 23, 2019

Model application date: June 11, 2014, onward

## Model-Calibration Dataset

All data were collected using USGS protocols (Wagner and others, 2006; U.S. Geological Survey, variously dated) and are stored in the National Water Information System (U.S. Geological Survey, 2020) database and available to the public. Ordinary least squares analysis was used to develop regression models using R programming language (R Core Team, 2020). Potential explanatory variables that were evaluated individually and in combination included streamflow, water temperature, SC, dissolved oxygen, pH, turbidity, fCHL, and phycocyanin fluorescence. The maximum time span between two continuous data points used for interpolation was 2 hours (in order to preserve the sample dataset, field monitor averages obtained during sample collection were used for model development data if no continuous data were available or if gaps larger than 1 hour in the continuous data record resulted in missing interpolated data). Seasonal components (sine and cosine variables) were also evaluated as potential explanatory variables.

The final selected regression model was based on 73 concurrent measurements of NO<sub>x</sub> concentration, sensor-measured SC, fCHL, and seasonal components (sine and cosine variables) during June 11, 2014, through September 23, 2019. Samples were collected throughout the range of continuously observed hydrologic conditions. No samples had concentrations below laboratory detection limits. Summary statistics and the complete model-calibration dataset are provided below. Potential outliers were identified using the methods described in Rasmussen and others (2009). Additionally, studentized residuals from the final model were inspected for values greater than three or less than negative three. Values outside of that range were considered potential outliers and were investigated. One of the sensor-measured SC samples, from July 28, 2014, was deemed an outlier and removed from the model calibration dataset. The removed sensor-measured SC value was significantly lower than the field monitor and laboratory result during this sample. All other potential outliers were not found to have errors associated with collection, processing, or analysis and were therefore considered valid.

This model is specific to the Kansas River at Wamego, Kans., during this study period and cannot be applied to data collected from other sites on the Kansas River or data collected from other waterbodies.

## Nitrate plus Nitrite Sampling Details

Cross-section samples typically were collected either from the downstream side of the bridge or instream within 100 feet of the bridge. The equal-width-increment collection method was used (although multiple vertical, single vertical, and grab samples were occasionally collected), and samples typically were composited for analysis (U.S. Geological Survey, variously dated). During July 2012 through June 2017, cross-section samples were collected every 2 weeks during March through October, once a month during

November through February, and during selected reservoir release and runoff events. During July 2017 through September 2019, cross-section samples were collected on a monthly to bimonthly basis, depending on flow conditions. A FISP US DH–81, DH–95, D–95, D–96a, or D–96 depth integrating sampler was used. Additional detail on sample collection is available in Foster and Graham (2016) and Graham and others (2018). Samples were analyzed for NO<sub>x</sub> concentration at the USGS National Water Quality Laboratory in Lakewood, Colorado.

## Model Development

Ordinary least squares regression analysis was done using R programming language (R Core Team, 2020) to relate discretely collected NO<sub>x</sub> concentration to sensor-measured SC, fCHL, and seasonal components (sine and cosine variables). The distribution of residuals was examined for normality, and the plots of residuals (the difference between the measured and computed values) were examined for homoscedasticity (departures from zero did not change substantially over the range of computed values). Previously published explanatory variables were also strongly considered for continuity.

SC, fCHL, and seasonal components (sine and cosine variables) were selected as good surrogates for NO<sub>x</sub> based on residual plots, coefficient of determination ( $R^2$ ), and model standard percentage error. Values for all the aforementioned statistics were computed and are included below along with all relevant sample data and additional statistical information.

## Model Summary

The following is a summary of final regression analysis for NO<sub>x</sub> concentration at USGS site 06887500:

NO<sub>x</sub> concentration-based model:

$$NO_x = -0.00065 \times SC - 0.0995 \times fCHL + 0.163 \times \sin(2\pi D) - 0.0823 \times \cos(2\pi D) + 1.77$$

where

$NO_x$  = nitrate plus nitrite concentration, in milligrams per liter;

$SC$  = specific conductance, in microsiemens per centimeter at 25 degrees Celsius;

$fCHL$  = chlorophyll fluorescence, in relative fluorescence units;

$\sin$  = sine;

$D$  = date, in decimal years; and

$\cos$  = cosine.

SC makes physical and statistical sense as an explanatory variable for NO<sub>x</sub> because of its correlation with charged ionic species, such as NO<sub>x</sub> (Hem, 1992). fCHL also was used as an explanatory variable in the model previously published by Foster and Graham (2016). Seasonal components (sine and cosine variables) are a logical addition to the model because NO<sub>x</sub> increases are often associated with precipitation runoff events in the Kansas River.

