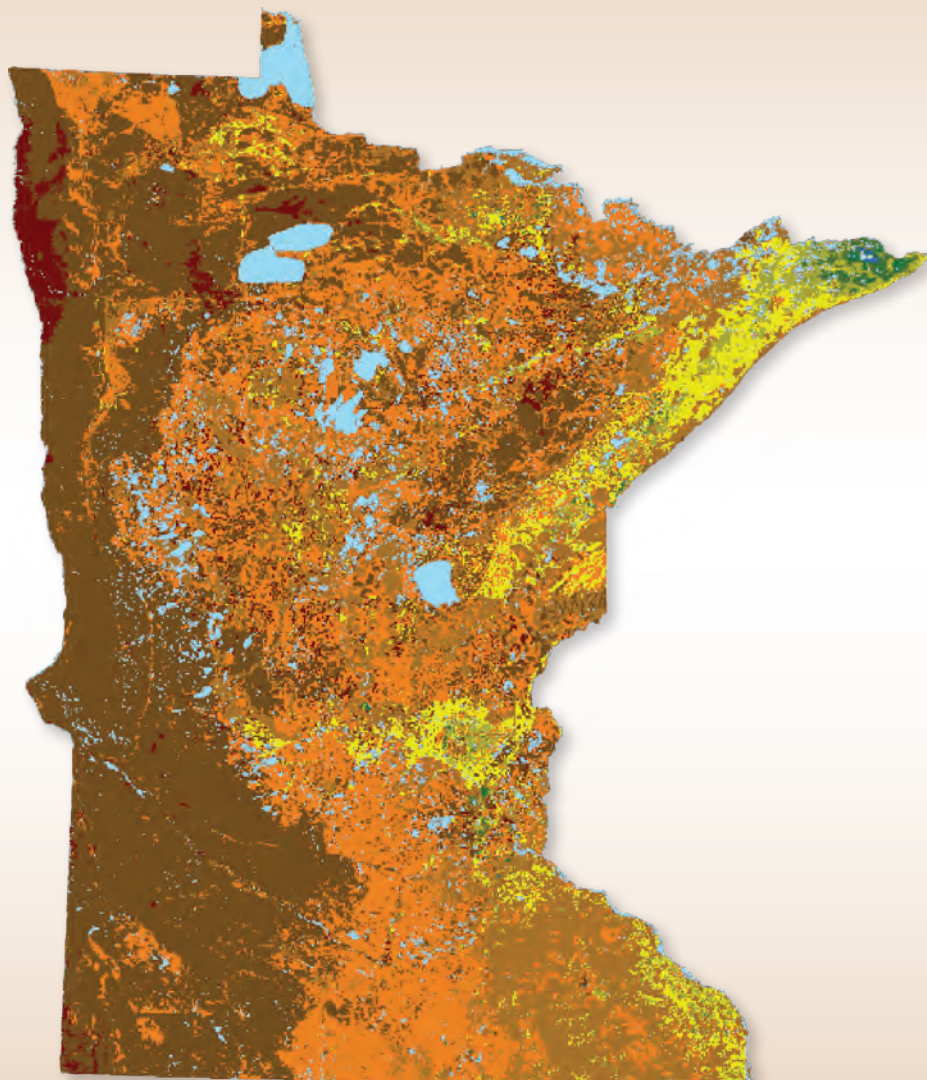


Prepared in cooperation with the Minnesota Pollution Control Agency

Potential Groundwater Recharge for the State of Minnesota Using the Soil-Water-Balance Model, 1996–2010



Scientific Investigations Report 2015–5038

Cover. Map showing mean annual potential recharge rates from 1996–2010 based on results from the Soil-Water-Balance model for Minnesota.

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By Erik A. Smith and Stephen M. Westenbroek

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Conversion Factors

Inch/Pound to International System of Units (primary units used within report)

Multiply	By	To obtain
Length		
inch (in.)	2.54	centimeter (cm)
inch (in.)	25.4	millimeter (mm)
foot (ft)	0.3048	meter (m)
mile (mi)	1.609	kilometer (km)
Flow rate		
inch per hour (in/h)	0.0254	meter per hour (m/h)
inch per year (in/yr)	25.4	millimeter per year (mm/yr)

International System of Units to Inch/Pound (used for spatial data and some model input values)

Multiply	By	To obtain
Length		
millimeter (mm)	0.03937	inch (in.)
meter (m)	3.281	foot (ft)
meter (m)	39.37	inches (in)
kilometer (km)	0.6214	mile (mi)
Area		
hectare (ha)	2.471	acre
square kilometer (km²)	0.3861	square mile (mi²)

Supplemental Information

Temperature in degrees Celsius (°C) may be converted to degrees Fahrenheit (°F) as follows:

°F=(1.8×°C)+32

Datum

Horizontal coordinate information is referenced to the North American Datum of 1983 (NAD 83).

Abbreviations

>	greater than
<	less than
AME	absolute mean error
APWL	accumulated potential water loss
ASCII	American Standard Code for Information Interchange
BFI	base-flow index
ET	evapotranspiration
GDD	growing degree days
GIS	geographic information system
Minn.	Minnesota
NCDC	National Climatic Data Center
NLCD	National Land Cover Database
NOAA	National Oceanic and Atmospheric Administration
NRCS	Natural Resources Conservation Service
NSE	Nash-Sutcliffe model efficiency coefficient
RMSE	root mean square error
RRR	regional regression recharge
SSURGO	Soil Survey Geographic [database]
STATSGO	State Soil Geographic [database]
SWB	Soil-Water-Balance
TCMA	Twin Cities Metropolitan Area
USDA	United States Department of Agriculture
USGS	U.S. Geological Survey

Variables

$\Delta_{\text{soil moisture}}$	change in soil moisture
ET	evapotranspiration
n	number of years
\bar{O}	mean of the observed data
O_i	observed value
P	precipitation
\bar{P}	mean of the predicted data
P_i	predicted (simulated) value
PE	potential evapotranspiration
$P-PE$	precipitation minus potential evapotranspiration
R^2	coefficient of determination

Potential Groundwater Recharge for the State of Minnesota Using the Soil-Water-Balance Model, 1995–2010

By Erik A. Smith and Stephen M. Westenbroek

Abstract

Groundwater recharge is one of the most difficult components of a water budget to ascertain, yet is an important boundary condition necessary for the quantification of water resources. In Minnesota, improved estimates of recharge are necessary because approximately 75 percent of drinking water and 90 percent of agricultural irrigation water in Minnesota are supplied from groundwater. The water that is withdrawn must be supplied by some combination of (1) increased recharge, (2) decreased discharge to streams, lakes, and other surface-water bodies, and (3) removal of water that was stored in the system. Recent pressure on groundwater resources has highlighted the need to provide more accurate recharge estimates for various tools that can assess the sustainability of long-term water use. As part of this effort, the U.S. Geological Survey, in cooperation with the Minnesota Pollution Control Agency, used the Soil-Water-Balance model to calculate gridded estimates of potential groundwater recharge across Minnesota for 1996–2010 at a 1-kilometer (0.621-mile) resolution. The potential groundwater recharge estimates calculated for Minnesota from the Soil-Water Balance model included gridded values (1-kilometer resolution) of annual mean estimates (that is, the means for individual years from 1996 through 2010) and mean annual estimates (that is, the mean for the 15-year period 1996–2010).

The Soil-Water-Balance model uses a modified Thornthwaite-Mather soil-water-balance approach, with components of the soil-water balance calculated on a daily basis. A key advantage of this approach includes the use of commonly available geographic information system data layers that incorporate land cover, soil properties, and daily meteorological data to produce temporally and spatially variable gridded estimates of potential recharge. The Soil-Water-Balance model was calibrated by using a combination of parameter estimation techniques, making manual adjustments of model parameters, and using parameter values from previously published Soil-Water-Balance models. Each calibration simulation compared the potential recharge estimate from the model against base-flow estimates derived from three separate hydrograph

separation techniques. A total of 35 Minnesota watersheds were selected for the model calibration.

Meteorological data necessary for the model included daily precipitation, minimum daily temperature, and maximum daily temperature. All of the meteorological data were provided by the Daymet dataset, which included daily continuous surfaces of key climatological data. Land-cover data were provided by the 2001 and 2006 National Land Cover Database: the 2001 classification was used from 1994 through 2003, and the 2006 classification was used from 2004 through 2010. Soil data used in the model included hydrologic soils group and the available soil-water capacity. These soil data were obtained from the Natural Resources Conservation Service Soil Survey Geographic (SSURGO) database and the State Soil Geographic (STATSGO) database.

The statewide mean annual potential recharge rate from 1996–2010 was 4.9 inches per year. Potential recharge estimates increased from west to east across Minnesota. The mean annual potential recharge estimates across Minnesota at a 1-km resolution for the overall simulation period (1996–2010) ranged from less than 0.1 to 17.8 inches per year. Some of the lowest potential recharge rates for the simulation period were in the Red River of the North Basin of northwestern Minnesota, and generally were between 1.0 and 1.5 inches per year. The highest potential recharge rates were in northeastern Minnesota and the Anoka Sand Plain in central Minnesota. Eighty-eight percent of the potential recharge rates (by grid cell) were between 2 and 8 inches per year from 1996–2010. Only about 3 percent of all the potential recharge estimates (by grid cell) were less than 2 inches per year, and 9 percent of estimates were greater than 8 inches per year.

On an annual basis, however, potential recharge rates were as high as 27.2 inches per year. The highest annual mean recharge estimate across the State was for 2010, and the lowest mean recharge estimate was for 2003. Although precipitation variability partially explained the annual differences in potential recharge estimates, precipitation alone did not account for these differences, and other factors such as antecedent moisture conditions likely were important. Also, because precipitation gradients across the State can vary from year to year, the dominant land-cover class and hydrologic soil

group combinations for a particular region had a large effect on the resulting potential recharge value. During 1996–2010, April had the greatest monthly mean potential recharge compared to all other months, accounting for a mean of 30 percent of annual potential recharge in this single month.

Introduction

Groundwater recharge is one of the most important boundary conditions necessary for the development of water budgets. Groundwater recharge is a natural component of the hydrologic cycle and replenishes groundwater that has been withdrawn for various anthropogenic uses. Because groundwater commonly discharges to streams, lakes, and other surface-water bodies, groundwater recharge has a connection to the sustainability of water resources and their ecological health. However, recharge is difficult to estimate because recharge varies spatially and temporally in response to a variety of factors such as climate, precipitation intensity and duration, evapotranspiration, overland runoff patterns, land-cover changes, aquifer properties, soil properties, and geomorphology (Healy and Scanlon, 2010). On a spatial scale, point estimates of recharge are not appropriate for regional-scale models, and on a temporal scale, multiyear hydrologic assessments based on static recharge estimates can misrepresent the overall water budget. For groundwater modelers, a simple approach is to assume that a fixed percentage of precipitation becomes recharge, although this approach does not take antecedent moisture conditions into consideration. Yet another approach is to use recharge as a calibration parameter in a model, adjusting the recharge rates until the measured water-table values match the simulated values. However, using a physically based recharge boundary condition rather than using recharge as a calibration parameter has been shown to improve groundwater models (Jyrkama and others, 2002) and underscores the importance of determining independent recharge rates.

Numerous techniques exist to estimate variable recharge rates. Example techniques include water-table fluctuation methods (Healy and Cook, 2002; Crosbie and others, 2005), Darcian methods (Nimmo and others, 1994), groundwater age dating (McMahon and others, 2011), recession curve displacement methods such as the RORA program (Rutledge, 1998), and water budget models (Vaccaro, 2007). Overall, dozens of possible recharge estimation methods exist, so choosing an appropriate technique can be difficult (Scanlon and others, 2002). Important considerations for the appropriate recharge estimation method include the time scale, the need for static or transient estimates, spatial scale of the recharge estimates, availability of the necessary data, and the ease of use of the recharge estimation method or model. In regards to the spatial scale, a balance of the local- and regional-scale recharge

estimates must be reached, because local estimates (scale from submeters to hectares; feet to acres) generally will not be appropriate for the watershed scale, whereas regional recharge estimates (scale between 10 and 1,000 square kilometers [km²]; thousands of acres to hundreds of square miles) do not capture local variability (Healy and Scanlon, 2010).

