# Appendix 16. Model Archival Summary for Nitrate plus Nitrite Concentration at U.S. Geological Survey Site 06892350, Kansas River at De Soto, Kansas, during June 2013 through September 2019

This model archival summary summarizes the nitrate plus nitrite (NO<sub>x</sub>; U.S. Geological Survey [USGS] parameter code 00631) concentration model developed to compute 15-minute NO<sub>x</sub> concentrations from June 2013 onward. This model supersedes all previous models.

Any use of trade, firm, or product names is for descriptive purposes only and does not imply endorsement by the U.S. Government.

### **Site and Model Information**

Site number: 06892350

Site name: Kansas River at De Soto, Kansas

Location: Lat 38°59'00", long 94°57'52" referenced to North American Datum of 1927, in NE 1/4 SE 1/4 SE 1/4 sec.28, T.12 S.,

R.22 E., Leavenworth County, Kans., hydrologic unit 10270104.

Equipment: A YSI 6600 water-quality monitor equipped with sensors for water temperature, specific conductance, dissolved oxygen, pH, and turbidity was installed from August 2012 through June 2014. A Xylem YSI EXO2 water-quality monitor equipped with sensors for water temperature, specific conductance, dissolved oxygen, pH, turbidity, and chlorophyll and phycocyanin fluorescence was installed during June 2014 through September 2019. A Hach Nitratax plus sc sensor (sNO<sub>x</sub>; 5-millimeter path length) that monitors ultraviolet (UV) nitrate concentrations was installed from June 2013 through September 2019. The monitors were housed in side-by-side 4-inch-diameter galvanized steel pipes. Readings from the water-quality and nitrate plus nitrite monitors were recorded every 15 minutes and transmitted by way of satellite, hourly.

Date model was created: March 31, 2020

Model calibration data period: June 17, 2013, through September 24, 2019

Model application date: June 17, 2013, onward

### **Model-Calibration Dataset**

All data were collected using USGS protocols (Wagner and others, 2006; U.S. Geological Survey, variously dated) and are stored in the National Water Information System (U.S. Geological Survey, 2020) database and available to the public. Ordinary least squares analysis was used to develop regression models using R programming language (R Core Team, 2020). Potential explanatory variables that were evaluated individually and in combination included streamflow, water temperature, specific conductance, dissolved oxygen, pH, turbidity, chlorophyll and phycocyanin fluorescence, and sNO<sub>x</sub>. The maximum time span between two continuous data points used for interpolation was 2 hours (in order to preserve the sample dataset, field monitor averages obtained during sample collection were used for model development data if no continuous data were available or if gaps larger than 1 hour in the continuous data record resulted in missing interpolated data). Seasonal components (sine and cosine variables) were also evaluated as potential explanatory variables.

The final selected regression model was based on 84 concurrent measurements of NO<sub>x</sub> concentration and sensor-measured sNO<sub>x</sub> during June 17, 2013, through September 24, 2019. Samples were collected throughout the range of continuously observed hydrologic conditions. Twenty samples had concentrations below laboratory detection limits; therefore, a Tobit regression model was developed to compute estimates of linear regression model parameters using the absolute maximum likelihood estimation approach (Cohen, 1950; Hald, 1949; Helsel and others, 2020; Tobin, 1958). Summary statistics and the complete model-calibration dataset are provided below. Potential outliers were identified using the methods described in Rasmussen and others (2009). Additionally, outlier test criteria, including leverage and Cook's distance (Cook's D; Cook, 1977), were used to estimate potential outlier influence on the final Tobit regression model. One of the NO<sub>x</sub> results, from May 9, 2019, was deemed an outlier and removed from the model calibration dataset. This sample was collected during 3 hours of rapidly changing conditions due to a runoff event and may not have been representative of the associated sample time. All other potential outliers were not found to have errors associated with collection, processing, or analysis and were therefore considered valid.