## Previous Models

Start Year	End Year	Model Equation	Reference
2012	2019	$NO_x = -0.00102SC - 0.0176fCHL + 1.85$	Foster and Graham (2016)
1999	2003	$NO_x = 1.09\log Q - 0.397\log WT - 2.53$  where Q = streamflow, in cubic feet per second; and, WT = water temperature, in degrees Celsius	Rasmussen and others (2005)

# Model Statistics, Data, and Plots

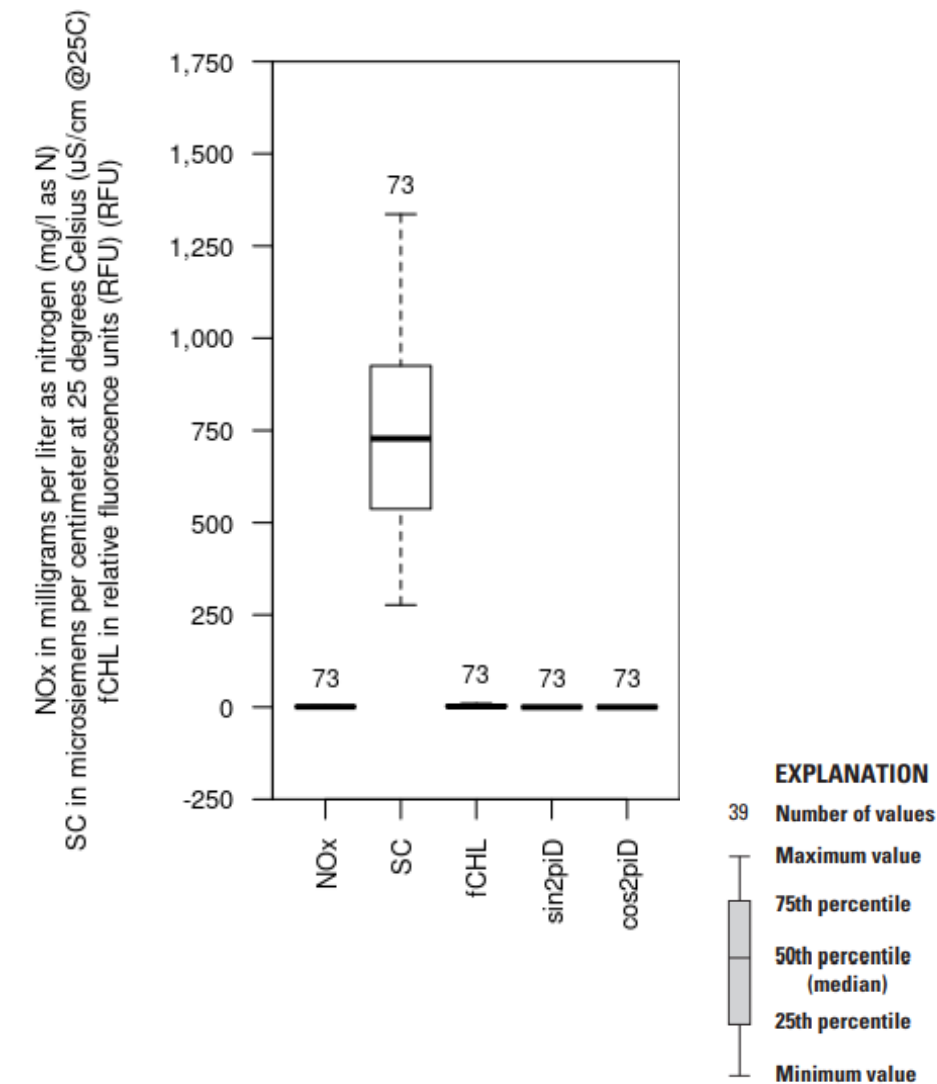
## Model

$$\text{NOx} = -0.00065 * \text{SC} - 0.0995 * \text{fCHL} + 0.163 * \text{sin2piD} - 0.0823 * \text{cos2piD} + 1.77$$

