

Appendix 21. Model Archival Summary for Chlorophyll *a* Concentration at U.S. Geological Survey Site 06887500, Kansas River at Wamego, Kansas, during June 2014 through September 2019

This model archival summary summarizes the chlorophyll *a* (Chla; U.S. Geological Survey [USGS] parameter code 32209 [June 11, 2014, through September 26, 2017] or 70953 [October 23, 2017, through September 23, 2019]) concentration model developed to compute 15-minute Chla concentrations from June 2014 onward. This model supersedes all previous models.

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Site and Model Information

Site number: 06887500

Site name: Kansas River at Wamego, Kansas

Location: Lat 39°11'54", long 96°18'19" referenced to North American Datum of 1927, in SW 1/4 NW 1/4 SE 1/4 sec.9, T.10 S., R.10 E., Pottawatomie County, Kans., hydrologic unit 10270102.

Equipment: A YSI 6600 water-quality monitor equipped with sensors for water temperature, specific conductance, dissolved oxygen, pH, and turbidity was installed from August 2012 through June 2014. A Xylem YSI EXO2 water-quality monitor equipped with sensors for water temperature, specific conductance, dissolved oxygen, pH, turbidity, and chlorophyll (fCHL) and phycocyanin fluorescence was installed during June 2014 through September 2019. The monitor was housed in a 4-inch-diameter galvanized steel pipe. Readings from the water-quality monitor were recorded every 15 minutes and transmitted by way of satellite, hourly.

Date model was created: April 2, 2020

Model calibration data period: June 11, 2014, through September 23, 2019

Model application date: June 11, 2014, onward

Model-Calibration Dataset

All data were collected using USGS protocols (Wagner and others, 2006; U.S. Geological Survey, variously dated) and are stored in the National Water Information System (U.S. Geological Survey, 2020) database and available to the public. Ordinary least squares analysis was used to develop regression models using R programming language (R Core Team, 2020). Potential explanatory variables that were evaluated individually and in combination included streamflow, water temperature, specific conductance, dissolved oxygen, pH, turbidity, fCHL, and phycocyanin fluorescence. These potential explanatory variables were interpolated within the 15-minute continuous record based on sample time. The maximum time span between two continuous data points used for interpolation was 2 hours (in order to preserve the sample dataset, field monitor averages obtained during sample collection were used for model development data if no continuous data were available or if gaps larger than 1 hour in the continuous data record resulted in missing interpolated data). Seasonal components (sine and cosine variables) were also evaluated as potential explanatory variables.

The final selected regression model was based on 74 concurrent measurements of Chla concentration and sensor-measured fCHL during June 11, 2014, through September 23, 2019. Samples were collected throughout the range of continuously observed hydrologic conditions. No samples had concentrations below laboratory detection limits. Seven sample concentrations were qualified as “estimated.” Summary statistics and the complete model-calibration dataset are provided below. Potential outliers were identified using the methods described in Rasmussen and others (2009). Additionally, studentized residuals from the final model were inspected for values greater than three or less than negative three. Values outside of that range were considered potential outliers and were investigated. All potential outliers were not found to have errors associated with collection, processing, or analysis and were therefore considered valid.

This model is specific to the Kansas River at Wamego, Kans., during this study period and cannot be applied to data collected from other sites on the Kansas River or data collected from other waterbodies.

Chlorophyll *a* Sampling Details

Cross-section samples typically were collected either from the downstream side of the bridge or instream within 100 feet of the bridge. The equal-width-increment collection method was used (although multiple vertical, single vertical, and grab samples were occasionally collected), and samples typically were composited for analysis (U.S. Geological Survey, variously dated). During July 2012 through June 2017, cross-section samples were collected every 2 weeks during March through October, once a month during

November through February, and during selected reservoir release and runoff events. During July 2017 through September 2019, cross-section samples were collected on a monthly to bimonthly basis, depending on flow conditions. A FISP US DH–81, DH–95, D–95, D–96a, or D–96 depth integrating sampler was used. Additional detail on sample collection is available in Foster and Graham (2016) and Graham and others (2018). Samples were analyzed for Chla concentration at the USGS Kansas Water Science Center in Lawrence, Kans., during June 11, 2014, through September 26, 2017 (USGS parameter code 32209), and at the USGS National Water Quality Laboratory in Lakewood, Colorado during October 23, 2017, through September 23, 2019 (USGS parameter code 70953).

Model Development

Ordinary least squares regression analysis was done using R programming language (R Core Team, 2020) to relate discretely collected Chla concentration to sensor-measured fCHL. The distribution of residuals was examined for normality, and the plots of residuals (the difference between the measured and computed values) were examined for homoscedasticity (departures from zero did not change substantially over the range of computed values). Previously published explanatory variables were also strongly considered for continuity.

fCHL was selected as a good surrogate for Chla based on residual plots, coefficient of determination (R^2), and model standard percentage error. Values for all the aforementioned statistics were computed and are included below along with all relevant sample data and additional statistical information.