This model is specific to the Kansas River at De Soto, Kans., during this study period and cannot be applied to data collected from other sites on the Kansas River or data collected from other waterbodies.

### **Nitrate plus Nitrite Sampling Details**

Cross-section samples typically were collected either from the downstream side of the bridge or instream within 100 feet of the

bridge. The equal-width-increment collection method was used (although multiple vertical, single vertical, and grab samples were occasionally collected), and samples typically were composited for analysis (U.S. Geological Survey, variously dated). During July 2012 through June 2017, cross-section samples were collected every 2 weeks during March through October, once a month during November through February, and during selected reservoir release and runoff events. During July 2017 through September 2019, cross-section samples were collected on a monthly to bimonthly basis, depending on flow conditions. A FISP US DH–81, DH–95, D–95, D–96a, or D–96 depth integrating sampler was used. Additional detail on sample collection is available in Foster and Graham (2016) and Graham and others (2018). Samples were analyzed for NO<sub>x</sub> concentration at the USGS National Water Quality Laboratory in Lakewood, Colorado.

## **Model Development**

Discretely collected  $NO_x$  was related to sensor-measured  $sNO_x$  and other continuous sensor-measured data using stepwise regression analysis in R programming language (R Core Team, 2020). The distribution of residuals was examined for normality, and the plots of residuals (the difference between the measured and computed values) were examined for homoscedasticity (departures from zero did not change substantially over the range of computed values). Previously published explanatory variables were also strongly considered for continuity.

23.8 percent of the model-calibration dataset were censored results (less than the minimum reporting level). Tobit regression models were developed using absolute maximum likelihood estimation methods to relate discretely collected NO<sub>x</sub> concentration to sensor-measured sNO<sub>x</sub>. Tobit model parameter estimates were calculated using the smwrQW(v0.7.9) package in R programming language (R Core Team, 2020).

 $sNO_x$  was selected as a good surrogate for  $NO_x$  based on residual plots, pseudocoefficient of determination (pseudo- $R^2$ ), and estimated residual standard error. Values for all the aforementioned statistics were computed and are included below along with all relevant sample data and additional statistical information.

### **Model Summary**

The following is a summary of final Tobit regression analysis for NO<sub>x</sub> concentration at USGS site 06892350:

NO<sub>x</sub> concentration-based model:

$$NO_x = 1.02 \times sNO_x - 0.325$$

where

 $NO_x$  = nitrate plus nitrite concentration, in milligrams per liter; and

 $sNO_x$  = sensor-measured nitrate plus nitrite, in milligrams per liter.

sNO<sub>x</sub> makes physical and statistical sense as an explanatory variable for NO<sub>x</sub>.

### **Previous Models**

Start Year	End Year	Model Equation	Reference
1999	2003	$NO_x = 0.914 log Q - 0.541 log WT - 2.04$	Rasmussen and others (2005)
		where	
		Q = streamflow, in cubic feet per second; and,	
		WT = water temperature, in degrees Celsius	

# **Model Statistics, Data, and Plots**

### Model

```
NO_x = +1.02 * sNO_x - 0.325
```

Computation method: Absolute Maximum Likelihood Estimation (AMLE)

# **Variable Summary Statistics**

```
NO_{\times}
Minimum
             <0.01
                     0.068
1st Ouartile 0.034
                     0.373
Median
             0.776
                     1.130
Mean
             0.667
                     1.024
3rd Ouartile 1.27
                     1.519
Maximum
        2.20 2.259
```

### **Basic Model Statistics**

```
Estimated residual standard error (unbiased)
                                                0.2209
Number of observations
                                                    84
Number censored
                                                    20 (23.8 percent)
Log-likelihood (model)
                                                -3.677
Log-likelihood (intercept only)
                                                  -146
      Chi-square
                                                 284.7
      Degrees of freedom
                                                     1
                                               <0.0001
      p-value
Pseudo-R-squared
                                                0.8975
Akaike Information Criterion
                                                 13.35
Bayesian Information Criterion
                                                 20.65
```