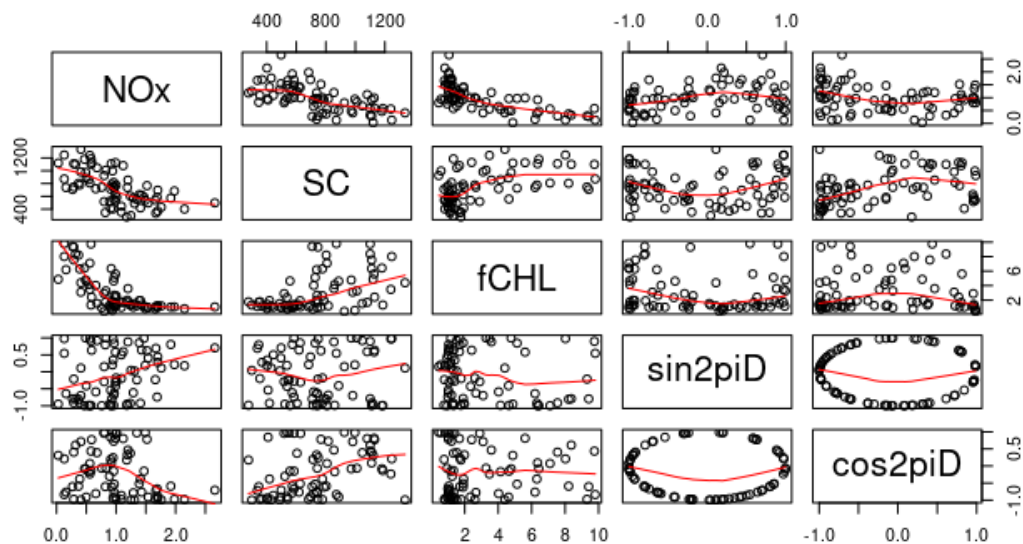
## Variable Summary Statistics

	NOx	SC	fCHL	sin2piD	cos2piD
Minimum	0.030	277	0.44	-0.9980	-1.000
1st Quartile	0.580	537	1.15	-0.7910	-0.809
Median	0.960	728	1.77	-0.1970	-0.234
Mean	0.988	737	3.06	-0.0876	-0.175
3rd Quartile	1.310	925	4.62	0.5950	0.390
Maximum	2.660	1340	9.80	0.9980	0.988

## Box Plots



## Exploratory Plots



Red line shows the locally weighted scatterplot smoothing (LOWESS).

The x- and y-axis labels for a given bivariate plot are defined by the intersecting row and column labels.

## Basic Model Statistics

Number of Observations 73  
 Standard error (RMSE) 0.326  
 Average Model standard percentage error (MSPE) 33  
 Coefficient of determination ( $R^2$ ) 0.636  
 Adjusted Coefficient of Determination (Adj.  $R^2$ ) 0.615

Variance Inflation Factors (VIF)

	SC	fCHL	sin2piD	cos2piD
	1.71	1.50	1.05	1.25

## Explanatory Variables

	Coefficients	Standard Error	t value	Pr(> t )
(Intercept)	1.77000	0.128000	13.80	2.02e-21
SC	-0.00065	0.000188	-3.45	9.78e-04
fCHL	-0.09950	0.017900	-5.56	4.82e-07
sin2piD	0.16300	0.055500	2.94	4.45e-03
cos2piD	-0.08230	0.062500	-1.32	1.93e-01

## Correlation Matrix

	Intercept	SC	fCHL	sin2piD	cos2piD
Intercept	1.000	-0.886	0.217	0.136	0.456
SC	-0.886	1.000	-0.567	-0.162	-0.442
fCHL	0.217	-0.567	1.000	0.204	0.266
sin2piD	0.136	-0.162	0.204	1.000	0.116
cos2piD	0.456	-0.442	0.266	0.116	1.000

