

In cooperation with the Illinois Department of Natural Resources—Office of Water Resources

# Control-Structure Ratings on the Fox River at McHenry and Algonquin, Illinois



Scientific Investigations Report 2009–5186

**Cover photograph:**

Downstream side of sluice gates, fish ladder, hinged-crest gate, and broad-crested weir on the Fox River at McHenry, Illinois.

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By Timothy D. Straub, Gary P. Johnson, Jon E. Hortness, and Joseph R. Parker

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**U.S. Department of the Interior**  
**U.S. Geological Survey**

**U.S. Department of the Interior**  
KEN SALAZAR, Secretary

**U.S. Geological Survey**  
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U.S. Geological Survey, Reston, Virginia: 2009

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## Conversion Factors and Vertical Datum

| Multiply                                   | By        | To obtain                                  |
|--|-----------|--|
|  | Length    |  |
| foot (ft)                                  | 0.3048    | meter (m)                                  |
| mile (mi)                                  | 1.609     | kilometer (km)                             |
|  | Area      |  |
| square mile (mi <sup>2</sup> )             | 259.0     | hectare (ha)                               |
| square mile (mi <sup>2</sup> )             | 2.590     | square kilometer (km <sup>2</sup> )        |
|  | Velocity  |  |
| foot per second (ft/s)                     | .3048     | meter per second (m-/s)                    |
|  | Flow rate |  |
| cubic foot per second (ft <sup>3</sup> /s) | .02832    | cubic meter per second (m <sup>3</sup> /s) |

Vertical coordinate information is referenced to the National Geodetic Vertical Datum of 1929 (NGVD 29).

## Abbreviations, Acronyms, and Symbols

|             |  |
|-------------|--|
| ADCP        | Acoustic Doppler Current Profiler  |
| AFF         | affected flow  |
| B           | length of weir, spillway, or gate  |
| BCW         | broad-crested weir   |
| C           | computed flow  |
| C/M         | ratio of computed and measured flow  |
| Comp.       | computed   |
| $C_{BCW}$   | free-weir coefficient for the broad-crested weir   |
| $C_{HCG}$   | free-weir coefficient for the hinged-crest gate  |
| $C_{HCG-S}$ | submerged-weir coefficient for the hinged-crest gate   |
| $C_{OS}$    | free-weir coefficient for the ogee spillway  |
| $C_{OS-A}$  | affected-weir coefficient for the ogee spillway  |
| $C_S$       | free-weir coefficient for the spillway, which includes flow over the hinged-crest gate set at the elevation of the ogee spillway |
| $C_{SLO}$   | free-orifice coefficient for the sluice gate   |
| $C_{SLO-S}$ | submerged-orifice coefficient for the sluice gate  |
| $C_{SLW}$   | free-weir coefficient for the sluice gate  |
| $C_{SLW-S}$ | submerged-weir coefficient for the sluice gate   |
| FO          | free-orifice flow  |
| FW          | free-weir flow   |

|            |   |
|------------|---|
| FW-FL      | free-weir flow with flow over the hinged-crest gate (crest at elevation of ogee spillway)   |
| FW-NF      | free-weir flow with no flow over the hinged-crest gate                                      |
| $h_{1BCW}$ | headwater depth above the broad-crested weir crest  |
| $h_{1HCG}$ | headwater depth above the hinged-crest gate crest   |
| $h_{1OS}$  | headwater depth above the ogee spillway crest   |
| $h_{1SL}$  | headwater depth above the sluice-gate sill  |
| $h_{3BCW}$ | tailwater depth above the broad-crested weir crest  |
| $h_{3HCG}$ | tailwater depth above the hinged-crest gate crest   |
| $h_{3OS}$  | tailwater depth above the ogee spillway crest   |
| $h_{3SL}$  | tailwater depth above the sluice-gate sill  |
| $h_{gHCG}$ | hinged-crest gate opening referenced to the broad-crested-weir crest or ogee spillway crest |
| $h_{gSL}$  | sluice gate opening referenced to the concrete sill   |
| HCG        | hinged-crest gate   |
| HW         | headwater stage   |
| IDNR–OWR   | Illinois Department of Natural Resources–Office of Water Resources                          |
| M          | measured flow   |
| Meas.      | measured  |
| NF         | no flow   |
| $p_{HCG}$  | height of hinged-crest gate crest above approach invert                                     |
| $R^2$      | coefficient of determination  |
| OS         | ogee spillway   |
| SL         | sluice gate   |
| SO         | submerged-orifice flow  |
| SW         | submerged-weir flow   |
| TW         | tailwater stage   |
| USGS       | U.S. Geological Survey  |
| WY         | water year  |



# Control-Structure Ratings on the Fox River at McHenry and Algonquin, Illinois

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## Abstract

The Illinois Department of Natural Resources—Office of Water Resources operates control structures on a reach of the Fox River in northeastern Illinois between McHenry and Algonquin. The structures maintain water levels in the river for flood-control and recreational purposes. This report documents flow ratings for hinged-crest gates, a broad-crested weir, sluice gates, and an ogee spillway on the control structures at McHenry and Algonquin. The ratings were determined by measuring headwater and tailwater stage along with streamflow at a wide range of flows at different gate openings. Standard control-structure rating techniques were used to rate each control structure.

The control structures at McHenry consist of a 221-foot(ft)-long broad-crested weir, a 4-ft-wide fish ladder, a 50-ft-wide hinged-crest gate, five 13.75-ft-wide sluice gates, and a navigational lock. Sixty measurements were used to rate the McHenry structures. The control structures at Algonquin consist of a 242-ft-long ogee spillway and a 50-ft-wide hinged-crest gate. Forty-one measurements were used to rate the Algonquin control structures.

## Introduction

The Illinois Department of Natural Resources—Office of Water Resources (IDNR—OWR) operates control structures on a reach of the Fox River in northeastern Illinois between McHenry and Algonquin (fig. 1). The McHenry control structure is at river mile 97.8 and has a drainage area of 1,250 mi<sup>2</sup>. The Algonquin control structure is at river mile 81.6 and has a drainage area of 1,403 mi<sup>2</sup> (fig. 1). Hinged-crest gates were installed at both structures in 2002, to allow more streamflow through the structures than was previously possible. This enhanced capability has had appreciable effects on the protocols for operating the control structures. To better understand these effects, a study was done during 2002–2008 by the U.S. Geological Survey (USGS), in cooperation with the IDNR—OWR.

## Purpose and Scope

This report documents development of flow ratings for hinged-crest gates, a broad-crested weir, sluice gates, and an ogee spillway on the Fox River control structures at McHenry and Algonquin, Illinois. Streamflow data collected during water years 2003–2008 are summarized and used in the analysis. Also, historic streamflow data at McHenry were used to aid in documenting the effects of the broad-crested weir and sluice gates.

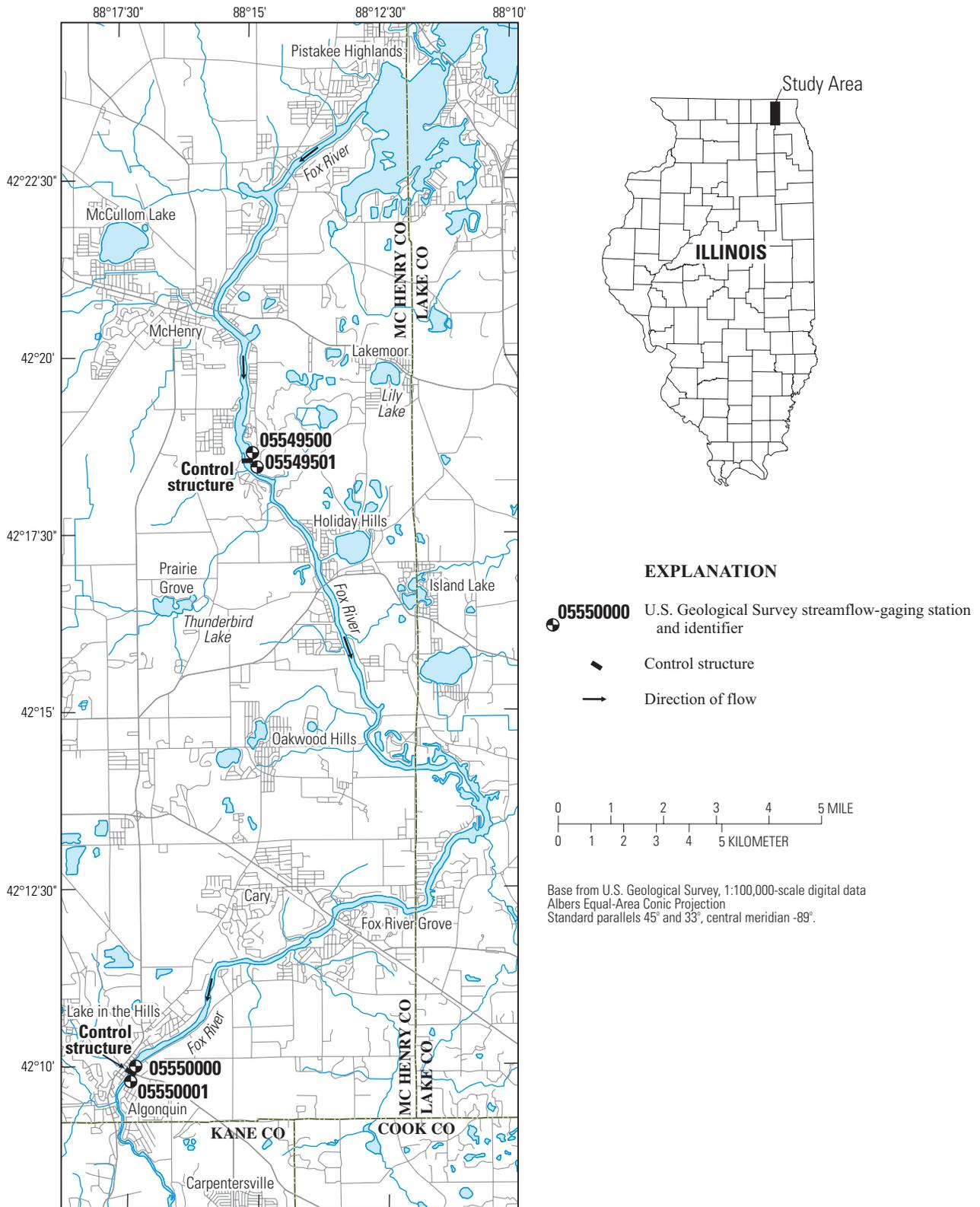
## Streamflow During Study Period

Statistical streamflow summaries at USGS streamflow gaging station (05550000) on the Fox River at Algonquin, Illinois, during the study for water years (WY) 2003–2008 are presented in table 1 and compared to statistics for the full period of record (WY 1916–2008) at this station. A water year (WY) is the 12-month period from October 1 through September 30 and is designated by the calendar year in which it ends and includes 9 of 12 months. For example, WY 2004 is from October 1, 2003, to September 30, 2004. The summary shows that both low and high streamflows occurred during the data-collection period, including the highest daily mean and peak flows.

## Approach

The Fox River control-structure ratings were determined by measuring headwater (HW) and tailwater (TW) stage along with streamflow at a wide range of flows at different gate openings. The HW and TW streamflow gaging stations used on the Fox River near McHenry were 05549500 and 05549501, respectively. The HW and TW stations were installed in 1941 and 1987, respectively. The stations were operated as stage-only with miscellaneous streamflow measurements during 1985, 1986, 1991, 1993, and 2002–2008. The 1985 and 1986 streamflow measurements also included TW measurements consistent with the datum for the TW station. The HW and TW stations used on the Fox River at

**2 Control-Structure Ratings on the Fox River at McHenry and Algonquin, Illinois**



**Figure 1.** Location of Fox River control structures at McHenry and Algonquin, Illinois.

**Table 1.** Statistical summary of streamflow on the Fox River at Algonquin, Illinois, at USGS streamflow-gaging station 0555000.[ft<sup>3</sup>/s, cubic foot per second; WY, water year]

| Water year  | Annual mean flow (ft <sup>3</sup> /s) | Daily mean flow                 |               |                                 |         | Maximum peak flow               |              |
|-------------|---------------------------------------|---------------------------------|---------------|---------------------------------|---------|---------------------------------|--------------|
|             |                                       | Highest                         |               | Lowest                          |         | Streamflow (ft <sup>3</sup> /s) | Date         |
|             |                                       | Streamflow (ft <sup>3</sup> /s) | Date          | Streamflow (ft <sup>3</sup> /s) | Date    |                                 |              |
| WY2003      | 516                                   | 2,000                           | May 13,14     | 90                              | Sep. 6  | 2,040                           | May 10,12–14 |
| WY2004      | 1,118                                 | 6,020                           | May 31        | 110                             | Oct. 3  | 6,720                           | May 22       |
| WY2005      | 665                                   | *2,500                          | Feb. 19–21    | 89                              | Jul. 18 | 2,600                           | Feb. 18      |
| WY2006      | 877                                   | 3,200                           | Mar. 17       | 140                             | Oct. 30 | 3,710                           | Mar. 14      |
| WY2007      | 1,673                                 | 6,690                           | Aug. 26       | 423                             | Jul. 25 | 6,720                           | Aug. 25      |
| WY2008      | 2,045                                 | 6,030                           | Jun. 19       | 449                             | Sept. 2 | 6,080                           | Jun. 19      |
| WY1916–2008 | 910                                   | 6,690                           | Aug. 26, 2007 | 12                              | A       | 6,720                           | B            |

\*estimated

A–Apr.6, 1960; Apr. 2, 1979

B–May 22, 2004; Aug. 25, 2007

Algonquin, were 05550000 and 05550001, respectively. The HW and TW gaging stations were installed in 1916 and 2002, respectively. Streamflow has been measured at the HW station since 1916.

To minimize the drawdown effect on the HW stage, the HW stations at the McHenry and Algonquin control structures are approximately 275 and 140 ft upstream of the structures, respectively. For the 50-ft-wide hinged-crest gates at both control structures, the upstream distances are greater than two times the contraction width recommended for a completely eccentric contraction with all flow on one bank (Matthai, 1967). The TW stage gages at both control structures are located beyond the influence of the hinged-crest gate and beyond the influence of the sluice gates at McHenry. Streamflow measurements were made for a wide range of streamflows and gate openings. Standard control-structure-rating techniques described in Chow (1959), Collins (1977), and Roberson and others (1998) were used to rate each structure.

## Previous Studies

To optimize the operational procedures of the gate structures for recreational and flood-control purposes, a hydraulic model (Franz and Melching, 1997a and 1997b) was applied to simulate flood-event scenarios on this reach of the Fox

River (Knapp and Ortel, 1992). Dam-break analyses also were completed by the IDNR–OWR (Illinois Department of Natural Resources, 1999). Inputs to the hydraulic model throughout the studied reach included surveyed cross sections, slope, roughness, and stage-discharge ratings at control structures and were collected and documented by IDNR–OWR and the USGS (Illinois Department of Transportation, 1992; Fisk, 1988). The application of the hydraulic model through this reach has been calibrated and verified (Illinois Department of Natural Resources, 1999; Ishii and Turner, 1996; and Knapp and Ortel, 1992).

## McHenry Control-Structure Ratings

The McHenry control structure is at river mile 97.8 on the Fox River in northeastern Illinois (fig. 1). The drainage area at the headwater gage is 1,250 mi<sup>2</sup>. The 8,900 acre reservoir created by the dam is part of the Fox Chain of Lakes and is used primarily for recreation and flood control. The control structures at McHenry consist of a 221-ft broad-crested weir, a 4-ft-wide fish ladder, a 50-ft-wide hinged-crest gate, five 13.75-ft wide sluice gates, and a navigational lock (figs. 2, 3, 4, and 5). The elevations of structure components and headwater and tailwater gage datums are presented in table 2.

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Figure 2. Layout of control structures on the Fox River at McHenry, Illinois.

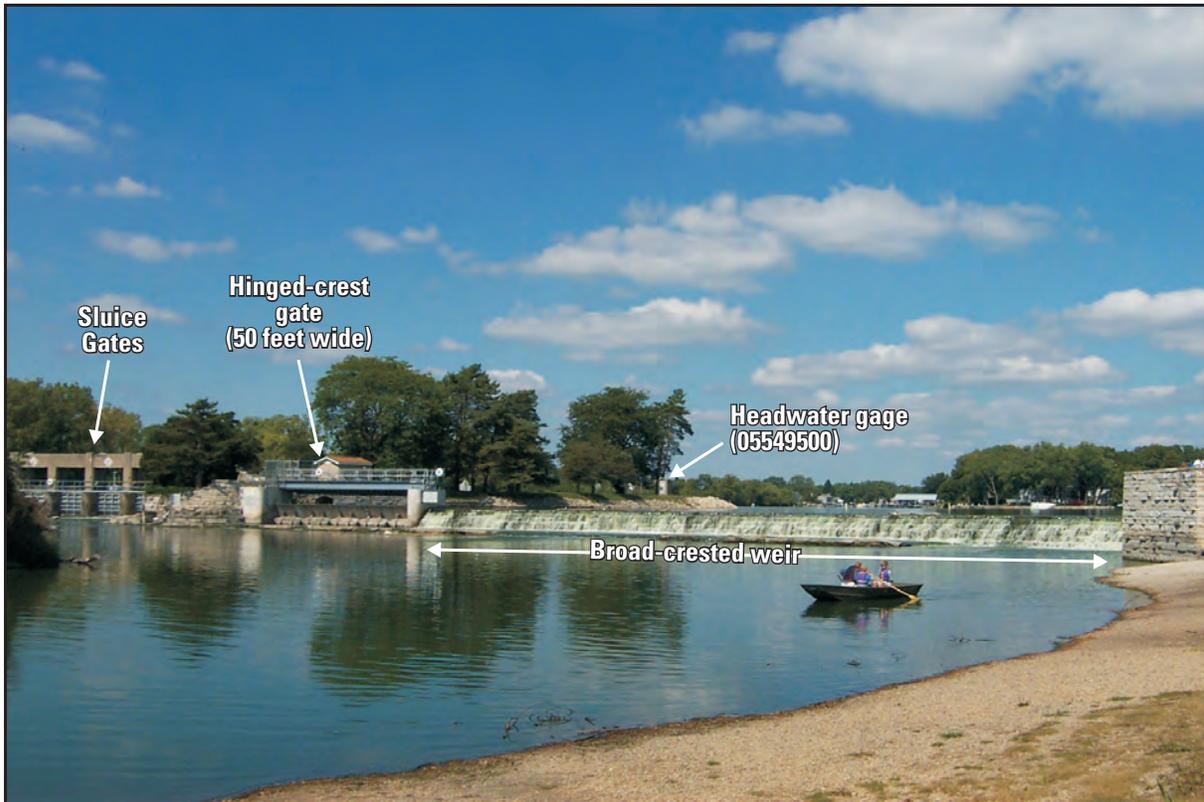
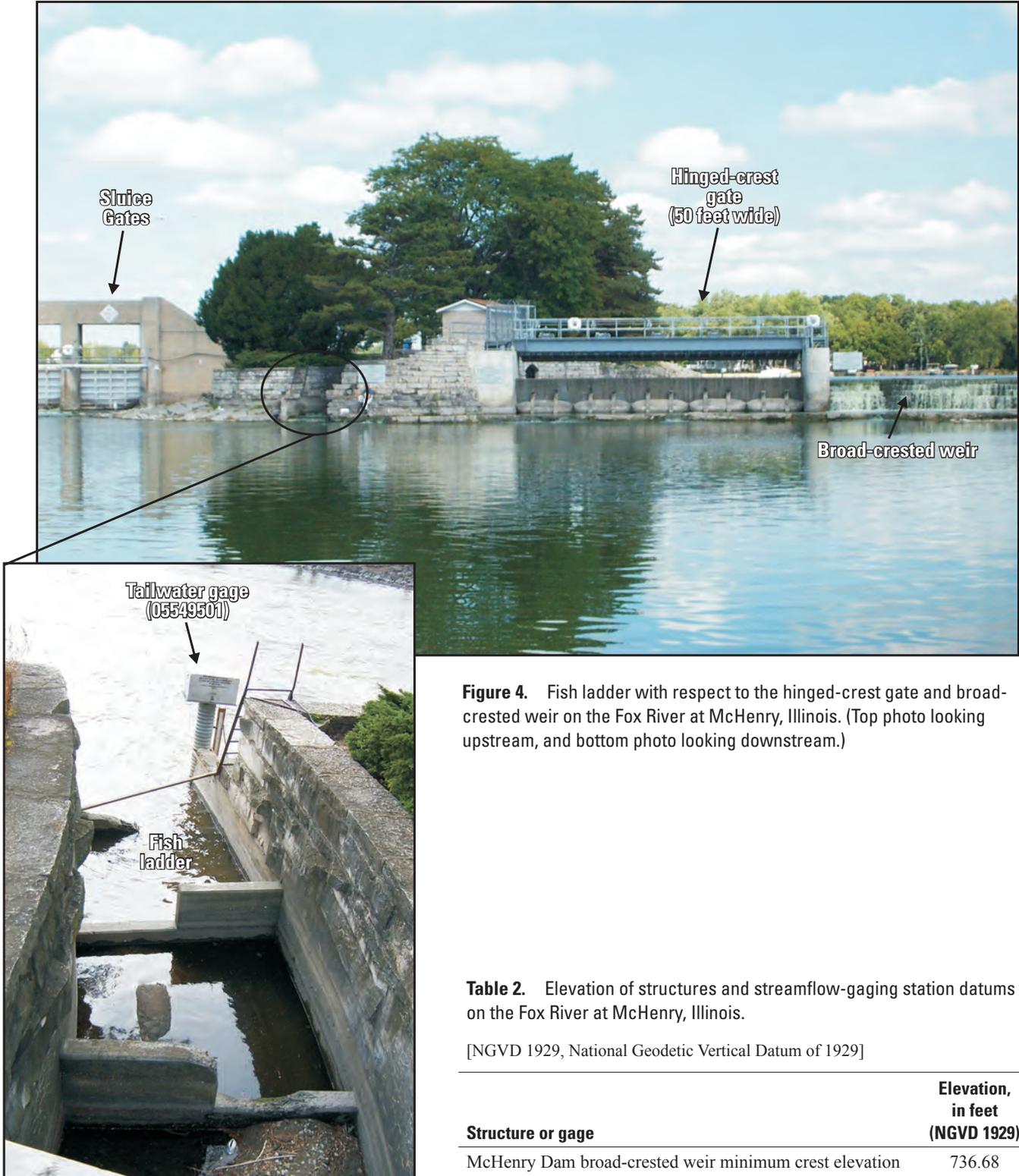


Figure 3. Downstream side of hinged-crest gate, broad-crested weir, and fish ladder on the Fox River at McHenry, Illinois.



**Figure 4.** Fish ladder with respect to the hinged-crest gate and broad-crested weir on the Fox River at McHenry, Illinois. (Top photo looking upstream, and bottom photo looking downstream.)

**Table 2.** Elevation of structures and streamflow-gaging station datums on the Fox River at McHenry, Illinois.

[NGVD 1929, National Geodetic Vertical Datum of 1929]

| Structure or gage                                       | Elevation, in feet (NGVD 1929) |
|---|--------------------------------|
| McHenry Dam broad-crested weir minimum crest elevation  | 736.68                         |
| McHenry Dam broad-crested weir average crest elevation  | 736.76                         |
| McHenry Dam hinged-crest gate floor elevation           | 730.08                         |
| McHenry Dam sluice gate concrete sill                   | 731.15                         |
| Headwater station datum, Fox River at McHenry, Illinois | 733.00                         |
| Tailwater station datum, Fox River at McHenry, Illinois | 730.15                         |

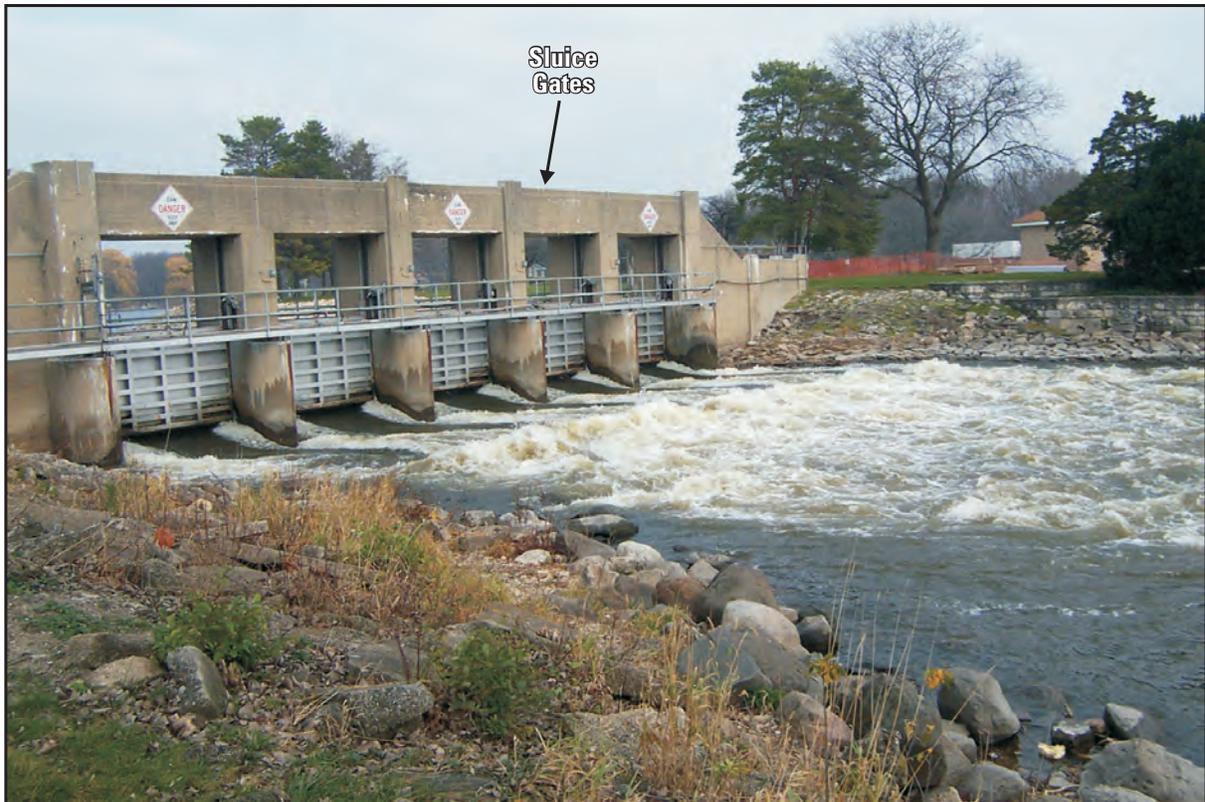
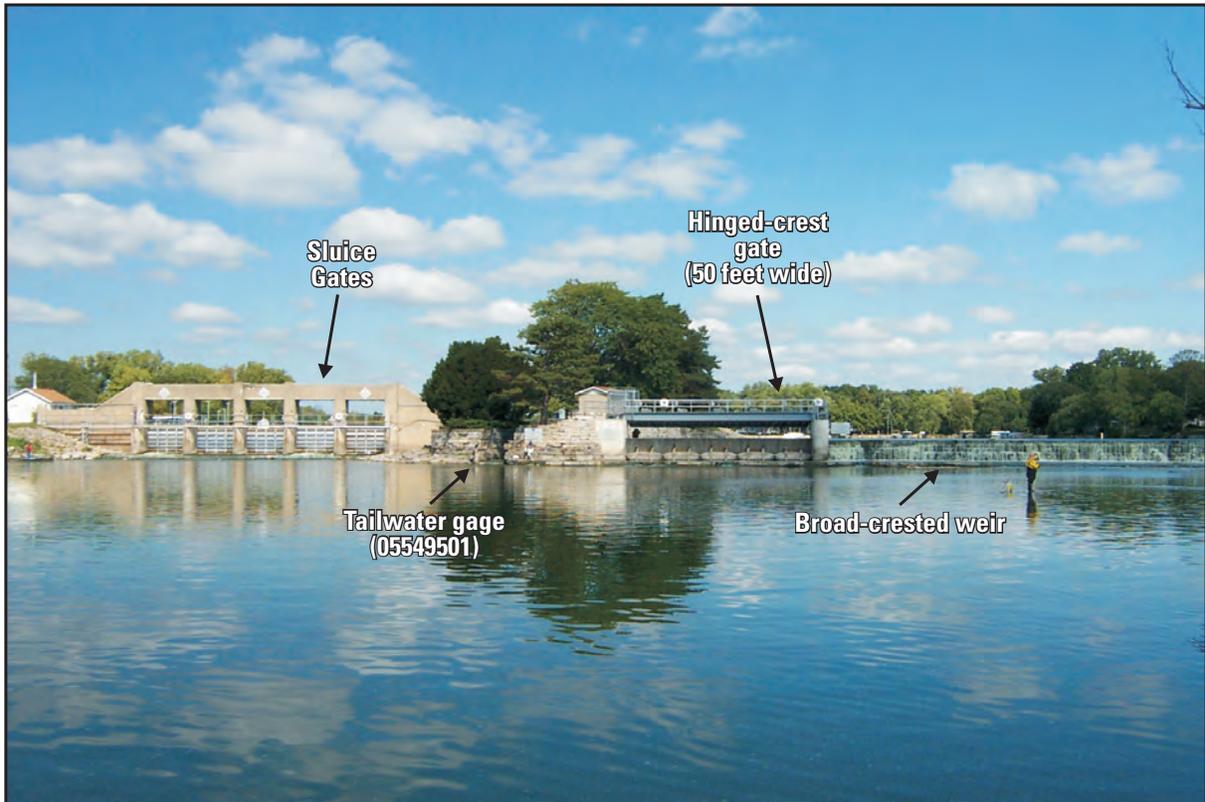


Figure 5. Downstream side of sluice gates on the Fox River near McHenry, Illinois.