Model Summary

The following is a summary of final regression analysis for Chla concentration at USGS site 06887500:

Chla concentration-based model:

$$\log Chla = 1.28 \times \log fCHL + 0.699$$

where

\log = logarithm base 10;

$Chla$ = chlorophyll *a* concentration, in micrograms per liter; and

$fCHL$ = chlorophyll fluorescence, in relative fluorescence units.

fCHL makes physical and statistical sense as an explanatory variable for Chla because chlorophyll *a* pigments fluoresce when irradiated by certain wavelengths of light emitted from the fCHL sensor.

The logarithmically (\log) transformed model may be retransformed to the original units so that Chla can be calculated directly. The retransformation introduces a bias in the calculated constituent. This bias may be corrected using Duan's bias correction factor (BCF; Duan, 1983). For this model, the calculated BCF is 1.09. The retransformed model, accounting for BCF is as follows:

$$Chla = 1.09 \times (fCHL^{1.28} \times 10^{0.699})$$

Previous Models

There are no previously published models for hardness as calcium carbonate at this site.

Model Statistics, Data, and Plots

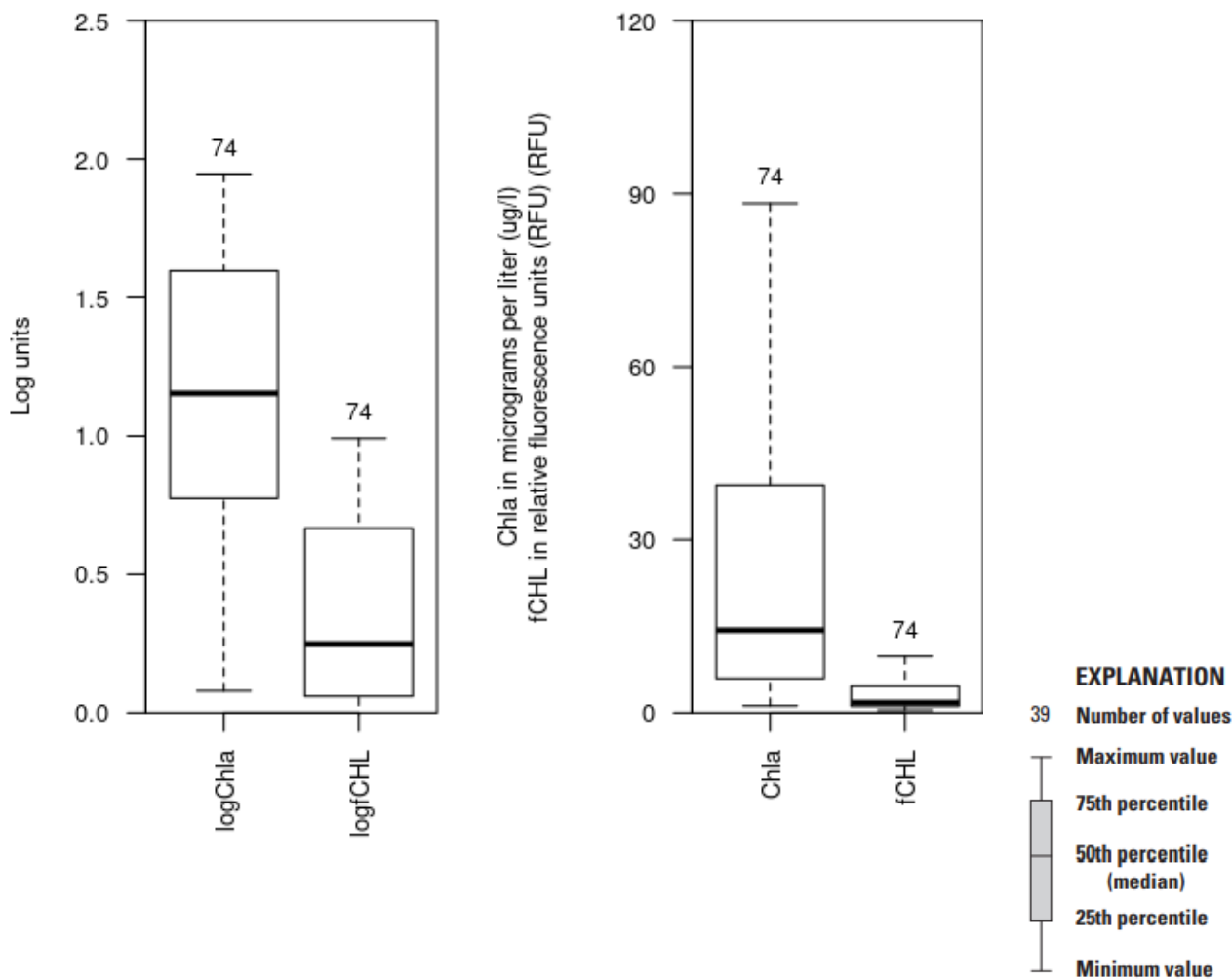
Model

$\text{logChla} = + 1.28 * \text{logfCHL} + 0.699$

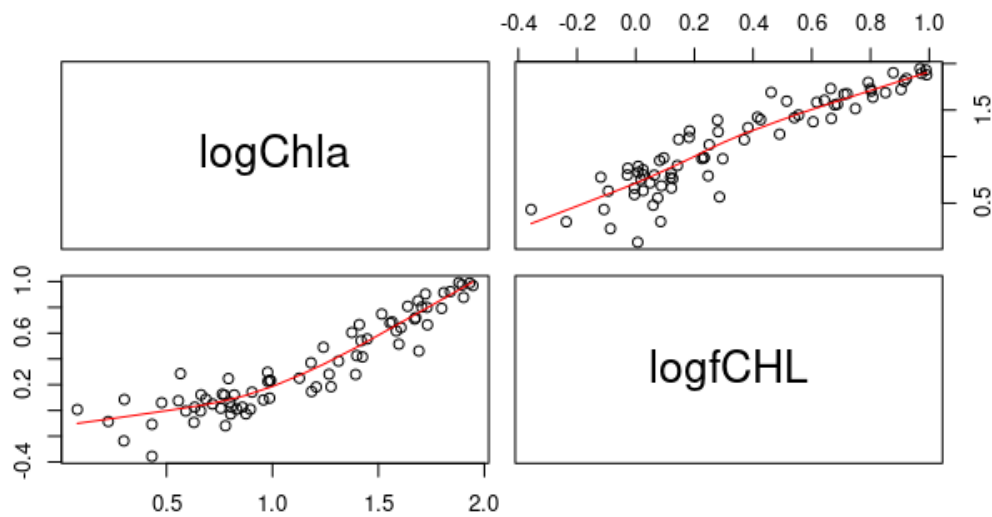
Variable Summary Statistics

	logChla	Chla	logfCHL	fCHL
Minimum	0.0792	1.20	-0.3570	0.44
1st Quartile	0.7750	5.95	0.0594	1.15
Median	1.1500	14.30	0.2490	1.77
Mean	1.1400	24.20	0.3460	3.09
3rd Quartile	1.6000	39.50	0.6670	4.64
Maximum	1.9500	88.30	0.9910	9.80

Box Plots



Exploratory Plots



Red line shows the locally weighted scatterplot smoothing (LOWESS).

The x- and y-axis labels for a given bivariate plot are defined by the intersecting row and column labels.

Basic Model Statistics

Number of Observations	74
Standard error (RMSE)	0.189
Average Model standard percentage error (MSPE)	44.9
Coefficient of determination (R^2)	0.854
Adjusted Coefficient of Determination (Adj. R^2)	0.852
Bias Correction Factor (BCF)	1.09

Explanatory Variables

	Coefficients	Standard Error	t value	Pr(> t)
(Intercept)	0.699	0.0308	22.7	1.63e-34
logfCHL	1.280	0.0625	20.5	7.76e-32