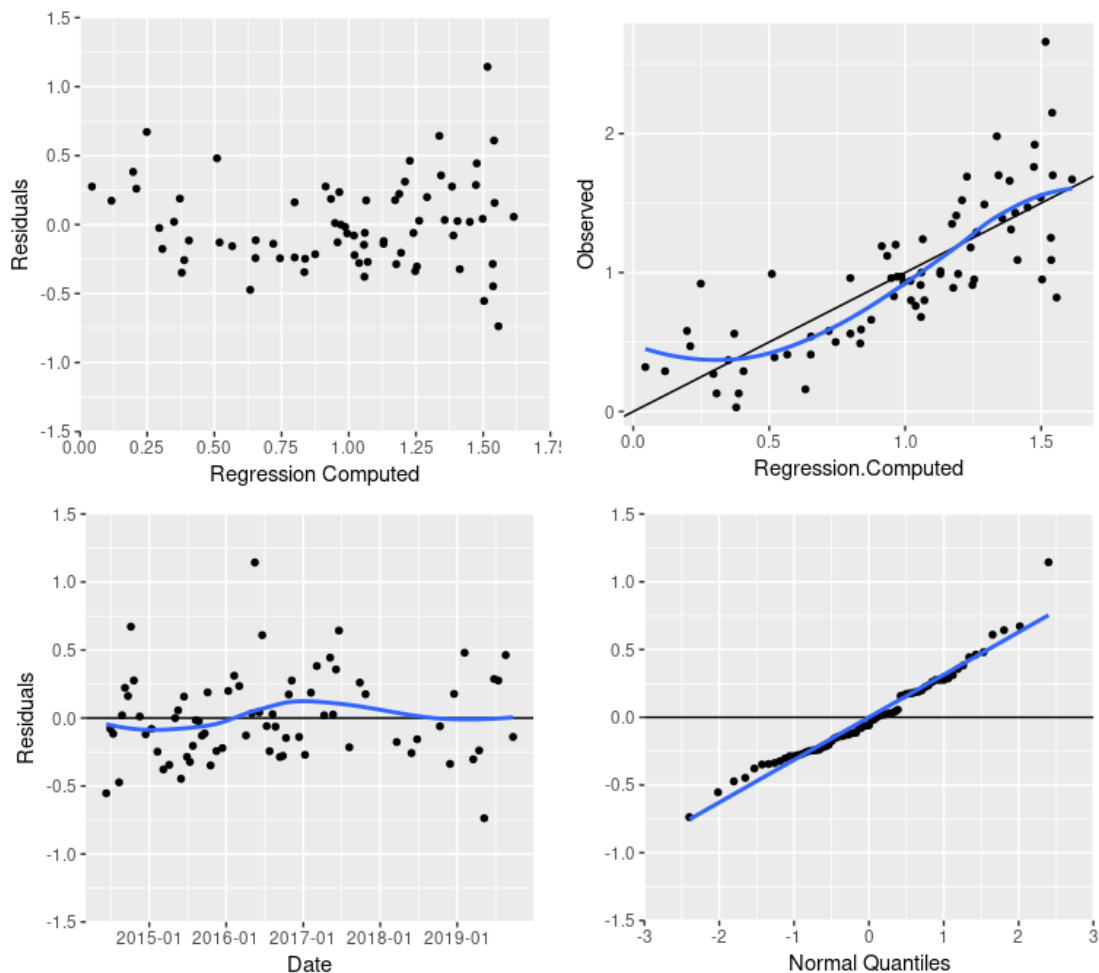
## Outlier Test Criteria

Leverage	Cook's D	DFFITS
0.205	0.363	0.523

## Flagged Observations

	NOx Estimate	Residual	Standard Residual	Studentized Residual	Leverage	Cook's D	DFFITS
201410060900	0.92	0.249	0.671	2.13	2.19	0.0678	0.0661
201605160850	2.66	1.520	1.140	3.59	3.96	0.0466	0.1260
201703060950	0.58	0.198	0.382	1.28	1.29	0.1660	0.0658
201905091520	0.82	1.560	-0.737	-2.34	-2.43	0.0710	0.0839

## Statistical Plots

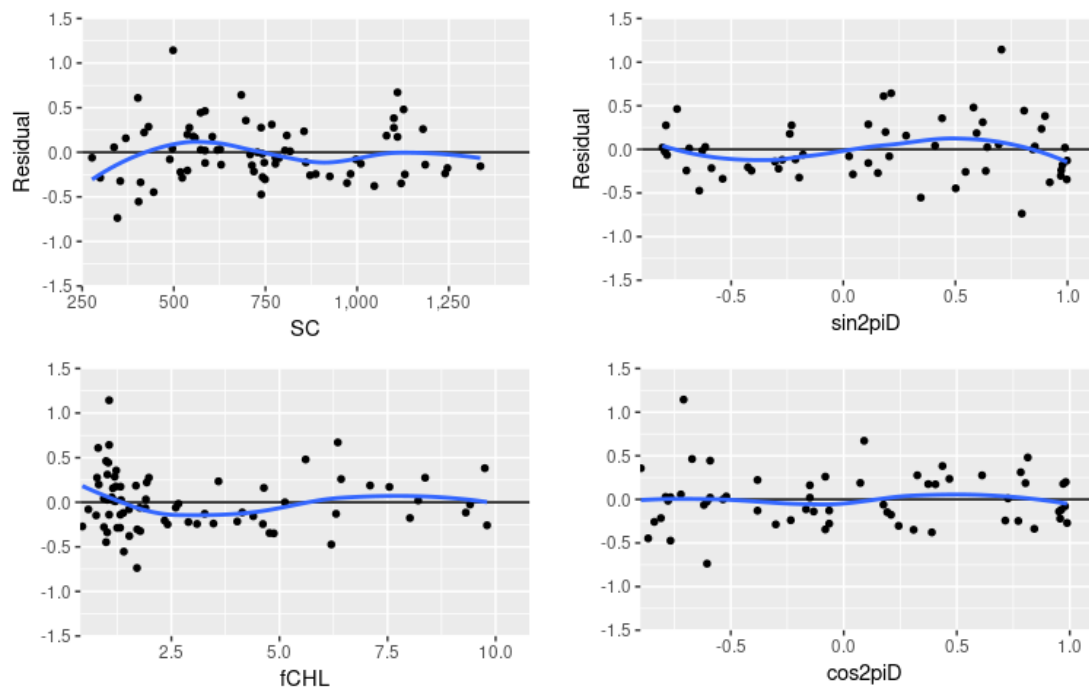


**First row (left):** Residual NOx related to regression computed NOx.

**First row (right):** Observed NOx related regression computed NOx with local polynomial regression fitting, or locally estimated scatterplot smoothing (LOESS), indicated by the blue line.