## Broad-Crested Weir

A side-view schematic of the broad-crested weir and parameters used in the control-structure rating are shown in figure 6. The broad-crested weir was rated by the USGS and the results were published in Fisk (1988). Streamflow measurements 5, 13, 15, and 20 listed in table 3 were used by Fisk to develop a free-weir-flow coefficient equation (fig. 7 and appendix A). A standard weir equation (equation 1 in table 4) described in Chow (1959), Collins (1977), and Roberson and others (1998) is used. Fisk used a total weir length of 288 ft, which included the fish ladder. The measured  $C_{BCW}$  in table 3 is obtained by using the measured BCW flow and measured headwater depth, and calculating for  $C_{BCW}$  from equation 1. The computed  $C_{BCW}$  in table 3 is obtained by using regression equation 2 (fig. 7 and table 4).

For the purposes of the current study, the free-weir coefficient equation is assumed valid and only the length of the weir is adjusted (221 ft for the new weir length after construction

of the HCG, plus 4 ft for the fish ladder, equals 225 ft) to compute broad-crested weir flow (tables 3 and 4). The hinged-crest gate was closed with no flow over it during measurement 48. The calculated flow (173 ft<sup>3</sup>/s) (using the modified Fisk equation (equation 3) with only the length of weir reduced) was 28 ft<sup>3</sup>/s greater than the measured flow (145 ft<sup>3</sup>/s) (table 3) with an average velocity of 0.102 ft/s.

As the tailwater depth increases, the submergence ratio ( $h_{3BCW}/h_{1BCW}$ ) approaches unity, and the flow potentially can be overestimated using the free-weir flow equation; therefore, a submerged-flow coefficient equation may need to be developed. The greatest  $h_{3BCW}/h_{1BCW}$  of 0.43 during a measurement occurred on August 27, 2007. Submerged flow, according to Collins (1977), occurs when the submergence ratio is equal to or greater than 0.60. Given that  $h_{3BCW}/h_{1BCW}$  did not exceed 0.60 during the study by Fisk (1988) or during this study, the submergence ratio suggested by Collins (1977) is assumed to be applicable and no submerged-flow coefficient equation could be developed.

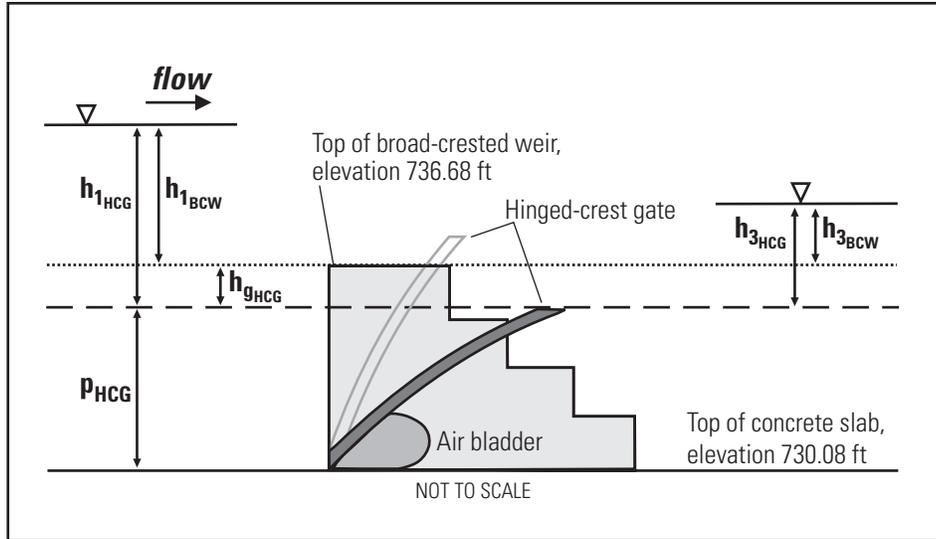
**Table 3.** Broad-crested weir flow characteristics and coefficients on the Fox River control structure near McHenry, Illinois.

[USGS, U.S. Geological Survey; BCW, broad-crested weir; HCG, hinged-crest gate; ft<sup>3</sup>/s, cubic foot per second;  $h_{1BCW}$ , headwater depth above the broad-crested weir crest; ft, foot;  $h_{3BCW}$ , tailwater depth above the broad-crested weir crest;  $C_{BCW}$ , free-weir coefficient for the broad-crested weir; FW, free-weir flow; NF, no flow; ---, not determined]

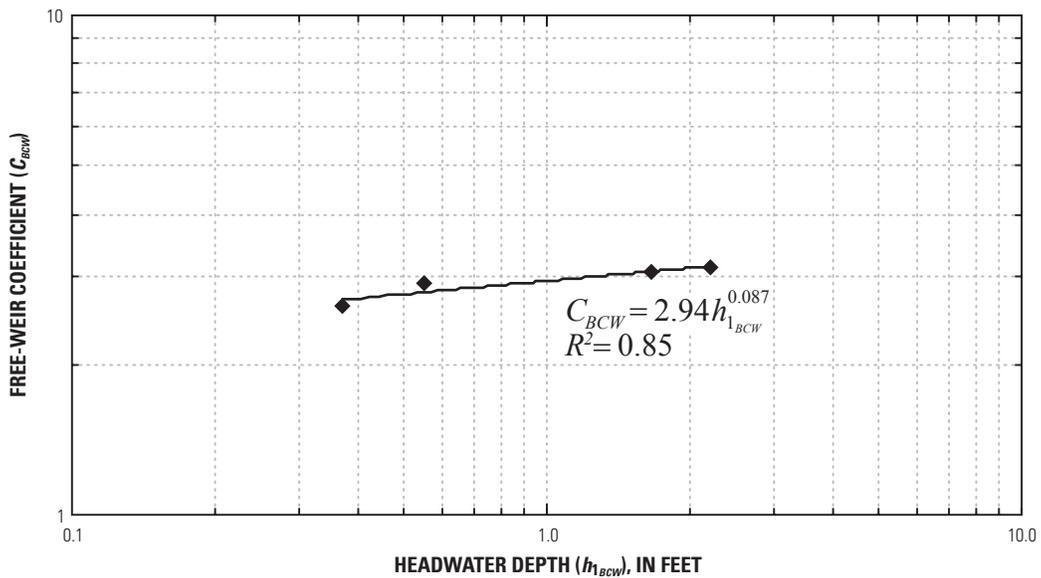
| USGS<br>measure-<br>ment<br>number | Date       | Measured<br>BCW and<br>(or)<br>HCG flow<br>(ft <sup>3</sup> /s) | Broad-Crested Weir |                    |                     |                |                       |                       | Computed<br>flow using<br>modified<br>Fisk <sup>1</sup> (ft <sup>3</sup> /s) |
|------------------------------------|------------|---|--------------------|--------------------|---------------------|----------------|-----------------------|-----------------------|--|
|                                    |            |   | $h_{1BCW}$<br>(ft) | $h_{3BCW}$<br>(ft) | $h_{3BCW}/h_{1BCW}$ | Flow<br>regime | Measured<br>$C_{BCW}$ | Computed<br>$C_{BCW}$ |  |
| 5                                  | 05/16/1985 | 169   | 0.37               | -5.18              | -14.0               | FW             | 2.61                  | 2.70                  | ---  |
| 13                                 | 08/28/1986 | 342   | .55                | -5.48              | -9.96               | FW             | 2.91                  | 2.79                  | ---  |
| 15                                 | 09/27/1986 | 1,880   | 1.66               | -.41               | -.25                | FW             | 3.05                  | 3.07                  | ---  |
| 20                                 | 09/30/1986 | 2,990   | 2.22               | .45                | .20                 | FW             | 3.14                  | 3.15                  | ---  |
| 44                                 | 11/18/2002 | 565   | .48                | -5.60              | -11.7               | FW             | ---                   | 2.76                  | 206  |
| 45                                 | 11/19/2002 | 1,012   | .30                | -4.92              | -16.4               | FW             | ---                   | 2.65                  | 98   |
| 46                                 | 11/19/2002 | 1,345   | -.06               | -4.93              | ---                 | NF             | ---                   | ---                   | 0  |
| 47                                 | 11/20/2002 | 1,775   | -.47               | -4.41              | ---                 | NF             | ---                   | ---                   | 0  |
| <sup>A</sup> 48                    | 04/04/2003 | 145   | .43                | -5.23              | -12.2               | FW             | 2.29                  | 2.73                  | 173  |
| 49                                 | 05/17/2004 | 803   | .62                | -3.03              | -4.89               | FW             | ---                   | 2.82                  | 310  |
| 50                                 | 05/17/2004 | 1,240   | .38                | -2.75              | -7.24               | FW             | ---                   | 2.70                  | 142  |
| 51                                 | 05/17/2004 | 2,040   | .12                | -2.54              | -21.2               | FW             | ---                   | 2.44                  | 23   |
| 52                                 | 05/24/2004 | 1,820   | .36                | -.68               | -1.89               | FW             | ---                   | 2.69                  | 131  |
| 53                                 | 03/17/2006 | 1,077   | -1.04              | -2.76              | ---                 | NF             | ---                   | ---                   | 0  |
| 54                                 | 03/17/2006 | 401   | -.31               | -3.22              | ---                 | NF             | ---                   | ---                   | 0  |
| 55                                 | 03/16/2007 | 1,132   | -1.04              | -2.21              | ---                 | NF             | ---                   | ---                   | 0  |
| 56                                 | 08/22/2007 | 1,710   | -.01               | -.95               | ---                 | NF             | ---                   | ---                   | 0  |
| 57                                 | 08/27/2007 | 2,550   | 1.15               | .50                | .43                 | FW             | ---                   | 2.98                  | 826  |
| 58                                 | 03/26/2008 | 1,440   | -1.20              | -2.15              | ---                 | NF             | ---                   | ---                   | 0  |
| 59                                 | 04/16/2008 | 1,930   | .48                | -.49               | -1.02               | FW             | ---                   | 2.76                  | 206  |
| 60                                 | 06/20/2008 | 2,450   | 1.08               | .25                | .23                 | FW             | ---                   | 2.96                  | 747  |

<sup>A</sup>No flow over hinged-crest gate. All other measurements from 2002–2008 had flow over the hinged-crest gate.

<sup>1</sup>Fisk (1988)



**Figure 6.** Schematic (side view) of hinged-crest gate and broad-crested weir on the Fox River at McHenry, Illinois (ft, foot;  $h_{1HCG}$ , headwater depth above the hinged-crest gate crest;  $h_{3HCG}$ , tailwater depth above the hinged-crest gate crest;  $h_{gHCG}$ , hinged-crest gate opening referenced to the broad-crested-weir crest;  $p_{HCG}$ , height of hinged-crest gate crest above approach invert;  $h_{1BCW}$ , headwater depth above the broad-crested weir crest;  $h_{3BCW}$ , tailwater depth above the broad-crested weir crest).



**Figure 7.** Discharge coefficient for free-weir flow and headwater depth for the broad-crested weir (fish ladder included) on the Fox River at McHenry, Illinois (from Fisk, 1988), ( $R^2$ , coefficient of determination).

**Table 4.** Hydraulic conditions, parameters, and equations for different flow regimes for the broad-crested weir and hinged-crest gate on the Fox River at McHenry, Illinois.

[  $h_{3BCW}$ , tailwater depth above the broad-crested weir crest, in feet;  $h_{1BCW}$ , headwater depth above the broad-crested weir crest, in feet;  $Q_{BCW}$ , flow over the broad-crested weir, in ft<sup>3</sup>/s;  $C_{BCW}$ , free-weir coefficient for the broad-crested weir; B, length of weir or gate, in feet;  $h_{3HCG}$ , tailwater depth above the hinged-crest gate crest, in feet;  $h_{1HCG}$ , headwater depth above the hinged-crest gate crest, in feet;  $Q_{HCG}$ , flow through the hinged-crest gate, in ft<sup>3</sup>/s;  $C_{HCG}$ , free-weir coefficient for the hinged-crest gate;  $p_{HCG}$ , height of hinged-crest gate crest above approach invert;  $C_{HCG-S}$ , submerged-weir coefficient for the hinged-crest gate]

| Structure          | Flow regime         | Hydraulic conditions                  | Parameters and equations   | Equation number |
|--------------------|---------------------|---------------------------------------|--|-----------------|
| Broad-crested weir | Free weir (FW)      | $\frac{h_{3BCW}}{h_{1BCW}} < 0.60$    | $Q_{BCW} = C_{BCW} B h_{1BCW}^{1.5}$                                 | 1               |
|                    |                     |                                       | $C_{BCW} = 2.94 h_{1BCW}^{0.087}$                                    | 2               |
|                    |                     |                                       | $B = 225 \text{ ft}$   |                 |
|                    |                     |                                       | $Q_{BCW} = 661.5 h_{1BCW}^{1.587}$                                   | 3               |
| Hinged-crest gate  | Free weir (FW)      | $\frac{h_{3HCG}}{h_{1HCG}} \leq 0.75$ | $Q_{HCG} = C_{HCG} B h_{1HCG}^{1.5}$                                 | 4               |
|                    |                     |                                       | $C_{HCG} = 3.87 \left( \frac{h_{1HCG}}{p_{HCG}} \right)^{-0.135}$    | 5               |
|                    |                     |                                       | $B = 50 \text{ ft}$  |                 |
|                    |                     |                                       | $Q_{HCG} = 193.5 h_{1HCG}^{1.365} p_{HCG}^{0.135}$                   | 6               |
| Hinged-crest gate  | Submerged weir (SW) | $\frac{h_{3HCG}}{h_{1HCG}} > 0.75$    | $Q_{HCG} = C_{HCG} C_{HCG-S} B h_{1HCG}^{1.5}$                       | 7               |
|                    |                     |                                       | $C_{HCG-S} = 0.471 \left( \frac{h_{3HCG}}{h_{1HCG}} \right)^{-2.94}$ | 8               |
|                    |                     |                                       | $Q_{HCG} = 91.14 h_{1HCG}^{4.305} h_{3HCG}^{-2.94} p_{HCG}^{0.135}$  | 9               |

### Hinged-Crest Gate

A side-view schematic of the hinged-crest gate and parameters used in control structure rating are shown in figure 6. Sixteen measurements, ranging from 359 to 2,017 ft<sup>3</sup>/s, were used to describe free and submerged flow through the hinged-crest gate. Characteristics of the flow and the measured and computed discharge coefficients are listed in table 5 and appendix A. A standard weir equation (equation 4 in table 4) described in Chow (1959), Collins (1977), and Roberson and others (1998) is used to describe flow over the hinged-crest

gate. Free- and submerged-weir coefficient equations are presented in table 4, and in figures 8 and 9. The data indicate submerged flow occurs when  $h_{3HCG}/h_{1HCG}$  is greater than 0.75.

The measured and computed broad-crested weir and hinged-crest gate flows for the control structures at McHenry are presented in table 6 and figure 10 for comparison. Thirteen of the 14 computed hinged-crest gate flows are within 10 percent of measured flows, and the remaining measurement is within 16 percent. The combined BCW and HCG flows show similar results, and all eight combined measured flows above 1,400 ft<sup>3</sup>/s were computed within 6 percent.

**Table 5. Hinged-crest gate flow characteristics and coefficients near McHenry, Illinois.**

[USGS, U.S. Geological Survey; ft<sup>3</sup>/s, cubic foot per second;  $h_{brcg}$ , hinged-crest gate opening referenced to the broad-crested-weir crest;  $h_{hrcg}$ , headwater depth above the hinged-crest gate crest; ft, foot;  $h_{brcg}$ , tailwater depth above the hinged-crest gate crest;  $p_{hrcg}$ , height of hinged-crest gate crest above approach invert;  $C_{hrcg}$ , free-weir coefficient for the hinged-crest gate;  $C_{hrcg-s}$ , submerged-weir coefficient for the hinged-crest gate; FW, free-weir flow; SW, submerged-weir flow; HCG, hinged-crest gate; BCW, broad-crested weir; SL, sluice gate; ---, not determined]

| USGS<br>measure-<br>ment<br>number | Date              | Measured<br>flow <sup>1</sup><br>(ft <sup>3</sup> /s) | Hinged-Crest Gate                  |                    |                    |                    |                     |                     |                |                        |                        |                                       |                          |
|------------------------------------|-------------------|---|------------------------------------|--------------------|--------------------|--------------------|---------------------|---------------------|----------------|------------------------|------------------------|---------------------------------------|--------------------------|
|                                    |                   |   | Gate<br>opening<br>$h_{brcg}$ (ft) | $h_{hrcg}$<br>(ft) | $h_{brcg}$<br>(ft) | $p_{hrcg}$<br>(ft) | $h_{hrcg}/p_{hrcg}$ | $h_{brcg}/h_{hrcg}$ | Flow<br>regime | Measured<br>$C_{hrcg}$ | Computed<br>$C_{hrcg}$ | Measured <sup>2</sup><br>$C_{hrcg-s}$ | Computed<br>$C_{hrcg-s}$ |
| 44                                 | 11/18/2002        | 359   | 1.0                                | 1.48               | -4.60              | 5.60               | 0.3                 | -3.11               | FW             | 3.98                   | 4.63                   | ---                                   | ---                      |
| 45                                 | 11/19/2002        | 914   | 2.2                                | 2.50               | -2.72              | 4.40               | .6                  | -1.09               | FW             | 4.63                   | 4.18                   | ---                                   | ---                      |
| 46                                 | 11/19/2002        | 1,345   | 4.1                                | 4.04               | -0.83              | 2.50               | 1.6                 | -0.21               | FW             | 3.31                   | 3.63                   | ---                                   | ---                      |
| 47                                 | 11/20/2002        | 1,775   | 6.0                                | 5.53               | 1.59               | .60                | 9.2                 | .29                 | FW             | 2.73                   | 2.87                   | ---                                   | ---                      |
| 49                                 | 05/17/2004        | 493   | 1.0                                | 1.62               | -2.03              | 5.60               | .3                  | -1.25               | FW             | 4.78                   | 4.58                   | ---                                   | ---                      |
| 50                                 | 05/17/2004        | 1,098   | 2.0                                | 2.38               | -0.75              | 4.60               | .5                  | -0.32               | FW             | ---                    | ---                    | ---                                   | ---                      |
| 51                                 | 05/17/2004        | 2,017   | 5.0                                | 5.12               | 2.46               | 1.60               | 3.2                 | .48                 | FW             | 3.48                   | 3.31                   | ---                                   | ---                      |
| <b>52</b>                          | <b>05/24/2004</b> | <b>1,689</b>  | <b>6.0</b>                         | <b>6.36</b>        | <b>5.32</b>        | <b>.60</b>         | <b>10.6</b>         | <b>.84</b>          | <b>SW</b>      | <b>2.11</b>            | <b>2.81</b>            | <b>0.75</b>                           | <b>0.80</b>              |
| 53                                 | 03/17/2006        | 1,077   | 4.0                                | 2.96               | 1.24               | 2.60               | 1.1                 | .42                 | FW             | 4.23                   | 3.80                   | ---                                   | ---                      |
| <sup>b</sup> 54                    | 03/17/2006        | 401   | 2.0                                | 1.69               | -1.22              | 4.60               | .4                  | -0.72               | FW             | ---                    | ---                    | ---                                   | ---                      |
| <sup>c</sup> 55                    | 03/16/2007        | 1,132   | 4.5                                | 3.46               | 2.29               | 2.10               | 1.6                 | .66                 | FW             | 3.52                   | 3.62                   | ---                                   | ---                      |
| <b>56</b>                          | <b>08/22/2007</b> | <b>1,710</b>  | <b>6.0</b>                         | <b>5.99</b>        | <b>5.05</b>        | <b>.60</b>         | <b>10.0</b>         | <b>.84</b>          | <b>SW</b>      | <b>2.33</b>            | <b>2.84</b>            | <b>.82</b>                            | <b>.78</b>               |
| <b>57</b>                          | <b>08/27/2007</b> | <b>1,724</b>  | <b>6.0</b>                         | <b>7.15</b>        | <b>6.50</b>        | <b>.60</b>         | <b>11.9</b>         | <b>.91</b>          | <b>SW</b>      | <b>1.80</b>            | <b>2.77</b>            | <b>.65</b>                            | <b>.62</b>               |
| <b>58</b>                          | <b>03/26/2008</b> | <b>1,440</b>  | <b>5.5</b>                         | <b>4.30</b>        | <b>3.35</b>        | <b>1.10</b>        | <b>3.9</b>          | <b>.78</b>          | <b>SW</b>      | <b>3.23</b>            | <b>3.22</b>            | <b>1.00</b>                           | <b>.98</b>               |
| <b>59</b>                          | <b>04/16/2008</b> | <b>1,724</b>  | <b>6.0</b>                         | <b>6.48</b>        | <b>5.51</b>        | <b>.60</b>         | <b>10.8</b>         | <b>.85</b>          | <b>SW</b>      | <b>2.09</b>            | <b>2.81</b>            | <b>.74</b>                            | <b>.76</b>               |
| <b>60</b>                          | <b>06/20/2008</b> | <b>1,703</b>  | <b>6.0</b>                         | <b>7.08</b>        | <b>6.25</b>        | <b>.60</b>         | <b>11.8</b>         | <b>.88</b>          | <b>SW</b>      | <b>1.81</b>            | <b>2.77</b>            | <b>.65</b>                            | <b>.68</b>               |

<sup>1</sup>Determined by subtracting the computed BCW flow from the measured total BCW and HCG flow.

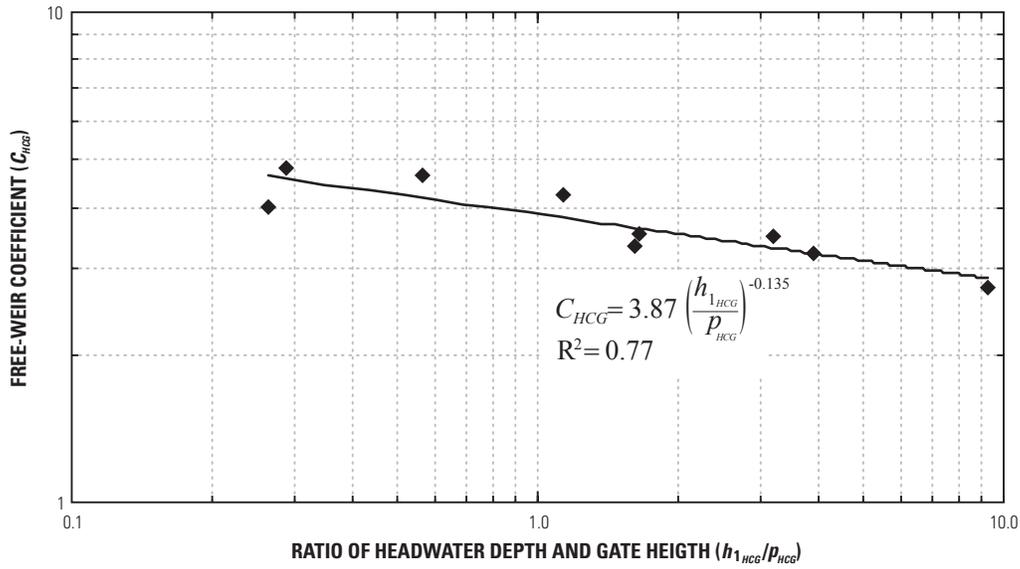
<sup>2</sup>Ratio of measured and computed  $C_{hrcg}$ .

<sup>3</sup>Hinged-crest gate opening changed 30 minutes before measurement, measurement not used in equation development.