In Minnesota, improved estimates of recharge rates are important because the State is dependent on groundwater resources. Approximately 75 percent of drinking water and 90 percent of agricultural irrigation water in Minnesota is supplied from groundwater (Minnesota Department of Natural Resources, 2014). The water that is withdrawn must be supplied by some combination of (1) increased recharge, (2) decreased discharge to streams, lakes, and other surface-water bodies, and (3) removal of water that was stored in the system. With such a heavy reliance on groundwater, proper accounting of groundwater resources is critical. As part of any assessment to determine groundwater resources available for withdrawal, reliable recharge estimates are helpful in determining the sustainable pumping rate out of an aquifer (Zhou, 2009). However, as pointed out by Bredehoeft (1997), it is important to note that using groundwater recharge as approximately equal to the safe yield of sustainable groundwater developments (for example, groundwater withdrawals for consumptive uses) can be fallacious. As noted by Alley (2006), even small changes in total groundwater storage can cause streamflow depletion.

Recent pressure on groundwater resources in Minnesota has highlighted the need to provide more accurate recharge estimates for various tools that can assess the sustainability of long-term water use. As part of this effort, the U.S. Geological Survey (USGS), in cooperation with the Minnesota Pollution Control Agency, used the Soil-Water-Balance (SWB) model (Westenbroek and others, 2010) to calculate mean gridded estimates of potential groundwater recharge across Minnesota from 1996–2010 at a 1-kilometer (0.621-mile) resolution. Potential recharge is infiltrating water that may or may not reach the water table because of unsaturated-zone processes or diversion before reaching the water table (Scanlon and others, 2002). In this report, the term “recharge” in context to any estimate determined by using the SWB model is synonymous with potential recharge. The SWB model is ideal for estimating recharge because the water table is fairly shallow across most of the State, so water that infiltrates beyond the root zone will likely recharge the aquifer.

The SWB model is based on a modified Thornthwaite-Mather soil-water-balance approach (Thornthwaite and Mather, 1955, 1957) that calculates water balance components at a daily time step (Westenbroek and others, 2010). This approach uses commonly available geographic information system (GIS) data layers that incorporate land cover, soil properties, and daily meteorological data to produce temporally and spatially variable gridded estimates of recharge.

Purpose and Scope

The purpose of this report is to document the development of potential recharge estimates for Minnesota using the SWB model (Westenbroek and others, 2010) at a 1-km resolution. The statewide recharge estimates were calibrated by using a combination of parameter estimation (Doherty, 2010), manual adjustments of model parameters, and parameter values from previously published SWB recharge models (Metropolitan Council, 2013; Westenbroek and others, 2010; Stanton and others, 2011; Masterson and others, 2013). Calibration simulations were completed using assumptions of steady-state conditions, in which no pumping was considered. Each calibration simulation compared the potential recharge estimate of the model against base-flow estimates derived from three separate hydrograph separation techniques. A total of 35 Minnesota watersheds were selected for the model calibration. A sensitivity analysis also was done to better understand the response of the model to some of its most important parameters and inputs. Limitations of the model also are described. Although recharge estimates and most model inputs are in units of inch/pound, spatial data such as model grid spacing and some model inputs use the International System of Units.

Previous Studies

Delin and others (2007) estimated the mean annual recharge to surficial materials from 1971 to 2000 for the State of Minnesota. This regional regression recharge (RRR) model regionalized RORA watershed-scale recharge estimates (Rutledge, 1998) based on a regression model that incorporated soil and meteorological information. Delin and others (2007) and Lorenz and Delin (2007) provided additional details on the approach used to estimate recharge. Instead of tracking the water balance components at a daily time step, the regression included precipitation and growing degree days (GDD), a commonly used measure of heat accumulation, to estimate the net precipitation available for recharge instead of a direct measure of evapotranspiration (ET). Although the GDD are a primary factor in estimating ET, the GDD do not account for the effects of land cover and soil characteristics on ET. Delin and others (2007) compared the RRR estimates to RORA watershed-scale recharge estimates as well as to three local-scale methods (unsaturated-zone water balance, water-table fluctuations using three approaches, and age dating of groundwater).

A study by Kanivetsky (1979) used as many as three independent recharge calculation methods for each of 39 watersheds in Minnesota. The three methods used for each watershed, where data were available, were base-flow separation from streamflow, water-table fluctuations from observation wells, and 30-day low-flow characterization of streamflow. For each watershed, a synthesis of the three methods was scaled up to the watershed-scale and compared. The final recharge rates for each watershed were used to estimate

available groundwater resources; however, a separate recharge map of recharge across Minnesota was not published.

Wolock (2003a) estimated the mean annual natural groundwater recharge in the conterminous United States, including all of Minnesota, as a 1-km resolution (grid) dataset. This 1-km grid was created by multiplying a grid of base-flow index (BFI) values by a grid of mean annual runoff values derived from a mean annual runoff contour map for 1951–80. Mean annual runoff is long-term mean streamflow expressed on a per-unit-area basis. The BFI grid used to compute groundwater recharge was interpolated from BFI point values estimated for USGS streamgages (Wolock, 2003b). The BFI point values were computed by using the automated hydrograph separation computer program called BFI (Wahl and Wahl, 2014).

Other studies have produced recharge estimates for parts of Minnesota; examples include Arnold and others (2000), Ruhl and others (2002), Neff and others (2006), and Metropolitan Council (2013). Arnold and others (2000) was limited to the USGS 8-digit watershed scale for the Upper Mississippi River Basin and represented recharge for a fixed period of time. Ruhl and others (2002) estimated recharge rates across broad areas of the seven-county Twin Cities Metropolitan Area (TCMA) using three different techniques: recharge as a percentage of precipitation, recharge based on streamflow-recession displacement, and recharge as determined by a watershed characteristics method. Neff and others (2006) estimated recharge for parts of northeast Minnesota adjacent to Lake Superior by applying base-flow estimates calculated from gaged watersheds equally to the entire watershed area. The Metropolitan Council (2013) used the SWB model to generate recharge estimates for the period of 1988 to 2011 for a more expansive 11-county TCMA.

Model Description

The SWB model uses a modified Thornthwaite-Mather soil-water-balance approach (Thornthwaite and Mather, 1955, 1957), calculated on a daily basis, to estimate potential recharge. These estimates can be imported into regional groundwater-flow models or other hydrologic assessments where accurate recharge estimates are necessary. Also, the gridded approach of the SWB model allows for potential recharge estimates to be re-scaled to match the resolution of the groundwater-flow model.

A primary feature of the SWB model is the use of the U.S. Department of Agriculture (USDA) Natural Resources Conservation Service (NRCS) curve number rainfall-runoff relation, also known as the curve number method (Cronshey and others, 1986). Beyond its simplicity and convenience, the curve number method is well established in hydrologic practice and has been used in numerous applications worldwide (Ponce and Hawkins, 1996). Only one unique parameter, the curve number (also known as the runoff curve number), is

4 Potential Groundwater Recharge for the State of Minnesota Using the Soil-Water-Balance Model, 1996–2010

necessary for each combination of land-use class and soil type. Most importantly, the curve number rainfall-runoff relations have been shown to perform reasonably well for the central United States (Hjelmfelt, 1991).

The SWB model uses a soil-water accounting method to calculate potential recharge for each grid cell in the model domain separately (Westenbroek and others, 2010). Computation of water-budget components relies on relations between surface runoff, land cover, hydrologic soil group, maximum soil-water capacity, ET estimates, and temperature. Within the soil-water-balance approach, potential recharge is calculated within each grid cell of the model domain based on the difference between sources (*precipitation*, *snowmelt*, *inflow*), sinks (*interception*, *outflow*, *ET*), and change in soil moisture ($\Delta\text{soil moisture}$) (equation 1):

$$\text{potential recharge} = (\text{precipitation} + \text{snowmelt} + \text{inflow}) - (\text{interception} + \text{outflow} + \text{ET}) - \Delta\text{soil moisture} \quad (1)$$

Each of the water-budget components in equation 1 is handled by one or more modules within the SWB model. For the potential sources, *precipitation* and *snowmelt* are described in the subsection “Meteorological Data (Precipitation, Temperature, and Snowmelt).” The *inflow* component (from adjacent cells) in the model was not included because surface routing was turned off based on the large grid size (1-km). Of the sinks, *ET* is handled by the model without user intervention, and only the Hargreaves-Samani ET method (Hargreaves and Samani, 1985) is available for simulations with spatially varying gridded data such as those used in the Minnesota SWB model. *Interception* is defined as the portion of precipitation intercepted by the plant canopy and lost to ET; it is controlled by user-defined values for each unique land-cover class in a lookup table. *Outflow* from each grid cell, also known as surface runoff, is calculated by the NRCS curve number rainfall-runoff relation (Cronshey and others, 1986). Additional theoretical and background details on *outflow* and the other hydrologic components are detailed in Westenbroek and others (2010).

Changes in soil moisture ($\Delta\text{soil moisture}$) are tabulated by the soil-water-balance methods published by Thornthwaite (1948) and Thornthwaite and Mather (1955, 1957) by using intermediary values. These changes in soil moisture are tabulated on a daily time step. The intermediary values important to understand for the Minnesota SWB model include precipitation (*P*) minus potential evapotranspiration (*PE*), also known as *P–PE*, and the accumulated potential water loss (APWL). The calculation of intermediary values of *P–PE* is the first step in calculating a new soil moisture value, where negative *P–PE* values represent potential water deficiencies in the soil moisture and positive *P–PE* values represent a potential water surplus in the soil moisture. The APWL is a running sum of the daily *P–PE* values when *P–PE* is negative, and represents the unsatisfied *PE* to which the soil has been subjected. During the first days in which *P–PE* is negative, soils typically yield water more easily than subsequent days. However, as

the APWL continues to increase, soil moisture is less readily given up. The process of yielding water from a soil profile is a nonlinear relation between soil moisture and APWL, and was described in detail by Thornthwaite and Mather (1957) in a series of tables. These Thornthwaite-Mather soil-water retention tables are incorporated into the SWB model code.

To calculate the new soil moisture value when *P–PE* is negative, the incorporated Thornthwaite-Mather soil-water retention table is used to match the current APWL to a soil moisture value. During days in which *P–PE* is positive, the *P–PE* term is added directly to the soil moisture value from the previous day. Until the soil moisture value reaches the maximum soil-water capacity, the Thornthwaite-Mather soil-water retention table is consulted to back-calculate an updated, reduced APWL value. Once the maximum soil-moisture capacity is exceeded, the soil-moisture value is capped at the maximum soil-water capacity value, the excess water beyond the capped maximum value becomes potential recharge and the APWL is reset to zero. In some cases, if the potential recharge exceeds a user-defined maximum recharge rate, any excess potential recharge beyond the maximum recharge rate is converted to “rejected recharge” and is removed from further consideration.

Precipitation within the SWB model is tracked on a daily basis, and the model determines whether it falls as rain or snow. If precipitation falls on a day when the daily mean air temperature minus one-third the difference between the daily maximum and minimum air temperature is less than or equal to the freezing point of water, the precipitation falls as snow (Dripps, 2003). Snowmelt computed by the model is based on a temperature-index method (Dripps and Bradbury, 2007) as follows: 1.5 millimeters (mm; 0.059 inch [in.]) of snow (expressed as snow water equivalent) is assumed to melt per day for every degree Celsius that the daily maximum air temperature is above the freezing point of water.

The SWB model uses soil and land-cover information to calculate a maximum soil-water capacity for each grid cell. The maximum soil-water capacity is roughly equivalent to field capacity, which is the soil water held after excess gravitational water has drained away (Veihmeyer and Hendrickson, 1931). The maximum soil-water capacity is calculated as follows:

$$\text{maximum soil-water capacity} = \text{available soil-water capacity} \times \text{root-zone depth} \quad (2)$$

where *available soil-water capacity* is the amount of water available for withdrawal by plants in inches of water per foot; *root-zone depth* has units of feet; and the final *maximum soil-water capacity* for each grid cell has units of inches, which is the maximum amount of soil-water storage that can take place in a grid cell.

The SWB model output is only limited by the resolution of the climatological data and available land-cover and soil-cover data layers. The model is capable of generating output at daily, monthly, or annual intervals for any of the

subcomponents, including (1) gross precipitation, (2) temperature (minimum, maximum, mean), (3) interception, (4) surface runoff, and (5) ET (actual, reference).