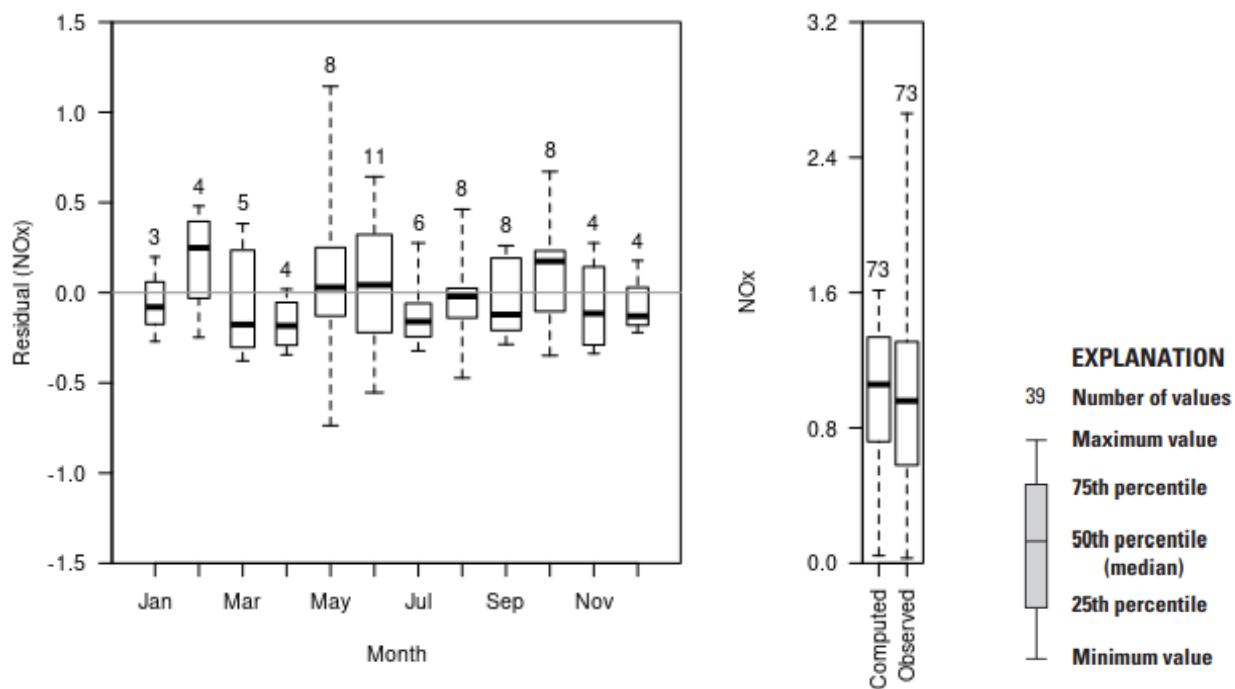
**Second row (left):** Residual NOx related to date with LOESS, indicated by the blue line.

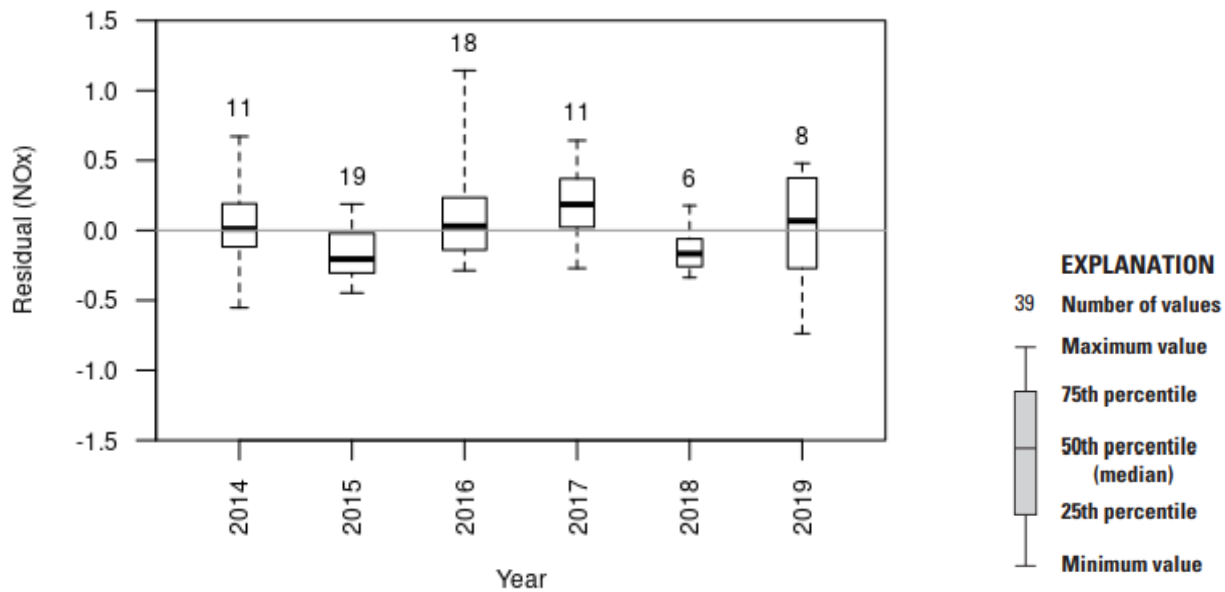
**Second row (right):** Residual NOx related to the corresponding normal quantile of the residual with simple linear regression, indicated by the blue line.