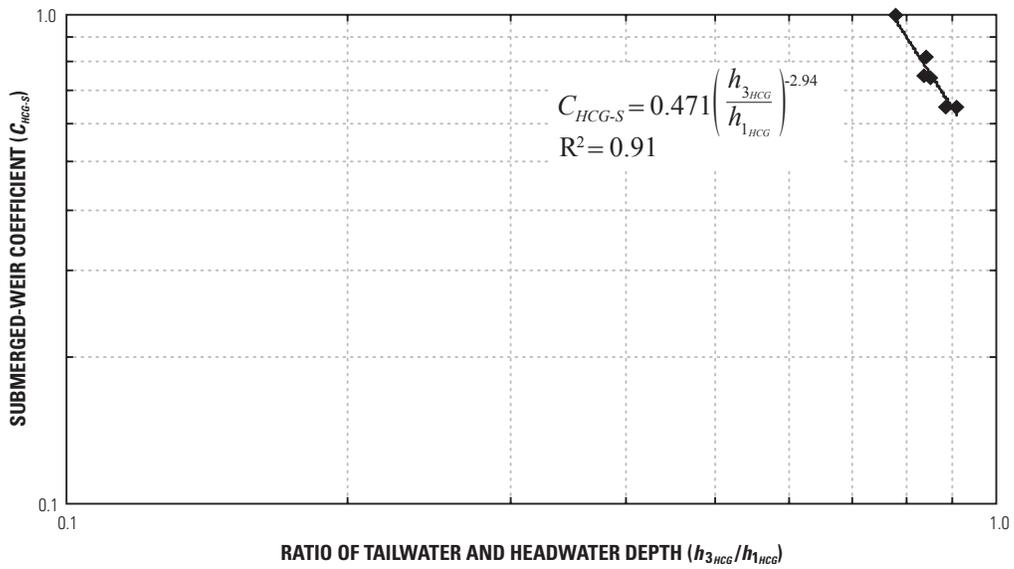
<sup>4</sup>Outlier, measurement not used in equation development.

<sup>5</sup>Total flow (BCW, HCG, and SL) measured without a separate measurement of sluice gate flow. The SL flow is calculated and subtracted from total flow.

Bold text rows indicate submerged HCG conditions.



**Figure 8.** Discharge coefficient for free-weir flow and the ratio of headwater depth and gate height for the hinged-crest gate on the Fox River at McHenry, Illinois, ( $R^2$ , coefficient of determination).



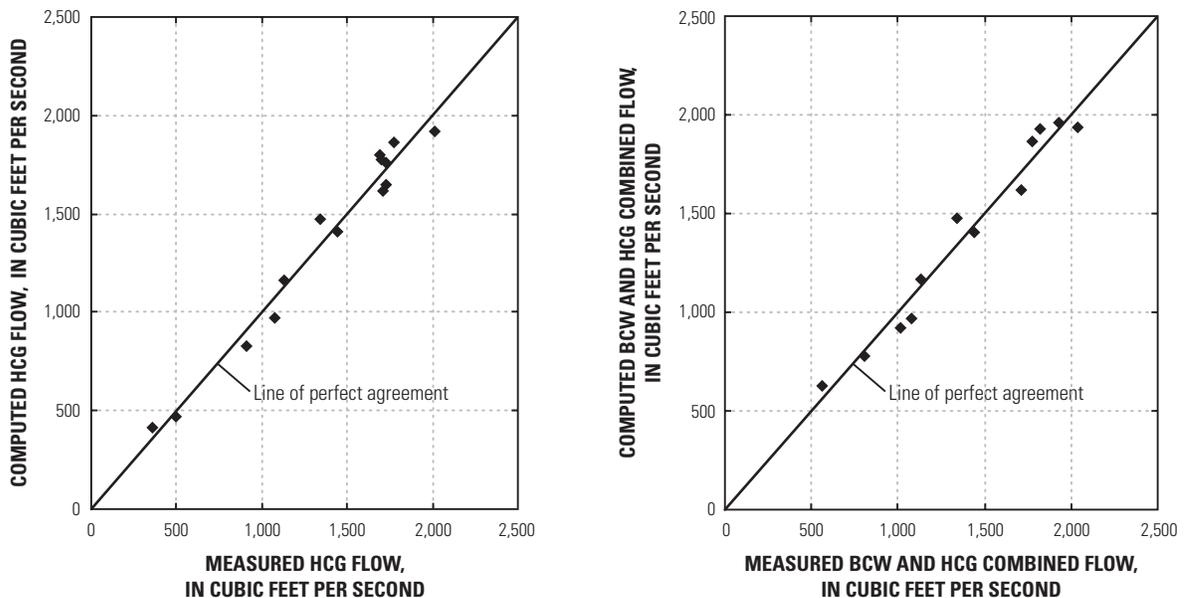
**Figure 9.** Discharge coefficient for submerged-weir flow and the ratio of headwater and tailwater depth for the hinged-crest gate on the Fox River at McHenry, Illinois, ( $R^2$ , coefficient of determination).

**Table 6.** Measured and computed flows for the broad-crested weir and hinged-crest gate near McHenry, Illinois.

[USGS, U.S. Geological Survey; BCW, broad-crested weir; ft<sup>3</sup>/s, cubic foot per second; HCG, hinged-crest gate; C/M, ratio of computed and measured flow]

| USGS measurement number | Date       | BCW computed flow (ft <sup>3</sup> /s) | HCG   |  | C/M  | BCW and HCG                            |  | C/M  |
|-------------------------|------------|--|---|--|------|--|--|------|
|                         |            |  | Measured flow <sup>1</sup> (M) (ft <sup>3</sup> /s) | Computed flow (C) (ft <sup>3</sup> /s) |      | Measured flow (M) (ft <sup>3</sup> /s) | Computed flow (C) (ft <sup>3</sup> /s) |      |
| 44                      | 11/18/2002 | 206                                    | 359   | 417                                    | 1.16 | 565                                    | 623                                    | 1.10 |
| 45                      | 11/19/2002 | 98                                     | 914   | 826                                    | .90  | 1,012                                  | 924                                    | .91  |
| 46                      | 11/19/2002 | 0                                      | 1,345   | 1,473                                  | 1.09 | 1,345                                  | 1,473                                  | 1.09 |
| 47                      | 11/20/2002 | 0                                      | 1,775   | 1,864                                  | 1.05 | 1,775                                  | 1,864                                  | 1.05 |
| 49                      | 05/17/2004 | 310                                    | 493   | 472                                    | .96  | 803                                    | 782                                    | .97  |
| 51                      | 05/17/2004 | 23                                     | 2,017   | 1,916                                  | .95  | 2,040                                  | 1,939                                  | .95  |
| 52                      | 05/24/2004 | 131                                    | 1,689   | 1,797                                  | 1.06 | 1,820                                  | 1,927                                  | 1.06 |
| 53                      | 03/17/2006 | 0                                      | 1,077   | 968                                    | .90  | 1,077                                  | 968                                    | .90  |
| 55                      | 03/16/2007 | 0                                      | 1,132   | 1,164                                  | 1.03 | 1,132                                  | 1,164                                  | 1.03 |
| 56                      | 08/22/2007 | 0                                      | 1,710   | 1,618                                  | .95  | 1,710                                  | 1,618                                  | .95  |
| 57                      | 08/27/2007 | 826                                    | 1,724   | 1,650                                  | .96  | 2,550                                  | 2,476                                  | .97  |
| 58                      | 03/26/2008 | 0                                      | 1,440   | 1,408                                  | .98  | 1,440                                  | 1,408                                  | .98  |
| 59                      | 04/16/2008 | 206                                    | 1,724   | 1,756                                  | 1.02 | 1,930                                  | 1,962                                  | 1.02 |
| 60                      | 06/20/2008 | 747                                    | 1,703   | 1,775                                  | 1.04 | 2,450                                  | 2,522                                  | 1.03 |

<sup>1</sup>Determined by subtracting the computed BCW flow from the measured total BCW and HCG flow.



**Figure 10.** Measured and computed flows for the broad-crested weir and hinged-crest gate near McHenry, Illinois, (BCW, broad-crested weir; HCG, hinged-crest gate).

### Sluice Gates

A side-view schematic of the sluice gates and parameters used in the control-structure rating are shown in figure 11. Fifty measurements, ranging from 64 to 4,054 ft<sup>3</sup>/s, were used to describe free- and submerged-weir and orifice flow through the sluice gates. Characteristics of the flow and the measured and computed discharge coefficients are listed in table 7 and appendix B. Standard weir and orifice equations (table 8) described in Chow (1959), Collins (1977), and Roberson and others (1998) are used to describe flow through the sluice gates. Chow (1959) stated the following regarding the orifice equation presented in table 8:

“For the purpose of experimental studies, ... The form of this equation is the same for both free and submerged flows.”

For this reason, a submergence coefficient is simply added to equation 16 (table 8) to develop the submerged-orifice equation (equation 19); Roberson and others (1998) show the same orifice equation. For the purpose of this study, the submerged-orifice equation presented by Collins (1977) and Fisk (1988) is not used.

Utilizing the measurement data, the resulting free- and submerged-weir and orifice-coefficient equations are presented in table 8, figures 12, 13, and 14. There is no figure for the free-orifice coefficient. Multiple-linear regression instead was used to develop the free-orifice coefficient equation in table 8. The coefficient of determination (R<sup>2</sup>) for this equation (0.80) regressing  $h_{gSL}$  and  $h_{1SL}$  was 0.15 higher compared to using the ratio  $h_{gSL}$  and  $h_{1SL}$ .

The data indicate the following flow-regime criteria conditions. Weir flow occurs when  $h_{gSL}/h_{1SL}$  is greater than or equal to 0.73. Submerged-weir flow occurs when  $h_{3SL}/h_{1SL}$  is greater than 0.80. Orifice flow occurs when  $h_{gSL}/h_{1SL}$  is less than 0.73 and either  $h_{3SL}/h_{gSL}$  is less than 1.0 or  $h_{3SL}/h_{1SL}$  is less than or equal to 0.70. Submerged-orifice flow occurs when  $h_{3SL}/h_{gSL}$  is greater than or equal to 1.0 and  $h_{3SL}/h_{1SL}$  is greater than 0.70.

The measured and computed sluice gate flows for McHenry are presented in table 7 and figure 15 for comparison. All 50 computed sluice gate flows are within 11 percent of measured flows. All 17 measured flows above 2,000 ft<sup>3</sup>/s were computed within 6 percent.

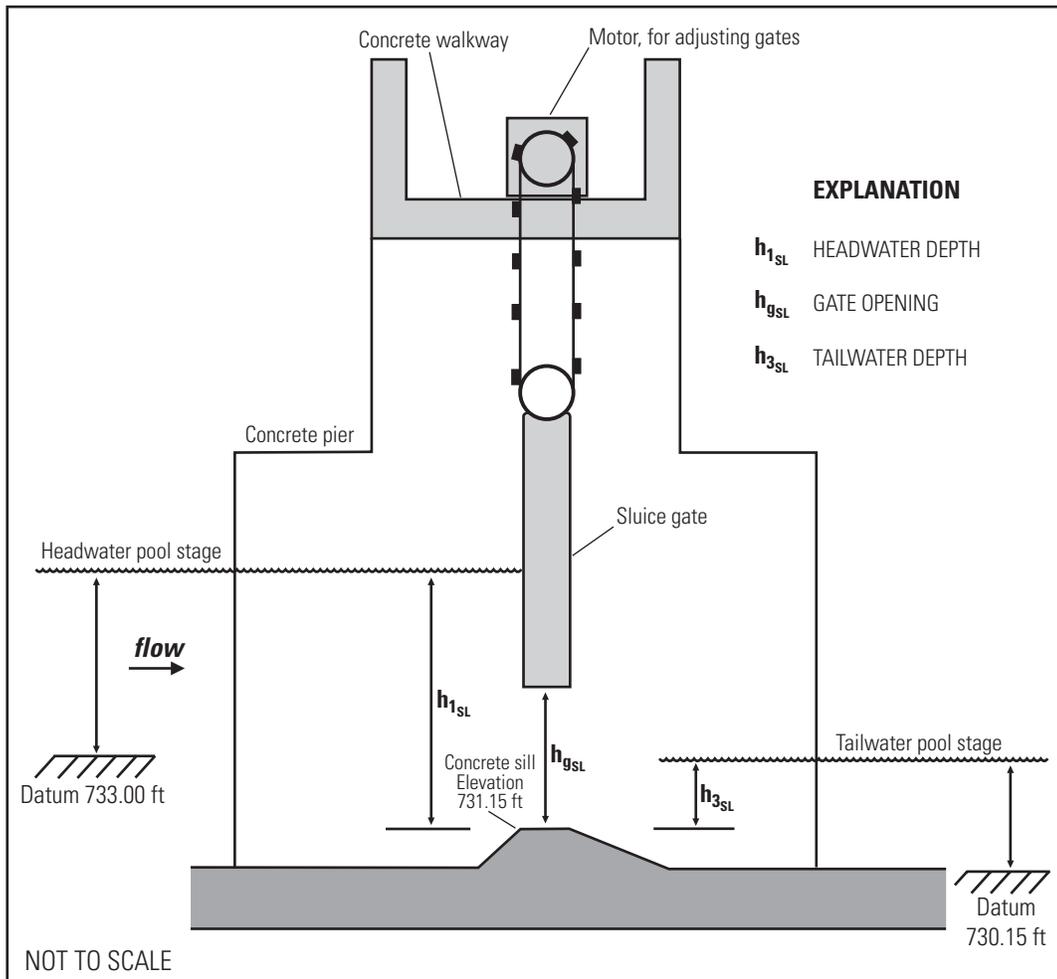


Figure 11. Schematic (side view) of sluice gates on the Fox River at McHenry, Illinois, (ft, foot).

**Table 7.** Sluice gate measured and computed flow characteristics and coefficients near McHenry, Illinois.

[USGS, U.S. Geological Survey; ft<sup>3</sup>/s, cubic foot per second; h<sub>gsl</sub>, sluice gate opening referenced to the concrete sill; ft, foot; h<sub>st</sub>, headwater depth above the sluice-gate sill; h<sub>st</sub>, tailwater depth above the sluice-gate sill; C<sub>slw</sub>, free-weir coefficient for the sluice gate; C<sub>slo</sub>, free-orifice coefficient for the sluice gate; C<sub>slws</sub>, submerged-weir coefficient for the sluice gate; C<sub>slws</sub>, submerged-orifice coefficient for the sluice gate; C/M, ratio of computed and measured flow; FW, free-weir flow; FO, free-orifice flow; SO, submerged-orifice flow; ---, not determined]

| USGS<br>measure-<br>ment<br>number | Date       | Measured<br>flow (M)<br>(ft <sup>3</sup> /s) | Gate<br>opening<br>h <sub>gsl</sub> (ft) | h <sub>st</sub><br>(ft) | h <sub>gsl</sub><br>(ft) | h <sub>st</sub> /h <sub>gsl</sub> | Flow<br>Regime | Measured                                |  | Computed                                |  | Computed<br>flow (C)<br>(ft <sup>3</sup> /s) | C/M |
|------------------------------------|------------|--|--|-------------------------|--------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|----------------|---|--|---|--|--|-----|
|                                    |            |  |  |                         |                          |                                   |                                   |                                   |                                   |                | C <sub>slw</sub> or<br>C <sub>slo</sub> | C <sub>slws</sub> or<br>C <sub>slo-s</sub> | C <sub>slw</sub> or<br>C <sub>slo</sub> | C <sub>slws</sub> or<br>C <sub>slo-s</sub> |  |     |
| 1                                  | 03/22/1985 | 2,790  | 4.0                                      | 5.36                    | 2.90                     | 0.54                              | 0.72                              | 0.75                              | FW                                | 3.27           | 3.17                                    | ---  | ---                                     | 2,700                                      | 0.97   |     |
| 2                                  | 03/22/1985 | 1,990  | 3.0                                      | 5.53                    | 2.70                     | 0.49                              | 0.90                              | .54                               | FO                                | .51            | .53                                     | ---  | ---                                     | 2,052                                      | 1.03   |     |
| 3                                  | 03/26/1985 | 2,100  | 3.8                                      | 4.49                    | 2.45                     | .55                               | .64                               | .85                               | FW                                | 3.21           | 3.22                                    | ---  | ---                                     | 2,108                                      | 1.00   |     |
| 4                                  | 03/26/1985 | 1,850  | 3.3                                      | 4.56                    | 2.42                     | .53                               | .73                               | .72                               | FO                                | .48            | .48                                     | ---  | ---                                     | 1,876                                      | 1.01   |     |
| 6                                  | 05/16/1985 | 448  | .6                                       | 5.88                    | .35                      | .06                               | .58                               | .10                               | FO                                | .56            | .60                                     | ---  | ---                                     | 480  | 1.07   |     |
| x7                                 | 10/04/1985 | 1,460  | 2.5                                      | 5.90                    | 1.75                     | .30                               | .70                               | .42                               | FO                                | .54            | .55                                     | ---  | ---                                     | 1,469                                      | 1.01   |     |
| x8                                 | 11/04/1985 | 1,830  | 3.15                                     | 5.83                    | 1.82                     | .31                               | .58                               | .54                               | FO                                | .55            | .54                                     | ---  | ---                                     | 1,805                                      | .99  |     |
| 9                                  | 03/17/1986 | 3,230  | 6.5                                      | 6.16                    | 4.03                     | .65                               | .62                               | 1.06                              | FW                                | 3.07           | 3.12                                    | ---  | ---                                     | 3,280                                      | 1.02   |     |
| 10                                 | 04/22/1986 | 833  | 1.2                                      | 5.08                    | .71                      | .14                               | .59                               | .24                               | FO                                | .56            | .54                                     | ---  | ---                                     | 803  | .96  |     |
| y11                                | 04/22/1986 | 1,047  | 2.0                                      | 4.98                    | .85                      | .17                               | .43                               | .40                               | FO                                | .53            | .52                                     | ---  | ---                                     | 1,018                                      | .97  |     |
| y11                                | 04/22/1986 | 133  | 1.0                                      | 4.98                    | .85                      | .17                               | .85                               | .20                               | FO                                | ---            | ---                                     | ---  | ---                                     | ---  | ---  |     |
| 12                                 | 05/23/1986 | 967  | 1.2                                      | 6.01                    | 1.25                     | .21                               | 1.04                              | .20                               | FO                                | .60            | .58                                     | ---  | ---                                     | 939  | .97  |     |
| 14                                 | 08/28/1986 | 180  | .2                                       | 6.07                    | .05                      | .01                               | .25                               | .03                               | FO                                | .66            | .65                                     | ---  | ---                                     | 176  | .98  |     |
| 16                                 | 09/27/1986 | 3,045  | 4.0                                      | 7.20                    | 5.15                     | .72                               | 1.29                              | .56                               | SO                                | .51            | .58                                     | 0.89                                       | 0.94                                    | 3,229                                      | 1.06   |     |
| 17                                 | 09/27/1986 | 4,054  | 7.0                                      | 7.05                    | 5.25                     | .74                               | .75                               | .99                               | FW                                | 3.15           | 3.08                                    | ---  | ---                                     | 3,962                                      | .98  |     |
| 18                                 | 09/27/1986 | 3,600  | 4.9                                      | 7.07                    | 5.25                     | .74                               | 1.07                              | .69                               | SO                                | .50            | .57                                     | .88  | .83                                     | 3,411                                      | .95  |     |
| 19                                 | 09/27/1986 | 3,320  | 4.5                                      | 7.11                    | 5.30                     | .75                               | 1.18                              | .63                               | SO                                | .50            | .57                                     | .88  | .82                                     | 3,127                                      | .94  |     |
| 21                                 | 09/30/1986 | 2,600  | 4.0                                      | 7.75                    | 5.98                     | .77                               | 1.50                              | .52                               | SO                                | .42            | .60                                     | .71  | .74                                     | 2,719                                      | 1.05   |     |
| 22                                 | 09/30/1986 | 2,920  | 4.5                                      | 7.71                    | 5.98                     | .78                               | 1.33                              | .58                               | SO                                | .42            | .59                                     | .71  | .73                                     | 2,973                                      | 1.02   |     |
| 23                                 | 10/15/1986 | 3,270  | 7.0                                      | 6.10                    | 4.10                     | .67                               | .59                               | 1.15                              | FW                                | 3.16           | 3.12                                    | ---  | ---                                     | 3,236                                      | .99  |     |
| 24                                 | 11/01/1990 | 636  | 1.0                                      | 4.44                    | .32                      | .07                               | .32                               | .23                               | FO                                | .55            | .51                                     | ---  | ---                                     | 597  | .94  |     |
| 25                                 | 11/01/1990 | 63.9   | .1                                       | 4.52                    | .11                      | .02                               | 1.10                              | .02                               | FO                                | .54            | .60                                     | ---  | ---                                     | 70   | 1.10   |     |
| 26                                 | 11/01/1990 | 74.4   | .1                                       | 4.48                    | .05                      | .01                               | .50                               | .02                               | FO                                | .64            | .59                                     | ---  | ---                                     | 69   | .93  |     |
| 27                                 | 11/02/1990 | 73.9   | .1                                       | 4.53                    | -.42                     | -.09                              | -.42                              | .02                               | FO                                | .63            | .60                                     | ---  | ---                                     | 70   | .95  |     |
| 28                                 | 11/03/1990 | 74.1   | .1                                       | 4.76                    | -.55                     | -.12                              | -.50                              | .02                               | FO                                | .62            | .61                                     | ---  | ---                                     | 73   | .99  |     |
| 29                                 | 11/04/1990 | 75   | .1                                       | 5.02                    | -.65                     | -.13                              | -.60                              | .02                               | FO                                | .61            | .62                                     | ---  | ---                                     | 77   | 1.03   |     |
| 30                                 | 11/04/1990 | 75.9   | .1                                       | 5.02                    | -.65                     | -.13                              | -.60                              | .02                               | FO                                | .61            | .62                                     | ---  | ---                                     | 77   | 1.02   |     |
| 31                                 | 11/05/1990 | 82.6   | .1                                       | 5.41                    | -.60                     | -.11                              | -.60                              | .02                               | FO                                | .64            | .64                                     | ---  | ---                                     | 83   | 1.00   |     |
| 32                                 | 11/05/1990 | 1,340  | 2.5                                      | 4.69                    | .74                      | .16                               | .30                               | .53                               | FO                                | .45            | .50                                     | ---  | ---                                     | 1,484                                      | 1.11   |     |
| 33                                 | 11/05/1990 | 1,310  | 2.5                                      | 4.61                    | .89                      | .19                               | .36                               | .54                               | FO                                | .44            | .49                                     | ---  | ---                                     | 1,461                                      | 1.11   |     |

**Table 7.** Sluice gate measured and computed flow characteristics and coefficients near McHenry, Illinois.—Continued

[USGS, U.S. Geological Survey; ft<sup>3</sup>/s, cubic foot per second; h<sub>gsl</sub>, sluice gate opening referenced to the concrete sill; ft, foot; h<sub>st</sub>, headwater depth above the sluice-gate sill; h<sub>st</sub>, tailwater depth above the sluice-gate sill; C<sub>slw</sub>, free-weir coefficient for the sluice gate; C<sub>slo</sub>, free-orifice coefficient for the sluice gate; C<sub>slws</sub>, submerged-weir coefficient for the sluice gate; C<sub>slo-s</sub>, submerged-orifice coefficient for the sluice gate; C/M, ratio of computed and measured flow; FW, free-weir flow; FO, free-orifice flow; SO, submerged-orifice flow; ---, not determined]