Model Limitations and Assumptions

A full understanding of model limitations and assumptions is necessary to better evaluate the performance of any hydrologic model. The SWB model was originally developed to allow for recharge calculations based on readily available data and standardized parameters (Dripps, 2003). With a similar purpose, the Minnesota SWB model described in this report is intended to serve as a resource for watershed planners and groundwater modelers to obtain potential recharge estimates for an area of interest as well as the possible ranges for potential recharge estimates over time. For this purpose, the 15-year mean annual potential recharge estimate (that is, the mean for the 15-year period 1996–2010) is the most reliable estimate, and the annual mean potential recharge estimates (that is, the means for individual years from 1996 through 2010) indicate the possible range over time.

For the SWB conceptual model used in this study, the base-flow component from the hydrograph separation technique is assumed to be correct, even though this base-flow estimate is a simulated result. For these comparisons all of the SWB potential recharge is assumed to become base flow to the respective gaged watershed. All groundwater exchange between the surficial aquifer and deep aquifers is assumed to be at steady state. Finally, it is assumed that the watershed boundaries of the gaged surface-water bodies coincide with the aquifer watersheds (that is, the areas contributing recharge to the aquifer), even though it is well understood these boundaries do not always coincide (Kanivetsky, 1979). Although these assumptions likely fail in some cases, this technique for validating recharge estimates has been used in many other recharge estimates (for example, Delin and others, 2007; Hart and others, 2008; Healy and Scanlon, 2010) and is an adequate approximation for the purposes of this modeling effort.

The SWB model is a difference model, so any errors in the various hydrologic components (for example, precipitation, snowmelt, outflow, and ET) will be superimposed on the potential recharge error. Errors from the original sources, such as precipitation or temperature (relating to snowmelt and ET), are difficult to quantify; thus, assigning reasonable uncertainty to the potential recharge estimate is challenging. Furthermore, current modeling capabilities are imprecise because recharge rates cannot be directly measured and instead multiple indirect methods need to be used to estimate recharge, all of which have associated errors (Healy and Scanlon, 2010). It is assumed that these errors are small and that these errors will not be as important once scaled up to generate annual potential recharge estimates.

In regards to the potential recharge estimates, it is assumed that the potential recharge eventually becomes actual recharge. Because the path or distance to the water table is

not known, the SWB model only represents water leaving the root zone, so it does not take into account lateral movement of water that discharges to nearby surface water bodies before reaching the water table. Most of the major water-table aquifers in Minnesota are unconfined and reasonably close to land surface (for example, outwash, alluvium, and sandy lake deposits). Therefore, the issues related to actual recharge are probably not as important (Kanivetsky, 1979) as for aquifers in other parts of the country, such as the western United States, where depths to the water table can be hundreds of feet.

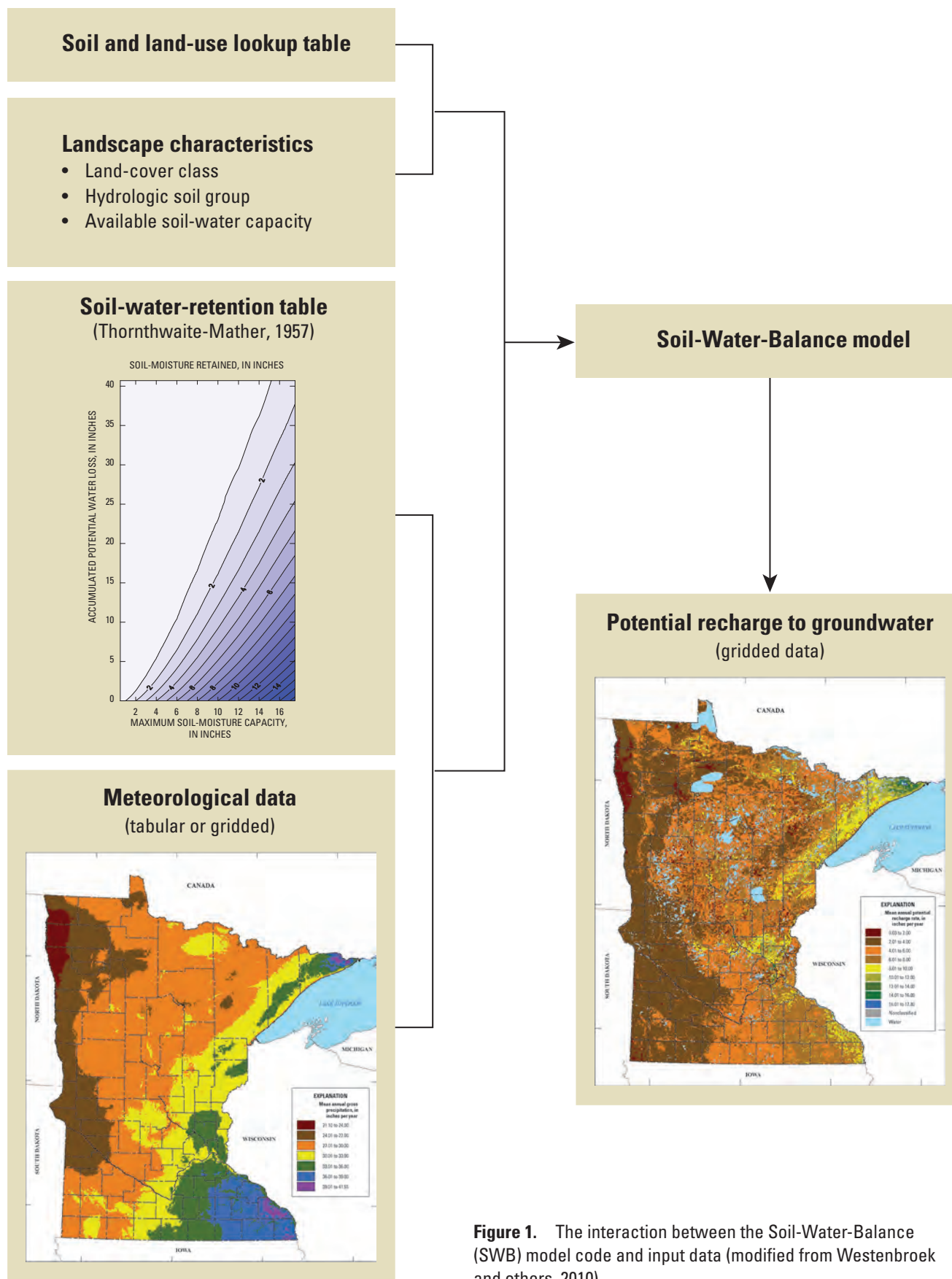
Lag time also is not accounted for in the SWB model. Recharge in the model is assumed to be instantaneous within the daily time step, whereas actual recharge can take months or even years. Even if the recharge reaches the water table in days to weeks, it can take a much longer period of time for the same recharge water to become base flow in the nearest stream. Because of the lag-time issue, the 15-year mean annual potential recharge estimate (that is, the mean for the 15-year period 1996–2010) is more reliable than the annual potential recharge estimates (that is, the means for individual years from 1996 through 2010), which should be used only as a guide for the range of potential recharge values.

Theoretical limitations to the SWB model relate to the aggregation of meteorological data to daily time steps. Precipitation is aggregated to the daily time step to limit the model run time, and the daily time step generally is the smallest time step available in large meteorological datasets. However, it is known that for an equal amount of precipitation, surface runoff will differ between a 30-minute storm event and a steady rainfall event lasting several hours; in this case, the SWB model cannot distinguish between the two events based on the daily time step. The accuracy of snowmelt timing also will suffer due to the same limitation, because snowmelt is triggered by air temperatures and snow will not always melt at the same rate. With the exception of groundwater-flow models for small areas, daily time steps are considered reasonable and are recommended for water-budget tabulations (Healy and Scanlon, 2010).

Model Description and Inputs

The SWB model consists of a 1-km grid spacing of 572 rows and 656 columns. The model boundaries are limited to the Minnesota State boundaries, resulting in an irregularly shaped area of approximately 219,000 cells.

This soil-water-balance application using the SWB model consists of the following gridded datasets to calculate recharge on a cell-by-cell basis, as detailed in Westenbroek and others (2010) and illustrated in figure 1: (1) meteorological data (daily precipitation in inches, daily maximum air temperature, daily minimum air temperature), (2) land-cover class, (3) hydrologic soil group, and (4) available soil-water capacity.



An optional grid for surface-water flow direction was not included as part of the Minnesota SWB application. This grid routes overland flow between cells, which is not pertinent at a 1-km resolution. The lookup tables for (1) soil and land cover and (2) soil-water retention lookup tables are necessary for the SWB code to run. Details of these two lookup tables are given in the “Lookup Tables and Control File” section.

Meteorological Data (Precipitation, Temperature, and Snowmelt)

All of the potential recharge estimates presented in this report were based on climatological data from the Daymet database (Thornton and others, 2012). This dataset is produced by interpolating available ground observation data with an inverse-distance weighting technique (Thornton and others, 2012). The Daymet data provided daily continuous surfaces of key climatological data, including precipitation and daily minimum/maximum air temperature, which have been broadly applied in hydrological and terrestrial vegetation growth models (Thornton and others, 1997). The Daymet data in Minnesota are based on source data from the Cooperative Summary of the Day network of weather stations, archived and distributed from the National Oceanic and Atmospheric Administration (NOAA) National Climatic Data Center (NCDC).

Mean annual gross precipitation (in inches per year) for 1996–2010 at a 1-km resolution is shown in figure 2. Generally, precipitation is lowest in the northwest and can be as much as 41 inches per year (in/yr) in the northeastern and southeastern parts of the State. The rates in northwest Minnesota are about 21 in/yr, or about one-half of the highest precipitation rates.

Land Cover

Land-cover data for 1994–2003 were obtained from the 2001 National Land Cover Database (NLCD) (Homer and others, 2007), available from the Multi-Resolution Land Characteristics Consortium. Land cover data for 2004–10 were obtained from the 2006 NLCD classification (Fry and others, 2011). For the NLCD-2001 and NLCD-2006 datasets the land-cover classification consists of 16 classes at a 30-meter (98-foot) spatial resolution. Fifteen of the 16 land-cover classes are found in Minnesota (table 1). However, three classes account for 67 percent of the land cover in NLCD-2006 (fig. 3): deciduous forest (15.5 percent), cultivated crops (39.0 percent), and woody wetlands (12.7 percent). For comparison, land-cover distributions from NLCD-2001 also are shown in table 1 with only minor differences in all of the 15 classes. For compatible usage with the SWB model, NLCD grids (2001, 2006) were resampled to a 1-km grid size using a majority resampling technique available in Esri ArcMap 10.1 (Esri, 2012) and processed into an American Standard Code for Information Interchange (ASCII) data grid.

Hydrologic Soil Groups

The USDA NRCS has classified more than 14,000 series of soils within the United States into one of four major hydrologic soil groups, which are assigned a letter designation (A–D) based on infiltration capacity. This classification describes soils with similar physical and runoff characteristics, focused specifically on the infiltration capacity of the soil. Soils in group A have a high infiltration capacity, and, consequently a low overland flow potential (Cronshey and others, 1986). In contrast, soils in group D have a very low infiltration capacity, and, consequently a high overland flow potential. As defined by Westenbroek and others (2010), soil group A soils have infiltration rates greater than ($>$) 0.30 inch per hour (in/h), and soil group D soils have infiltration rates less than ($<$) 0.05 in/h. Soils in groups B and C have intermediate infiltration capacities from group A and D.

Hydrologic soil group data used in the SWB model were obtained from two separate soil geographic databases, distributed by and available for download from the USDA NRCS (Natural Resources Conservation Service, 2014): (1) the Soil Survey Geographic (SSURGO) database and (2) the State Soil Geographic (STATSGO) database. Both databases are available as georeferenced digital map data and as a relational database. The SSURGO database provides more detailed information than the STATSGO database, so the SSURGO database was used wherever data were available and STATSGO was used to fill in the missing areas. Presently (2014), the SSURGO database has been completed for most of Minnesota except for parts of northeast Minnesota (missing all or part of Cook, Lake, St. Louis, and Pine Counties) and Crow Wing County in north-central Minnesota.

In order to prepare the hydrologic soils group grid, the SSURGO georeferenced digital maps (available at the county scale) were merged with the STATSGO georeferenced digital map that covered the parts of the State not covered by the SSURGO database. This merged digital map was converted to a 1-km grid using the Esri ArcMap 10.1 polygon to raster tool (Esri, 2012), using the maximum combined area option for the cell assignment type (fig. 4). In some cases, the assigned soil group is listed as A/D, B/D, or C/D in the databases; the first letter is for the drained condition and the second letter is for the natural condition (Natural Resources Conservation Service, 2005). In these cases, the soil group was truncated to the soil group A (for A/D), soil group B (for B/D), or soil group C (for C/D), given that these soils were generally classified in parts of the State with extensive artificial drainage and in most cases would fall into the drained condition. Next, the hydrologic soil groups (A through D) were converted to a numerical code (1 through 4), and exported to an ASCII file.