### **Explanatory Variables**

### Coefficients:

	Estimate	Std.	Error	z-score	p-value
(Intercept)	-0.3246	0.	05456	-5.95	0
sNO <sub>x</sub>	1.0160	0.	04269	23.80	0

### **Outlier Test Criteria**

Leverage Cook's D 0.03571 0.69897

### **Flagged Observations**

```
Observations exceeding at least one test criterion NOx ycen yhat resids leverage cooksD

1 2.03 FALSE 1.9705 0.05953 0.05688 0.002323

2 1.69 FALSE 1.7563 -0.06626 0.04284 0.002104

27 0.01 TRUE -0.2022 -0.06676 0.03596 0.001767

33 1.98 FALSE 1.7716 0.20844 0.04375 0.021311

35 0.01 TRUE -0.2558 -0.04822 0.03885 0.001002

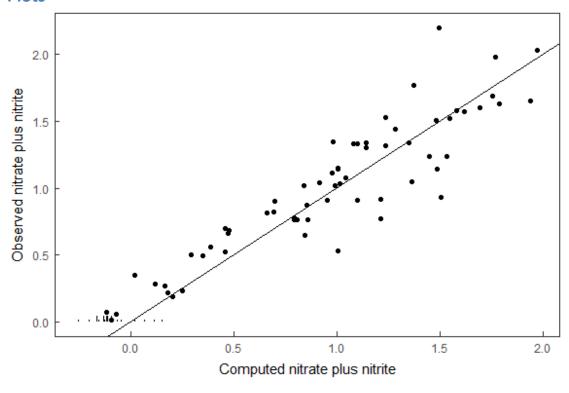
50 1.65 FALSE 1.9399 -0.28987 0.05472 0.052742

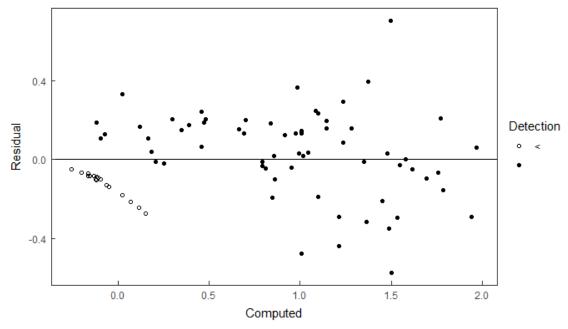
51 1.60 FALSE 1.6951 -0.09506 0.03931 0.003945

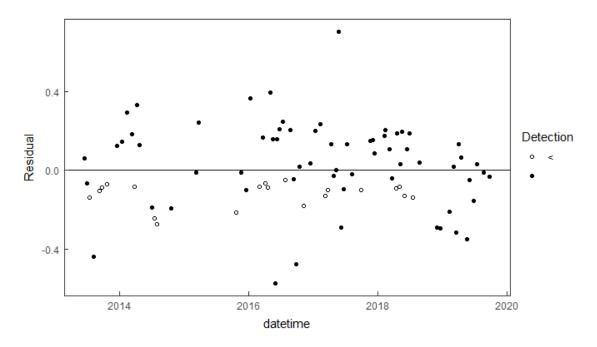
81 1.63 FALSE 1.7869 -0.15686 0.04468 0.012350
```