Correlation Matrix

	Intercept	E.vars
Intercept	1.000	-0.702
E.vars	-0.702	1.000

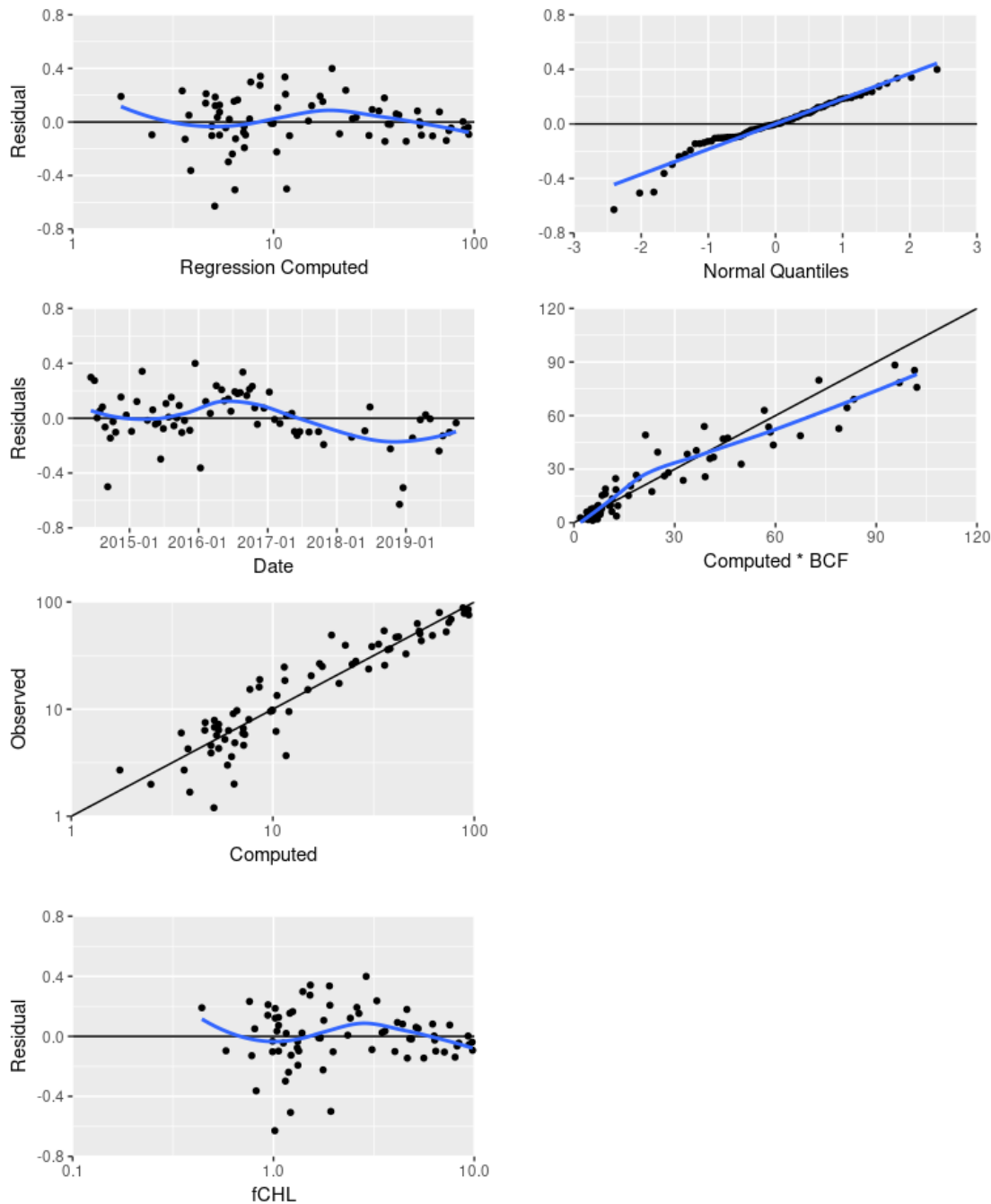
Outlier Test Criteria

Leverage	Cook's D	DFFITS
0.0811	0.1942	0.3288

Flagged Observations

	logChla	Estimate	Residual	Standard Residual	Studentized Residual	Leverage	Cook's D	DFFITS
201409080800	0.5660	1.070	-0.500	-2.67	-2.79	0.0139	0.0502	-0.331
201601110930	0.2250	0.588	-0.363	-1.96	-2.00	0.0340	0.0673	-0.374
201811281120	0.0792	0.708	-0.628	-3.37	-3.65	0.0261	0.1530	-0.598
201812170910	0.3010	0.808	-0.507	-2.71	-2.84	0.0210	0.0790	-0.417

Statistical Plots



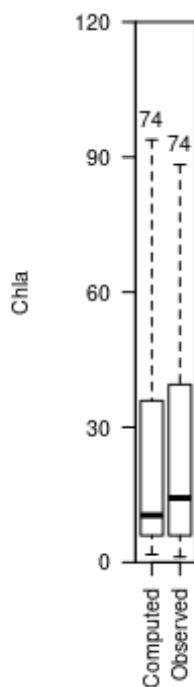
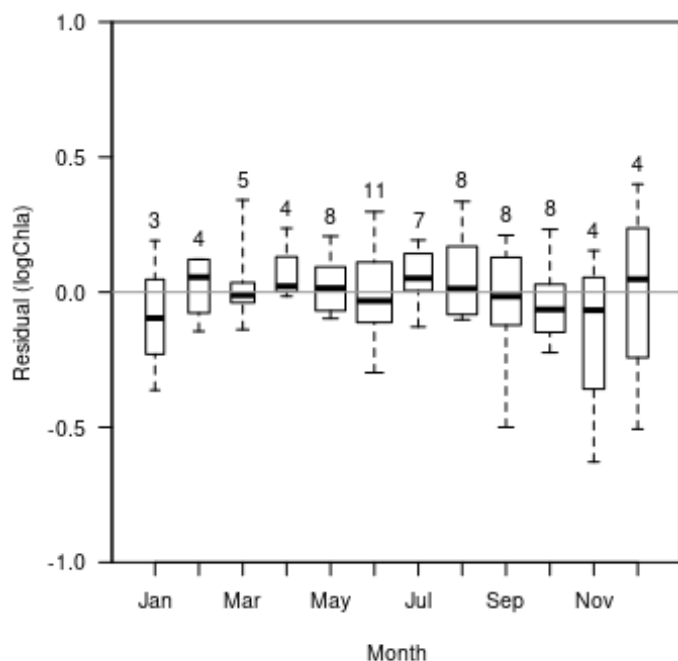
First row (left): Residual Chla related to regression computed Chla with local polynomial regression fitting, or locally estimated scatterplot smoothing (LOESS), indicated by the blue line.