| USGS<br>measure-<br>ment<br>number | Date              | Measured<br>flow (M)<br>(ft <sup>3</sup> /s) | Gate<br>opening<br>h <sub>gst</sub> (ft) | h <sub>stl</sub><br>(ft) | h <sub>gsl</sub><br>(ft) | h <sub>stl</sub> /h <sub>gsl</sub> | h <sub>stl</sub> /h <sub>gst</sub> | h <sub>stl</sub> /h <sub>stl</sub> | Flow<br>Regime | Measured                                   |   | Computed                                   |   | C/M          |             |
|------------------------------------|-------------------|--|--|--------------------------|--------------------------|------------------------------------|------------------------------------|------------------------------------|----------------|--|---|--|---|--------------|-------------|
|                                    |                   |  |  |                          |                          |                                    |                                    |                                    |                | C <sub>slw</sub><br>or<br>C <sub>slo</sub> | C <sub>slws</sub><br>or<br>C <sub>slo-s</sub> | C <sub>slw</sub><br>or<br>C <sub>slo</sub> | C <sub>slws</sub><br>or<br>C <sub>slo-s</sub> |              |             |
| 34                                 | 11/06/1990        | 1,370  | 2.5                                      | 4.51                     | 1.19                     | 0.26                               | 0.48                               | 0.55                               | FO             | 0.47                                       | ---   | ---  | ---   | 1.431        | 1.04        |
| 35                                 | 11/06/1990        | 1,500  | 2.5                                      | 4.45                     | 1.38                     | .31                                | .55                                | .56                                | FO             | .52  | ---   | ---  | ---   | 1,413        | .94         |
| 36                                 | 11/07/1990        | 1,360  | 2.5                                      | 4.54                     | 1.52                     | .33                                | .61                                | .55                                | FO             | .46  | ---   | ---  | ---   | 1,440        | 1.06        |
| 37                                 | 11/07/1990        | 1,510  | 2.5                                      | 4.54                     | 1.52                     | .33                                | .61                                | .55                                | FO             | .51  | ---   | ---  | ---   | 1,440        | .95         |
| 38                                 | 11/07/1990        | 1,480  | 2.5                                      | 4.54                     | 1.56                     | .34                                | .62                                | .55                                | FO             | .50  | ---   | ---  | ---   | 1,440        | .97         |
| 39                                 | 11/08/1990        | 1,480  | 2.5                                      | 4.56                     | 1.60                     | .35                                | .64                                | .55                                | FO             | .50  | ---   | ---  | ---   | 1,446        | .98         |
| 40                                 | 11/08/1990        | 1,580  | 2.5                                      | 4.56                     | 1.60                     | .35                                | .64                                | .55                                | FO             | .54  | ---   | ---  | ---   | 1,446        | .92         |
| 41                                 | 11/09/1990        | 1,460  | 2.5                                      | 4.54                     | 1.58                     | .35                                | .63                                | .55                                | FO             | .50  | ---   | ---  | ---   | 1,440        | .99         |
| <b>42</b>                          | <b>04/24/1993</b> | <b>3,920</b>                                 | <b>6.0</b>                               | <b>7.02</b>              | <b>2.24</b>              | <b>.32</b>                         | <b>.37</b>                         | <b>.85</b>                         | <b>FW</b>      | <b>3.07</b>                                | <b>---</b>                                    | <b>---</b>                                 | <b>---</b>                                    | <b>3,938</b> | <b>1.00</b> |
| <b>43</b>                          | <b>04/28/1993</b> | <b>3,664</b>                                 | <b>6.0</b>                               | <b>6.83</b>              | <b>1.78</b>              | <b>.26</b>                         | <b>.30</b>                         | <b>.88</b>                         | <b>FW</b>      | <b>2.99</b>                                | <b>---</b>                                    | <b>---</b>                                 | <b>---</b>                                    | <b>3,790</b> | <b>1.03</b> |
| 49                                 | 05/17/2004        | 1,760  | 2.2                                      | 6.14                     | 2.50                     | .41                                | 1.14                               | .36                                | FO             | .59  | ---   | ---  | ---   | 1,691        | .96         |
| 50                                 | 05/17/2004        | 1,690  | 2.2                                      | 5.95                     | 2.74                     | .46                                | 1.25                               | .37                                | FO             | .57  | ---   | ---  | ---   | 1,642        | .97         |
| 51                                 | 05/17/2004        | 1,250  | 2.2                                      | 5.62                     | 3.00                     | .53                                | 1.36                               | .39                                | FO             | .54  | ---   | ---  | ---   | 1,246        | 1.00        |
| <b>52</b>                          | <b>05/24/2004</b> | <b>3,020</b>                                 | <b>5.7</b>                               | <b>5.89</b>              | <b>4.85</b>              | <b>.82</b>                         | <b>.85</b>                         | <b>.97</b>                         | <b>SW</b>      | <b>3.07</b>                                | <b>0.98</b>                                   | <b>0.97</b>                                | <b>---</b>                                    | <b>2,992</b> | <b>.99</b>  |
| 53                                 | 03/17/2006        | 1,664  | 3.0                                      | 4.49                     | 2.77                     | .62                                | .92                                | .67                                | FO             | .47  | ---   | ---  | ---   | 1,691        | 1.02        |
| 54                                 | 03/17/2006        | 1,890  | 3.0                                      | 5.22                     | 2.31                     | .44                                | .77                                | .57                                | FO             | .50  | ---   | ---  | ---   | 1,945        | 1.03        |
| <b>55</b>                          | <b>03/16/2007</b> | <b>---</b>                                   | <b>4.0</b>                               | <b>4.49</b>              | <b>3.32</b>              | <b>.74</b>                         | <b>.83</b>                         | <b>.89</b>                         | <b>FW</b>      | <b>---</b>                                 | <b>---</b>                                    | <b>---</b>                                 | <b>---</b>                                    | <b>2,108</b> | <b>---</b>  |
| <b>56A</b>                         | <b>08/22/2007</b> | <b>2,760</b>                                 | <b>5.0</b>                               | <b>5.58</b>              | <b>4.59</b>              | <b>.82</b>                         | <b>.92</b>                         | <b>.90</b>                         | <b>SW</b>      | <b>3.05</b>                                | <b>.97</b>                                    | <b>.97</b>                                 | <b>---</b>                                    | <b>2,778</b> | <b>1.01</b> |
| <b>57A</b>                         | <b>08/27/2007</b> | <b>3,140</b>                                 | <b>6.2</b>                               | <b>6.68</b>              | <b>6.03</b>              | <b>.90</b>                         | <b>.97</b>                         | <b>.93</b>                         | <b>SW</b>      | <b>2.65</b>                                | <b>.85</b>                                    | <b>.86</b>                                 | <b>---</b>                                    | <b>3,158</b> | <b>1.01</b> |
| <b>58A</b>                         | <b>03/26/2008</b> | <b>1,970</b>                                 | <b>4.5</b>                               | <b>4.32</b>              | <b>3.36</b>              | <b>.78</b>                         | <b>.75</b>                         | <b>1.04</b>                        | <b>FW</b>      | <b>3.19</b>                                | <b>---</b>                                    | <b>---</b>                                 | <b>---</b>                                    | <b>1,997</b> | <b>1.01</b> |
| <b>59A</b>                         | <b>04/16/2008</b> | <b>2,960</b>                                 | <b>5.3</b>                               | <b>5.99</b>              | <b>5.02</b>              | <b>.84</b>                         | <b>.95</b>                         | <b>.88</b>                         | <b>SW</b>      | <b>2.94</b>                                | <b>.94</b>                                    | <b>.95</b>                                 | <b>---</b>                                    | <b>2,992</b> | <b>1.01</b> |
| <b>60A</b>                         | <b>06/20/2008</b> | <b>3,280</b>                                 | <b>6.0</b>                               | <b>6.60</b>              | <b>5.76</b>              | <b>.87</b>                         | <b>.96</b>                         | <b>.91</b>                         | <b>SW</b>      | <b>2.81</b>                                | <b>.91</b>                                    | <b>.90</b>                                 | <b>---</b>                                    | <b>3,247</b> | <b>.99</b>  |

<sup>x</sup>Four gates open, one gate closed. All other measurements had five gates open, unless otherwise noted.

<sup>y</sup>Four gates were set to 2.0 ft, and one gate was set to 1.0 ft. Equations developed in this study were used to subtract flow from the gate open to 1.0 ft; a coefficient for a 2.0 ft opening was determined from the measurement.

<sup>z</sup>Sluice gate flow was not measured directly. The sluice gate flow is calculated to help determine the broad-crested weir and hinged-crest gate flow.

Black plain text indicates free-orifice measurements.

**Red bold** text indicates submerged-orifice measurements.

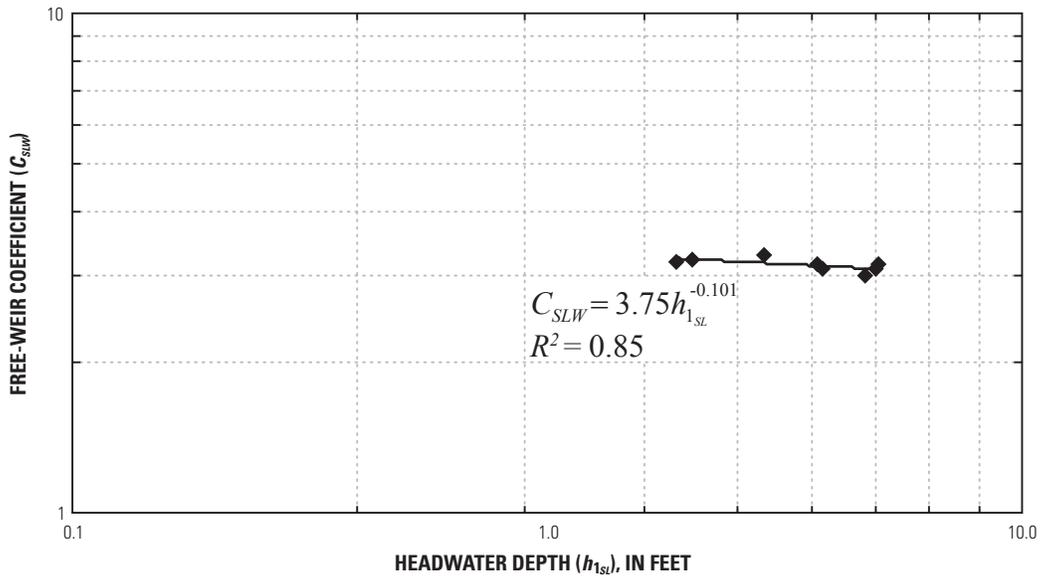
**Blue italic** text indicates free-weir measurements.

**Green bold italic** text indicates submerged-weir measurements.

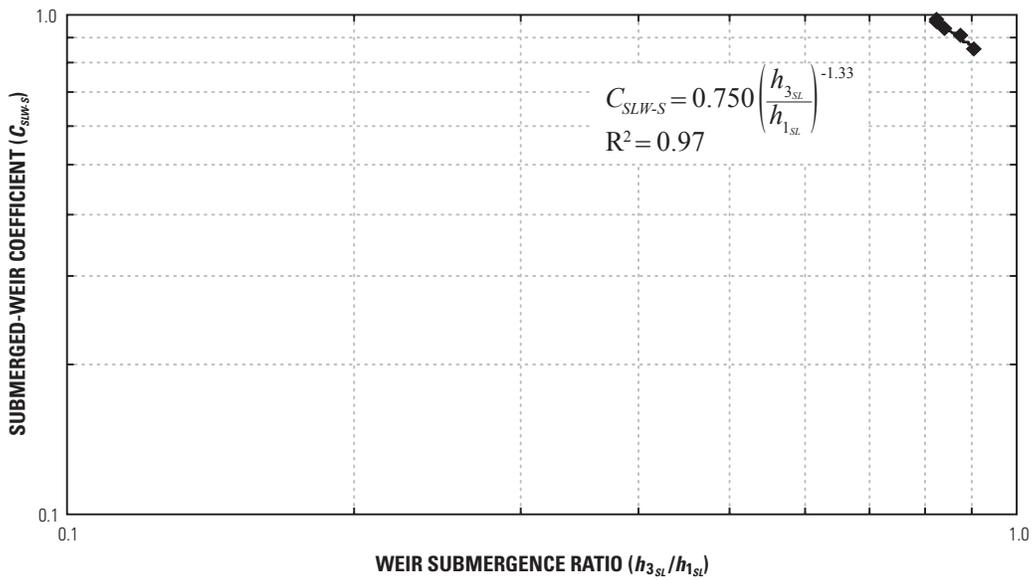
**Table 8.** Hydraulic conditions, parameters, and equations for different flow regimes for the sluice gates on the Fox River at McHenry, Illinois.

[ $h_{g_{SL}}$ , sluice gate opening referenced to the concrete sill, in feet;  $h_{1_{SL}}$ , headwater depth above the sluice-gate sill, in feet;  $h_{3_{SL}}$ , tailwater depth above the sluice-gate sill, in feet;  $Q_{SL}$ , flow through the sluice gates, ft<sup>3</sup>/s;  $C_{SLW}$ , free-weir coefficient for the sluice gate; B, length of gates, in feet;  $C_{SLW-S}$ , submerged-weir coefficient for the sluice gate;  $C_{SLO}$ , free-orifice coefficient for the sluice gate;  $C_{SLO-S}$ , submerged-orifice coefficient for the sluice gate]

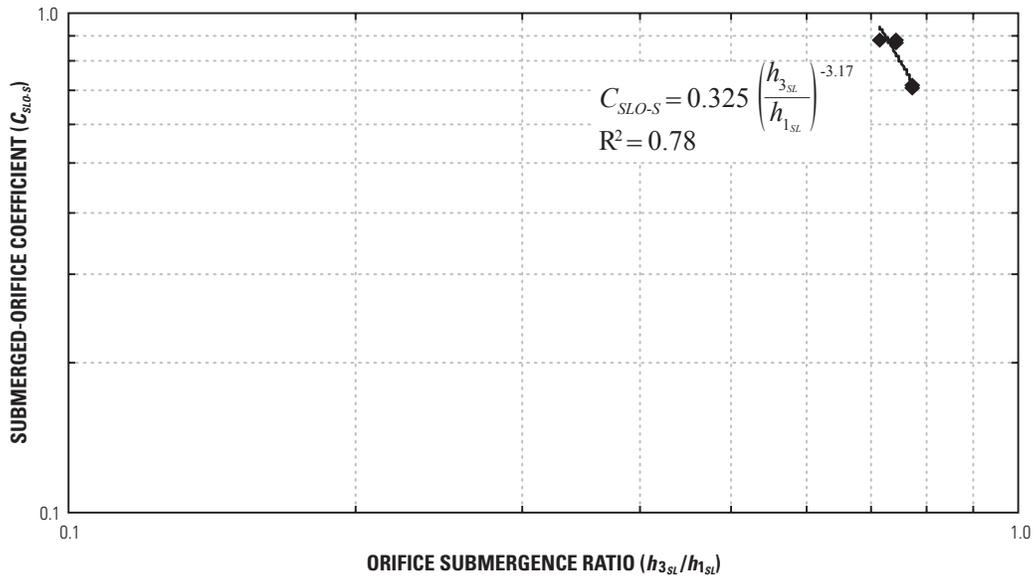
| Structure           | Flow regime       | Hydraulic conditions                                   | Parameters and equations   | Equation number  |
|---------------------|-------------------|--|--|--|
| Sluice gate weir    | Free weir (FW)    | $\frac{h_{g_{SL}}}{h_{1_{SL}}} \geq 0.73$ and          | $Q_{SL} = C_{SLW} B h_{1_{SL}}^{1.5}$                                    | 10   |
|                     |                   |  | $\frac{h_{3_{SL}}}{h_{1_{SL}}} \leq 0.80$                                | $C_{SLW} = 3.75 h_{1_{SL}}^{-0.101}$                                     |
|                     |                   |  | $B = 5 \text{ gates} \times 13.75 \text{ ft} = 68.75 \text{ ft}$         |  |
|                     |                   |  | $Q_{SL} = 257.8 h_{1_{SL}}^{1.401}$                                      | 12   |
| Sluice gate weir    | Submerged weir    | $\frac{h_{g_{SL}}}{h_{1_{SL}}} \geq 0.73$ and          | $Q_{SL} = C_{SLW} C_{SLW-S} B h_{1_{SL}}^{1.5}$                          | 13   |
|                     |                   |  | $\frac{h_{3_{SL}}}{h_{1_{SL}}} > 0.80$                                   | $C_{SLW-S} = 0.750 \left( \frac{h_{3_{SL}}}{h_{1_{SL}}} \right)^{-1.33}$ |
|                     |                   |  | $Q_{SL} = 193.4 h_{1_{SL}}^{2.731} h_{3_{SL}}^{-1.33}$                   | 15   |
| Sluice gate orifice | Free orifice      | $\frac{h_{g_{SL}}}{h_{1_{SL}}} < 0.73$ and             | $Q_{SL} = C_{SLO} B h_{g_{SL}} (2gh_{1_{SL}})^{0.5}$                     | 16   |
|                     |                   |  | $\frac{h_{3_{SL}}}{h_{g_{SL}}} < 1$ or                                   | $C_{SLO} = 0.271 h_{1_{SL}}^{0.429} h_{g_{SL}}^{-0.062}$                 |
|                     |                   | $\frac{h_{3_{SL}}}{h_{1_{SL}}} \leq 0.70$              | $B = 5 \text{ gates} \times 13.75 \text{ ft} = 68.75 \text{ ft}$         |  |
|                     |                   |  | $g = 32.2 \text{ ft} / \text{s}^2$                                       |  |
|                     |                   | $Q_{SL} = 149.5 h_{1_{SL}}^{0.929} h_{g_{SL}}^{0.938}$ | 18   |  |
| Sluice gate orifice | Submerged orifice | $\frac{h_{g_{SL}}}{h_{1_{SL}}} < 0.73$ and             | $Q_{SL} = C_{SLO} C_{SLO-S} B h_{g_{SL}} (2gh_{1_{SL}})^{0.5}$           | 19   |
|                     |                   |  | $\frac{h_{3_{SL}}}{h_{g_{SL}}} \geq 1$ and                               | $C_{SLO-S} = 0.325 \left( \frac{h_{3_{SL}}}{h_{1_{SL}}} \right)^{-3.17}$ |
|                     |                   | $\frac{h_{3_{SL}}}{h_{1_{SL}}} > 0.70$                 | $Q_{SL} = 48.6 h_{1_{SL}}^{4.099} h_{g_{SL}}^{0.938} h_{3_{SL}}^{-3.17}$ | 21   |



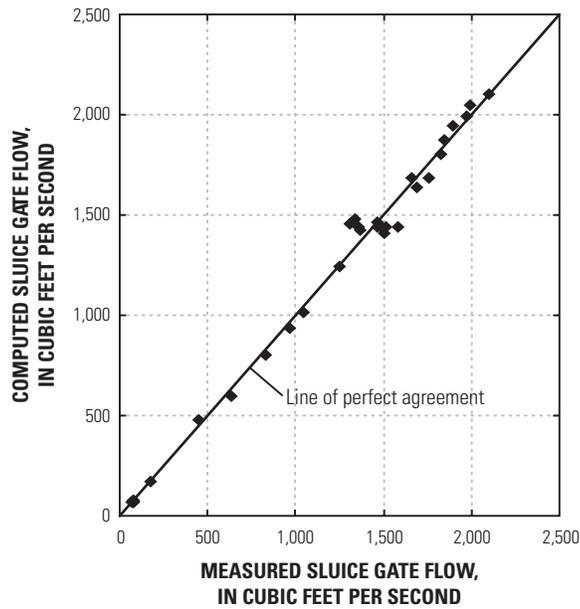
**Figure 12.** Discharge coefficient for free-weir flow and headwater depth for sluice gates on the Fox River at McHenry, Illinois, ( $R^2$ , coefficient of determination).



**Figure 13.** Discharge coefficient for submerged-weir flow and ratio of tailwater and headwater depth for sluice gates on the Fox River at McHenry, Illinois, ( $R^2$ , coefficient of determination).



**Figure 14.** Discharge coefficient for submerged-orifice flow and submergence ratio for sluice gates on the Fox River at McHenry, Illinois, ( $R^2$ , coefficient of determination).



**Figure 15.** Measured and computed flows for the sluice gates near McHenry, Illinois.

## Example Calculations

The following are examples of how streamflow was calculated using equations in table 8 and table 4. Note that total flow on the Fox River at McHenry is the summation of flow through the sluice gates, broad-crested weir, and hinged-crest gate. Thus, flow must be calculated at each of those structures separately. At times, the broad-crested weir may experience no flow over it, as shown in example 2.

**Example 1:** The following conditions exist:

Headwater pool stage is 5.15 ft, tailwater pool stage is 6.20 ft, all gates are opened to 7.0 ft ( $h_{g_{SL}}$ ), and the hinged-crest gate opening is 1.0 ft ( $h_{g_{HCG}}$ ). See figures 6 and 11 for schematic of hinged-crest gate, broad crested weir, sluice gate, and variables.

Flow over the broad-crested weir (which includes the fish ladder) is determined by first converting the headwater stage to depth above the weir crest. This is done by subtracting the difference between headwater gage datum (733.00 ft) and the elevation of the spillway crest (736.68) from the headwater stage reading,

$$h_{1_{BCW}} = 5.15 - (736.68 - 733.00) = 1.47 \text{ ft},$$

and using equation 3 from table 4.

$$\begin{aligned} Q_{BCW} &= 661.5h_{1_{BCW}}^{1.587} \\ &= 661.5(1.47)^{1.587} \\ &= 1219 \text{ ft}^3 / \text{s}. \end{aligned}$$

Flow over the hinged-crest gate is determined by first converting the stages to depths above the crest of the gate. This is done by subtracting the difference between headwater gage datum (733.00 ft) and the elevation of the gate crest (736.68 ft -  $h_{g_{HCG}}$ ) from the headwater stage and then subtracting the difference between the tailwater gage datum (730.15 ft) and the elevation of gate crest from the tailwater stage.

$$h_{1_{HCG}} = 5.15 - [(736.68 - 1.00) - 733.00] = 2.47 \text{ ft}$$

$$h_{3_{HCG}} = 6.20 - [(736.68 - 1.00) - 730.15] = .67 \text{ ft}$$

Because  $h_{3_{HCG}} / h_{1_{HCG}}$  ( $0.67/2.47=0.27$ ) is less than 0.75, FW flow exists. Before calculating flow, the depth from the concrete slab to the crest of the gate must be determined by calculating the difference between the gate crest elevation (736.68 ft -  $h_{g_{HCG}}$ ) and the elevation of the top of the concrete slab (730.08).

$$p_{HCG} = (736.68 - 1.00) - 730.08 = 5.6 \text{ ft}.$$

Using equation 6 from table 4, flow is

$$\begin{aligned} Q_{HCG} &= 193.5h_{1_{HCG}}^{1.365} p_{HCG}^{0.135} \\ &= 193.5(2.47)^{1.365}(5.6)^{0.135} \\ &= 838.9 \text{ ft}^3 / \text{s} \end{aligned}$$

Flow through the sluice gates is determined by first converting the stages to depths above the sluice-gate sill. This is done by adding the difference between headwater gage datum and the elevation of the sill (1.85) to the headwater stage and then subtracting the difference between the tailwater gage datum and the elevation of the sill (1.00) from the tailwater stage.

$$h_{1_{SL}} = 5.15 + 1.85 = 7.00 \text{ ft}$$

$$h_{3_{SL}} = 6.20 - 1.00 = 5.20 \text{ ft}$$

Because  $h_{g_{SL}} / h_{1_{SL}}$  ( $7.0/7.0=1.0$ ) is greater than 0.73 and  $h_{3_{SL}} / h_{1_{SL}}$  (0.74) is less than 0.80 (table 8), free-weir flow exists.

Using equation 12 from table 8, flow is,

$$\begin{aligned} Q_{SL} &= 257.8h_{1_{SL}}^{1.401} \\ &= 257.8(7.00)^{1.401} \\ &= 3938 \text{ ft}^3 / \text{s} \end{aligned}$$

Therefore, total flow,  $Q_{TOTAL}$ , is

$$Q_{TOTAL} = 838.9 + 1219 + 3938 = 5996 \text{ ft}^3 / \text{s}$$

**Example 2:** The following conditions exist:

Headwater pool stage is 2.57 ft, tailwater pool stage is 3.70 ft, all sluice gates are set to 3.0 ft ( $h_{g_{SL}}$ ), and the hinged-crest gate opening is 5.0 ft ( $h_{g_{HCG}}$ ).

To find flow over the broad-crested weir, first, convert pool stages to depths above weir crest as in example 1.

$$h_{1_{BCW}} = 2.57 - (736.68 - 733.00) < 0 \text{ ft}$$

Because  $h_{1_{BCW}}$  is a negative number, the weir experiences zero flow.

Flow over the hinged-crest gate is determined using the same method as in example 1.

$$h_{1_{HCG}} = 2.57 - [(736.68 - 5.00) - 733.00] = 3.89 \text{ ft}$$

$$h_{3_{HCG}} = 3.70 - [(736.68 - 5.00) - 730.15] = 2.17 \text{ ft}$$

Because  $h_{3_{HCG}} / h_{1_{HCG}}$  ( $2.17/3.89 = 0.56$ ) is less than 0.75, FW flow exists.

$$p_{HCG} = (736.68 - 5.00) - 730.08 = 1.6 \text{ ft.}$$

Using equation 6 from table 4:

$$Q_{HCG} = 193.5(3.89)^{1.365}(1.6)^{0.135}$$

$$Q_{HCG} = 1317 \text{ ft}^3 / \text{s}$$

To find flow through the sluice gates, pool stages must be converted to depths above the sluice-gate sill

$$h_{1_{SL}} = 2.57 + 1.85 = 4.42 \text{ ft}$$

$$h_{3_{SL}} = 3.70 - 1.00 = 2.70 \text{ ft}$$

Because  $h_{g_{SL}} / h_{1_{SL}}$  ( $3.0/4.42=0.68$ ) is less than 0.73, orifice flow exists. Since  $h_{3_{SL}} / h_{g_{SL}}$  ( $2.70/3.0=0.90$ ) is less than 1.0, free-orifice flow exists. Alternatively, free-orifice flow also exists because  $h_{3_{SL}} / h_{1_{SL}}$  ( $2.70/4.42=0.61$ ) is less than 0.70.

Using equation 18 from table 8, the flow is.

$$\begin{aligned} Q_{SL} &= 149.5 h_{1_{SL}}^{0.929} h_{g_{SL}}^{0.938} \\ &= 149.5(4.42)^{0.929}(3.0)^{0.938} \\ &= 1666 \text{ ft}^3 / \text{s} \end{aligned}$$

Therefore, total flow,  $Q_{TOTAL}$ , is

$$Q_{TOTAL} = 1317 + 1666 = 2983 \text{ ft}^3 / \text{s}$$

**Example 3:** The following conditions exist:

Headwater pool stage is 4.14 ft, tailwater pool stage is 5.95 ft, all gates are set to 5.7 ft ( $h_{g_{SL}}$ ), and the hinged-crest gate opening is 6.0 ft ( $h_{g_{HCG}}$ ).

Flow over the broad-crested weir is calculated in the same manner as in example 1.

$$h_{1_{BCW}} = 4.14 - (736.68 - 733.00) = 0.46 \text{ ft}$$

Using Equation 3 from table :

$$\begin{aligned} Q_{BCW} &= 661.5 h_{1_{BCW}}^{1.587} \\ &= 661.5(0.46)^{1.587} \\ Q_{BCW} &= 192.9 \text{ ft}^3 / \text{s} \end{aligned}$$

Flow over the hinged-crest gate is determined by first converting the pool stages to depths above the gate and determining the value of  $p_{HCG}$ .

$$h_{1_{HCG}} = 4.14 - [(736.68 - 6.0) - 733.00] = 6.46 \text{ ft}$$

$$h_{3_{HCG}} = 5.95 - [(736.68 - 6.0) - 730.15] = 5.42 \text{ ft}$$

$$p_{HCG} = (736.68 - 6.0) - 730.08 = 0.6 \text{ ft.}$$

Because  $h_{3_{HCG}} / h_{1_{HCG}}$  ( $5.42/6.46=0.84$ ) is greater than 0.75, submerged-weir flow exists.

Using equation 9 from table 4,

$$\begin{aligned} Q_{HCG} &= 91.14 h_{1_{HCG}}^{4.305} h_{3_{HCG}}^{-2.94} p_{HCG}^{0.135} \\ &= 91.14(6.46)^{4.305}(5.42)^{-2.94}(0.6)^{0.135} \\ &= 1819 \text{ ft}^3 / \text{s} \end{aligned}$$

To find flow through the sluice gates, pool stages must be converted to depths above the sluice-gate sill

$$h_{1_{SL}} = 4.14 + 1.85 = 5.99 \text{ ft}$$

$$h_{3_{SL}} = 5.95 - 1.00 = 4.95 \text{ ft}$$

Because  $h_{g_{SL}} / h_{1_{SL}}$  ( $5.7/5.99 = 0.95$ ) is greater than 0.73 and  $h_{3_{SL}} / h_{1_{SL}}$  ( $4.95/5.99 = 0.83$ ) is greater than 0.80, submerged-weir flow exists.

Using equation 15 from table 8,

$$\begin{aligned} Q_{SL} &= 193.4 h_{1_{SL}}^{2.73} h_{3_{SL}}^{-1.33} \\ &= 193.4(5.99)^{2.73}(4.95)^{-1.33} \\ &= 3060 \text{ ft}^3 / \text{s} \end{aligned}$$

Therefore, total flow,  $Q_{TOTAL}$ , is

$$Q_{TOTAL} = 192.9 + 1819 + 3060 = 5072 \text{ ft}^3 / \text{s}$$

**Example 4:** The following conditions exist:

Headwater pool stage is 5.30 ft, tailwater pool stage is 6.10 ft, all sluice gates are set to 4.0 ft ( $h_{g_{SL}}$ ), and the hinged-crest gate opening is 5.5 ft ( $h_{g_{HCG}}$ ).