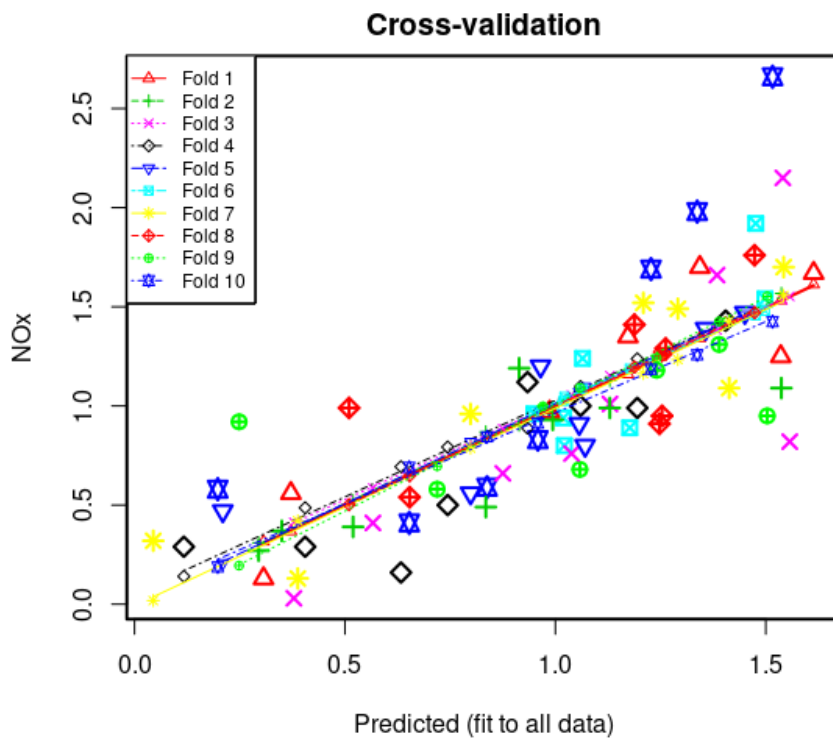
**First row:** Residual NOx related to SC (left) and sin2piD (right) with LOESS, indicated by the blue line.

**Second row:** Residual NOx related to fCHL (left) and cos2piD (right) with LOESS, indicated by the blue line.





## Cross-Validation



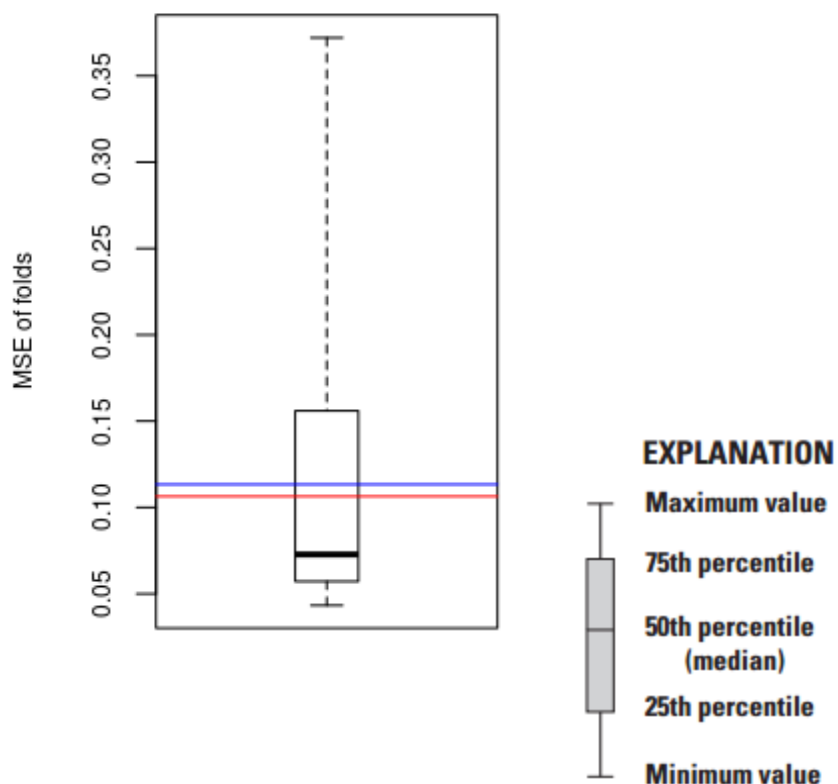
Fold - equal partition of the data (10 percent of the data).

Large symbols - observed value of a data point removed in a fold.

Small symbols - recomputed value of a data point removed in a fold.