First row (right): Residual Chla related to the corresponding normal quantile of the residual with simple linear regression, indicated by the blue line.

Second row: Residual Chla related to date (left) and regression computed Chla multiplied by the BCF (right) with LOESS, indicated by the blue line.

Third row: Observed Chla related to regression computed Chla.

Fourth row: Residual Chla related to fCHL with LOESS, indicated by the blue line.



EXPLANATION

39 Number of values

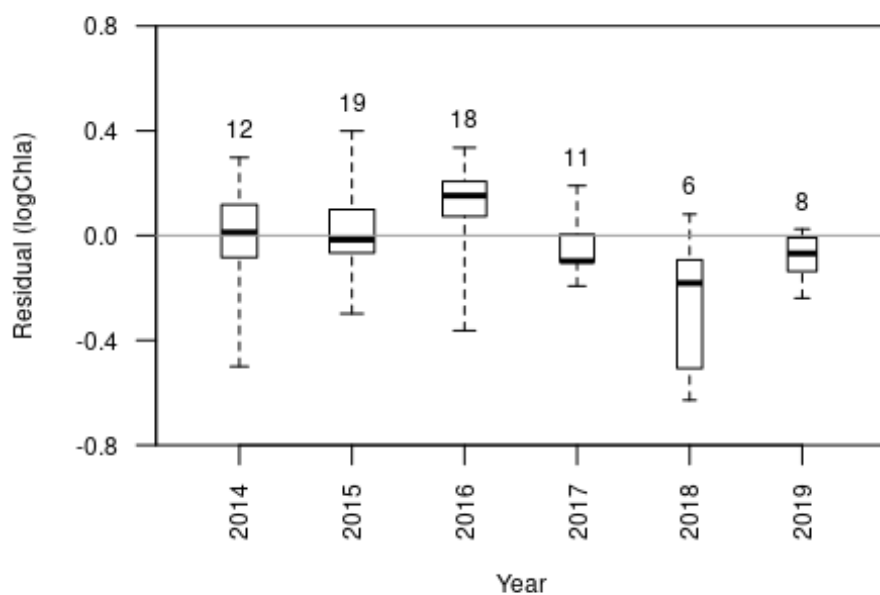
Maximum value

75th percentile

50th percentile (median)