Flow over the broad-crested weir is calculated in the same manner as in example 1.

$$h_{1_{BCW}} = 5.30 - (736.68 - 733.00) = 1.62 \text{ ft}$$

$$\begin{aligned} Q_{BCW} &= 661.5 h_{1_{BCW}}^{1.587} \\ &= 661.5(1.62)^{1.587} \\ &= 1422 \text{ ft}^3 / \text{s} \end{aligned}$$

Flow over the hinged-crest gate is characterized as free-weir flow, so the flow can be found in the same manner as in example 1.

$$h_{1_{HCG}} = 5.30 - [(736.68 - 5.50) - 733.00] = 7.12 \text{ ft}$$

$$h_{3_{HCG}} = 6.10 - [(736.68 - 5.5) - 730.15] = 5.07 \text{ ft}$$

Because  $h_{3_{HCG}} / h_{1_{HCG}}$  ( $5.07/7.12=0.71$ ) is less than 0.75, FW flow exists.

$$p_{HCG} = (736.68 - 5.50) - 730.08 = 1.10 \text{ ft.}$$

Using equation 6 from table 4, flow is

$$\begin{aligned} Q_{HCG} &= 193.5h_{1_{HCG}}^{1.365} p_{HCG}^{0.135} \\ &= 193.5(7.12)^{1.365} (1.10)^{0.135} \\ &= 2857 \text{ ft}^3 / \text{s} \end{aligned}$$

To calculate flow through the sluice gates, headwater and tailwater pool stages must be converted to depths above the sluice gate sill.

$$h_{1_{SL}} = 5.30 + 1.85 = 7.15 \text{ ft}$$

$$h_{3_{SL}} = 6.10 - 1.00 = 5.10 \text{ ft}$$

Because  $h_{g_{SL}} / h_{1_{SL}}$  ( $4.0/7.15 = 0.56$ ) is less than 0.73,  $h_{3_{SL}} / h_{g_{SL}}$  ( $5.10/4.0 = 1.28$ ) is greater than 1, and  $h_{3_{SL}} / h_{1_{SL}}$  ( $5.10/7.15 = 0.71$ ) is greater than 0.70, submerged-orifice flow exists.

Using equation 21 from table 8,

$$\begin{aligned} Q_{SL} &= 48.6h_{1_{SL}}^{4.099} h_{g_{SL}}^{0.938} h_{3_{SL}}^{-3.17} \\ Q_{SL} &= 48.6(7.15)^{4.099} (4.0)^{0.938} (5.10)^{-3.17} \\ &= 3237 \text{ ft}^3 / \text{s} \end{aligned}$$

Therefore, total flow,  $Q_{TOTAL}$ , is

$$Q_{TOTAL} = 1422 + 2857 + 3237 = 7516 \text{ ft}^3 / \text{s}$$

## Algonquin Control-Structure Ratings

The Algonquin control structure is at river mile 81.6 on the Fox River in northeastern Illinois (fig. 1), 16.2 miles downstream of McHenry control structure. The drainage area at the headwater gage is 1,403 mi<sup>2</sup>. The 894-acre reservoir created by the dam is primarily for recreation. The control structures at Algonquin consist of a 242-ft ogee spillway and a 50-ft-wide hinged-crest gate (figs. 16, 17, and 18). The elevation of structure components and headwater and tailwater gage datums are presented in table 9.

At the Algonquin control structure, streamflow measurements collected by the USGS at high flows during this study were made with a tethered ADCP boat off the downstream end of the Route 62 Bridge (fig. 16). Given the ability to measure flows within a close proximity to the structure, the total flow could be separated into flow through the hinged-crest gate and flow over the ogee spillway for the majority of the measurements.

The flow separation was completed by analyzing the velocity data obtained by the ADCP during each measurement and determining the approximate location where the flow “splits” between the hinged-crest gate and the ogee spillway. The vertically averaged velocity vectors (fig. 19) show a clear separation in the area where the flow splits between the gate and the spillway. A similar separation can be seen in the velocity contour plot (fig. 20) where the velocities decrease appreciably in the area of the flow split.

The flow separations are more obvious under certain flow conditions and gate settings than others. Typically, the actual separation point was chosen to be at the center of the break in velocity vectors (fig. 19) or at the center of the slower velocity section (fig. 20). A sensitivity analysis was performed to determine the potential accuracy of this method. In general, selecting separation points at either end of the slower velocity section affected the estimated flow through the gate by about 5 to 8 percent.

**Table 9.** Elevation of structure and streamflow-gaging station datums on the Fox River at Algonquin, Illinois.

[NGVD 1929, National Geodetic Vertical Datum of 1929]

| Structure or gage   | Elevation, in feet<br>(NGVD 1929) |
|---|-----------------------------------|
| Algonquin Dam ogee spillway crest elevation               | 730.10                            |
| Algonquin Dam hinged-crest gate floor elevation           | 723.58                            |
| Headwater station datum, Fox River at Algonquin, Illinois | 729.48                            |
| Tailwater station datum, Fox River at Algonquin, Illinois | 719.48                            |



Figure 16. Location of control structures on the Fox River at Algonquin, Illinois.

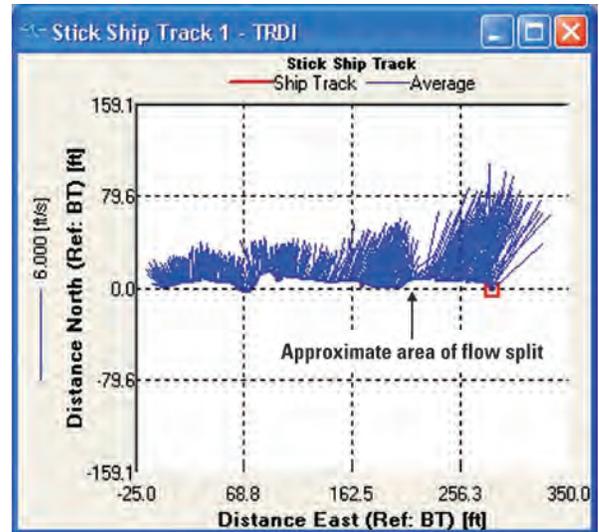


**Figure 17.** Downstream side of hinged-crest gate and ogee spillway on the Fox River at Algonquin, Illinois.

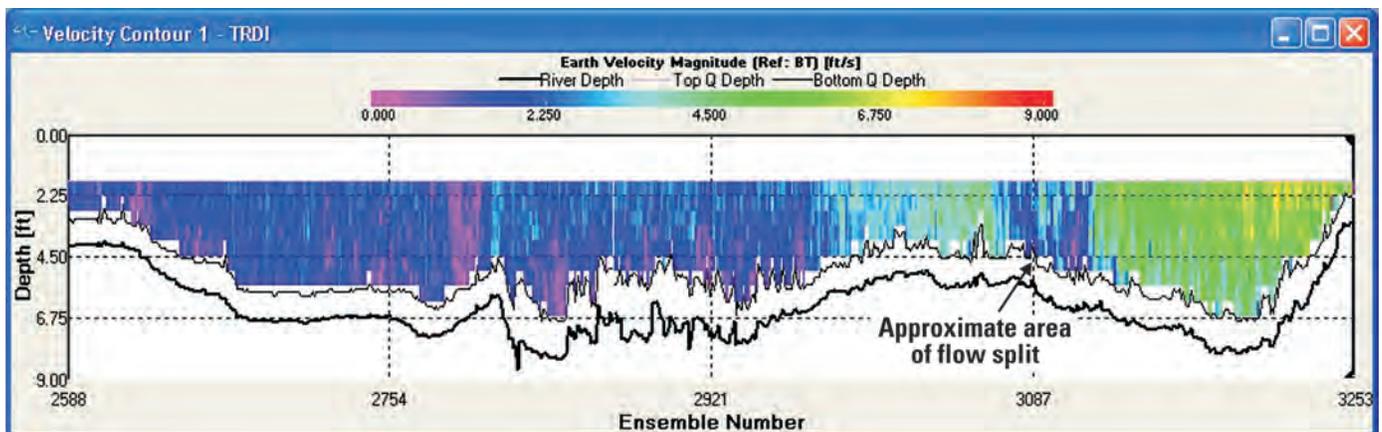


Figure 18. Close-up of downstream side of hinged-crest gate on the Fox River at Algonquin, Illinois.

**Figure 19.** Vertically averaged velocity vectors for a typical Acoustic Doppler Current Profiler streamflow measurement upstream of the control structure at Algonquin, Illinois, (ft, foot; ft/s, foot per second; BT, bottom tracking).



**Figure 20.** Velocity contour plot for the Acoustic Doppler Current Profiler streamflow measurement shown in figure 19 upstream of the control structure at Algonquin, Illinois, (ft, foot; ft/s, foot per second; BT, bottom tracking; Q, streamflow).



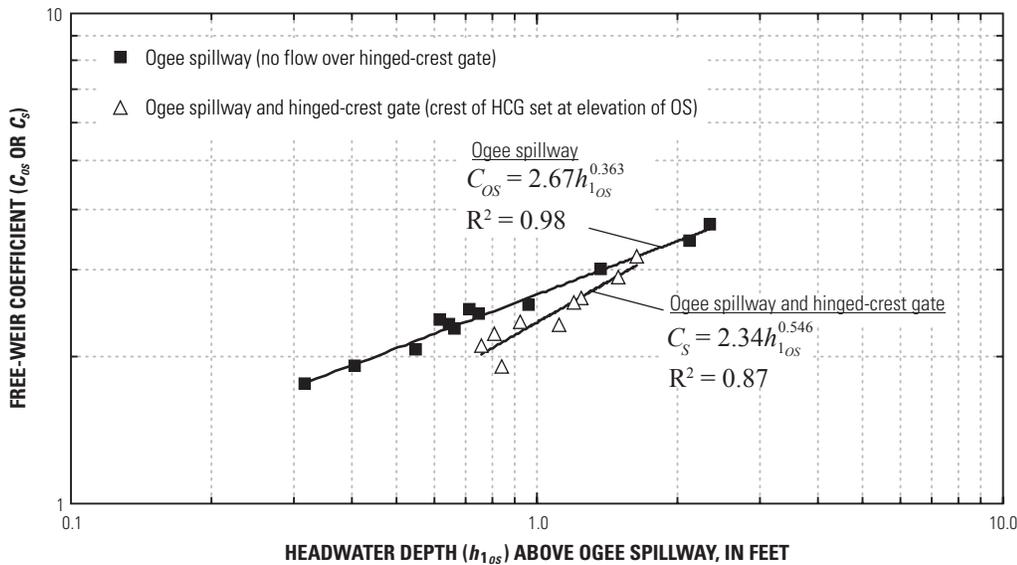
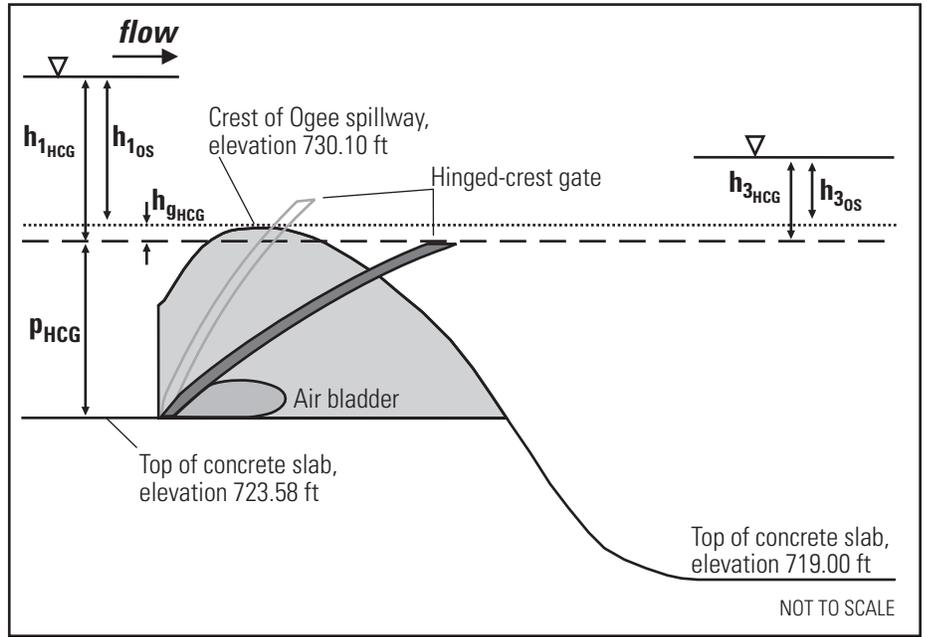
### Ogee Spillway with Hinged-Crest Gate Closed (with and without flow over gate)

A side-view schematic of the ogee spillway, hinged-crest gate, and parameters used in the control-structure rating are shown in figure 21. Twelve measurements, ranging from 77 to 3,260 ft<sup>3</sup>/s, were used to describe free-weir flow over the ogee spillway with the hinged-crest gate completely closed and no flow over the gate. Nine measurements, ranging from 406 to 1,960 ft<sup>3</sup>/s, were used to describe free-weir flow over the ogee spillway and the crest of the hinged-crest gate set at the elevation of the ogee spillway with flow over the gate. Characteristics of the flow and the measured and computed discharge coefficients are listed in table 10 and appendix C. A standard weir equation (table 11) described in Chow (1959), Collins (1977), and Roberson and others (1998) is used to describe flow over the ogee spillway. The resulting free-weir equations are presented in table 11 and figure 22 for the conditions of

flow over only the ogee spillway ( $Q_{os}$ ) and for flow over both the ogee spillway and the hinged-crest gate (denoted as  $Q_s$  for flow over the combined 292-ft “spillway”). Equations for conditions when the hinged-crest gate is open also are presented in tables 11 and 12 and are discussed in the next section. With the hinged-crest gate closed, the submergence ratios ( $h_{3os} / h_{1os}$ ) were negative for all of the flow measurements, so submergence ratios could not be evaluated.

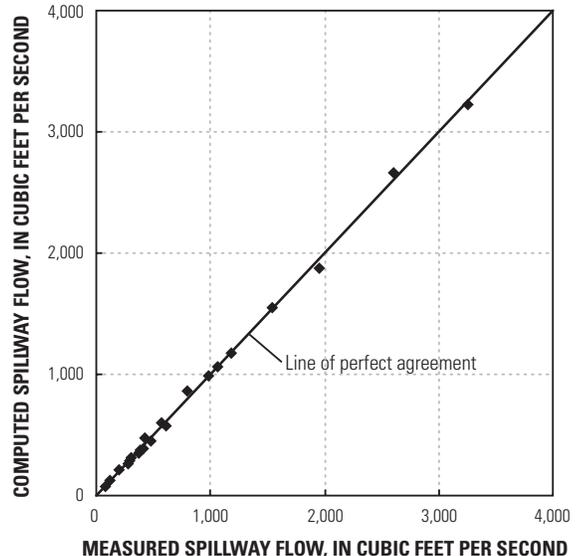
The measured and computed flows for the structure with the hinged-crest gate completely closed or with the crest set at the elevation of the ogee spillway at Algonquin are presented in table 10 and figure 23 for comparison. All 12 computed ogee spillway flows with the hinged-crest gate completely closed (no flow over the gate) are within 5 percent of measured flows. All nine computed ogee spillway flows with the crest of the hinged-crest gate set at the elevation of the ogee spillway with flow over the gate are within 11 percent of measured.

**Figure 21.** Schematic (side view) of hinged-crest gate and ogee spillway on the Fox River at Algonquin, Illinois, (ft, foot;  $h_{1HCG}$ , headwater depth above the hinged-crest gate crest;  $h_{3HCG}$ , tailwater depth above the hinged-crest gate crest;  $h_{gHCG}$ , hinged-crest gate opening referenced to the ogee spillway crest;  $p_{HCG}$ , height of hinged-crest gate crest above approach invert;  $h_{1OS}$ , headwater depth above the ogee spillway crest;  $h_{3OS}$ , tailwater depth above the ogee spillway crest).



**Figure 22.** Discharge coefficient for free-weir flow and headwater depth for ogee spillway and hinged-crest gate (closed or at elevation of ogee spillway) on the Fox River at Algonquin, Illinois ( $R^2$ , coefficient of determination).

**Figure 23.** Measured and computed flows for the structure with the hinged-crest gate completely closed or with the crest set at the elevation of the ogee spillway at Algonquin, Illinois.



**Table 10.** Ogee spillway and hinged-crest gate (closed or crest at elevation of ogee-spillway crest) measured and computed flow characteristics and coefficients at Algonquin, Illinois.

[USGS, U.S. Geological Survey; ft<sup>3</sup>/s, cubic foot per second;  $h_{1os}$ , headwater depth above the ogee spillway crest; ft, foot;  $h_{3os}$ , tailwater depth above the ogee spillway crest;  $C_{os}$ , free-weir coefficient for the ogee spillway;  $C_s$ , free-weir coefficient for the spillway which includes flow over the hinged-crest gate set at the elevation of the ogee spillway; C/M, ratio of computed and measured flow; FW-NF, free-weir flow with no flow over the hinged-crest gate; FW-FL, free-weir flow with flow over the hinged-crest gate (crest at elevation of ogee spillway); ---, not determined]

| USGS<br>measure-<br>ment<br>number | Date       | Measured<br>flow (M)<br>(ft <sup>3</sup> /s) | $h_{1os}$<br>(ft) | $h_{3os}$<br>(ft) | $h_{3os}/h_{1os}$ | Flow<br>regime | Measured<br>$C_{os}$ or $C_s$ | Computed<br>$C_{os}$ or $C_s$ | Computed<br>flow (C)<br>(ft <sup>3</sup> /s) | C/M         |
|------------------------------------|------------|--|-------------------|-------------------|-------------------|----------------|-------------------------------|-------------------------------|--|-------------|
| <sup>A</sup> 505                   | 03/26/2002 | 1,180  | 1.38              | ---               | ---               | FW-NF          | 3.01                          | 3.00                          | 1,177  | 1.00        |
| <sup>A</sup> 506                   | 04/11/2002 | 2,600  | 2.14              | ---               | ---               | FW-NF          | 3.43                          | 3.52                          | 2,666  | 1.03        |
| <sup>A</sup> 507                   | 06/11/2002 | 3,260  | 2.37              | ---               | ---               | FW-NF          | 3.69                          | 3.65                          | 3,225  | .99         |
| <sup>A</sup> 508                   | 07/23/2002 | 280  | .62               | ---               | ---               | FW-NF          | 2.37                          | 2.24                          | 265  | .95         |
| <b>509</b>                         | 09/24/2002 | 577  | .96               | -3.64             | -3.79             | FW-NF          | 2.53                          | 2.63                          | 599  | 1.04        |
| <b>510</b>                         | 11/07/2002 | 381  | .75               | -3.98             | -5.31             | FW-NF          | 2.42                          | 2.41                          | 378  | 0.99        |
| 511                                | 01/09/2003 | 406  | .76               | -3.52             | -4.63             | FW-FL          | 2.10                          | 2.01                          | 390  | 0.96        |
| <sup>B</sup> 512                   | 03/12/2003 | 267  | .55               | -4.15             | -7.55             | ---            | ---                           | ---                           | ---  | ---         |
| 513                                | 05/05/2003 | 1,060  | 1.24              | -2.66             | -2.15             | FW-FL          | 2.63                          | 2.63                          | 1,061  | 1.00        |
| 514                                | 05/07/2003 | 1,960  | 1.64              | -1.81             | -1.10             | FW-FL          | 3.20                          | 3.07                          | 1,880  | .96         |
| 515                                | 06/18/2003 | 473  | .81               | -3.74             | -4.62             | FW-FL          | 2.22                          | 2.09                          | 444  | .94         |
| <b>516</b>                         | 09/03/2003 | <b>76.5</b>                                  | <b>.32</b>        | <b>-4.57</b>      | <b>-14.28</b>     | FW-NF          | <b>1.75</b>                   | <b>1.77</b>                   | <b>77</b>                                    | <b>1.01</b> |
| <b>517</b>                         | 10/15/2003 | <b>203</b>                                   | <b>.55</b>        | <b>-3.85</b>      | <b>-7.00</b>      | FW-NF          | <b>2.06</b>                   | <b>2.15</b>                   | <b>212</b>                                   | <b>1.05</b> |
| 518                                | 12/02/2003 | 605  | .92               | -3.49             | -3.79             | FW-FL          | 2.35                          | 2.24                          | 576  | .95         |
| <sup>B</sup> 519                   | 02/02/2004 | 382  | .72               | -4.00             | -5.56             | ---            | ---                           | ---                           | ---  | ---         |
| 520                                | 03/23/2004 | 989  | 1.20              | -2.85             | -2.37             | FW-FL          | 2.58                          | 2.58                          | 992  | 1.00        |
| <sup>C</sup> 525                   | 07/08/2004 | 1,240  | 1.14              | -2.74             | -2.40             | ---            | ---                           | ---                           | ---  | ---         |
| <b>526</b>                         | 09/14/2004 | <b>301</b>                                   | <b>.67</b>        | <b>-4.23</b>      | <b>-6.31</b>      | FW-NF          | <b>2.27</b>                   | <b>2.31</b>                   | <b>306</b>                                   | <b>1.02</b> |
| 527                                | 11/08/2004 | 800  | 1.12              | -3.46             | -3.09             | FW-FL          | 2.31                          | 2.49                          | 862  | 1.08        |
| 528                                | 03/10/2005 | 1,540  | 1.49              | -2.52             | -1.69             | FW-FL          | 2.90                          | 2.91                          | 1,545  | 1.00        |
| <b>529</b>                         | 06/28/2005 | <b>121</b>                                   | <b>.41</b>        | <b>-4.45</b>      | <b>-10.85</b>     | FW-NF          | <b>1.90</b>                   | <b>1.93</b>                   | <b>123</b>                                   | <b>1.01</b> |
| <b>530</b>                         | 10/04/2005 | <b>294</b>                                   | <b>.65</b>        | <b>-4.17</b>      | <b>-6.42</b>      | FW-NF          | <b>2.32</b>                   | <b>2.28</b>                   | <b>290</b>                                   | <b>.99</b>  |
| <b>535</b>                         | 07/28/2006 | <b>368</b>                                   | <b>.72</b>        | <b>-4.07</b>      | <b>-5.65</b>      | FW-NF          | <b>2.49</b>                   | <b>2.37</b>                   | <b>350</b>                                   | <b>.95</b>  |
| 536                                | 10/02/2006 | 429  | .84               | -4.03             | -4.80             | FW-FL          | 1.91                          | 2.13                          | 478  | 1.11        |
| <sup>D</sup> 538                   | 06/28/2007 | 801  | 1.03              | -3.56             | -3.46             | ---            | ---                           | ---                           | ---  | ---         |
| <sup>E</sup> 541                   | 11/09/2007 | 703  | .91               | -3.53             | -3.88             | ---            | ---                           | ---                           | ---  | ---         |
| <sup>E</sup> 542                   | 12/17/2007 | 1,140  | 1.12              | -3.03             | -2.71             | ---            | ---                           | ---                           | ---  | ---         |

<sup>A</sup>Tailwater gage was not yet installed. Flow regime conditions are considered free weir for computations.

<sup>B</sup>Ice-affected measurement, not used in equation development.

<sup>C</sup>Outlier, measurement not used in equation development.

<sup>D</sup>Hinged-crest gate opening changed 20 minutes before measurement, not used in equation development.

<sup>E</sup>Hinged-crest gate repairs, measurement not used in equation development.

Measurements in **bold** indicate that the hinged-crest gate was closed, and no flow was overtopping it.

**Table 11.** Hydraulic conditions, parameters, and equations for different flow regimes for the ogee spillway and hinged-crest gate on the Fox River at Algonquin, Illinois.

[  $h_{1os}$ , headwater depth above the ogee spillway crest, in feet;  $h_{3os}$ , tailwater depth above the ogee spillway crest, in feet;  $Q_{OS}$ , flow through the ogee spillway, in ft<sup>3</sup>/s;  $C_{OS}$ , free-weir coefficient for the ogee spillway;  $C_{OS-A}$ , affected-weir coefficient for the ogee spillway;  $C_S$ , free-weir coefficient for the spillway which includes flow over the hinged-crest gate set at the elevation of the ogee spillway; FW-NF, free-weir flow with no flow over the hinged-crest gate; FW-FL, free-weir flow with flow over the hinged-crest gate (crest at elevation of ogee spillway)]

| Structure  | Flow regime                          | Hydraulic conditions                 | Parameters and equations   | Eq. No. |
|--|--------------------------------------|--------------------------------------|--|---------|
| Ogee spillway (hinged-crest gate closed)   | Free weir–no flow over HCG (FW-NF)   | $\frac{h_{3os}}{h_{1os}} < 0.60$     | $Q_{OS} = C_{OS} B h_{1os}^{1.5}$  | 22      |
| Ogee spillway (hinged-crest gate open)   | Free weir (FW)                       | $\frac{h_{3os}}{h_{1os}} < -5.0$     | $C_{OS} = 2.67 h_{1os}^{0.363}$<br><br>$B = 242 \text{ ft}$  | 23      |
|  |                                      |                                      | $Q_{OS} = 646.1 h_{1os}^{1.863}$   | 24      |
| Ogee spillway and hinged-crest gate (crest of the hinged-crest gate set at elevation of ogee spillway) | Free weir with-flow over HCG (FW-FL) | $\frac{h_{3os}}{h_{1os}} < 0.60$     | $Q_S = C_S B h_{1os}^{1.5}$  | 25      |
|  |                                      |                                      | $C_S = 2.34 h_{1os}^{0.546}$   | 26      |
|  |                                      |                                      | $B = 292 \text{ ft}$   |         |
|  |                                      |                                      | $Q_S = 683.3 h_{1os}^{2.046}$  | 27      |
| Ogee spillway (hinged-crest gate open)   | Affected                             | $-5.0 < \frac{h_{3os}}{h_{1os}} < 1$ | $Q_{OS} = C_{OS} C_{OS-A} B h_{1os}^{1.5}$   | 28      |
|  |                                      |                                      | $C_{OS-A} = 0.442 p_{HCG}^{0.149} \left( \frac{h_{1os} - h_{3os}}{h_{1os}} \right)^{0.930} \left( \frac{h_{1HCG} - h_{3HCG}}{h_{1HCG}} \right)^{-0.905}$ | 29      |
|  |                                      |                                      | $Q_{OS} = 285.5 h_{1os}^{0.933} p_{HCG}^{0.149} (h_{1os} - h_{3os})^{0.930} \left( \frac{h_{1HCG} - h_{3HCG}}{h_{1HCG}} \right)^{-0.905}$                | 30      |

**Table 12.** Hydraulic conditions, parameters, and equations for different flow regimes for the hinged-crest gate on the Fox River at Algonquin, Illinois.