Recomputed regression lines - adjusted regression line with one fold removed.

Minimum MSE of folds: 0.0433  
Mean MSE of folds: 0.1130  
Median MSE of folds: 0.0728  
Maximum MSE of folds: 0.3720  
(Mean MSE of folds) / (Model MSE): 1.0700



Red line - Model MSE

Blue line - Mean MSE of folds

### Model-Calibration Dataset

	Date	NOx	SC	fCHL	sin2piD	cos2piD	Computed NOx	Residual	Normal Quantiles	Censored Values
0										
1	2014-06-11	0.95	404	1.4	0.346	-0.938	1.5	-0.553	-2.02	--
2	2014-06-30	1.31	489	1.52	0.0258	-1	1.39	-0.0792	-0.103	--
3	2014-07-14	0.29	747	9.31	-0.214	-0.977	0.405	-0.115	-0.207	--
4	2014-08-11	0.16	738	6.2	-0.642	-0.767	0.633	-0.473	-1.81	--
5	2014-08-25	0.37	803	8.21	-0.806	-0.591	0.35	0.0202	0.207	--
6	2014-09-08	1.41	419	1.93	-0.924	-0.382	1.19	0.222	0.75	--
7	2014-09-22	0.96	558	4.64	-0.989	-0.15	0.798	0.162	0.461	--
8	2014-10-06	0.92	1110	6.35	-0.996	0.0903	0.249	0.671	2.02	--
9	2014-10-20	1.19	738	1.98	-0.946	0.325	0.914	0.276	1	--
10	2014-11-17	0.96	817	1.21	-0.687	0.727	0.949	0.0112	0.137	--
11	2014-12-15	1.01	585	1.39	-0.272	0.962	1.13	-0.12	-0.242	--
12	2015-01-12	0.94	997	0.58	0.205	0.979	1.02	-0.0795	-0.137	--
13	2015-02-09	0.59	1130	2.41	0.635	0.772	0.838	-0.248	-0.796	--
14	2015-03-09	0.68	1050	1.53	0.921	0.39	1.06	-0.378	-1.53	--
15	2015-04-06	0.49	972	4.77	0.997	-0.0817	0.835	-0.345	-1.34	--
16	2015-05-04	0.97	728	5.13	0.845	-0.534	0.97	-0.000498	0.103	--
17	2015-05-18	1.67	337	1.12	0.693	-0.721	1.61	0.0562	0.386	--
18	2015-06-01	1.09	445	0.99	0.501	-0.865	1.54	-0.447	-1.65	--
19	2015-06-15	1.7	369	1.15	0.28	-0.96	1.54	0.157	0.423	--
20	2015-06-29	1.25	299	1.31	0.043	-0.999	1.54	-0.286	-1	--