A special class was created for this SWB application, listed with a numerical code 5 and shown in figure 4 as group “organic,” which generally denotes peat deposits. This unique class was created because of its ability to hold more water than the same volume of a mineral soil (that is, non-organic)

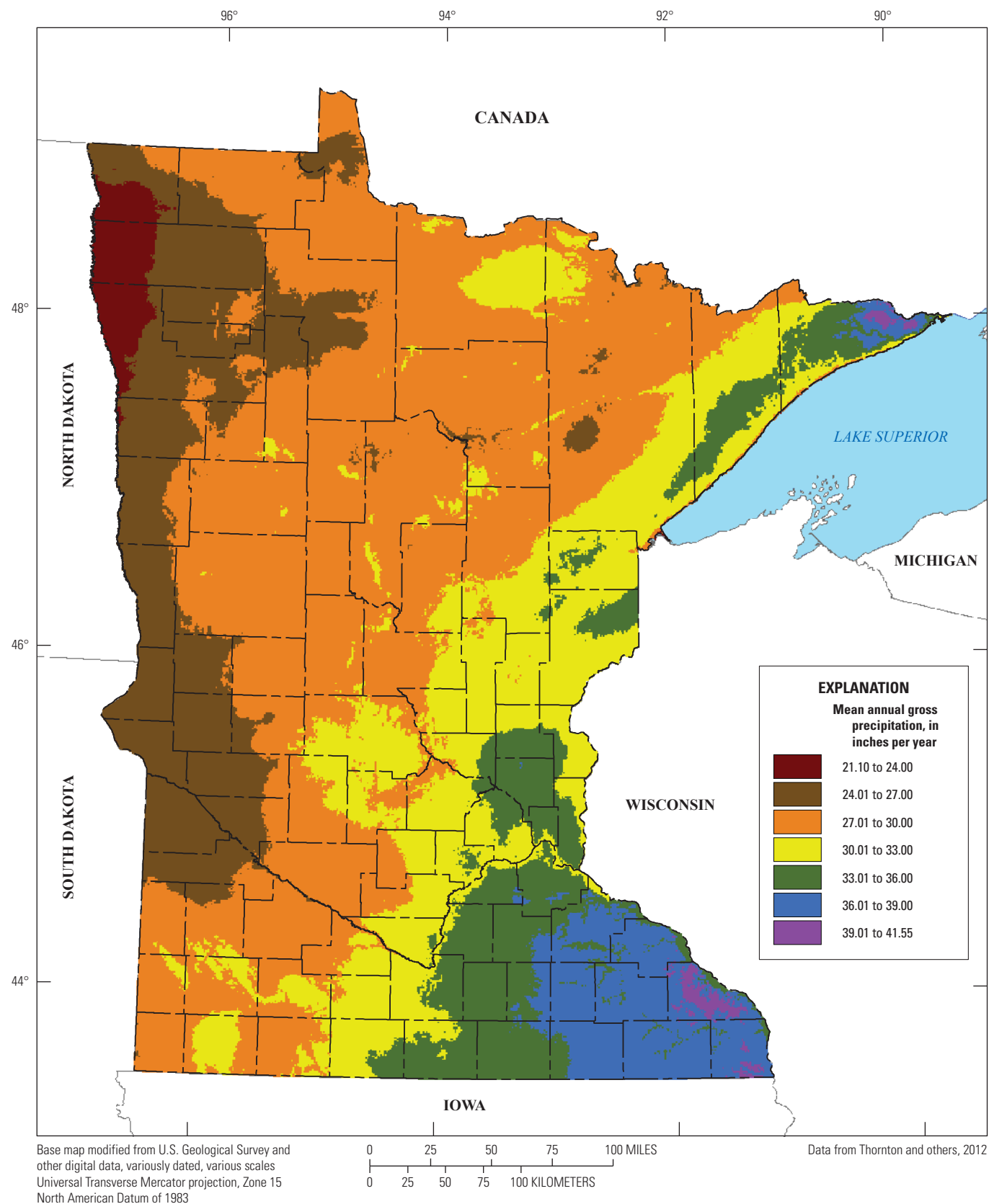


Figure 2. Mean annual gross precipitation in Minnesota at a 1-kilometer resolution, 1996–2010. (Mean gross precipitation rates were reconstructed from gridded datasets from the Soil-Water Balance model output, based on the Daymet climatological dataset [Thornton and others, 2012].)

Table 1. Distribution of land cover in Minnesota based on the 2001 National Land Cover Database (Homer and others, 2007) and the 2006 National Land Cover Database (Fry and others, 2011).

Land-cover class	Description	Land-cover distribution, in percent	
		National Land Cover Dataset, 2001	National Land Cover Dataset, 2006
11	Open water	6.1	6.2
21	Developed, open space	2.1	2.2
22	Developed, low intensity	1.0	1.0
23	Developed, medium intensity	0.3	0.4
24	Developed, high intensity	0.1	0.2
31	Barren land (rock/sand/clay)	0.1	0.1
41	Deciduous forest	15.5	15.4
42	Evergreen forest	3.0	2.9
43	Mixed forest	2.6	2.6
52	Shrubland	1.5	1.5
71	Grasslands	2.0	2.0
81	Pasture/hay	8.2	8.2
82	Cultivated crops	39.0	38.9
90	Woody wetlands	12.7	12.7
95	Herbaceous wetlands	5.6	5.7

(Natural Resources Conservation Service, 2008) that potentially would be underpredicted by the SSURGO available soil-water capacity. This special class was derived from the representative organic matter column within the horizon table, defined as the weight percentage of decomposed plant and animal residue in the <2-mm (<0.079-in.) soil material fraction. Based on a definition of organic soils from Donahue and others (1983), which classified soils with greater than 20 percent organic matter and between 0 and 50 percent clay as an organic soil, soils in this threshold were aggregated with the map unit key to the statewide digital map.

Two of the five hydrologic soil group classes account for 72.1 percent of the hydrologic soil groups (table 2): soil group B (41.3 percent) and soil group C (30.8 percent). Soil group B is the dominant hydrologic soil group across southern and western Minnesota, with soil group C as a secondary hydrologic soil group in the same regions in addition to northeastern Minnesota (fig. 4). The special organic group is found primarily in northern Minnesota, in conjunction with the expansive woody and emergent herbaceous wetlands located in that part of the State.

Available Soil-Water Capacity

The SWB model uses soil information, together with land-cover information, to calculate the maximum soil-water capacity and the available soil-water capacity. Soil-water capacity data were obtained similar to the hydrologic soil group data, whereby the SSURGO database was used wherever data were available and the STATSGO database was

used to fill in the missing areas. Both the available soil-water capacity and root-zone depth were extracted from the horizon table (in either the SSURGO or STATSGO database) and aggregated with the map unit key to the statewide digital map. For the available soil-water capacity, the weighted mean of the available soil-water capacity was calculated throughout the soil depth. Similar to the hydrologic soil group grid, the digital map for available soil-water capacity was converted to a 1-km grid using the Esri ArcMap 10.1 polygon to raster tool (Esri, 2012), using the maximum combined area option for the cell assignment type (fig. 5).

Lookup Tables and Control File

The SWB model uses two lookup tables to assign model cell properties related to soils and land cover: (1) the soil and land-cover lookup table and (2) the extended Thornthwaite-Mather soil-water retention table (Thornthwaite and Mather, 1957). The soil and land-cover lookup table cross-references the 15 land-cover classes in Minnesota to the 5 soil classes (4 hydrologic soil group classes plus the special organic soil class) to assign the curve number (Cronshey and others, 1986) (dimensionless number), the maximum recharge rate (inches per day), and the root-zone depth (feet). Additional information includes the interception storage values (inches), both for the growing season and the dormant season. Growing season is triggered by annual GDD exceeding 90 degrees-Fahrenheit-days when the model run is currently in the dormant season, and the dormant season is triggered by the minimum daily air temperature going below 28 degrees Fahrenheit (-2.2 degrees

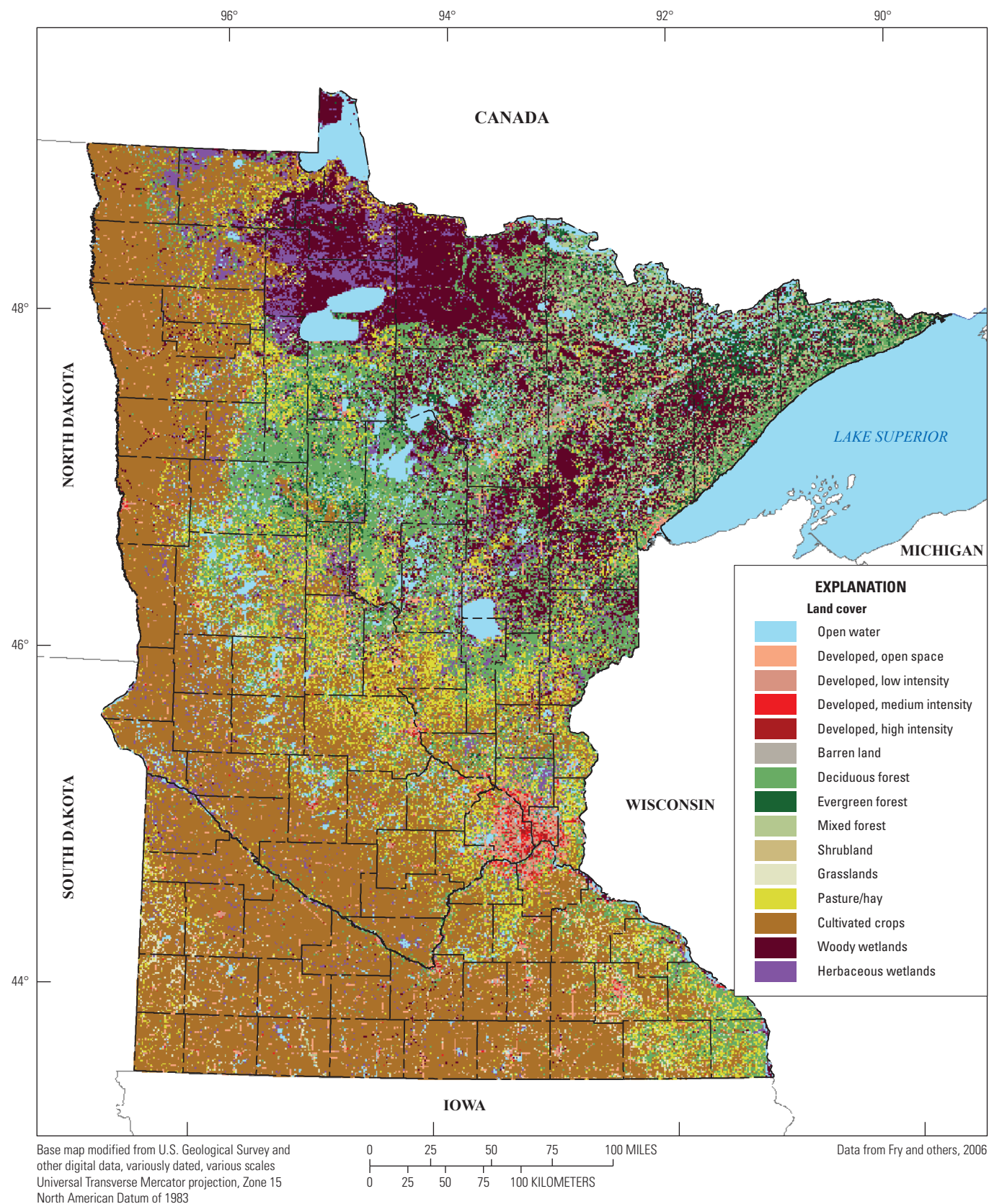


Figure 3. Land cover in Minnesota at a 1-kilometer resolution, from the 2006 National Land Cover Database (Fry and others, 2011).