[  $h_{3HCG}$ , tailwater depth above the hinged-crest gate crest, in feet;  $h_{1HCG}$ , headwater depth above the hinged-crest gate crest, in feet;  $Q_{HCG}$ , flow through the hinged-crest gate;  $C_{HCG}$ , free-weir coefficient for the hinged-crest gate;  $B$ , length of gate, in feet;  $p_{HCG}$ , height of hinged-crest gate crest above approach invert, in feet;  $C_{HCG-S}$ , submerged-weir coefficient for the hinged-crest gate]

| Structure         | Flow regime | Hydraulic conditions                  | Parameters and equations  | Eq. No. |
|-------------------|-------------|---------------------------------------|---|---------|
| Hinged-crest gate | Free        | $\frac{h_{3HCG}}{h_{1HCG}} \leq 0.77$ | $Q_{HCG} = C_{HCG} B h_{1HCG}^{1.5}$                                  | 4       |
|                   |             |                                       | $C_{HCG} = 3.33 \left( \frac{h_{1HCG}}{p_{HCG}} \right)^{-0.152}$     | 31      |
|                   |             |                                       | $B = 50 \text{ ft}$   |         |
|                   |             |                                       | $Q_{HCG} = 166.5 h_{1HCG}^{1.348} p_{HCG}^{0.152}$                    | 32      |
| Hinged-crest gate | Submerged   | $\frac{h_{3HCG}}{h_{1HCG}} > 0.77$    | $Q_{HCG} = C_{HCG} C_{HCG-S} B h_{1HCG}^{1.5}$                        | 7       |
|                   |             |                                       | $C_{HCG-S} = 0.882 \left( \frac{h_{3HCG}}{h_{1HCG}} \right)^{-0.472}$ | 33      |
|                   |             |                                       | $Q_{HCG} = 146.9 h_{1HCG}^{1.820} h_{3HCG}^{-0.472} p_{HCG}^{0.152}$  | 34      |

### Ogee Spillway and Hinged-Crest Gate Open

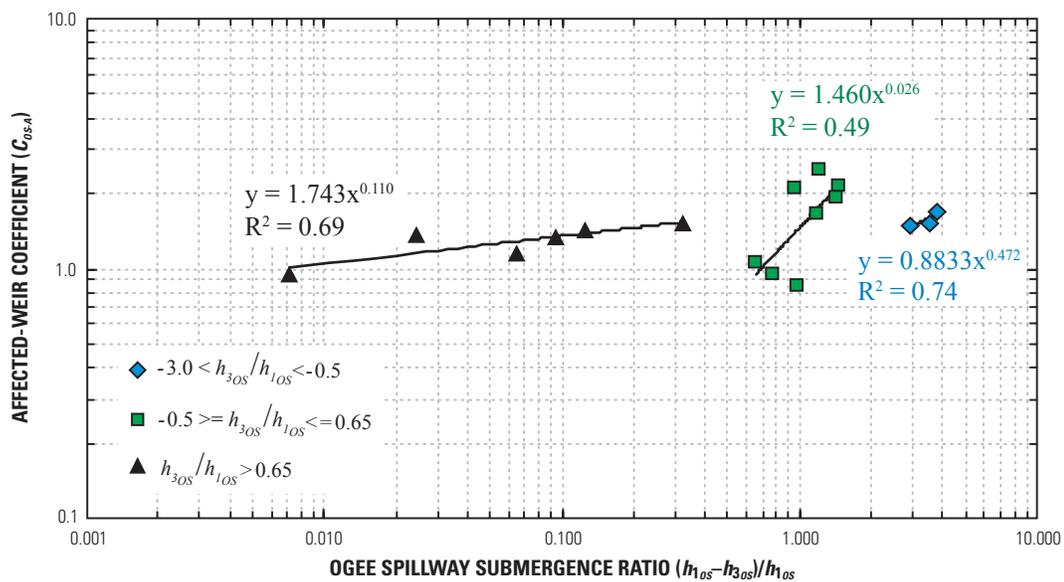
A side-view schematic of the ogee spillway, hinged-crest gate, and parameters used in the control-structure rating are shown in figure 21. Twenty-one measurements, ranging from 868 to 6,600 ft<sup>3</sup>/s, were used to describe free, affected, and submerged flow over the ogee spillway and hinged-crest gate. Characteristics of the flow and the measured and computed discharge coefficients are listed in table 13 and 14, and appendix D. A standard-weir equation (table 11 and 12) described in Chow (1959), Collins (1977), and Roberson and others (1998) is used to describe flow over the ogee spillway and hinged-crest gate.

The ogee spillway free-weir coefficients in table 13 were computed with equation 23 in table 11. Determination of a submerged-weir coefficient was attempted, but 14 out of 17 coefficient values were greater than one, indicating more flow than expected going over the ogee spillway for the majority of the measurements. The resulting coefficients are labeled C<sub>OS-A</sub> for “affected”-weir coefficient (table 13 and fig. 24). When the data are subdivided into three submergence ratio ranges, equations for C<sub>OS-A</sub> are developed with R<sup>2</sup> values of 0.69, 0.49, and 0.74. With the majority of the coefficient values above one, the relation of the three submergence ranges show that there is more affecting the flow than submergence when the hinged-crest gate is open (for example: hinged-crest gate height, upstream and downstream flow paths, proximity and height of streambank downstream of HCG, and (or) narrow channel downstream of the structure (fig. 16)). Multiple-linear regression analysis using gate height and hinged-crest gate and ogee spillway submergence ratios yields an affected-weir coefficient equation for the ogee spillway with an R<sup>2</sup> of 0.97 (equation 29,

table 11). From the range of measurements used, the resulting affected ogee spillway flow equation with the HCG open (table 11) is applicable for  $h_{3OS} / h_{1OS}$  less than 1.0 and greater than -5.0. Split-flow values (OS and HCG separate) for the measurements in November 2002 could not be determined. Using the available OS equations presented in table 11 and the HCG equations described below and presented in table 12, it appears that the ogee spillway flow with the HCG open and with  $h_{3OS} / h_{1OS}$  less than -5.0 are best described by equation 24 (table 11). Note that there are only two measurements in this range with computed ogee spillway flow values of 21 and 158 ft<sup>3</sup>/s.

Hinged-crest gate free- and submerged-weir coefficient equations are presented in table 12, figures 25 and 26. The free-weir coefficient equation at Algonquin is similar to the one at McHenry for the hinged-crest gate. Also similarly, the data at Algonquin indicate submerged flow occurs when  $h_{3HCG} / h_{1HCG}$  is greater than 0.77. The submerged-weir coefficient equation deviates from the McHenry equation, and this difference could be attributed to the complexities mentioned in the above paragraph.

The measured and computed ogee spillway and hinged-crest gate flows for Algonquin are presented in table 15 and figure 27 for comparison. Twelve of the 17 computed ogee spillway flows are within 5 percent of measured and the remaining 5 are within 11 percent. Eight of the 17 computed hinged-crest gate flows are within 5 percent of measured, 6 are within 10 percent, 2 are within 15 percent, and the remaining measurement is within 24 percent. The combined OS and HCG flows show similar results, and all 11 combined measured flows above 3,300 ft<sup>3</sup>/s were computed within 7 percent.



**Figure 24.** Discharge coefficient for affected-weir flow and ogee spillway submergence ratio on the Fox River at Algonquin, Illinois, (R<sup>2</sup>, coefficient of determination).

**Table 13.** Ogee spillway weir-flow characteristics and coefficients at Algonquin, Illinois.

[USGS, U.S. Geological Survey; OS, ogee spillway; HCG, hinged-crest gate;  $ft^3/s$ , cubic foot per second;  $h_{1OS}$ , headwater depth above the ogee spillway crest; ft, foot;  $h_{3OS}$ , tailwater depth above the ogee spillway crest;  $C_{OS}$ , free-weir coefficient for the ogee spillway;  $C_{OS-A}$ , affected-weir coefficient for the ogee spillway; C/M, ratio of computed and measured flow; F/W, free-weir flow; NF, no flow; AFF, affected flow; IDNR, Illinois Department of Natural Resources—Office of Water Resources; ---, not determined]

| USGS measure-number | Date       | Measured OS and (or) HCG flow ( $ft^3/s$ ) | Measured flow (M) ( $ft^3/s$ ) | Ogee Spillway  |                |                   |             |                             |                   |                   |                                  |                     |                                |      |     |
|---------------------|------------|--|--------------------------------|----------------|----------------|-------------------|-------------|-----------------------------|-------------------|-------------------|----------------------------------|---------------------|--------------------------------|------|-----|
|                     |            |  |                                | $h_{1OS}$ (ft) | $h_{3OS}$ (ft) | $h_{3OS}/h_{1OS}$ | Flow regime | $(h_{1OS}-h_{3OS})/h_{1OS}$ | Measured $C_{OS}$ | Computed $C_{OS}$ | Measured <sup>1</sup> $C_{OS-A}$ | Computed $C_{OS-A}$ | Computed flow (C) ( $ft^3/s$ ) | C/M  |     |
| ---                 | 11/19/2002 | 868  | ---                            | 0.47           | -2.85          | -6.06             | FW          | 7.06                        | ---               | 2.03              | ---                              | ---                 | ---                            | 158  | --- |
| ---                 | 11/19/2002 | 1,410                                      | ---                            | .16            | -1.85          | -11.56            | FW          | 12.56                       | ---               | 1.37              | ---                              | ---                 | ---                            | 21   | --- |
| ---                 | 11/20/2002 | 1,800                                      | ---                            | -0.2           | -1.43          | ---               | NF          | ---                         | ---               | ---               | ---                              | ---                 | 0                              | ---  | --- |
| 523                 | 05/18/2004 | 3,570                                      | 2,470                          | 2.24           | .04            | .02               | AFF         | .98                         | 3.04              | 3.57              | 0.85                             | 0.80                | 2,306                          | 0.93 |     |
| 522                 | 05/18/2004 | 3,730                                      | 2,330                          | 2.04           | .44            | .22               | AFF         | .78                         | 3.30              | 3.45              | .96                              | .97                 | 2,369                          | 1.02 |     |
| 521                 | 05/18/2004 | 3,890                                      | 2,340                          | 1.94           | .67            | .35               | AFF         | .65                         | 3.58              | 3.39              | 1.06                             | 1.12                | 2,481                          | 1.06 |     |
| 524                 | 05/24/2004 | 5,580                                      | 3,340                          | 2.04           | 1.99           | .98               | AFF         | .02                         | 4.74              | 3.45              | 1.37                             | 1.26                | 3,078                          | .92  |     |
| 531                 | 02/02/2006 | 1,580                                      | 830                            | .86            | -2.39          | -2.78             | AFF         | 3.78                        | 4.30              | 2.53              | 1.70                             | 1.70                | 827                            | 1.00 |     |
| 533                 | 03/17/2006 | 3,160                                      | 1,550                          | 1.07           | -.49           | -.46              | AFF         | 1.46                        | 5.79              | 2.73              | 2.12                             | 2.09                | 1,532                          | .99  |     |
| 532                 | 03/17/2006 | 3,320                                      | 1,410                          | .93            | -.20           | -.22              | AFF         | 1.22                        | 6.50              | 2.60              | 2.50                             | 2.53                | 1,425                          | 1.01 |     |
| 534                 | 05/31/2006 | 2,000                                      | 1,060                          | 1.04           | -2.59          | -2.49             | AFF         | 3.49                        | 4.13              | 2.71              | 1.53                             | 1.51                | 1,046                          | .99  |     |
| 537                 | 03/14/2007 | 3,220                                      | 1,660                          | 1.26           | -.25           | -.20              | AFF         | 1.20                        | 4.85              | 2.90              | 1.67                             | 1.86                | 1,843                          | 1.11 |     |
| 539                 | 08/22/2007 | 5,000                                      | 2,910                          | 1.85           | 1.62           | .88               | AFF         | .12                         | 4.78              | 3.33              | 1.43                             | 1.41                | 2,856                          | .98  |     |
| 540                 | 08/27/2007 | 6,600                                      | 4,220                          | 2.83           | 2.81           | .99               | AFF         | .01                         | 3.66              | 3.89              | .94                              | .99                 | 4,443                          | 1.05 |     |
| 543                 | 01/11/2008 | 3,010                                      | 1,570                          | 1.14           | -.49           | -.43              | AFF         | 1.43                        | 5.33              | 2.80              | 1.91                             | 1.87                | 1,542                          | .98  |     |
| 544                 | 02/22/2008 | 1,980                                      | 920                            | .98            | -1.87          | -1.91             | AFF         | 2.91                        | 3.92              | 2.65              | 1.48                             | 1.55                | 966                            | 1.05 |     |
| 545                 | 03/26/2008 | 3,850                                      | 2,050                          | 1.25           | .06            | .05               | AFF         | .95                         | 6.06              | 2.89              | 2.10                             | 1.86                | 1,815                          | .89  |     |
| 546                 | 04/16/2008 | 5,510                                      | 3,140                          | 2.00           | 1.81           | .90               | AFF         | .10                         | 4.59              | 3.43              | 1.34                             | 1.32                | 3,110                          | .99  |     |
| 547                 | 06/11/2008 | 4,560                                      | 2,540                          | 1.66           | 1.12           | .67               | AFF         | .33                         | 4.91              | 3.21              | 1.53                             | 1.55                | 2,580                          | 1.02 |     |
| 548                 | 06/20/2008 | 6,030                                      | 3,550                          | 2.33           | 2.18           | .94               | AFF         | .06                         | 4.12              | 3.62              | 1.14                             | 1.19                | 3,698                          | 1.04 |     |
| IDNR                | 09/16/2008 | 2,936                                      | ---                            | 1.60           | -.54           | -.34              | AFF         | 1.34                        | ---               | 3.16              | ---                              | 1.16                | 1,798                          | ---  |     |

<sup>1</sup>Ratio of measured and computed  $C_{OS}$ .

Black plain text indicates free-weir or no flow conditions.

Green bold text indicates "Affected" conditions with  $h_{3OS}/h_{1OS}$  ranging from -0.5 to 0.65.

Black bold italic text indicates "Affected" conditions with  $h_{3OS}/h_{1OS}$  greater than 0.65.

Blue italic text indicates "Affected" conditions with  $h_{3OS}/h_{1OS}$  less than -0.5 and greater than -5.0.

**Table 14. Hinged-crest gate weir-flow characteristics and coefficients at Algonquin, Illinois.**

[USGS, U.S. Geological Survey; Meas., Measured; ft<sup>3</sup>/s, cubic foot per second;  $h_{eg}$ , hinged-crest gate opening referenced to the broad-crested-weir crest; ft, foot;  $h_{hcg}$ , headwater depth above the hinged-crest gate crest;  $h_{hcg}^2$ , tailwater depth above the hinged-crest gate crest;  $p_{hcg}$ , height of hinged-crest gate crest above approach invert;  $C_{hcg}$ , free-weir coefficient for the hinged-crest gate; Comp., computed;  $C_{hcg-S}$ , submerged-weir coefficient for the hinged-crest gate; C/M, ratio of computed and measured flow; FW, free-weir flow; SW, submerged-weir flow; IDNR, Illinois Department of Natural Resources—Office of Water Resources; OS, ogee spillway; HCG, hinged-crest gate; ---, not determined]

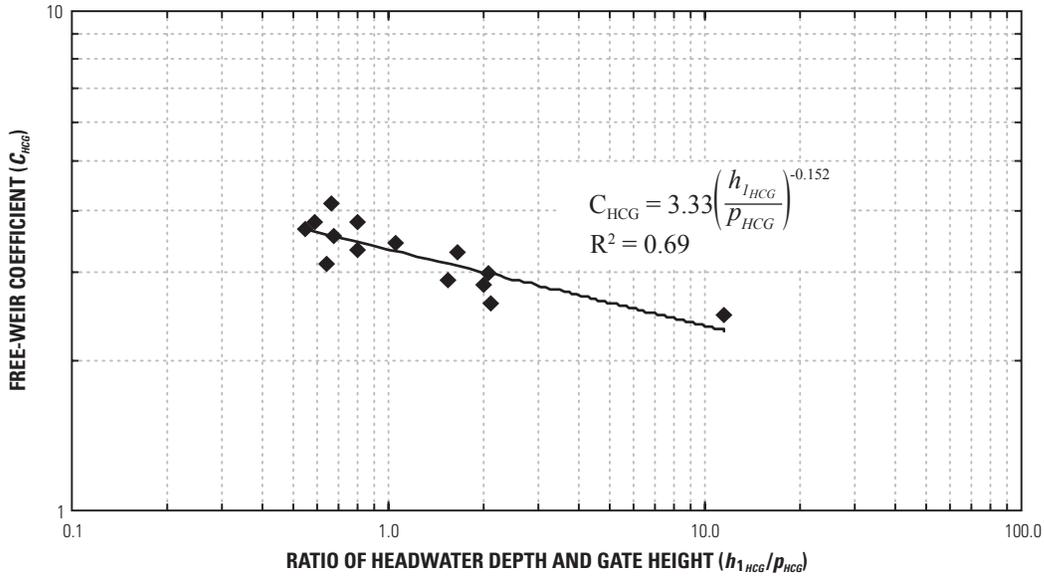
| USGS measure-number | Date       | Meas. flow <sup>1</sup> (M) (ft <sup>3</sup> /s) | Gate opening   |                           | $h_{hcg}$ (ft) | $h_{3hcg}$ (ft) | $h_{hcg} - h_{3hcg}$ (ft) | Flow regime | $(h_{hcg} - h_{3hcg}) / h_{hcg}$ | $p_{hcg}$ (ft) | $(h_{hcg} - p_{hcg}) / h_{hcg}$ | Meas. $C_{hcg}$ | Comp. $C_{hcg}$ | Meas. <sup>2</sup> $C_{hcg-S}$ | Comp. $C_{hcg-S}$ | Comp. flow (C) (ft <sup>3</sup> /s) | C/M         |
|---------------------|------------|--|----------------|---------------------------|----------------|-----------------|---------------------------|-------------|----------------------------------|----------------|---------------------------------|-----------------|-----------------|--------------------------------|-------------------|-------------------------------------|-------------|
|                     |            |  | $h_{hcg}$ (ft) | $h_{hcg} - h_{3hcg}$ (ft) |                |                 |                           |             |                                  |                |                                 |                 |                 |                                |                   |                                     |             |
| ---                 | 11/19/2002 | 710  | 2.0            | 2.47                      | -0.85          | -0.344          | FW                        | 1.34        | 4.52                             | 0.55           | 3.66                            | 3.65            | ---             | ---                            | ---               | 709                                 | ---         |
| ---                 | 11/19/2002 | 1,389  | 4.0            | 4.16                      | 2.15           | .517            | FW                        | .48         | 2.52                             | 1.65           | 3.27                            | 3.09            | ---             | ---                            | ---               | 1,309                               | ---         |
| ---                 | 11/20/2002 | 1,800  | 6.0            | 5.98                      | 4.57           | .764            | FW                        | .24         | .52                              | 11.50          | 2.46                            | 2.30            | ---             | ---                            | ---               | 1,680                               | ---         |
| 523                 | 05/18/2004 | 1,100  | 1.0            | 3.24                      | 1.04           | .321            | FW                        | .68         | 5.52                             | .59            | 3.77                            | 3.61            | ---             | ---                            | ---               | 1,053                               | 0.96        |
| 522                 | 05/18/2004 | 1,400  | 1.8            | 3.80                      | 2.20           | .579            | FW                        | .42         | 4.76                             | .80            | 3.78                            | 3.45            | ---             | ---                            | ---               | 1,276                               | .91         |
| 521                 | 05/18/2004 | 1,550  | 2.4            | 4.34                      | 3.07           | .707            | FW                        | .29         | 4.12                             | 1.05           | 3.43                            | 3.30            | ---             | ---                            | ---               | 1,494                               | .96         |
| 524                 | 05/24/2004 | <b>2,240</b>                                     | <b>6.0</b>     | <b>8.04</b>               | <b>7.99</b>    | <b>.994</b>     | <b>SW</b>                 | <b>.01</b>  | <b>.52</b>                       | <b>15.46</b>   | <b>1.97</b>                     | <b>2.20</b>     | <b>0.89</b>     | <b>0.88</b>                    | <b>0.88</b>       | <b>2,215</b>                        | <b>.99</b>  |
| 531                 | 02/02/2006 | 750  | 2.0            | 2.86                      | -.39           | -.136           | FW                        | 1.14        | 4.52                             | .63            | 3.10                            | 3.57            | ---             | ---                            | ---               | 863                                 | 1.15        |
| 533                 | 03/17/2006 | 1,610  | 4.0            | 5.07                      | 3.51           | .692            | FW                        | .31         | 2.52                             | 2.01           | 2.82                            | 2.99            | ---             | ---                            | ---               | 1,709                               | 1.06        |
| 532                 | 03/17/2006 | <b>1,910</b>                                     | <b>5.0</b>     | <b>5.93</b>               | <b>4.80</b>    | <b>.809</b>     | <b>SW</b>                 | <b>.19</b>  | <b>1.52</b>                      | <b>3.90</b>    | <b>2.65</b>                     | <b>2.71</b>     | <b>.98</b>      | <b>.97</b>                     | <b>.97</b>        | <b>1,905</b>                        | <b>1.00</b> |
| 534                 | 05/31/2006 | 940  | 2.0            | 3.04                      | -.59           | -.194           | FW                        | 1.19        | 4.52                             | .67            | 3.55                            | 3.54            | ---             | ---                            | ---               | 937                                 | 1.00        |
| 537                 | 03/14/2007 | 1,560  | 4.0            | 5.26                      | 3.75           | .713            | FW                        | .29         | 2.52                             | 2.09           | 2.59                            | 2.98            | ---             | ---                            | ---               | 1,796                               | 1.15        |
| 539                 | 08/22/2007 | <b>2,090</b>                                     | <b>6.0</b>     | <b>7.85</b>               | <b>7.62</b>    | <b>.971</b>     | <b>SW</b>                 | <b>.03</b>  | <b>.52</b>                       | <b>15.10</b>   | <b>1.90</b>                     | <b>2.20</b>     | <b>.86</b>      | <b>.89</b>                     | <b>.89</b>        | <b>2,168</b>                        | <b>1.04</b> |
| 540                 | 08/27/2007 | <b>2,380</b>                                     | <b>6.0</b>     | <b>8.83</b>               | <b>8.81</b>    | <b>.998</b>     | <b>SW</b>                 | <b>.002</b> | <b>.52</b>                       | <b>16.98</b>   | <b>1.81</b>                     | <b>2.17</b>     | <b>.84</b>      | <b>.88</b>                     | <b>.88</b>        | <b>2,508</b>                        | <b>1.05</b> |
| 543                 | 01/11/2008 | 1,440  | 3.5            | 4.64                      | 3.01           | .649            | FW                        | .35         | 3.02                             | 1.54           | 2.88                            | 3.12            | ---             | ---                            | ---               | 1,559                               | 1.08        |
| 544                 | 02/22/2008 | 1,060  | 2.0            | 2.98                      | .13            | .044            | FW                        | .96         | 4.52                             | .66            | 4.12                            | 3.55            | ---             | ---                            | ---               | 913                                 | .86         |
| 545                 | 03/26/2008 | <b>1,800</b>                                     | <b>4.0</b>     | <b>5.25</b>               | <b>4.06</b>    | <b>.773</b>     | <b>SW</b>                 | <b>.23</b>  | <b>2.52</b>                      | <b>2.08</b>    | <b>2.99</b>                     | <b>2.98</b>     | <b>1.00</b>     | <b>1.00</b>                    | <b>1.00</b>       | <b>1,784</b>                        | <b>.99</b>  |
| 546                 | 04/16/2008 | <b>2,370</b>                                     | <b>6.0</b>     | <b>8.00</b>               | <b>7.81</b>    | <b>.976</b>     | <b>SW</b>                 | <b>.02</b>  | <b>.52</b>                       | <b>15.38</b>   | <b>2.09</b>                     | <b>2.20</b>     | <b>.95</b>      | <b>.89</b>                     | <b>.89</b>        | <b>2,218</b>                        | <b>.94</b>  |
| 547                 | 06/11/2008 | <b>2,020</b>                                     | <b>6.0</b>     | <b>7.66</b>               | <b>7.12</b>    | <b>.930</b>     | <b>SW</b>                 | <b>.07</b>  | <b>.52</b>                       | <b>14.73</b>   | <b>1.91</b>                     | <b>2.21</b>     | <b>.86</b>      | <b>.91</b>                     | <b>.91</b>        | <b>2,141</b>                        | <b>1.06</b> |
| 548                 | 06/20/2008 | <b>2,480</b>                                     | <b>6.0</b>     | <b>8.33</b>               | <b>8.18</b>    | <b>.982</b>     | <b>SW</b>                 | <b>.02</b>  | <b>.52</b>                       | <b>16.02</b>   | <b>2.06</b>                     | <b>2.18</b>     | <b>.94</b>      | <b>.89</b>                     | <b>.89</b>        | <b>2,336</b>                        | <b>.94</b>  |
| IDNR                | 09/16/2008 | 1,138  | 2.0            | 3.60                      | 1.46           | .406            | FW                        | .59         | 4.52                             | .80            | 3.33                            | 3.45            | ---             | ---                            | ---               | 1,177                               | ---         |

<sup>1</sup>November 2002 and September 16, 2008, "measured" values determined by subtracting the computed OS flow from the measured total OS and HCG flow.

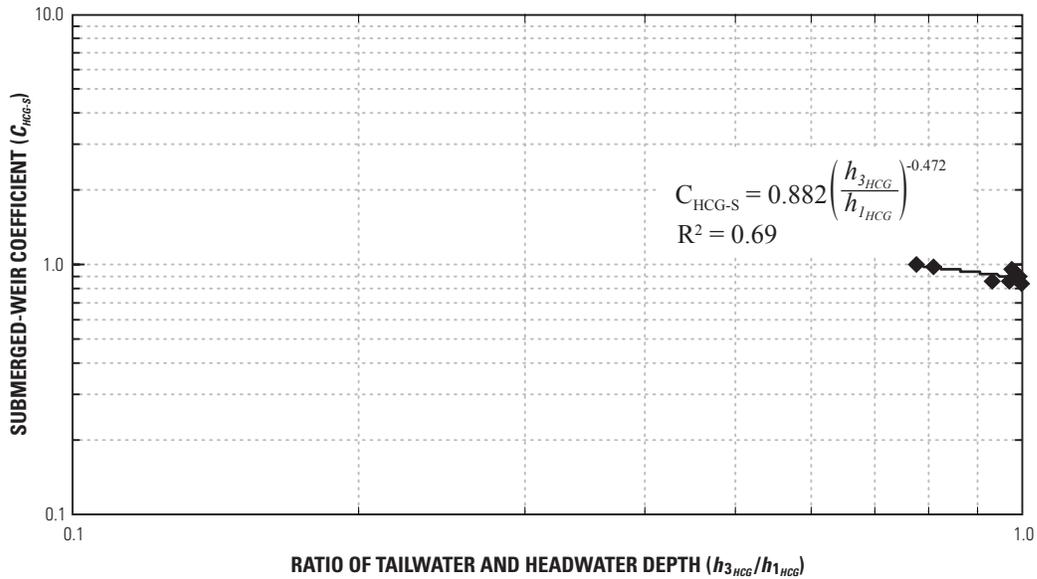
<sup>2</sup>Ratio of measured and computed  $C_{hcg}$

Black plain text indicates free-weir conditions.