# **95 Percent Confidence Interval**

# **Plots**







### **Model-Calibration Dataset**

```
datetime
                            NO_{x}
                                   sNO<sub>x</sub> Computed NO<sub>x</sub>
1
   2013-06-17 12:30:00
                           2.03 2.2590
                                              1.9705
2
   2013-07-01 13:20:00
                           1.69 2.0482
                                              1.7563
   2013-07-15 10:40:00
                          <0.01 0.2711
                                             -0.0492
4
   2013-08-05 11:30:00
                          0.772 1.5135
                                              1.2131
5
   2013-09-09 10:30:00
                          <0.01 0.2033
                                             -0.1180
6
   2013-09-23 09:40:00
                          <0.04 0.2033
                                             -0.1180
7
   2013-10-21 10:30:00
                          <0.04 0.1581
                                             -0.1639
8
   2013-12-16 08:00:00
                           1.04 1.2199
                                              0.9148
9
   2014-01-13 08:00:00
                           1.15 1.3102
                                              1.0066
10 2014-02-10 07:40:00
                           1.53 1.5361
                                              1.2361
11 2014-03-10 13:40:00
                           1.02 1.1446
                                              0.8383
12 2014-03-24 12:50:00
                          <0.04 0.1883
                                             -0.1333
13 2014-04-07 11:40:00
                           0.35 0.3388
                                              0.0197
14 2014-04-21 12:00:00
                          0.057 0.2485
                                             -0.0721
15 2014-06-30 12:20:00
                           0.91 1.4006
                                              1.0984
16 2014-07-14 12:50:00
                          <0.01 0.4292
                                              0.1115
17 2014-07-28 13:50:00
                          <0.01 0.4669
                                              0.1497
18 2014-10-20 14:00:00
                           0.65 1.1521
                                              0.8459
19 2015-03-09 12:20:00
                           0.78 1.0994
                                              0.7924
20 2015-03-23 10:50:00
                          0.696 0.7681
                                              0.4557
21 2015-10-19 09:30:00
                          <0.01 0.3840
                                              0.0656
22 2015-11-16 09:10:00
                                              0.2033
                           0.19 0.5196
23 2015-12-14 15:10:00
                           0.76 1.1671
                                              0.8612
24 2016-01-11 10:10:00
                           1.35 1.2876
                                              0.9836
25 2016-03-03 09:00:00
                          <0.01 0.1581
                                             -0.1639
26 2016-03-21 10:50:00
                          0.285 0.4367
                                              0.1191
27 2016-04-04 09:20:00
                          <0.01 0.1205
                                             -0.2022
28 2016-04-18 09:30:00
                          <0.04 0.2033
                                             -0.1180
29 2016-05-02 09:30:00
                           1.77 1.6717
                                              1.3738
30 2016-05-16 09:10:00
                           1.44 1.5813
                                              1.2820
                           0.93 1.7997
31 2016-05-28 13:20:00
                                              1.5039
32 2016-06-06 11:30:00
                            1.3 1.4458
                                              1.1443
33 2016-06-20 08:20:00
                           1.98 2.0632
                                              1.7716
34 2016-07-11 08:40:00
                           1.33 1.3855
                                              1.0831
```

```
35 2016-07-25 08:30:00
                         <0.01 0.0678
                                           -0.2557
36 2016-08-22 09:00:00
                           0.5 0.6099
                                            0.2951
37 2016-09-12 08:50:00
                         0.76 1.1144
                                            0.8077
38 2016-09-26 10:30:00
                                            1.0066
                         0.53 1.3102
39 2016-10-11 09:20:00
                         0.87 1.1596
                                            0.8536
40 2016-11-07 08:40:00
                         <0.01 0.3388
                                            0.0197
41 2016-12-12 09:50:00
                         1.08 1.3479
                                            1.0448
42 2017-01-09 09:50:00
                          0.9 1.0090
                                            0.7006
43 2017-02-06 10:00:00
                         1.33 1.4006
                                            1.0984
44 2017-03-06 10:40:00
                         <0.01 0.2560
                                           -0.0645