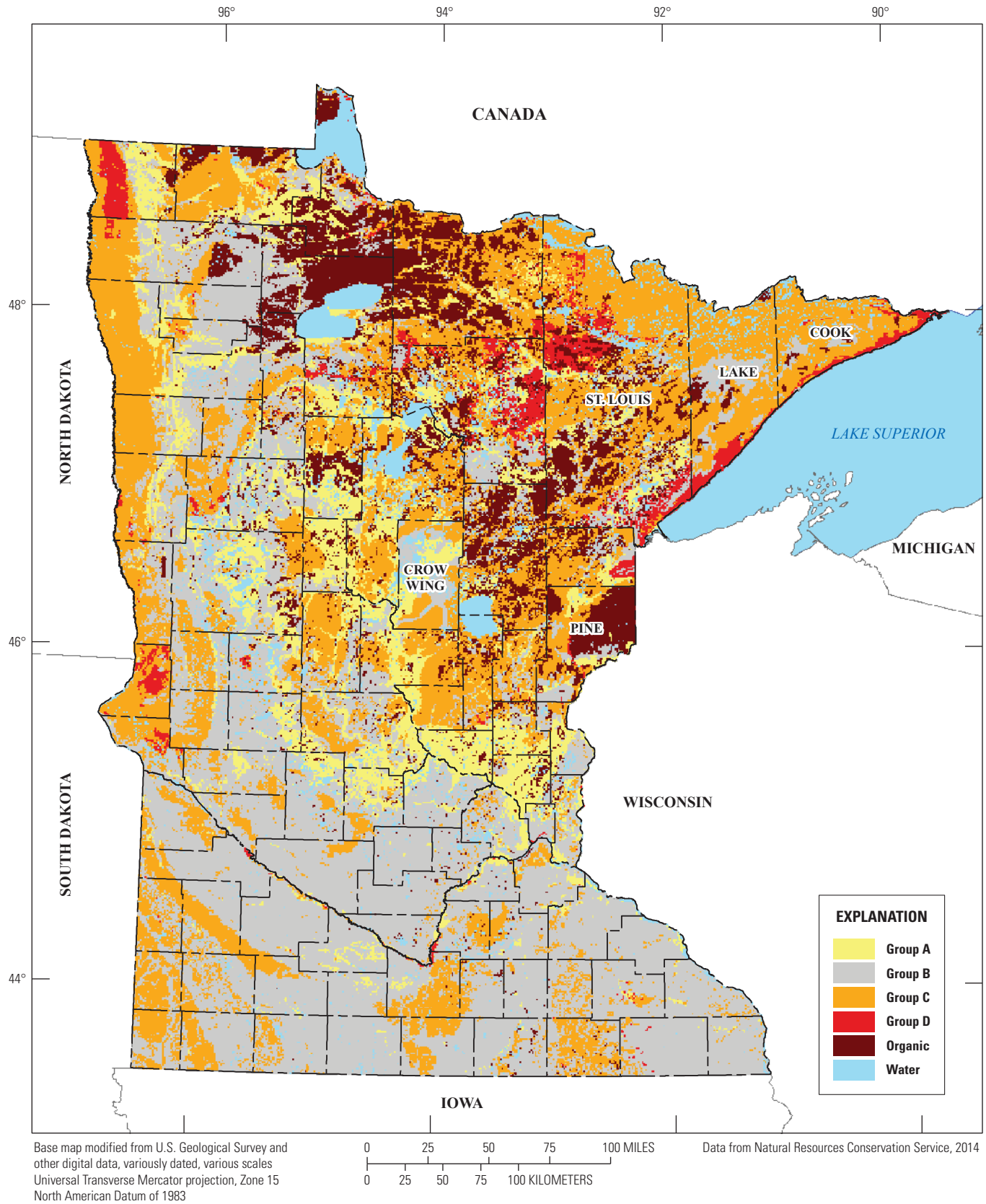


Figure 4. Hydrologic soil groups in Minnesota at a 1-kilometer resolution based on the merged Soil Survey Geographic (SSURGO) and the State Soil Geographic (STATSGO) databases (Natural Resources Conservation Service, 2014).

Table 2. Distribution of soils in Minnesota based on the Soil Survey Geographic (SSURGO) and the State Soil Geographic (STATSGO) databases (Natural Resources Conservation Service, 2014).

[Details on the designation of the organic soil group are provided in “Hydrologic Soil Groups” section.]

Hydrologic soil group	Percentage of total Minnesota area
A	13.0
B	41.3
C	30.8
D	3.0
Organic	11.9

Celsius) when the model run is currently in the growing season. The interception storage values only have a dependence on the NLCD land-cover class and do not have a dependence on the hydrologic soil group. The extended Thornthwaite-Mather soil-water retention table describes the ability of different soils to hold water (Thornthwaite and Mather, 1957). This table assists in the calculation of soil moisture adjustments during periods of unsatisfied potential ET.

The lookup table for the SWB model is presented in table 3. The primary calibration for the SWB potential recharge model mainly included adjustments to the soil and land-cover lookup table. Details on calibrating the final recharge model are included in the “Model Calibration” section. No adjustments to the extended Thornthwaite-Mather soil-water retention table were made.

The SWB control file handles all of the user-defined options on how each SWB simulation is run, such as the growing season length, model domain grid definition, the routing method, location of input files, and control over the SWB output. The control file for the SWB model is in appendix 1.

Model Calibration

Previous SWB model usage included alterations mainly within the soil and land-cover lookup table to attain a reasonable recharge grid (Hart and others, 2009; Hart and Schoephoester, 2011; Masterson and others, 2013; Stanton and others, 2011; Westenbroek and others, 2010). In some cases, comparisons against other simulated results were completed (Hart and others, 2008; Hart and Schoephoester, 2014; Metropolitan Council, 2013). The SWB model for estimating potential recharge in Minnesota described in this report advances SWB model usage beyond previous publications by reporting how well the simulated results fit against the base-flow component derived from three separate hydrograph separation techniques during model calibration. This added complexity provides an independent measure of model performance and the potential

uncertainty associated with the final reported potential recharge grid.

The first phase of the SWB model calibration was completed using the parameter estimation code PEST (Doherty, 2010), comparing the potential recharge estimates to base-flow estimates from the hydrograph separation program HYSEP using the local-minimum method (Sloto and Crouse, 1996) for 16 watersheds (table 4). Additional details of the first phase of model calibration using PEST are included in the “Parameter Estimation” subsection. After this initial parameter estimation effort, the potential recharge estimates were manually calibrated with the annual base-flow estimates for 35 watersheds (fig. 6) computed by 3 different hydrograph separation programs. Additional details of the manual calibration are included in the “Hydrograph Separation Comparisons” subsection.

Parameter Estimation

The first phase of model calibration included adjustments to the SWB model lookup table values of runoff curve number, maximum recharge rate (inches per day), and root-zone depth (feet) using the parameter estimation code PEST (Doherty, 2010). The PEST code was used to improve the match between the estimated potential recharge simulated by using the SWB model and the base-flow component of the hydrograph separation program HYSEP using the local-minimum method. Previously published SWB recharge models (Metropolitan Council, 2013; Westenbroek and others, 2010; Stanton and others, 2011; Masterson and others, 2013) were referred to for starting values for the lookup table. Additionally, table 2.2a–d from Cronshey and others (1986) was referred to throughout the calibration process for guidance on curve numbers; this table is a compilation of runoff curve numbers for different land-cover types, although not directly transferable to the NLCD classification.

The time-series process program TSPROC (Westenbroek and others, 2012) was used by the PEST code as a post-processor to generate the time series for comparison. The TSPROC program and PEST code were part of a composite model that contained multiple processing steps. The TSPROC program imported the streamflow data for a subset of the 35 USGS streamgages (U.S. Geological Survey, 2015), screened out periods with no streamflow data, separated base flow from total flow by using the HYSEP local-minimum technique, and converted the base flow to acre-feet per year. The subset of streamgages included only 16 of the 35 streamgages selected as part of the manual calibration process that is described in detail in the following subsection “Hydrograph Separation Comparisons,” and is identified in table 4. For the first model run, the TSPROC program created the PEST control and instruction files. Also as part of the composite model, the PAR2PAR preprocessor (part of the PEST suite of programs; Doherty, 2010) enforced relations between particular parameters to lower the overall total

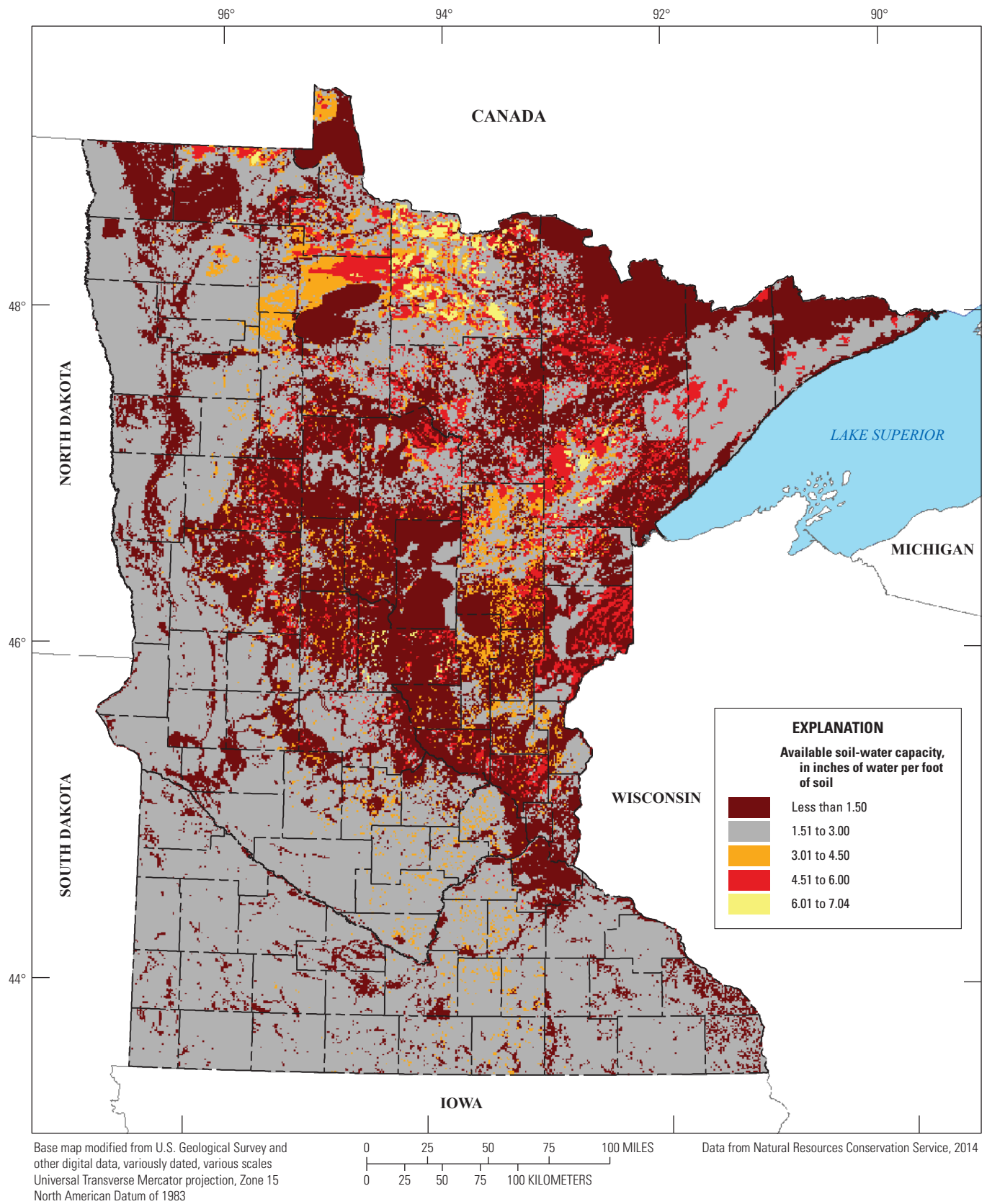


Figure 5. Available soil-water capacity in Minnesota at a 1-kilometer resolution based on the Geographic (SSURGO) and the State Soil Geographic (STATSGO) databases (Natural Resources Conservation Service Soil Survey, 2014).

Table 3. Lookup table for the Soil-Water-Balance (SWB) model, corresponding land cover to runoff curve number (by hydrologic soil group), maximum recharge rate (by hydrologic soil group), interception storage (growing season/dormant season), and root-zone depth (by hydrologic soil group).