**Red bold** text indicates submerged conditions.



**Figure 25.** Discharge coefficient for free-weir flow, and the ratio of headwater depth and gate height for the hinged-crest gate on the Fox River at Algonquin, Illinois, ( $R^2$ , coefficient of determination).



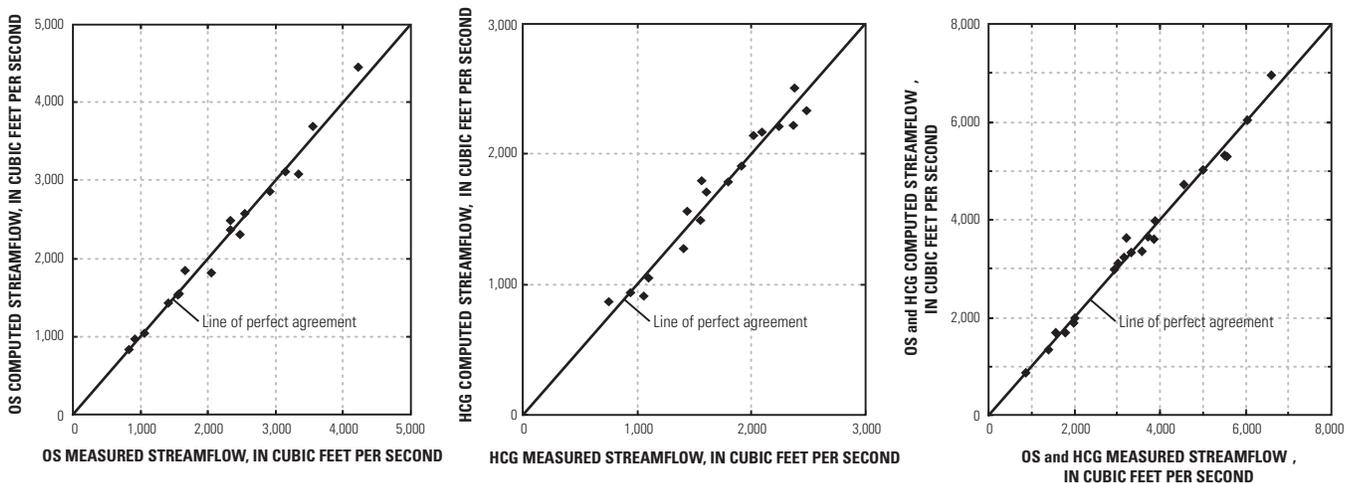
**Figure 26.** Discharge coefficient for submerged-weir flow, and the ratio of headwater and tailwater depth for the hinged-crest gate on the Fox River at Algonquin, Illinois, ( $R^2$ , coefficient of determination).

**Table 15.** Measured and computed flows for the ogee spillway and hinged-crest gate on the Fox River at Algonquin, Illinois.

[USGS, U.S. Geological Survey; OS, ogee spillway; ft<sup>3</sup>/s, cubic foot per second; C/M, ratio of computed and measured flow; HCG, hinged-crest gate; IDNR, Illinois Department of Natural Resources–Office of Water Resources; ---, not determined]

| USGS measurement number | Date       | OS                                     |  |      | HCG   |  |      | Total OS and HCG flow                  |  |      |
|-------------------------|------------|--|--|------|---|--|------|--|--|------|
|                         |            | Measured flow (M) (ft <sup>3</sup> /s) | Computed flow (C) (ft <sup>3</sup> /s) | C/M  | Measured flow <sup>1</sup> (M) (ft <sup>3</sup> /s) | Computed flow (C) (ft <sup>3</sup> /s) | C/M  | Measured flow (M) (ft <sup>3</sup> /s) | Computed flow (C) (ft <sup>3</sup> /s) | C/M  |
| ---                     | 11/19/2002 | ---                                    | 158                                    | ---  | 710   | 709                                    | ---  | 868                                    | 867                                    | 1.00 |
| ---                     | 11/19/2002 | ---                                    | 21                                     | ---  | 1,389   | 1,309                                  | ---  | 1,410                                  | 1,330                                  | .94  |
| ---                     | 11/20/2002 | ---                                    | 0                                      | ---  | 1,800   | 1,680                                  | ---  | 1,800                                  | 1,680                                  | .93  |
| 523                     | 05/18/2004 | 2,470                                  | 2,306                                  | 0.93 | 1,100   | 1,053                                  | 0.96 | 3,570                                  | 3,359                                  | .94  |
| 522                     | 05/18/2004 | 2,330                                  | 2,369                                  | 1.02 | 1,400   | 1,276                                  | .91  | 3,730                                  | 3,646                                  | .98  |
| 521                     | 05/18/2004 | 2,340                                  | 2,481                                  | 1.06 | 1,550   | 1,494                                  | .96  | 3,890                                  | 3,974                                  | 1.02 |
| 524                     | 05/24/2004 | 3,340                                  | 3,078                                  | .92  | 2,240   | 2,215                                  | .99  | 5,580                                  | 5,292                                  | .95  |
| 531                     | 02/02/2006 | 830                                    | 827                                    | 1.00 | 750   | 863                                    | 1.15 | 1,580                                  | 1,690                                  | 1.07 |
| 533                     | 03/17/2006 | 1,550                                  | 1,532                                  | .99  | 1,610   | 1,709                                  | 1.06 | 3,160                                  | 3,241                                  | 1.03 |
| 532                     | 03/17/2006 | 1,410                                  | 1,425                                  | 1.01 | 1,910   | 1,905                                  | 1.00 | 3,320                                  | 3,330                                  | 1.00 |
| 534                     | 05/31/2006 | 1,060                                  | 1,046                                  | .99  | 940   | 937                                    | 1.00 | 2,000                                  | 1,984                                  | .99  |
| 537                     | 03/14/2007 | 1,660                                  | 1,843                                  | 1.11 | 1,560   | 1,796                                  | 1.15 | 3,220                                  | 3,639                                  | 1.13 |
| 539                     | 08/22/2007 | 2,910                                  | 2,856                                  | .98  | 2,090   | 2,168                                  | 1.04 | 5,000                                  | 5,025                                  | 1.00 |
| 540                     | 08/27/2007 | 4,220                                  | 4,443                                  | 1.05 | 2,380   | 2,508                                  | 1.05 | 6,600                                  | 6,951                                  | 1.05 |
| 543                     | 01/11/2008 | 1,570                                  | 1,542                                  | .98  | 1,440   | 1,559                                  | 1.08 | 3,010                                  | 3,101                                  | 1.03 |
| 544                     | 02/22/2008 | 920                                    | 966                                    | 1.05 | 1,060   | 913                                    | .86  | 1,980                                  | 1,879                                  | .95  |
| 545                     | 03/26/2008 | 2,050                                  | 1,815                                  | .89  | 1,800   | 1,784                                  | .99  | 3,850                                  | 3,599                                  | .93  |
| 546                     | 04/16/2008 | 3,140                                  | 3,110                                  | .99  | 2,370   | 2,218                                  | .94  | 5,510                                  | 5,328                                  | .97  |
| 547                     | 06/11/2008 | 2,540                                  | 2,580                                  | 1.02 | 2,020   | 2,141                                  | 1.06 | 4,560                                  | 4,721                                  | 1.04 |
| 548                     | 06/20/2008 | 3,550                                  | 3,698                                  | 1.04 | 2,480   | 2,336                                  | .94  | 6,030                                  | 6,034                                  | 1.00 |
| IDNR                    | 09/16/2008 | ---                                    | 1,798                                  | ---  | 1,138   | 1,177                                  | ---  | 2,936                                  | 2,975                                  | 1.01 |

<sup>1</sup>November 2002 and September 16, 2008, “measured” values determined by subtracting the computed OS flow from the measured total OS and HCG flow.



**Figure 27.** Measured and computed flows for the ogee spillway and hinged-crest gate on the Fox River at Algonquin, Illinois, (OS, ogee spillway; HCG, hinged-crest gate).

### Example Calculations

The following are examples of how flow was calculated using equations in table 11 and table 12.

**Example 1:** The following conditions exist:

Headwater pool stage is 1.37 ft, tailwater pool stage is 6.64 ft, and the flow over the hinged-crest gate is zero because the crest is closed to an elevation above the ogee spillway and (or) the bulkheads are closed. See figure 21 for a schematic.

Flow is determined by first converting the stages to depths above the crest of the ogee spillway. This is done by subtracting the difference between the crest of the spillway (730.10 ft) and headwater gage datum (729.48 ft) from the headwater stage and then subtracting the difference between the spillway crest and tailwater gage datum (719.48 ft) from the tailwater stage.

$$h_{1_{OS}} = 1.37 - (730.10 - 729.48) = 0.75 \text{ ft}$$

$$h_{3_{OS}} = 6.64 - (730.10 - 719.48) = -3.98 \text{ ft}$$

Because  $h_{3_{OS}} / h_{1_{OS}}$  ( $-3.98/0.75 = -5.31$ ) is less than 0.60 and the hinged-crest gate is closed, free-weir flow exists for the spillway and there is zero flow over the gate.

Using equation 24 from table 11,

$$\begin{aligned} Q_{OS} &= 646.1h_{1_{OS}}^{1.863} \\ &= 646.1(0.75)^{1.863} \\ &= 378.0 \text{ ft}^3 / \text{s} . \end{aligned}$$

Therefore the total flow is

$$Q_{TOTAL} = Q_{OS} = 378.0 \text{ ft}^3 / \text{s}$$

**Example 2:** The following conditions exist:

Headwater pool stage is 1.86 ft, tailwater pool stage is 7.96 ft, there is flow over the hinged-crest gate because the crest is at the same elevation as the crest of the ogee spillway.

Flow is determined by first converting the pool stages to depths above the crest of the spillway, as in example 1.

$$h_{1_{OS}} = 1.86 - 0.62 = 1.24 \text{ ft}$$

$$h_{3_{OS}} = 7.96 - 10.62 = -2.66 \text{ ft}$$

Because  $h_{3_{OS}} / h_{1_{OS}}$  ( $-2.66/1.24 = -2.15$ ) is less than 0.60 and the crest of the hinged-crest gate is the same elevation as the crest of the spillway, free-weir flow exists for the spillway and there is flow over the gate.

Using equation 27 from table 11,

$$\begin{aligned} Q_S &= 683.3h_{1_{OS}}^{2.046} \\ &= 683.3(1.24)^{2.046} \\ &= 1061 \text{ ft}^3 / \text{s} . \end{aligned}$$

Therefore the total flow is

$$Q_{TOTAL} = Q_S = 1061 \text{ ft}^3 / \text{s}$$

**Example 3:** The following conditions exist:

Headwater pool stage is 0.78 ft, tailwater pool stage is 8.77 ft, and the hinged-crest gate opening is 4.0 ft.

Flow over the spillway is determined by first converting the stages to depths above the crest of the spillway.

$$h_{1_{OS}} = 0.78 - 0.62 = 0.16 \text{ ft}$$

$$h_{3_{OS}} = 8.77 - 10.62 = -1.85 \text{ ft}$$

Because  $h_{3_{OS}} / h_{1_{OS}}$  ( $-1.85/0.16 = -11.56$ ) is less than -5.0 and the hinged-crest gate is open, free-weir flow exists.

Using equation 24 from table 11,

$$\begin{aligned} Q_{OS} &= 646.1h_{1_{OS}}^{1.863} \\ &= 646.1(0.16)^{1.863} \\ &= 21.26 \text{ ft}^3 / \text{s} . \end{aligned}$$

Flow over the gate is determined by first converting the stages to depths above the crest of the gate. This is done by subtracting the difference between headwater gage datum (729.48 ft) and the elevation of the gate crest (730.10 ft -  $h_{g_{HCG}}$ ) from the headwater stage and then subtracting the difference between the tailwater gage datum (719.48 ft) and the elevation of gate crest from the tailwater stage.

$$h_{1_{HCG}} = 0.78 - [(730.10 - 4.00) - 729.48] = 4.16 \text{ ft}$$

$$h_{3_{HCG}} = 8.77 - [(730.10 - 4.00) - 719.48] = 2.15 \text{ ft}$$

Because  $h_{3_{HCG}} / h_{1_{HCG}}$  ( $2.15/4.16 = 0.52$ ) is less than 0.77, free-weir flow exists. Before calculating flow, the depth from the concrete slab to the crest of the gate must be determined by calculating the difference between the gate crest elevation (730.10 ft -  $h_{g_{HCG}}$ ) and the elevation of the top of the concrete slab (723.58).

$$p_{HCG} = (730.10 - 4.00) - 723.58 = 2.52 \text{ ft}.$$

Using equation 32 from table 12,

$$\begin{aligned} Q_{HCG} &= 166.5h_{1_{HCG}}^{1.348} p_{HCG}^{0.152} \\ &= 166.5(4.16)^{1.348} (2.52)^{0.152} \\ &= 1309 \text{ ft}^3 / \text{s} , \end{aligned}$$

Therefore the total flow is

$$Q_{TOTAL} = 21.26 + 1309 = 1330 \text{ ft}^3 / \text{s}$$

**Example 4:** The following conditions exist:

Headwater pool stage is 2.45 ft, tailwater pool stage is 12.22 ft, and the hinged-crest gate opening is 6.0 ft.

Flow over the spillway is determined by first converting the stages to depths above the crest of the spillway.

$$h_{1_{OS}} = 2.45 - 0.62 = 1.83 \text{ ft}$$

$$h_{3_{OS}} = 12.22 - 10.62 = 1.60 \text{ ft}$$

Because  $h_{3_{OS}}/h_{1_{OS}}$  ( $1.60/1.83=0.87$ ) is between -5.0 and 1 and the hinged-crest gate is open, affected flow exists. For affected flow, the values of  $h_{1_{HCG}}$ ,  $h_{3_{HCG}}$ , and  $P_{HCG}$  must be determined.

$$h_{1_{HCG}} = 2.45 - [(730.10 - 6.0) - 729.48] = 7.83 \text{ ft}$$

$$h_{3_{HCG}} = 12.22 - [(730.10 - 6.0) - 719.48] = 7.60 \text{ ft}$$

$$P_{HCG} = (730.10 - 6.0) - 723.58 = 0.52 \text{ ft.}$$

Using equation 30 from table 11,

$$\begin{aligned} Q_{OS} &= 285.5 h_{1_{OS}}^{0.933} P_{HCG}^{0.149} (h_{1_{OS}} - h_{3_{OS}})^{0.930} \left( \frac{h_{1_{HCG}} - h_{3_{HCG}}}{h_{1_{HCG}}} \right)^{-0.905} \\ &= 285.5 (1.83)^{0.933} (0.52)^{0.149} ((1.83) - (1.60))^{0.930} \left( \frac{(7.83) - (7.60)}{(7.83)} \right)^{-0.905} \\ &= 2825 \text{ ft}^3 / \text{s} . \end{aligned}$$

Because  $h_{3_{HCG}}/h_{1_{HCG}}$  ( $7.60/7.83 = 0.97$ ) is greater than 0.77, submerged-weir flow exists. \*Note: there are instances when free-weir flow, rather than submerged-weir flow, exists over the gate while the spillway experiences affected flow. Refer to example 3 for calculations of free-weir flow over the hinged-crest gate.

Using equation 34 from table 12,

$$\begin{aligned} Q_{HCG} &= 146.9 h_{1_{HCG}}^{1.820} h_{3_{HCG}}^{-0.472} P_{HCG}^{0.152} \\ &= 146.9 (7.83)^{1.820} (7.60)^{-0.472} (0.52)^{0.152} \\ &= 2162 \text{ ft}^3 / \text{s} , \end{aligned}$$

Therefore the total flow is

$$Q_{TOTAL} = 2825 + 2162 = 4987 \text{ ft}^3 / \text{s}$$

## Summary

The Illinois Department of Natural Resources—Office of Water Resources operates control structures on a reach of the Fox River in northeastern Illinois between McHenry and Algonquin. These structures are used to maintain water levels in the river for flood-control and recreational purposes. The McHenry control structure is at river mile 97.8 and has a drainage area of 1,250 square miles (mi<sup>2</sup>). The Algonquin control structure is at river mile 81.6 and has a drainage area of 1,403 mi<sup>2</sup>. This report documents the effects of the hinged-crest gates, a broad-crested weir, sluice gates, and an ogee spillway on the Fox River control-structure ratings at McHenry and Algonquin.

The Fox River control-structure ratings were determined by measuring headwater and tailwater stage along with streamflow at a wide range of flows at different gate openings. Standard control-structure rating techniques were used to rate each structure.

The control structures at McHenry consist of a 221-foot (ft) broad-crested weir, a 4-ft-wide fish ladder, a 50-ft wide hinged-crest gate, five 13.75-ft-wide sluice gates, and a navigational lock. Sixty measurements were used to rate the McHenry control structures. The flow regime for the broad-crested weir included free weir, and the hinged-crest gate included both free and submerged weir. The flow regimes for the sluice gate included free and submerged weir and free and submerged orifice.

The control structures at Algonquin, consist of a 242-ft ogee spillway and a 50-ft-wide hinged-crest gate. Forty-one measurements were used to rate the Algonquin control structures. The flow regimes for the ogee spillway included both free and affected weir. The flow regimes for the hinged-crest gate included free and submerged weir.

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# Appendixes A–F

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## Appendix A: Fox River near McHenry, Illinois, Headwater and Tailwater Stages for Broad-Crested Weir and Hinged-Crest Gate Measurements.

[USGS, U.S. Geological Survey; ft, foot; BCW, Broad-Crested Weir; HCG, Hinged-Crest Gate; ft<sup>3</sup>/s, cubic foot per second;  $h_{\text{HCG}}$ , hinged-crest gate opening referenced to the broad-crested-weir crest; ---, not applicable]

| USGS<br>measure-<br>ment<br>number | Date       | Central<br>Standard<br>Time | Water surface |                |            |                | Measured<br>BCW and (or)<br>HCG Flow<br>(ft <sup>3</sup> /s) | Gate<br>opening<br>$h_{\text{HCG}}$ (ft) |
|------------------------------------|------------|-----------------------------|---------------|----------------|------------|----------------|--|--|
|                                    |            |                             | Headwater     |                | Tailwater  |                |  |  |
|                                    |            |                             | Stage (ft)    | Elevation (ft) | Stage (ft) | Elevation (ft) |  |  |
| 5                                  | 05/16/1985 | 1350                        | 4.05          | 737.05         | 1.35       | 731.50         | 169  | ---                                      |
| 13                                 | 08/28/1986 | 1500                        | 4.23          | 737.23         | 1.05       | 731.20         | 342  | ---                                      |
| 15                                 | 09/27/1986 | 1345                        | 5.34          | 738.34         | 6.12       | 736.27         | 1,880  | ---                                      |
| 20                                 | 09/30/1986 | 1120                        | 5.90          | 738.90         | 6.98       | 737.13         | 2,990  | ---                                      |
| 44                                 | 11/18/2002 | 1436–1521                   | 4.16          | 737.16         | .93        | 731.08         | 565  | 1.0                                      |
| 45                                 | 11/19/2002 | 0830–0915                   | 3.98          | 736.98         | 1.61       | 731.76         | 1,012  | 2.2                                      |
| 46                                 | 11/19/2002 | 1339–1440                   | 3.62          | 736.62         | 1.60       | 731.75         | 1,345  | 4.1                                      |
| 47                                 | 11/20/2002 | 0922–1004                   | 3.21          | 736.21         | 2.12       | 732.27         | 1,775  | 6.0                                      |
| <sup>A</sup> 48                    | 04/04/2003 | 1127–1217                   | 4.11          | 737.11         | 1.30       | 731.45         | 145  | 0.0                                      |
| 49                                 | 05/17/2004 | 1134–1155                   | 4.30          | 737.30         | 3.50       | 733.65         | 803  | 1.0                                      |
| <sup>B</sup> 50                    | 05/17/2004 | 1509–1537                   | 4.06          | 737.06         | 3.78       | 733.93         | 1,240  | 2.0                                      |
| 51                                 | 05/17/2004 | 1703–1728                   | 3.80          | 736.80         | 3.99       | 734.14         | 2,040  | 5.0                                      |
| 52                                 | 05/24/2004 | 0800–0838                   | 4.04          | 737.04         | 5.85       | 736.00         | 1,820  | 6.0                                      |
| 53                                 | 03/17/2006 | 1033–1048                   | 2.64          | 735.64         | 3.77       | 733.92         | 1,077  | 4.0                                      |
| <sup>C</sup> 54                    | 03/17/2006 | 1551–1628                   | 3.37          | 736.37         | 3.31       | 733.46         | 401  | 2.0                                      |
| <sup>D</sup> 55                    | 03/16/2007 | 1055–1113                   | 2.64          | 735.64         | 4.32       | 734.47         | 1,132  | 4.5                                      |
| 56                                 | 08/22/2007 | 1010–1024                   | 3.67          | 736.67         | 5.58       | 735.73         | 1,710  | 6.0                                      |
| 57                                 | 08/27/2007 | 1012–1026                   | 4.83          | 737.83         | 7.03       | 737.18         | 2,550  | 6.0                                      |
| 58                                 | 03/26/2008 | 1113–1129                   | 2.48          | 735.48         | 4.38       | 734.53         | 1,440  | 5.5                                      |
| 59                                 | 04/16/2008 | 1201–1220                   | 4.16          | 737.16         | 6.04       | 736.19         | 1,930  | 6.0                                      |
| 60                                 | 06/20/2008 | 0728–0740                   | 4.76          | 737.76         | 6.78       | 736.93         | 2,450  | 6.0                                      |

<sup>A</sup>No flow over hinged-crest gate. All other measurements from 2002–2008 had flow over the hinged-crest gate.

<sup>B</sup>Hinged-crest gate opening changed 30 minutes before measurement; measurement not used in equation development.

<sup>C</sup>Outlier, measurement not used in equation development.

<sup>D</sup>Total flow (BCW, HCG, and SL) measured without a separate measurement of sluice gate flow. The sluice gate flow is calculated and subtracted from total flow.

## Appendix B: Fox River near McHenry, Illinois, Headwater and Tailwater Stages for Sluice Gate Measurements.

[USGS, U.S. Geological Survey;  $h_{gsl}$ , sluice gate opening; ft, foot; ft<sup>3</sup>/s, cubic foot per second]

| USGS<br>measure-<br>ment<br>number | Date       | Central<br>Standard<br>Time | Gate<br>opening<br>$h_{gsl}$ (ft) | Gates<br>open | Headwater  |                   | Tailwater  |                   | Measured<br>Flow<br>(ft <sup>3</sup> /s) |
|------------------------------------|------------|-----------------------------|-----------------------------------|---------------|------------|-------------------|------------|-------------------|--|
|                                    |            |                             |                                   |               | Stage (ft) | Elevation<br>(ft) | Stage (ft) | Elevation<br>(ft) |  |
| 1                                  | 03/22/1985 | 1250                        | 4.0                               | 5             | 3.51       | 736.51            | 3.90       | 734.05            | 2,790                                    |
| 2                                  | 03/22/1985 | 1400                        | 3.0                               | 5             | 3.68       | 736.68            | 3.70       | 733.85            | 1,990                                    |
| 3                                  | 03/26/1985 | 1230                        | 3.8                               | 5             | 2.64       | 735.64            | 3.45       | 733.60            | 2,100                                    |
| 4                                  | 03/26/1985 | 1430                        | 3.3                               | 5             | 2.71       | 735.71            | 3.42       | 733.57            | 1,850                                    |
| 6                                  | 05/16/1985 | 1350                        | .6                                | 5             | 4.03       | 737.03            | 1.35       | 731.50            | 448                                      |
| 7                                  | 10/04/1985 | 1205                        | 2.5                               | 4             | 4.05       | 737.05            | 2.75       | 732.90            | 1,460                                    |
| 8                                  | 11/04/1985 | 1026                        | 3.15                              | 4             | 3.98       | 736.98            | 2.82       | 732.97            | 1,830                                    |
| 9                                  | 03/17/1986 | 1350                        | 6.5                               | 5             | 4.31       | 737.31            | 5.03       | 735.18            | 3,230                                    |
| 10                                 | 04/22/1986 | 1105                        | 1.2                               | 5             | 3.23       | 736.23            | 1.71       | 731.86            | 833                                      |
| <sup>B</sup> 11                    | 04/22/1986 | 1340                        | 2.0                               | 4             | 3.13       | 736.13            | 1.85       | 732.00            | 1,180                                    |
| <sup>B</sup> 11                    | 04/22/1986 | 1340                        | 1.0                               | 1             | 3.13       | 736.13            | 1.85       | 732.00            | 0  |
| 12                                 | 05/23/1986 | 115                         | 1.2                               | 5             | 4.16       | 737.16            | 2.25       | 732.40            | 967                                      |
| 14                                 | 08/28/1986 | 1500                        | .2                                | 5             | 4.22       | 737.22            | 1.05       | 731.20            | 180                                      |
| 16                                 | 09/27/1986 | 1530                        | 4.0                               | 5             | 5.35       | 738.35            | 6.15       | 736.30            | 3,045                                    |
| 17                                 | 09/27/1986 | 1710                        | 7.0                               | 5             | 5.20       | 738.20            | 6.25       | 736.40            | 4,054                                    |
| 18                                 | 09/27/1986 | 1805                        | 4.9                               | 5             | 5.22       | 738.22            | 6.25       | 736.40            | 3,600                                    |
| 19                                 | 09/27/1986 | 1850                        | 4.5                               | 5             | 5.26       | 738.26            | 6.30       | 736.45            | 3,320                                    |
| 21                                 | 09/30/1986 | 1345                        | 4.0                               | 5             | 5.90       | 738.90            | 6.98       | 737.13            | 2,600                                    |
| 22                                 | 09/30/1986 | 1505                        | 4.5                               | 5             | 5.86       | 738.86            | 6.98       | 737.13            | 2,920                                    |
| 23                                 | 10/15/1986 | 1040                        | 7.0                               | 5             | 4.25       | 737.25            | 5.10       | 735.25            | 3,270                                    |
| 24                                 | 11/01/1990 | 936                         | 1.0                               | 5             | 2.59       | 735.59            | 1.32       | 731.47            | 636                                      |
| 25                                 | 11/01/1990 | 1137                        | .1                                | 5             | 2.67       | 735.67            | 1.11       | 731.26            | 63.9                                     |
| 26                                 | 11/01/1990 | 1350                        | .1                                | 5             | 2.63       | 735.63            | 1.05       | 731.20            | 74.4                                     |
| 27                                 | 11/02/1990 | 1243                        | .1                                | 5             | 2.68       | 735.68            | .58        | 730.73            | 73.9                                     |
| 28                                 | 11/03/1990 | 825                         | .1                                | 5             | 2.91       | 735.91            | .45        | 730.60            | 74.1                                     |
| 29                                 | 11/04/1990 | 815                         | .1                                | 5             | 3.17       | 736.17            | .35        | 730.50            | 75.0                                     |
| 30                                 | 11/04/1990 | 1355                        | .1                                | 5             | 3.17       | 736.17            | .35        | 730.50            | 75.9                                     |
| 31                                 | 11/05/1990 | 1024                        | .1                                | 5             | 3.56       | 736.56            | .40        | 730.55            | 82.6                                     |
| 32                                 | 11/05/1990 | 1812                        | 2.5                               | 5             | 2.84       | 735.84            | 1.74       | 731.89            | 1,340                                    |
| 33                                 | 11/05/1990 | 2035                        | 2.5                               | 5             | 2.76       | 735.76            | 1.89       | 732.04            | 1,310                                    |
| 34                                 | 11/06/1990 | 230                         | 2.5                               | 5             | 2.66       | 735.66            | 2.19       | 732.34            | 1,370                                    |
| 35                                 | 11/06/1990 | 1300                        | 2.5                               | 5             | 2.60       | 735.60            | 2.38       | 732.53            | 1,500                                    |
| 36                                 | 11/07/1990 | 1049                        | 2.5                               | 5             | 2.69       | 735.69            | 2.52       | 732.67            | 1,360                                    |
| 37                                 | 11/07/1990 | 1430                        | 2.5                               | 5             | 2.69       | 735.69            | 2.52       | 732.67            | 1,510                                    |

<sup>B</sup>Four gates were set to 2.0 ft, and one gate was set to 1.0 ft. Equations developed in this study were used to subtract flow from the gate open to 1.0 ft; a coefficient for a 2.0 ft opening was determined from the measurement.