25th percentile

Minimum value



EXPLANATION

39 Number of values

Maximum value

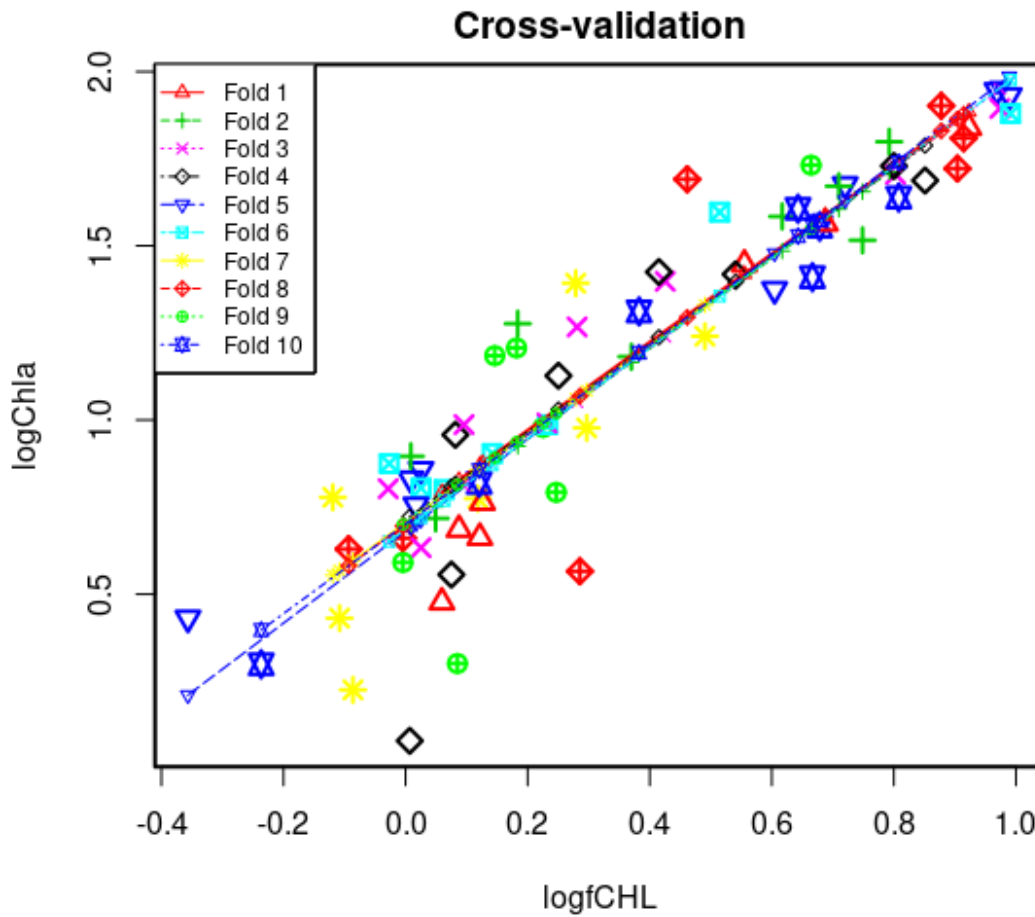
75th percentile

50th percentile (median)

25th percentile

Minimum value

Cross-Validation



Fold - equal partition of the data (10 percent of the data).

Large symbols - observed value of a data point removed in a fold.

Small symbols - recomputed value of a data point removed in a fold.

Recomputed regression lines - adjusted regression line with one fold removed.