[NA, not applicable; %, percent]

Land-cover class	Description	Assumed imperviousness	Runoff curve number					Maximum recharge rate (inches per day)					Interception storage (inches)		Root-zone depth (feet)				
			Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group	Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group	Growing season	Dormant season	Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group
11	Open water	NA	100	100	100	100	100	4.50	2.25	1.50	0.75	1.88	0.00	0.00	0.00	0.00	0.00	0.00	0.00
21	Developed, open space	NA	54	70	83	88	76	2.50	1.50	0.83	0.42	1.04	0.03	0.00	2.66	3.32	2.12	1.33	2.72
22	Developed, low intensity	30%	70	80	87	92	84	2.50	1.50	0.83	0.42	1.04	0.04	0.00	3.08	3.83	2.45	1.53	3.14
23	Developed, me- dium intensity	60%	82	90	95	97	93	2.50	1.50	0.83	0.42	1.04	0.04	0.00	3.08	3.83	2.45	1.53	3.14
24	Developed, high intensity	90%	89	92	94	97	93	2.50	1.50	0.83	0.42	1.04	0.04	0.00	3.08	3.83	2.45	1.53	3.14
31	Barren land (rock/sand/clay)	NA	90	93	95	96	94	6.00	3.50	2.75	2.00	3.13	0.06	0.00	1.00	1.00	1.00	1.00	1.00
41	Deciduous forest	NA	30	55	70	77	63	6.00	3.50	2.75	2.00	3.13	0.02	0.00	2.70	2.31	1.85	1.62	2.08
42	Evergreen forest	NA	36	60	73	79	67	6.00	3.50	2.75	2.00	3.13	0.02	0.02	3.16	2.65	2.12	1.85	2.39
43	Mixed forest	NA	33	58	72	78	65	6.00	3.50	2.75	2.00	3.13	0.02	0.02	2.93	2.48	1.99	1.74	2.24
52	Shrubland	NA	39	61	74	80	68	6.00	3.50	2.75	2.00	3.13	0.04	0.02	2.45	3.06	2.45	1.63	2.75
71	Grasslands	NA	39	61	74	80	68	6.00	3.50	2.75	2.00	3.13	0.04	0.02	2.24	2.80	2.24	1.49	2.51
81	Pasture/hay	NA	49	69	79	84	74	6.00	3.50	2.75	2.00	3.13	0.04	0.02	2.56	3.20	2.56	1.70	2.87
82	Cultivated crops	NA	67	78	85	89	82	6.00	3.50	2.75	2.00	3.13	0.04	0.00	2.12	1.93	1.89	1.35	1.91
90	Woody wetlands	NA	60	60	60	60	60	2.00	1.00	0.67	0.33	0.83	0.02	0.00	1.30	1.44	1.30	1.14	1.37
95	Herbaceous wetlands	NA	60	60	60	60	60	2.00	1.00	0.67	0.33	0.83	0.02	0.00	1.58	1.76	1.58	1.40	1.67

Table 4. Mean annual base-flow estimates from 1996–2010 using 3 hydrograph separation techniques for the watersheds of 35 streamgages used in model calibration in comparison to the estimated potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.

[USGS, U.S. Geological Survey; mi², square miles; in/yr, inches per year; SWB, Soil-Water-Balance; Minn., Minnesota; NA, not applicable]

Map number for watershed associated with streamgage (fig. 6)	USGS streamgage name or statistic	USGS streamgage number	Drainage area (mi ²)	PEST ^a calibra- tion	Manual calibration, period analyzed	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^d
						PART ^b (in/yr)	HYSEP fixed- interval method ^c	HYSEP sliding method ^c		
1	Knife River near Two Harbors, Minn.	04015330	84	Yes	1996–2010	7.33	7.58	7.50	8.40	0.12
2	Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	1,740	No	1996–2010	5.00	4.91	4.90	4.49	-0.09
3	Buffalo River near Dilworth, Minn.	05062000	975	No	1996–2010	3.47	3.27	3.33	4.05	0.20
4	Wild River River at Twin Valley, Minn.	05062500	934	Yes	1996–2010	4.34	4.12	4.14	4.35	0.03
5	Sand Hill River at Climax, Minn.	05069000	420	Yes	1996–2010	3.11	3.08	3.03	3.58	0.17
6	Red Lake River near Red Lake, Minn.	05074500	1,950	No	2000–2010	2.92	3.04	3.03	3.72	0.24
7	Thief River near Thief River Falls, Minn.	05076000	985	No	1996–1999, 2001–05, 2008–10	4.61	4.47	4.47	3.92	-0.13
8	Clearwater River at Plummer, Minn.	05078000	555	Yes	1996–2010	4.03	3.73	3.77	3.62	-0.06
9	Lost River at Oklee, Minn.	05078230	254	Yes	1996–2010	3.01	2.75	2.77	3.24	0.14
10	Middle River at Argyle, Minn.	05087500	255	Yes	1996–2010	3.09	2.68	2.76	3.43	0.21
11	South Branch Two Rivers at Lake Bronson, Minn.	05094000	422	No	1996–2010	3.59	3.50	3.48	3.93	0.12
12	Kawishiwi River near Winton, Minn.	05127000	1,230	No	1996–2010	7.16	7.41	7.41	7.68	0.05
13	Little Fork River at Littlefork, Minn.	05131500	1,680	Yes	1996–2010	6.07	5.47	5.47	5.33	-0.06
14	Big Fork River at Big Falls, Minn.	05132000	1,480	No	1998–2010	5.44	5.03	5.01	4.68	-0.09
15	Crow Wing River at Nimrod, Minn.	05244000	1,030	Yes	1996–2010	6.20	5.98	5.97	5.38	-0.11
16	Long Prairie River at Long Prairie, Minn.	05245100	434	Yes	1996–2010	5.23	4.99	4.99	4.22	-0.17
17	Sauk River near St. Cloud, Minn.	05270500	1,030	No	1996–2010	4.68	4.44	4.43	4.85	0.07
18	Elk River near Big Lake, Minn.	05275000	599	No	1996–2010	5.68	5.44	5.43	6.22	0.13
19	Rum River near St. Francis, Minn.	05286000	1,360	Yes	1996–2010	5.56	5.31	5.28	6.16	0.14
20	Elk Creek near Champlin, Minn.	05287890	86	No	1996–2010	4.89	4.75	4.72	4.80	0.00
21	Pomme de Terre River at Appleton, Minn.	05294000	905	No	1996–98, 2004–10	3.36	3.33	3.31	3.93	0.18
22	Chippewa River near Milan, Minn.	05304500	1,880	Yes	1996–2010	3.54	3.35	3.32	3.62	0.06
23	Yellow Medicine River near Granite Falls, Minn.	05313500	666	Yes	1996–2010	2.97	2.89	2.81	3.17	0.10

Table 4. Mean annual base-flow estimates from 1996–2010 using 3 hydrograph separation techniques for the watersheds of 35 streamgages used in model calibration in comparison to the estimated potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued[USGS, U.S. Geological Survey; mi², square miles; in/yr, inches per year; SWB, Soil-Water-Balance; Minn., Minnesota; NA, not applicable]

Map number for watershed associated with streamgage (fig. 6)	USGS streamgage name or statistic	USGS streamgage number	Drainage area (mi ²)	PEST ^a calibra- tion	Manual calibration, period analyzed	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^d
						PART ^b (in/yr)	HYSEP fixed- interval method ^c	HYSEP sliding method ^c		
24	Redwood River near Marshall, Minn.	05315000	259	Yes	1996–2010	3.94	3.49	3.51	3.67	0.01
25	Cottonwood River near New Ulm, Minn.	05317000	1,300	No	1996–2010	4.02	3.52	3.60	3.68	-0.01
26	Little Cottonwood River near Courtland, Minn.	05317200	170	No	1996–2009	4.40	4.35	4.38	3.58	-0.18
27	Watonwan River near Garden City, Minn.	05319500	851	No	1996–2010	4.92	4.76	4.70	4.00	-0.16
28	Le Sueur River near Rapidan, Minn.	05320500	1,110	Yes	1996–2010	6.04	5.26	5.32	4.99	-0.10
29	High Island Creek near Henderson, Minn.	05327000	238	No	1996–2010	4.41	4.44	4.42	3.98	-0.10
30	Kettle River below Sandstone, Minn.	05336700	868	Yes	1996–2010	7.48	6.82	6.91	6.92	-0.02
31	Snake River near Pine City, Minn.	05338500	974	Yes	1996–2010	6.64	6.47	6.49	5.44	-0.17
32	Vermillion River near Empire, Minn.	05345000	129	No	1996–2010	7.15	6.90	6.93	7.04	0.01
33	Cannon River at Welch, Minn.	05355200	1,340	No	1996–2010	7.01	6.31	6.38	6.05	-0.08
34	South Fork Zumbro River at Rochester, Minn.	05372995	303	No	1996–2010	7.17	6.63	6.57	6.57	-0.03
35	Cedar River near Austin, Minn.	05457000	399	No	1996–2010	7.28	6.83	6.82	6.14	-0.12
NA	Minimum	NA	84	NA	NA	2.92	2.68	2.76	3.17	-0.18
NA	Maximum	NA	1,950	NA	NA	7.48	7.58	7.50	8.40	0.24

^aDoherty (2010).^bRutledge (1998).^cSloto and Crouse (1996).^dThe relative error is the SWB potential recharge estimate to the mean of the three different base-flow estimates (equation 7).

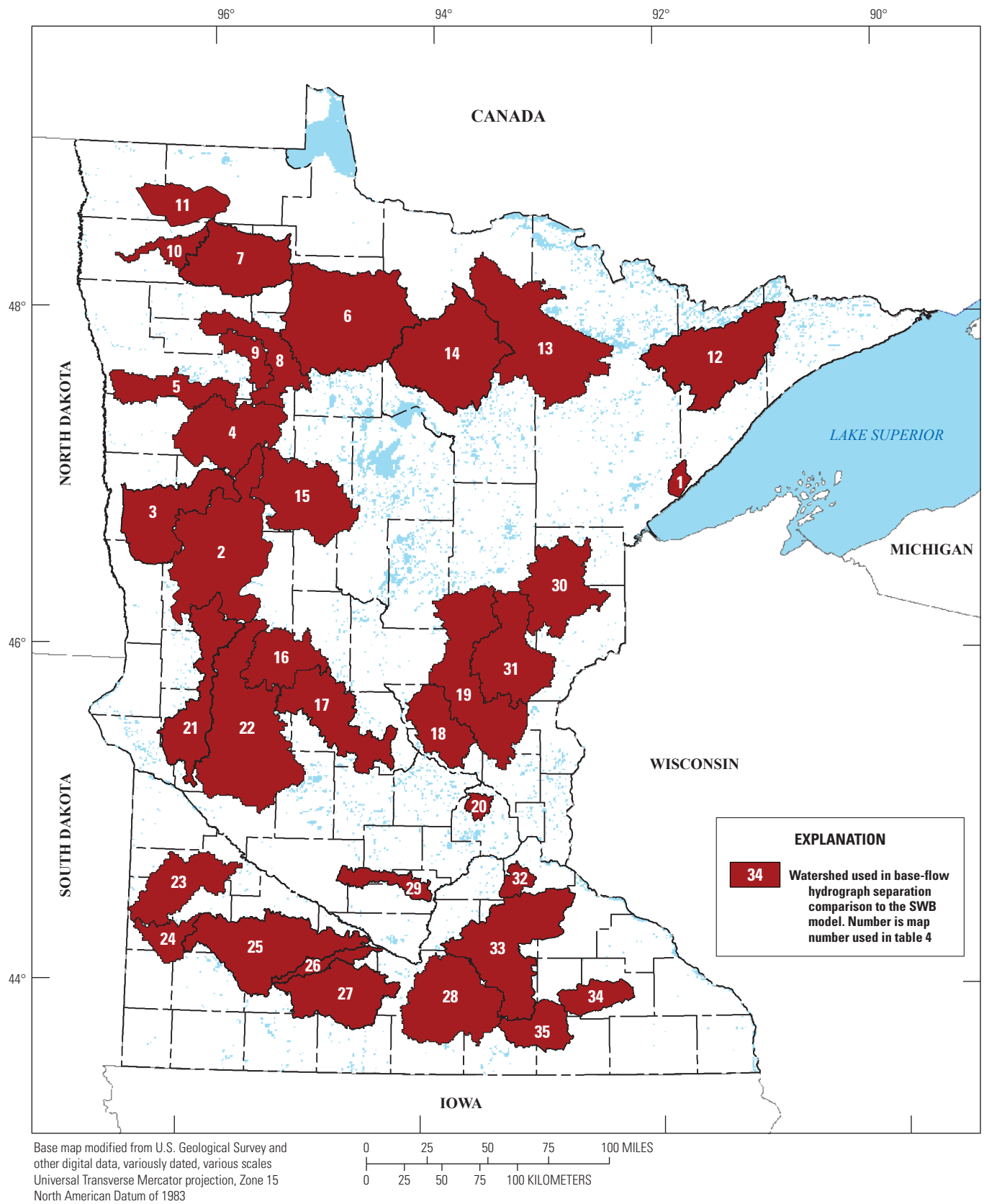


Figure 6. Watersheds with continuous streamflow data from 1996–2010 used for calibration of the Soil-Water-Balance (SWB) model.

of estimated parameters. For example, because runoff curve numbers increase from soil group A to soil group D, a relation calculated the runoff curve number for soil group C based on the estimated runoff curve number for soil group B. Likewise, similar relations were enforced by relating all other soil groups to soil group B, thereby reducing the number of parameters to be estimated from five to one. Because Minnesota has 15 different land-cover classes, a total of 75 combinations exist between land-cover classes and the 5 soil groups. By enforcing these relations, only 15 parameters needed to be estimated. Likewise, similar relations were enforced for root-zone depth and for particular land-cover types such as the four different types of urban land cover, further reducing the number of parameters to be estimated.