45 2017-03-20 10:30:00
                         <0.04 0.2259
                                           -0.0951
46 2017-04-10 09:20:00
                         1.11 1.2801
                                            0.9760
47 2017-04-25 10:10:00
                         1.52 1.8449
                                            1.5498
48 2017-05-08 09:20:00
                         1.58 1.8750
                                            1.5804
49 2017-05-22 09:20:00
                          2.2 1.7921
                                            1.4962
50 2017-06-05 08:50:00
                         1.65 2.2289
                                            1.9399
                          1.6 1.9879
51 2017-06-19 09:10:00
                                            1.6951
52 2017-07-10 09:10:00
                         0.825 1.0015
                                            0.6929
53 2017-08-07 09:30:00
                         0.23 0.5647
                                            0.2492
54 2017-09-26 10:20:00
                                           -0.1257
                         < 0.01 0.1958
55 2017-11-17 14:40:00
                        0.496 0.6626
                                            0.3486
56 2017-12-01 09:00:00
                         0.814 0.9714
                                            0.6623
57 2017-12-11 10:30:00
                         1.32 1.5361
                                            1.2361
58 2018-02-05 10:00:00
                         0.56 0.7003
                                            0.3869
59 2018-02-09 09:30:00
                        0.684 0.7906
                                            0.4787
60 2018-03-05 10:10:00
                         0.27 0.4819
                                            0.1650
61 2018-03-20 08:20:00
                         0.91 1.2575
                                            0.9530
62 2018-04-11 13:00:00
                        <0.04 0.2090
                                           -0.1123
63 2018-04-16 09:30:00
                         0.07 0.2033
                                           -0.1180
64 2018-04-30 09:20:00
                         <0.01 0.1657
                                           -0.1563
65 2018-05-07 10:40:00
                         1.02 1.2952
                                            0.9913
66 2018-05-15 09:30:00
                         1.34 1.4458
                                            1.1443
67 2018-05-29 08:40:00
                        <0.01 0.2560
                                           -0.0645
68 2018-06-11 10:00:00
                         0.01 0.2259
                                           -0.0951
69 2018-06-25 07:20:00
                         0.66 0.7831
                                            0.4710
70 2018-07-16 11:00:00
                         <0.01 0.2711
                                           -0.0492
71 2018-08-21 10:40:00
                         0.22 0.4970
                                            0.1803
72 2018-11-29 12:20:00
                         0.92 1.5135
                                            1.2131
73 2018-12-18 10:40:00
                         1.24 1.8298
                                            1.5345
74 2019-02-06 10:20:00
                         1.24 1.7470
                                            1.4503
75 2019-03-06 07:50:00
                         1.03 1.3177
                                            1.0142
76 2019-03-19 09:20:00
                         1.05 1.6641
                                            1.3662
77 2019-04-01 12:00:00
                                            1.0066
                         1.14 1.3102
78 2019-04-16 09:30:00
                         0.52 0.7681
                                            0.4557
79 2019-05-20 12:30:00
                         1.14 1.7846
                                            1.4886
80 2019-06-03 10:20:00
                         1.57 1.9126
                                            1.6186
81 2019-06-26 12:30:00
                         1.63 2.0783
                                            1.7869
82 2019-07-16 10:10:00
                         1.51 1.7771
                                            1.4809
83 2019-08-20 09:20:00
                         1.34 1.6491
                                            1.3509
84 2019-09-24 09:50:00
                         0.76 1.0994
                                            0.7924
```

### **Definitions**

Cook's D: Cook's distance (Helsel and others, 2020).

Leverage: An outlier's measure in the x direction (Helsel and others, 2020).

 $NO_x$ : Inorganic nitrogen (nitrate and nitrite), in milligrams per liter as nitrogen (00631).

**p-value:** The probability that the independent variable has no effect on the dependent variable (Helsel and others, 2020).

**Pseudo-R-squared:** Pseudocoefficient of determination. An estimation of the proportion of variance in the response variable explained by the model (McKelvey and Zavoina, 1975).

 $sNO_x$ : Sensor measured inorganic nitrogen (nitrate and nitrite), in milligrams per liter as nitrogen (99133).

**z-score:** The estimated coefficient divided by its associated standard error (Helsel and others, 2020).

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