21	2015-07-13	1.09	354	1.78	-0.197	-0.98	1.41	-0.323	-1.19	--
22	2015-07-27	0.99	537	2.34	-0.425	-0.905	1.19	-0.205	-0.539	--
23	2015-08-10	0.97	741	2.66	-0.629	-0.778	0.986	-0.0163	0.0685	--
24	2015-08-24	0.27	708	9.41	-0.796	-0.605	0.295	-0.0249	0.0343	--
25	2015-09-08	0.39	777	6.31	-0.924	-0.382	0.519	-0.129	-0.313	--
26	2015-09-21	0.54	860	4.14	-0.986	-0.167	0.654	-0.114	-0.172	--
27	2015-10-05	0.56	808	7.1	-0.997	0.0731	0.372	0.188	0.662	--
28	2015-10-19	0.03	1120	4.87	-0.951	0.309	0.379	-0.349	-1.43	--
29	2015-11-16	0.41	982	3.09	-0.699	0.715	0.653	-0.243	-0.705	--
30	2015-12-14	0.8	518	2.89	-0.288	0.957	1.02	-0.221	-0.62	--
31	2016-01-11	1.49	537	0.82	0.188	0.982	1.29	0.199	0.705	--
32	2016-02-08	1.52	767	1.02	0.622	0.783	1.21	0.311	1.12	--
33	2016-03-03	1.2	855	3.59	0.884	0.467	0.965	0.235	0.796	--
34	2016-04-04	0.83	1010	3.27	0.998	-0.0645	0.958	-0.128	-0.277	--
35	2016-05-02	1.39	626	1.91	0.854	-0.52	1.36	0.033	0.313	--
36	2016-05-16	2.66	498	1.06	0.706	-0.709	1.52	1.14	2.4	--
37	2016-06-06	1.54	496	0.937	0.409	-0.912	1.5	0.0419	0.349	--
38	2016-06-20	2.15	402	0.807	0.18	-0.984	1.54	0.61	1.65	--
39	2016-07-11	1	777	2.6	-0.18	-0.984	1.06	-0.0597	0	--
40	2016-07-25	0.5	887	4.62	-0.409	-0.912	0.744	-0.244	-0.75	--
41	2016-08-08	1.29	573	1.02	-0.615	-0.788	1.26	0.028	0.277	--
42	2016-08-22	0.93	787	1.9	-0.786	-0.619	0.994	-0.0639	-0.0685	--
43	2016-09-12	0.89	523	1.25	-0.954	-0.301	1.18	-0.287	-1.06	--
44	2016-09-26	0.76	742	0.94	-0.998	-0.0645	1.04	-0.278	-0.946	--
45	2016-10-11	0.91	713	0.76	-0.981	0.192	1.06	-0.147	-0.423	--
46	2016-10-24	0.29	1110	7.54	-0.914	0.405	0.117	0.173	0.499	--
47	2016-11-07	0.32	1100	8.37	-0.791	0.612	0.0445	0.275	0.894	--
48	2016-12-12	0.99	629	1.06	-0.305	0.952	1.13	-0.139	-0.386	--
49	2017-01-09	0.8	925	0.44	0.154	0.988	1.07	-0.271	-0.894	--
50	2017-02-06	1.12	1080	1.68	0.595	0.804	0.934	0.186	0.62	--
51	2017-03-06	0.58	1100	9.75	0.9	0.437	0.198	0.382	1.26	--
52	2017-04-10	1.47	585	1.16	0.989	-0.15	1.45	0.0197	0.172	--
53	2017-05-08	1.92	573	1.04	0.806	-0.591	1.48	0.444	1.34	--
54	2017-05-22	1.43	619	1.34	0.642	-0.767	1.4	0.0253	0.242	--
55	2017-06-05	1.7	696	1.22	0.441	-0.898	1.34	0.357	1.19	--
56	2017-06-19	1.98	684	1.06	0.214	-0.977	1.34	0.643	1.81	--
57	2017-08-07	0.66	718	4.02	-0.588	-0.809	0.875	-0.215	-0.579	--
58	2017-09-26	0.47	1180	6.43	-0.997	-0.0817	0.21	0.26	0.844	--
59	2017-10-23	1.24	605	1.32	-0.928	0.374	1.06	0.175	0.539	--
60	2018-03-20	0.13	1250	8.02	0.978	0.209	0.307	-0.177	-0.499	--
61	2018-05-29	0.13	872	9.8	0.545	-0.838	0.388	-0.258	-0.844	--
62	2018-06-25	0.41	1340	4.39	0.112	-0.994	0.566	-0.156	-0.461	--
63	2018-10-11	1.18	277	1.77	-0.984	0.176	1.24	-0.0607	-0.0343	--
64	2018-11-28	0.91	409	1.02	-0.538	0.843	1.25	-0.337	-1.26	--
65	2018-12-17	1.35	553	1.22	-0.239	0.971	1.17	0.178	0.579	--
66	2019-02-05	0.99	1130	5.61	0.581	0.814	0.51	0.48	1.53	--
67	2019-03-18	0.95	749	1.71	0.97	0.243	1.25	-0.304	-1.12	--
68	2019-04-15	0.56	1240	3.47	0.972	-0.234	0.799	-0.239	-0.662	--
69	2019-05-09	0.82	346	1.7	0.796	-0.605	1.56	-0.737	-2.4	--
70	2019-06-25	1.76	431	1.19	0.112	-0.994	1.47	0.287	1.06	--
71	2019-07-15	1.66	542	0.78	-0.23	-0.973	1.38	0.276	0.946	--
72	2019-08-19	1.69	585	0.99	-0.741	-0.671	1.23	0.463	1.43	--
73	2019-09-23	0.58	1190	1.32	-0.991	-0.133	0.719	-0.139	-0.349	--

## Definitions

**D:** Date, in decimal years.

**Cook's D:** Cook's distance (Helsel and others, 2020).

**DIFFITS:** Difference in fits statistic (Helsel and others, 2020).

**E.vars:** Explanatory variables.

**fCHL:** Chlorophyll fluorescence, in relative fluorescence units (32320).

**Leverage:** An outlier's measure in the x direction (Helsel and others, 2020).

**LOESS:** Local polynomial regression fitting, or locally estimated scatterplot smoothing (Helsel and others, 2020).

**LOWESS:** Locally weighted scatterplot smoothing (Cleveland, 1979; Helsel and others, 2020).

**MSE:** Model standard error (Helsel and others, 2020).

**MSPE:** Model standard percentage error (Helsel and others, 2020).

**NOx:** Inorganic nitrogen (nitrate and nitrite), in milligrams per liter as nitrogen (00631).

**Probability(>|t|):** The probability that the independent variable has no effect on the dependent variable (Helsel and others, 2020).

**RMSE:** Root mean square error (Helsel and others, 2020).

**SC:** Specific conductance, in microsiemens per centimeter at 25 degrees Celsius (00095).

**t value:** Student's t value; the coefficient divided by its associated standard error (Helsel and others, 2020).

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