The PEST code was used to carry out parameter estimation by modifying the model parameters incrementally. For an individual iteration, a single model parameter was altered by an automatically adjusted percentage to determine if the new parameter value improved the difference between the simulated and measured (observed) values. An individual iteration consisted of running the SWB model for each of the 16 watersheds separately from 2000 to 2007. The new parameter value was retained if the overall objective function was reduced; for the SWB model, the objective function was the sum of squared deviations (also known as discrepancies) between the simulated values (the annual SWB potential recharge estimates in acre-feet per year) and the measured values (the base-flow estimated from the HYSEP local-minimum method in acre-feet per year) for all 16 watersheds. As part of the process, the various discrepancies can be weighted in different amounts to favor certain measured (observed) values, such as those with a smaller standard deviation. After completion of the individual SWB model runs for each watershed, the TSPROC program was called to generate the output files for comparison, a new objective function was calculated, and a new model parameter was adjusted. This parameter estimation cycle continued until PEST failed to lower the objective function over four iterations.

Overall, the parameter estimation process did not result in the final calibrated parameter values for the SWB model lookup table. Part of the challenge of the parameter estimation process was correctly assigning the weighting factors for the measured (observed) data. Also, because of the many parameters for estimation and the fact that different combinations of curve numbers and root-zone depths for the same land cover can yield the same results, leading to a non-unique solution, additional simulations using the SWB model were carried out through manual parameter adjustments.

Hydrograph Separation Comparisons

The second phase of the model calibration consisted of manually calibrating the potential recharge estimates by using the annual base-flow estimates for 35 watersheds. The annual base-flow estimates were generated by using three different hydrograph separation techniques using USGS groundwater

software (<http://water.usgs.gov/software/lists/groundwater>): PART (Rutledge, 1998), HYSEP fixed-interval method (Sloto and Crouse, 1996), and HYSEP sliding method (Sloto and Crouse, 1996). These three different hydrograph separation techniques were chosen to avoid a potential singular bias had only one hydrograph separation technique been used, providing a consensus approach among the three different hydrograph separation techniques for calibrating the model. All 35 watersheds selected (fig. 6) for the manual calibration process have at least 10 years of continuous streamflow data for the calibration period 1996–2010 (table 4) and combined, represent a similar distribution of land cover (table 5) as the State. The calibration watersheds range in size from 84 to 1,950 mi².

The goodness-of-fit between the 15-year mean annual potential recharge estimates from the SWB model and the 15-year mean annual base-flow estimates from the three different hydrograph separation techniques was considered during model calibration. The five quantities used to evaluate the goodness-of-fit were (1) the absolute mean error (AME), (2) the root mean square error (RMSE), (3) the Nash-Sutcliffe model efficiency coefficient (NSE), (4) the coefficient of determination (R^2), and (5) the relative error. The AME, computed by equation 3 for each of the 35 calibration watersheds, is a measure of the mean difference between the simulated (potential recharge estimate) and measured (hydrograph separation base-flow estimate) values:

$$AME = \frac{1}{n} \sum_{i=1}^n |P_i - O_i| \quad (3)$$

where n is the number of years of streamflow data at each streamgage, P_i is the predicted (simulated) value, and O_i is the observed value. For example, an AME of 1.0 in/yr for the SWB potential recharge estimate means that this predicted value is on average within 1.0 in/yr of the observed value. In this case, the observed estimate is the base-flow estimate from the hydrograph separation technique.

The RMSE indicates the amount of deviation between the simulated value and the measured value. The RMSE, computed by equation 4, yields the deviation between the simulated (potential recharge estimate) and measured (hydrograph separation base-flow estimate) values approximately 67 percent of the time:

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (P_i - O_i)^2} \quad (4)$$

The AME and RMSE were evaluated at two different spatial scales for each of the three hydrograph separation techniques: (1) the State as a single metric, shown as the overall mean of the AME and RMSE values for the 35 gaged watersheds (table 6); and (2) for each of the 35 individual gaged watersheds (table 6).

Table 5. Distribution of land cover in Minnesota for the 35 selected watersheds and for the State, based on the 2006 National Land Cover Database (Fry and others, 2011).

Land-cover class	Description	Land-cover distribution, in percent		Percent difference between selected watersheds and entire State
		35 Selected watersheds (table 4)	Entire State	
11	Open water	6.8	6.2	0.6
21	Developed, open space	2.0	2.2	-0.2
22	Developed, low intensity	0.6	1.0	-0.4
23	Developed, medium intensity	0.2	0.4	-0.2
24	Developed, high intensity	0.1	0.2	-0.1
31	Barren land (rock/sand/clay)	0.4	0.1	0.2
41	Deciduous forest	15.7	15.4	0.2
42	Evergreen forest	3.0	2.9	0.1
43	Mixed forest	2.0	2.6	-0.6
52	Shrubland	1.1	1.5	-0.4
71	Grasslands	2.0	2.0	0.0
81	Pasture/hay	9.5	8.2	1.3
82	Cultivated crops	39.5	38.9	0.6
90	Woody wetlands	11.4	12.7	-1.3
95	Herbaceous wetlands	5.7	5.7	0.1

The third statistical measure used for comparison, the NSE (Nash and Sutcliffe, 1970), was evaluated between the 15-year mean annual base-flow estimates from all three hydrograph separation techniques (PART, HYSEP fixed-interval method, and HYSEP sliding method) and the 15-year mean annual potential recharge estimates from the SWB model. The NSE is a commonly used estimate of the goodness-of-fit for hydrologic models (Legates and McCabe, 1999). Although commonly used for the evaluation of transient models, the NSE, in this case, can evaluate if the 15-year mean annual potential recharge estimates from the SWB model are better than the 15-year mean annual base-flow estimates for each of the three hydrograph separation techniques. The NSE was computed by equation 5:

$$NSE = 1 - \frac{\frac{1}{n} \sum_{i=1}^n (O_i - P_i)^2}{\frac{1}{n} \sum_{i=1}^n (O_i - \bar{O})^2} \quad (5)$$

where \bar{O} is the mean of the observed data. For the NSE, a value of 1 is considered a perfect match between the model simulations and observations, a value of 0 denotes that the

observed mean is as good as a predictor as the model simulations, and negative values for NSE indicate that the observed mean is a better predictor than the model. Although there was not an official threshold of acceptability for the SWB model, an NSE value >0.80 was assumed to be a good model fit.

The fourth statistical measure used was the coefficient of determination (R^2). Linear models were constructed comparing the 15-year mean annual base-flow estimate to the 15-year mean annual potential recharge estimate for each of the 35 watersheds. A linear model was constructed for each of the hydrograph separation base-flow estimates, with the goodness-of-fit evaluated by the coefficient of determination (R^2). The R^2 value was calculated with equation 6:

$$R^2 = \left\{ \frac{\sum_{i=1}^n (O_i - \bar{O})(P_i - \bar{P})}{\left[\sum_{i=1}^n (O_i - \bar{O})^2 \right]^{0.5} \left[\sum_{i=1}^n (P_i - \bar{P})^2 \right]^{0.5}} \right\}^2 \quad (6)$$

where \bar{P} is the mean of the predicted data. As with the NSE, an R^2 value of >0.80 for each linear model was assumed to be a good model fit.

Table 6. Absolute mean error (AME) and root mean square error (RMSE) between the annual mean potential recharge estimate from the Soil-Water-Balance (SWB) model and the annual mean base-flow estimates from the three hydrograph separation techniques for the overall calibration period (1996–2010) for 35 selected watersheds.

[USGS, U.S. Geological Survey; in/yr, inches per year; Minn., Minnesota; NA, not applicable]

Map number for watershed associated with streamgage (fig. 6)	USGS streamgage name or statistic	USGS streamgage number	AME (in/yr)			RMSE (in/yr)		
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b	PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b
1	Knife River near Two Harbors, Minn.	04015330	1.66	1.73	1.61	2.27	2.25	2.16
2	Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	1.48	1.43	1.43	1.67	1.63	1.62
3	Buffalo River near Dilworth, Minn.	05062000	1.14	1.31	1.24	1.41	1.62	1.56
4	Wild River River at Twin Valley, Minn.	05062500	1.63	1.71	1.70	1.80	1.93	1.90
5	Sand Hill River at Climax, Minn.	05069000	1.18	1.32	1.31	1.47	1.52	1.55
6	Red Lake River near Red Lake, Minn.	05074500	1.65	1.68	1.67	1.98	1.99	1.98
7	Thief River near Thief River Falls, Minn.	05076000	1.63	1.47	1.49	2.05	1.95	1.97
8	Clearwater River at Plummer, Minn.	05078000	1.21	1.21	1.17	1.43	1.47	1.46
9	Lost River at Oklee, Minn.	05078230	1.16	1.31	1.23	1.42	1.60	1.48
10	Middle River at Argyle, Minn.	05087500	1.39	1.74	1.59	1.88	2.21	2.11
11	South Branch Two Rivers at Lake Bronson, Minn.	05094000	1.85	1.77	1.76	2.29	2.15	2.18
12	Kawishiwi River near Winton, Minn.	05127000	1.90	1.93	1.97	2.23	2.36	2.36
13	Little Fork River at Littlefork, Minn.	05131500	1.34	1.20	1.16	1.77	1.54	1.52
14	Big Fork River at Big Falls, Minn.	05132000	1.39	1.15	1.16	1.54	1.35	1.34
15	Crow Wing River at Nimrod, Minn.	05244000	1.64	1.54	1.55	1.91	1.80	1.81
16	Long Prairie River at Long Prairie, Minn.	05245100	1.77	1.68	1.66	2.11	1.99	1.98
17	Sauk River near St. Cloud, Minn.	05270500	1.50	1.58	1.59	1.78	1.89	1.90
18	Elk River near Big Lake, Minn.	05275000	1.96	2.10	2.08	2.29	2.43	2.41
19	Rum River near St. Francis, Minn.	05286000	1.97	2.05	2.08	2.44	2.57	2.57
20	Elk Creek near Champlin, Minn.	05287890	1.76	1.88	1.83	2.11	2.16	2.13
21	Pomme de Terre River at Appleton, Minn.	05294000	1.09	1.07	1.08	1.32	1.33	1.33
22	Chippewa River near Milan, Minn.	05304500	1.39	1.41	1.39	1.75	1.83	1.82
23	Yellow Medicine River near Granite Falls, Minn.	05313500	1.34	1.23	1.22	1.62	1.52	1.51
24	Redwood River near Marshall, Minn.	05315000	1.39	1.30	1.32	1.57	1.51	1.53
25	Cottonwood River near New Ulm, Minn.	05317000	1.65	1.63	1.65	1.78	1.77	1.77
26	Little Cottonwood River near Courtland, Minn.	05317200	1.97	1.96	1.98	2.12	2.14	2.13
27	Watsonwan River near Garden City, Minn.	05319500	1.82	1.73	1.73	2.14	2.09	2.08
28	Le Sueur River near Rapidan, Minn.	05320500	1.61	1.25	1.20	1.71	1.49	1.39

Table 6. Absolute mean error (AME) and root mean square error (RMSE) between the annual mean potential recharge estimate from the Soil-Water-Balance (SWB) model and the annual mean base-flow estimates from the three hydrograph separation techniques for the overall calibration period (1996–2010) for 35 selected watersheds.—Continued

[USGS, U.S. Geological Survey; in/yr, inches per year; Minn., Minnesota; NA, not applicable]

Map number for watershed associated with streamgage (fig. 6)	USGS streamgage name or statistic	USGS streamgage number	AME (in/yr)			RMSE (in/yr)		
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b	PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b
29	High Island Creek near Henderson, Minn.	05327000	1.69	1.57	1.57	1.94	1.87	1.86
30	Kettle River below Sandstone, Minn.	05336700	2.09	1.86	1.93	2.35	2.17	2.24
31	Snake River near Pine City, Minn.	05338500	1.79	1.67	1.74	2.20	2.10	2.14
32	Vermillion River near Empire, Minn.	05345000	1.62	1.68	1.63	2.02	2.03	1.99
33	Cannon River at Welch, Minn.	05355200	1.51	1.25	1.27	1.77	1.60	1.63
34	South Fork Zumbro River at Rochester, Minn.	05372995	1.44	1.30	1.40	1.98	1.93	1.97
35	Cedar River near Austin, Minn.	05457000	1.49	1.39	1.35	1.79	1.63	1.61
NA	Overall mean	NA	1.57	1.54	1.54	1.88	1.87	1.86
NA	Minimum	NA	1.09	1.07	1.08	1.32	1.33	1.33
NA	Maximum	NA	2.09	2.10	2.08	2.44	2.57	2.57

^aRutledge (1998).