## Appendix B: Fox River near McHenry, Illinois, Headwater and Tailwater Stages for Sluice Gate Measurements.—Continued

[USGS, U.S. Geological Survey;  $h_{g_{SL}}$ , sluice gate opening; ft, foot; ft<sup>3</sup>/s, cubic foot per second]

| USGS<br>measure-<br>ment<br>number | Date       | Central<br>Standard<br>Time | Gate<br>opening<br>$h_{g_{SL}}$ (ft) | Gates<br>open | Headwater  |                   | Tailwater  |                   | Measured<br>Flow<br>(ft <sup>3</sup> /s) |
|------------------------------------|------------|-----------------------------|--------------------------------------|---------------|------------|-------------------|------------|-------------------|--|
|                                    |            |                             |                                      |               | Stage (ft) | Elevation<br>(ft) | Stage (ft) | Elevation<br>(ft) |  |
| 38                                 | 11/07/1990 | 1640                        | 2.5                                  | 5             | 2.69       | 735.69            | 2.56       | 732.71            | 1,480                                    |
| 39                                 | 11/08/1990 | 1202                        | 2.5                                  | 5             | 2.71       | 735.71            | 2.60       | 732.75            | 1,480                                    |
| 40                                 | 11/08/1990 | 1200                        | 2.5                                  | 5             | 2.71       | 735.71            | 2.60       | 732.75            | 1,580                                    |
| 41                                 | 11/09/1990 | 947                         | 2.5                                  | 5             | 2.69       | 735.69            | 2.58       | 732.73            | 1,460                                    |
| 42                                 | 04/24/1993 | 1100                        | 6.0                                  | 5             | 5.17       | 738.17            | 3.24       | 733.39            | 3,920                                    |
| 43                                 | 04/28/1993 | 845                         | 6.0                                  | 5             | 4.98       | 737.98            | 2.78       | 732.93            | 3,664                                    |
| 49                                 | 05/17/2004 | 1244–1257                   | 2.2                                  | 5             | 4.29       | 737.29            | 3.50       | 733.65            | 1,760                                    |
| 50                                 | 05/17/2004 | 1434–1447                   | 2.2                                  | 5             | 4.10       | 737.10            | 3.74       | 733.89            | 1,690                                    |
| 51                                 | 05/17/2004 | 1759–1811                   | 2.2                                  | 4             | 3.77       | 736.77            | 4.00       | 734.15            | 1,250                                    |
| 52                                 | 05/24/2004 | 0902–0919                   | 5.7                                  | 5             | 4.04       | 737.04            | 5.85       | 736.00            | 3,020                                    |
| 53                                 | 03/17/2006 | 1033–1048                   | 3.0                                  | 5             | 2.64       | 735.64            | 3.77       | 733.92            | 1,664                                    |
| 54                                 | 03/17/2006 | 1536–1546                   | 3.0                                  | 5             | 3.37       | 736.37            | 3.31       | 733.46            | 1,890                                    |
| 56A                                | 08/22/2007 | 1122–1130                   | 5.0                                  | 5             | 3.73       | 736.73            | 5.59       | 735.74            | 2,760                                    |
| 57A                                | 08/27/2007 | 1107–1116                   | 6.2                                  | 5             | 4.83       | 737.83            | 7.03       | 737.18            | 3,140                                    |
| 58A                                | 03/26/2008 | 1248–1258                   | 4.5                                  | 5             | 2.47       | 735.47            | 4.36       | 734.51            | 1,970                                    |
| 59A                                | 04/16/2008 | 1306–1319                   | 5.3                                  | 5             | 4.14       | 737.14            | 6.02       | 736.17            | 2,960                                    |
| 60A                                | 06/20/2008 | 0848–0854                   | 6.0                                  | 5             | 4.75       | 737.75            | 6.76       | 736.91            | 3,280                                    |

<sup>B</sup>Four gates were set to 2.0 ft, and one gate was set to 1.0 ft. Equations developed in this study were used to subtract flow from the gate open to 1.0 ft; a coefficient for a 2.0 ft opening was determined from the measurement.

## Appendix C. Fox River at Algonquin, Illinois, Headwater and Tailwater Stages for Ogee Spillway and Hinged-Crest Gate Measurements with the Hinged-Crest Gate Closed.

[USGS, U.S. Geological Survey; ft, foot; ft<sup>3</sup>/s, cubic foot per second; measurements in bold indicate that the hinged-crest gate was closed, and no flow was overtopping it; ---, not determined]

| USGS<br>measure-<br>ment<br>number | Date              | Time             | Water-surface elevation |                |                |                | Measured<br>flow (M)<br>(ft <sup>3</sup> /s) | Flow over<br>hinged-<br>crest gate |
|------------------------------------|-------------------|------------------|-------------------------|----------------|----------------|----------------|--|------------------------------------|
|                                    |                   |                  | Headwater (HW)          |                | Tailwater (TW) |                |  |                                    |
|                                    |                   |                  | Stage (ft)              | Elevation (ft) | Stage (ft)     | Elevation (ft) |  |                                    |
| <sup>A</sup> 505                   | 03/26/2002        | 0803–1020        | <b>2.00</b>             | <b>731.48</b>  | ---            | ---            | <b>1,180</b>                                 | No                                 |
| <sup>A</sup> 506                   | 04/11/2002        | 0845–1015        | <b>2.76</b>             | <b>732.24</b>  | ---            | ---            | <b>2,600</b>                                 | No                                 |
| <sup>A</sup> 507                   | 06/11/2002        | 0915–1100        | <b>2.99</b>             | <b>732.47</b>  | ---            | ---            | <b>3,260</b>                                 | No                                 |
| <sup>A</sup> 508                   | 07/23/2002        | 1250–1350        | <b>1.24</b>             | <b>730.72</b>  | ---            | ---            | <b>280</b>                                   | No                                 |
| <b>509</b>                         | <b>09/24/2002</b> | <b>1330–1440</b> | <b>1.58</b>             | <b>731.06</b>  | <b>6.98</b>    | <b>726.46</b>  | <b>577</b>                                   | No                                 |
| <b>510</b>                         | <b>11/07/2002</b> | <b>1405–1510</b> | <b>1.37</b>             | <b>730.85</b>  | <b>6.64</b>    | <b>726.12</b>  | <b>381</b>                                   | No                                 |
| 511                                | 01/09/2003        | 1125–1235        | 1.38                    | 730.86         | 7.10           | 726.58         | 406  | Yes                                |
| <sup>B</sup> 512                   | 03/12/2003        | 1145–1230        | 1.17                    | 730.65         | 6.47           | 725.95         | 267  | Yes                                |
| 513                                | 05/05/2003        | 1040–1140        | 1.86                    | 731.34         | 7.96           | 727.44         | 1,060  | Yes                                |
| 514                                | 05/07/2003        | 0950–1140        | 2.26                    | 731.74         | 8.81           | 728.29         | 1,960  | Yes                                |
| 515                                | 06/18/2003        | 0800–0900        | 1.43                    | 730.91         | 6.88           | 726.36         | 473  | Yes                                |
| 516                                | 09/03/2003        | 1255–1355        | .94                     | 730.42         | 6.05           | 725.53         | 76.5   | No                                 |
| <b>517</b>                         | <b>10/15/2003</b> | <b>0815–0920</b> | <b>1.17</b>             | <b>730.65</b>  | <b>6.77</b>    | <b>726.25</b>  | <b>203</b>                                   | No                                 |
| 518                                | 12/02/2003        | 1130–1240        | 1.54                    | 731.02         | 7.13           | 726.61         | 605  | Yes                                |
| <sup>B</sup> 519                   | 02/02/2004        | 1525–1615        | 1.34                    | 730.82         | 6.62           | 726.10         | 382  | Yes                                |
| 520                                | 03/23/2004        | 1300–1450        | 1.82                    | 731.30         | 7.77           | 727.25         | 989  | Yes                                |
| <sup>C</sup> 525                   | 07/08/2004        | 1145–1420        | 1.76                    | 731.24         | 7.88           | 727.36         | 1,240  | Yes                                |
| <b>526</b>                         | <b>09/14/2004</b> | <b>1010–1135</b> | <b>1.29</b>             | <b>730.77</b>  | <b>6.39</b>    | <b>725.87</b>  | <b>301</b>                                   | No                                 |
| 527                                | 11/08/2004        | 1120–1320        | 1.74                    | 731.22         | 7.16           | 726.64         | 800  | Yes                                |
| 528                                | 03/10/2005        | 1200–1400        | 2.11                    | 731.59         | 8.10           | 727.58         | 1540   | Yes                                |
| <b>529</b>                         | <b>06/28/2005</b> | <b>1035–1200</b> | <b>1.03</b>             | <b>730.51</b>  | <b>6.17</b>    | <b>725.65</b>  | <b>121</b>                                   | No                                 |
| <b>530</b>                         | <b>10/04/2005</b> | <b>0850–1005</b> | <b>1.27</b>             | <b>730.75</b>  | <b>6.45</b>    | <b>725.93</b>  | <b>294</b>                                   | No                                 |
| <b>535</b>                         | <b>07/28/2006</b> | <b>0830–0930</b> | <b>1.34</b>             | <b>730.82</b>  | <b>6.55</b>    | <b>726.03</b>  | <b>368</b>                                   | No                                 |
| 536                                | 10/02/2006        | 1010–1140        | 1.46                    | 730.94         | 6.59           | 726.07         | 429  | Yes                                |
| <sup>D</sup> 538                   | 06/28/2007        | 1009–1023        | 1.65                    | 731.13         | 7.06           | 726.54         | 801  | ---                                |
| <sup>E</sup> 541                   | 11/09/2007        | 1043–1056        | 1.53                    | 731.01         | 7.09           | 726.57         | 703  | ---                                |
| <sup>E</sup> 542                   | 12/17/2007        | 1354–1409        | 1.74                    | 731.22         | 7.59           | 727.07         | 1,140  | ---                                |

<sup>A</sup>Tailwater gage was not yet installed. Flow-regime conditions are considered free weir for computations.

<sup>B</sup>Ice-affected measurement, not used in equation development.

<sup>C</sup>Outlier, measurement not used in equation development.

<sup>D</sup>Hinged-crest gate opening changed 20 minutes before measurement, not used in equation development.

<sup>E</sup>Hinged-crest gate repairs, measurement not used in equation development.

## Appendix D. Fox River at Algonquin, Illinois, Headwater and Tailwater Stages for Ogee Spillway and Hinged-Crest Gate Measurements with the Hinged-Crest Gate Open.

[USGS, U.S. Geological Survey; ft, foot; ft<sup>3</sup>/s, cubic foot per second;  $h_{gHCG}$ , hinged-crest gate opening referenced to the broad-crested-weir crest; IDNR, Illinois Department of Natural Resources—Office of Water Resources; ---, not determined]

| USGS<br>measure-<br>ment<br>number | Date       | Central<br>Standard<br>Time | Water-surface elevation |                |                |                | Measured<br>OS and (or)<br>HCG flow<br>(ft <sup>3</sup> /s) | Gate<br>opening<br>$h_{gHCG}$ (ft) |
|------------------------------------|------------|-----------------------------|-------------------------|----------------|----------------|----------------|---|------------------------------------|
|                                    |            |                             | Headwater (HW)          |                | Tailwater (TW) |                |   |                                    |
|                                    |            |                             | Stage (ft)              | Elevation (ft) | Stage (ft)     | Elevation (ft) |   |                                    |
| ---                                | 11/19/2002 | 1118–1200                   | 1.09                    | 730.57         | 7.77           | 727.25         | 868   | 2.0                                |
| ---                                | 11/19/2002 | 1649–1735                   | .78                     | 730.26         | 8.77           | 728.25         | 1,410   | 4.0                                |
| ---                                | 11/20/2002 | 1220–1310                   | .60                     | 730.08         | 9.19           | 728.67         | 1,800   | 6.0                                |
| 523                                | 05/18/2004 | 1313–1328                   | 2.86                    | 732.34         | 10.66          | 730.14         | 3,570   | 1.0                                |
| 522                                | 05/18/2004 | 0821–0841                   | 2.66                    | 732.14         | 11.06          | 730.54         | 3,730   | 1.8                                |
| 521                                | 05/18/2004 | 0659–0722                   | 2.56                    | 732.04         | 11.29          | 730.77         | 3,890   | 2.4                                |
| 524                                | 05/24/2004 | 1234–1253                   | 2.66                    | 732.14         | 12.61          | 732.09         | 5,580   | 6.0                                |
| 531                                | 02/02/2006 | 0959–1011                   | 1.48                    | 730.96         | 8.23           | 727.71         | 1,580   | 2.0                                |
| 533                                | 03/17/2006 | 1402–1435                   | 1.69                    | 731.17         | 10.13          | 729.61         | 3,160   | 4.0                                |
| 532                                | 03/17/2006 | 1210–1247                   | 1.55                    | 731.03         | 10.42          | 729.90         | 3,320   | 5.0                                |
| 534                                | 05/31/2006 | 1156–1216                   | 1.66                    | 731.14         | 8.03           | 727.51         | 2,000   | 2.0                                |
| 537                                | 03/14/2007 | 1332–1350                   | 1.88                    | 731.36         | 10.37          | 729.85         | 3,220   | 4.0                                |
| 539                                | 08/22/2007 | 1327–1341                   | 2.47                    | 731.95         | 12.24          | 731.72         | 5,000   | 6.0                                |
| 540                                | 08/27/2007 | 1311–1328                   | 3.45                    | 732.93         | 13.43          | 732.91         | 6,600   | 6.0                                |
| 543                                | 01/11/2008 | 1033–1047                   | 1.76                    | 731.24         | 10.13          | 729.61         | 3,010   | 3.5                                |
| 544                                | 02/22/2008 | 1232–1243                   | 1.60                    | 731.08         | 8.75           | 728.23         | 1,980   | 2.0                                |
| 545                                | 03/26/2008 | 0912–0941                   | 1.87                    | 731.35         | 10.68          | 730.16         | 3,850   | 4.0                                |
| 546                                | 04/16/2008 | 1038–1053                   | 2.62                    | 732.10         | 12.43          | 731.91         | 5,510   | 6.0                                |
| 547                                | 06/11/2008 | 0948–1005                   | 2.28                    | 731.76         | 11.74          | 731.22         | 4,560   | 6.0                                |
| 548                                | 06/20/2008 | 0954–1007                   | 2.95                    | 732.43         | 12.80          | 732.28         | 6,030   | 6.0                                |
| IDNR                               | 09/16/2008 | 1130                        | 2.22                    | 731.70         | 10.08          | 729.56         | 2,936   | 2.0                                |

## Appendix E: Photographs of Various Flow Conditions, Fox River near McHenry, Illinois

### Acronyms

BCW – broad-crested weir  
FW – free-weir flow  
HCG – hinged-crest gate  
NF – no flow  
SW – submerged-weir flow



**Figure E1.** Looking from left to right at tailwater conditions for sluice gates, December 1, 2003.



**Figure E2.** Looking at the upstream face of open hinged-crest gate, measurement 58, March 26, 2008. HCG flow regime=SW.



**Figure E3.** Looking at tailwater conditions of open hinged-crest gate, measurement 58, March 26, 2008. HCG flow regime=SW. BCW flow regime=NF.



**Figure E4.** Looking from right to left at headwater conditions for open hinged-crest gate and weir, measurement 58, March 26, 2008. HCG flow regime=SW. BCW flow regime=NF.



**Figure E5.** Looking from left to right at tailwater conditions for sluice gates, measurement 58A, March 26, 2008. Sluice gate flow regime=FW.



**Figure E6.** Looking from right to left at headwater conditions for sluice gates, measurement 59A, April 16, 2008. Sluice gate flow regime=SW.



**Figure E7.** Looking from right to left at hinged-crest gate and weir, showing both headwater and tailwater conditions, measurement 59, April 16, 2008. HCG flow regime=SW. BCW flow regime=FW

## Appendix F: Photographs of Various Flow Conditions, Fox River at Algonquin, Illinois

### Acronyms

AFF – affected flow

FW – free-weir flow

FW-FL – free-weir flow with flow over the hinged-crest gate (crest at elevation of ogee spillway)

FW-NF – free-weir flow with no flow over the hinged-crest gate

HCG – hinged-crest gate

NF – no flow

OS – ogee spillway

SW – submerged-weir flow



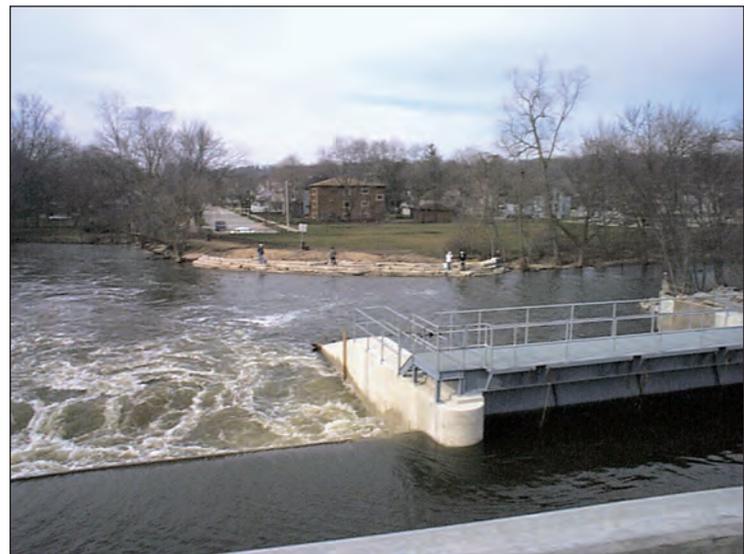
**Figure F1.** Looking at the downstream face of the hinged-crest gate, measurement 506, April 11, 2002. Flow regime=FW-NF.



**Figure F2.** Looking from right to left at both headwater and tailwater conditions, measurement 506, April 11, 2002. Flow regime=FW-NF.



**Figure F3.** Looking from right to left at tailwater conditions, measurement 506, April 11, 2002.  
Flow regime=FW-NF.



**Figure F4.** Looking downstream at hinged-crest gate and spillway from bridge, measurement 506, April 11, 2002.  
Flow regime=FW-NF.

**Figure F5.** Looking from right to left at headwater and tailwater conditions while gate is fully open, November 20, 2002.  
 HCG flow regime=FW.  
 OS flow regime=NF.



**Figure F6.** Looking downstream at headwater and tailwater conditions when gate is fully open, November 20, 2002.  
 HCG flow regime=FW.  
 OS flow regime=NF.

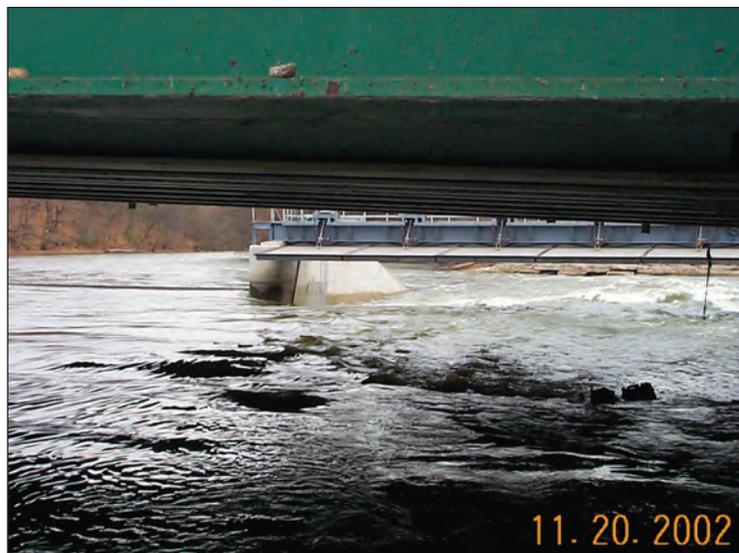


**Figure F7.** Looking downstream of gate at tailwater conditions, November 20, 2002.  
 HCG flow regime=FW.  
 OS flow regime=NF.

**Figure F8.** Looking upstream from riprap at tailwater conditions, November 20, 2002.  
HCG flow regime=FW.  
OS flow regime=NF.



**Figure F9.** Looking downstream at headwater conditions from upstream side of bridge, November 20, 2002.  
HCG flow regime=FW.  
OS flow regime=NF.





**Figure F10.** Looking upstream at spillway, measurement 511, January 9, 2003. Flow regime=FW-FL.



**Figure F11.** Looking downstream along new rock deposition, measurement 511, January 9, 2003. Flow regime=FW-FL.



**Figure F12.** Looking upstream at gate and spillway, measurement 511, January 9, 2003. Flow regime=FW-FL.



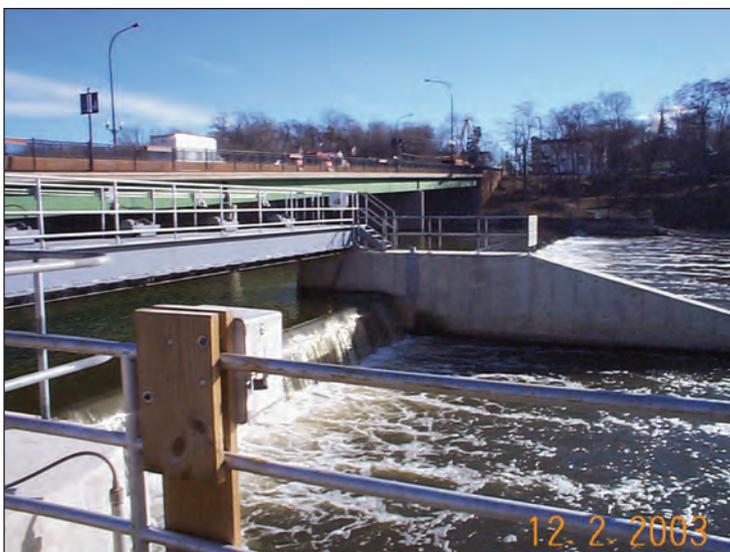
**Figure F13.** Looking downstream of gate and spillway, measurement 511, January 9, 2003. Flow regime=FW-FL.



**Figure F14.** Looking at conditions of hinged-crest gate, measurement 515, June 18, 2003.  
Flow regime=FW-FL.



**Figure F15.** Looking downstream from gate, measurement 516, September 3, 2003.  
Flow regime=FW-NF.



**Figure F16.** Looking from right to left at tailwater conditions, measurement 518, December 2, 2003.  
Flow regime=FW-FL.



**Figure F17.** Looking at upstream side of hinged-crest gate as well as tailwater conditions during flood, measurement 521 May 18, 2004.  
HCG flow regime=SW.  
OS flow regime=AFF.



**Figure F18.** Looking right to left at tailwater conditions, measurement 525, July 8, 2004.  
Flow regime=FW-FL.



**Figure F19.** Looking at downstream face of gate, measurement 527, November 8, 2004.  
Flow regime=FW-FL.

**Figure F21.** Looking right to left at dam crest with ice, February 15, 2007.



**Figure F20.** Looking downstream of gate and spillway at tailwater conditions, February 15, 2007.



**Figure F22.** Looking right to left at headwater conditions, February 15, 2007.

**Figure F23.** Looking downstream of gate and spillway at tailwater conditions, measurement 537, March 14, 2007. HCG flow regime=FW. OS flow regime=AFF.



**Figure F24.** Looking right to left at headwater conditions, measurement 537, March 14, 2007. HCG flow regime=FW. OS flow regime=AFF.





**Figure F25.** Looking right to left at tailwater conditions, measurement 543, January 11, 2008. HCG flow regime=FW. OS flow regime=AFF.



**Figure F26.** Looking downstream, measurement 543, January 11, 2008. HCG flow regime=FW. OS flow regime=AFF.



**Figure F27.** Looking right to left at tailwater conditions, measurement 545, March 26, 2008. HCG flow regime=SW. OS flow regime=AFF.



**Figure F28.** Looking downstream of gate at tailwater conditions, measurement 545, March 26, 2008. HCG flow regime=SW. OS flow regime=AFF.



**Figure F29.** Looking downstream of gate at tailwater conditions, measurement 546, April 16, 2008. HCG flow regime=SW. OS flow regime=AFF.



**Figure F30.** Looking right to left at headwater and tailwater conditions, measurement 546, April 16, 2008. HCG flow regime=SW. OS flow regime=AFF.