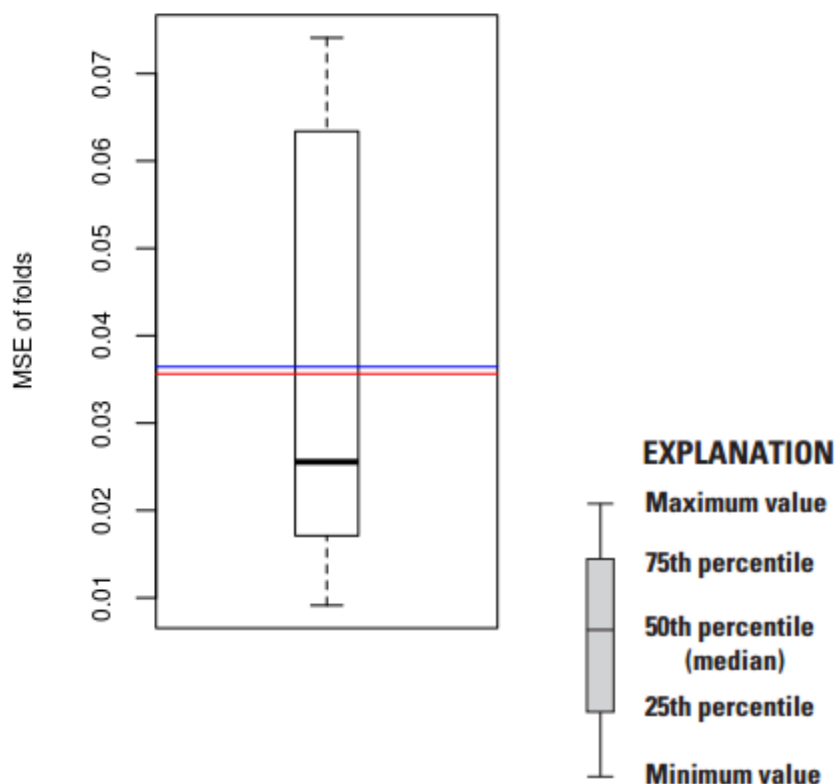
Minimum MSE of folds: 0.00913

Mean MSE of folds: 0.03640

Median MSE of folds: 0.02560

Maximum MSE of folds: 0.07410

(Mean MSE of folds) / (Model MSE): 1.02000



Red line - Model MSE

Blue line - Mean MSE of folds

Model-Calibration Dataset

0	Date	logChla	logfCHL	Chla	fCHL	Computed logChla	Computed Chla	Residual	Normal Quantiles	Censored Values
1	2014-06-11	1.18	0.146	15.3	1.4	0.887	8.38	0.298	1.66	--
2	2014-06-30	1.21	0.182	16.1	1.52	0.932	9.31	0.274	1.54	--
3	2014-07-14	1.95	0.969	88.3	9.31	1.94	95.5	0.00231	0.0169	--
4	2014-07-28	1.68	0.72	47.4	5.25	1.62	45.8	0.0517	0.327	--
5	2014-08-11	1.8	0.792	62.9	6.2	1.72	56.7	0.0818	0.511	--
6	2014-08-25	1.81	0.914	64.4	8.21	1.87	81.3	-0.0646	-0.436	--
7	2014-09-08	0.566	0.286	3.68	1.93	1.07	12.7	-0.5	-1.81	--
8	2014-09-22	1.41	0.667	25.7	4.64	1.56	39.1	-0.145	-1.2	--
9	2014-10-06	1.71	0.803	50.7	6.35	1.73	58.4	-0.0252	-0.187	--
10	2014-10-20	0.977	0.297	9.49	1.98	1.08	13.1	-0.103	-0.853	--
11	2014-11-17	0.958	0.0816	9.07	1.21	0.804	6.92	0.154	0.853	--
12	2014-12-15	0.904	0.142	8.01	1.39	0.881	8.28	0.0224	0.153	--
13	2015-01-12	0.299	-0.237	1.99	0.58	0.395	2.7	-0.0961	-0.59	--
14	2015-02-09	1.31	0.383	20.5	2.41	1.19	16.9	0.121	0.672	--
15	2015-03-09	1.28	0.184	18.9	1.53	0.935	9.37	0.342	2.02	--
16	2015-04-06	1.56	0.679	35.9	4.77	1.57	40.5	-0.0155	-0.119	--
17	2015-05-04	1.67	0.71	46.9	5.13	1.61	44.4	0.0604	0.362	--
18	2015-05-18	0.718	0.0492	5.22	1.12	0.762	6.29	-0.0444	-0.327	--
19	2015-06-01	0.661	-0.00436	4.58	0.99	0.693	5.37	-0.0324	-0.221	--
20	2015-06-15	0.477	0.0594	3	1.15	0.775	6.48	-0.298	-1.54	--

21	2015-06-29	0.775	0.118	5.95	1.31	0.851	7.72	-0.0764	-0.473	--
22	2015-07-13	1.13	0.25	13.4	1.78	1.02	11.4	0.107	0.59	--
23	2015-07-27	1.18	0.37	15.2	2.34	1.17	16.2	0.00785	0.0846	--
24	2015-08-10	1.4	0.425	25	2.66	1.25	19.1	0.153	0.806	--
25	2015-08-24	1.89	0.974	78.4	9.41	1.95	96.9	-0.0553	-0.399	--
26	2015-09-08	1.73	0.8	53.6	6.31	1.73	58	0.00252	0.0507	--
27	2015-09-21	1.58	0.617	38.4	4.14	1.49	33.7	0.0928	0.55	--
28	2015-10-05	1.69	0.851	48.7	7.1	1.79	67.4	-0.105	-0.903	--
29	2015-10-19	1.56	0.688	36.7	4.87	1.58	41.6	-0.0175	-0.153	--
30	2015-11-16	1.24	0.49	17.4	3.09	1.33	23.2	-0.0884	-0.511	--
31	2015-12-14	1.69	0.461	49.1	2.89	1.29	21.3	0.399	2.4	--
32	2016-01-11	0.225	-0.0862	1.68	0.82	0.588	4.21	-0.363	-1.66	--
33	2016-02-08	0.831	0.0086	6.78	1.02	0.71	5.58	0.121	0.631	--
34	2016-03-03	1.45	0.555	28	3.59	1.41	28.1	0.0352	0.256	--
35	2016-04-04	1.6	0.515	39.5	3.27	1.36	24.9	0.237	1.44	--
36	2016-05-02	1.27	0.281	18.5	1.91	1.06	12.5	0.207	1.2	--
37	2016-05-16	0.858	0.0253	7.21	1.06	0.731	5.86	0.127	0.715	--
38	2016-06-06	0.803	-0.0284	6.35	0.937	0.662	5	0.14	0.76	--
39	2016-06-20	0.629	-0.0933	4.26	0.807	0.579	4.13	0.0504	0.291	--
40	2016-07-11	1.42	0.415	26.6	2.6	1.23	18.6	0.193	1.13	--
41	2016-07-25	1.73	0.664	53.9	4.62	1.55	38.8	0.179	0.955	--
42	2016-08-08	0.896	0.0086	7.87	1.02	0.71	5.58	0.186	1.01	--
43	2016-08-22	1.39	0.279	24.7	1.9	1.06	12.4	0.336	1.81	--
44	2016-09-12	0.987	0.0958	9.7	1.25	0.822	7.22	0.165	0.903	--
45	2016-09-26	0.875	-0.0269	7.5	0.94	0.664	5.02	0.211	1.27	--
46	2016-10-11	0.778	-0.119	6	0.76	0.546	3.82	0.232	1.35	--
47	2016-10-24	1.9	0.878	79.8	7.54	1.83	72.9	0.0758	0.436	--
48	2016-11-07	1.84	0.923	69.1	8.37	1.88	83.3	-0.0448	-0.362	--
49	2016-12-12	0.805	0.0253	6.38	1.06	0.731	5.86	0.0734	0.399	--
50	2017-01-09	0.431	-0.357	2.7	0.44	0.241	1.89	0.191	1.07	--
51	2017-02-06	0.979	0.225	9.52	1.68	0.988	10.6	-0.00969	-0.0507	--
52	2017-03-06	1.93	0.989	85.3	9.75	1.97	101	-0.0385	-0.291	--
53	2017-04-10	0.8	0.0632	6.31	1.16	0.78	6.56	0.0199	0.119	--
54	2017-05-08	0.756	0.017	5.7	1.04	0.721	5.72	0.0351	0.221	--
55	2017-05-22	0.763	0.126	5.8	1.34	0.861	7.9	-0.0974	-0.631	--
56	2017-06-05	0.686	0.0875	4.85	1.22	0.811	7.05	-0.126	-0.955	--
57	2017-06-19	0.633	0.0253	4.3	1.06	0.731	5.86	-0.0979	-0.672	--
58	2017-08-07	1.37	0.605	23.7	4.02	1.48	32.5	-0.101	-0.76	--
59	2017-09-26	1.64	0.808	43.5	6.43	1.74	59.4	-0.0984	-0.715	--
60	2017-10-23	0.663	0.122	4.6	1.32	0.855	7.79	-0.192	-1.27	--
61	2018-03-20	1.72	0.904	52.7	8.02	1.86	78.9	-0.139	-1.07	--
62	2018-05-29	1.88	0.991	75.8	9.8	1.97	102	-0.0927	-0.55	--
63	2018-06-25	1.61	0.643	40.4	4.39	1.52	36.4	0.0816	0.473	--
64	2018-10-11	0.792	0.247	6.2	1.77	1.02	11.3	-0.224	-1.35	--
65	2018-11-28	0.0792	0.0068	1.2	1.02	0.708	5.55	-0.628	-2.4	--
66	2018-12-17	0.301	0.0849	2	1.22	0.808	6.99	-0.507	-2.02	--
67	2019-02-05	1.52	0.749	32.8	5.61	1.66	49.8	-0.145	-1.13	--
68	2019-03-18	0.987	0.233	9.7	1.71	0.998	10.8	-0.0114	-0.0846	--
69	2019-04-15	1.42	0.541	26.2	3.47	1.39	26.9	0.0247	0.187	--
70	2019-05-09	0.991	0.232	9.8	1.7	0.996	10.8	-0.00509	-0.0169	--
71	2019-06-25	0.556	0.0751	3.6	1.19	0.795	6.79	-0.239	-1.44	--
72	2019-07-15	0.431	-0.108	2.7	0.78	0.56	3.95	-0.129	-1.01	--
73	2019-08-19	0.591	-0.00436	3.9	0.99	0.693	5.37	-0.102	-0.806	--
74	2019-09-23	0.82	0.121	6.6	1.32	0.854	7.77	-0.0342	-0.256	--

Definitions

Chla: Chlorophyll *a*, in micrograms per liter (32209 during June 11, 2014, through September 26, 2017; 70953 during October 23, 2017, through September 23, 2019).

Cook's D: Cook's distance (Helsel and others, 2020).

DIFFITS: Difference in fits statistic (Helsel and others, 2020).

E.vars: Explanatory variables.

fCHL: Chlorophyll fluorescence, in relative fluorescence units (32320).

Leverage: An outlier's measure in the *x* direction (Helsel and others, 2020).

LOESS: Local polynomial regression fitting, or locally estimated scatterplot smoothing (Helsel and others, 2020).

LOWESS: Locally weighted scatterplot smoothing (Cleveland, 1979; Helsel and others, 2020).

MSE: Model standard error (Helsel and others, 2020).

MSPE: Model standard percentage error (Helsel and others, 2020).

Probability(>|t|): The probability that the independent variable has no effect on the dependent variable (Helsel and others, 2020).

RMSE: Root mean square error (Helsel and others, 2020).

t value: Student's *t* value; the coefficient divided by its associated standard error (Helsel and others, 2020).

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