^bSloto and Crouse (1996).

In order to begin the second phase of the calibration process, the final lookup table values from the PEST-derived simulations were used as initial values for the manual calibration process. For an individual iteration, model parameters were altered to determine if the new set of parameter values improved the difference between the model simulations and observations. An individual iteration consisted of running the SWB model for each of the 35 watersheds separately from 1996–2010. After each iteration, the mean annual base-flow estimate (1996–2010) for each of the three hydrograph separation techniques and the mean annual potential recharge estimate (1996–2010) were calculated for all 35 watersheds. These means were used as inputs into the statistical measures for AME, RMSE, NSE, and R^2 . For the NSE and R^2 measures, the observed mean (\bar{O}) was the mean of all 35 mean annual base-flow estimates (1996–2010) and the predicted mean (\bar{P}) was the mean of all 35 mean annual potential recharge estimates (1996–2010).

This process was not as straightforward as reducing the objective function during the first phase. Instead, the following conditions were considered to determine if the new parameter set was retained: (1) decreased the differences between the SWB potential recharge and the base-flow estimates for the individual watersheds, as measured by AME and RMSE (table 6); (2) improved NSE values; and (3) improved R^2 values. With improvements in the fit, such as lower AME and RMSE values and higher NSE and R^2 values, these new parameter values were retained for succeeding calibration runs. These newly retained parameter values, particular in the case of curve numbers, were compared against previous curve number method applications, including those from other published SWB models, to determine if the values seemed reasonable (Westenbroek and others, 2010; Wehmeyer and others, 2011; Metropolitan Council, 2013). Considering the vast number of combinations possible in the lookup table, the same relations set earlier by using the PAR2PAR program (Doherty, 2010) and described previously in section “Parameter Estimation” were retained. To proceed in the calibration effort, individual watersheds with high AME/RMSE values were identified and evaluated for the largest overall land cover. Generally, a critical adjustment for a few selected lookup table parameters would improve the AME and RMSE values for these selected watersheds. Obviously, this approach would potentially cause other calibrated watersheds to become less calibrated; hence, this effort required many iterations to develop the final calibrated lookup table.

The final mean potential recharge rates for the model calibration in table 4 include all the 35 individual watersheds in addition to base-flow estimates calculated by using the hydrograph separation techniques of PART, HYSEP fixed-interval method, and HYSEP sliding method. Only slight differences in the overall range of mean annual base-flow values for the 15-year period exist among the three different hydrograph separation techniques, but some larger differences did exist for individual watersheds. Mean annual base-flow values from 1996–2010 ranged from 2.92 to 7.48 in/yr as calculated by PART, 2.68 to 7.58 in/yr as calculated by the HYSEP fixed-interval method, and 2.76 to 7.50 in/yr as calculated by the HYSEP sliding method (table 4). Annual mean base-flow values for individual years for the 35 selected watersheds from 1996–2010 ranged from 0.30 to 12.45 in/yr as calculated by PART, from 0.32 to 13.13 in/yr as calculated by the HYSEP fixed-interval method, and from 0.30 to 12.80 in/yr as calculated by the HYSEP sliding method (appendix 2, table 2–1). For the calibration procedure, it was assumed that the base flow estimated by the hydrograph separation techniques reflects long-term groundwater discharge attributable to recharge.

The relative error (dimensionless) of the potential recharge estimate from the SWB model for each watershed in table 4 was calculated by using equation 7:

$$\text{relative error} = \frac{\text{potential recharge} - (\text{mean, three base-flow estimates})}{\text{mean, three base-flow estimates}} \quad (7)$$

where *potential recharge* is the from the SWB model, in inches per year, and *mean, three base-flow estimates* is the mean of the three base-flow estimates determined by using hydrograph separation techniques, in inches per year. The relative errors for all 35 watersheds ranged from -0.18 to 0.24 (table 4), demonstrating a robust calibration given the number of watersheds, various watershed sizes, and the spatial extent across the State (fig. 6). Only 9 of the 35 watersheds had a relative error more than ± 0.15 .

The final AME and RMSE values for the calibration period (1996–2010) are summarized in table 6. This table lists the AME and RMSE values for each of the 35 individual watersheds for the three hydrograph separation techniques compared to the SWB potential recharge estimate, and also lists the overall mean AME and RMSE values. The range of values across the individual watersheds ranged from 1.07 to 2.10 in/yr for the AME and from 1.32 to 2.57 in/yr for the RMSE. The overall mean of the AME values was about 1.60 in/yr, and the overall mean of the RMSE values was about 1.90 in/yr for all three hydrograph separation base-flow estimates compared to the SWB potential recharge estimates. Although the AME and RMSE values do not have as much usefulness as a relative error, R^2 , or NSE for quickly evaluating the goodness-of-fit, the AME and RMSE values were a useful metric. For example, the AME and RMSE can give at least an indication of the uncertainty for the potential recharge estimates. Also, for different parts of Minnesota, the AME and RMSE values for the individual watersheds can provide additional guidance on the uncertainty of the potential recharge estimate.

The NSE between the 15-year mean annual base-flow estimates and the 15-year mean annual potential recharge estimate from the SWB model was greater than or equal to 0.80 for all three comparisons, which is greater than or equal to the threshold of acceptability for the model calibration (table 7). Another metric, the R^2 , was at least 0.80 for all three comparisons (fig. 7). The linear model slope also was >0.80 for all three comparisons with an intercept of approximately 0.60.

Table 7. Nash-Sutcliffe model efficiency coefficient (NSE) between annual mean base-flow estimates from three different hydrograph separation techniques and the annual mean potential recharge estimate from the Soil-Water-Balance (SWB) model.

Hydrograph separation technique	NSE
PART ^a	0.80
HYSEP fixed-interval method ^b	0.86
HYSEP sliding method ^b	0.86

^aRutledge (1998).

^bSloto and Crouse (1996).

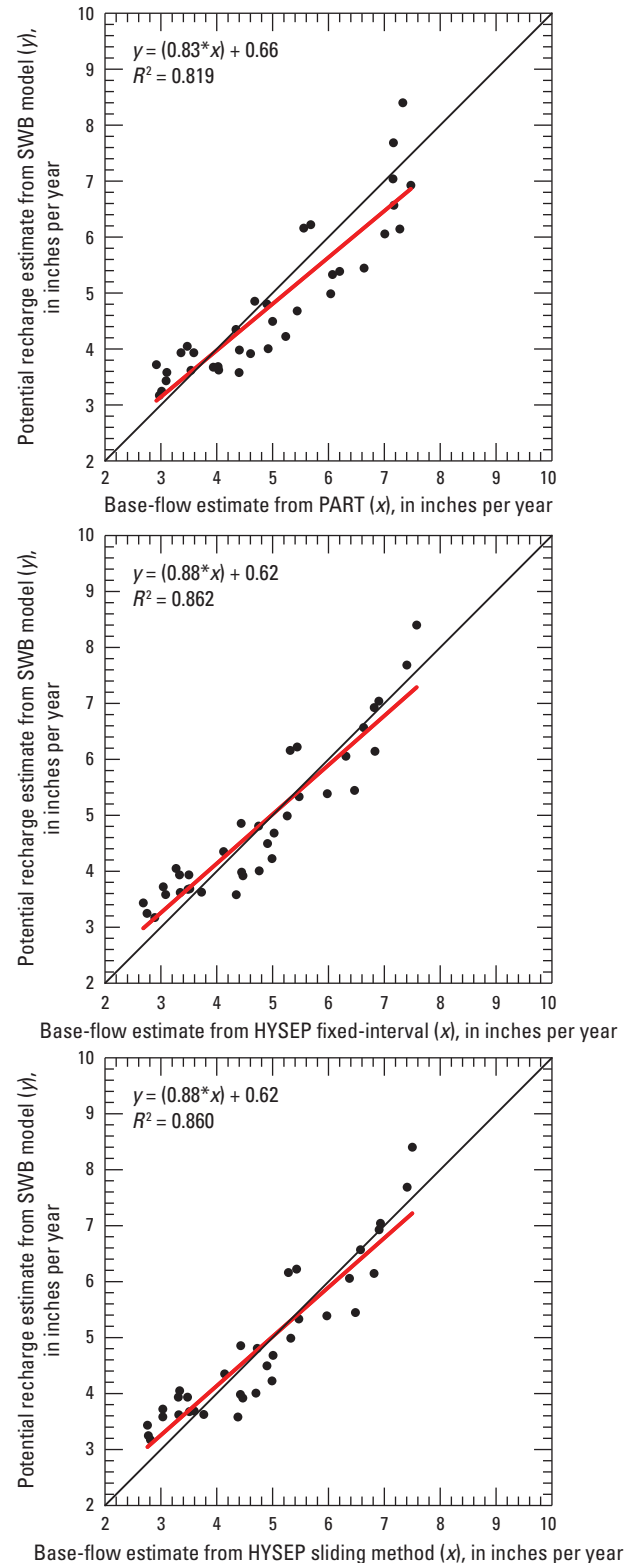


Figure 7. Relation between 15-year mean base-flow estimates from three different hydrograph separation techniques and the 15-year mean potential recharge estimates from the Soil-Water-Balance (SWB) model for 35 selected watersheds, along with linear trendline (in red), 1:1 line, linear model equation, and the coefficient of determination (R^2).

Potential Groundwater Recharge Estimates

Following calibration, the SWB model was run for the years 1996 through 2010 to simulate potential groundwater recharge rates for Minnesota, with the years 1994 to 1995 used to initialize soil-moisture values. Annual mean potential recharge estimates (that is, the means for individual years from 1996 through 2010) and 15-year mean annual potential recharge estimates (that is, the mean for the 15-year period 1996–2010) were determined for Minnesota based on the SWB model results.

Annual Mean Potential Recharge Estimates

As mentioned previously in the section “Model Limitations and Assumptions,” lag time was not accounted for in the SWB model; recharge was assumed as instantaneous within the daily time step. Also, as mentioned previously in that section, the 15-year mean annual potential recharge estimate (1996–2010) is the most reliable estimate (described in the next section, “Mean Annual Potential Recharge Estimates”) because of the lag-time issue with the annual potential recharge estimates. To further illustrate that the annual mean recharge estimates (that is, the means for individual years from 1996 through 2010) were not as suitable for usage as the 15-year mean annual potential recharge estimates for the overall period (fig. 7), the annual mean base-flow estimates from the three different hydrograph separation techniques (PART, HYSEP fixed-interval method, and HYSEP sliding method) were compared to the annual mean potential recharge estimates from the SWB model (fig. 8) for the 35 selected watersheds. Although the relation for the three comparisons was nearly linear, the R^2 values were between 0.526 and 0.533. Although the relations for the annual mean potential recharge estimates are not as strong as the relation for the overall period, the annual mean potential recharge maps are useful for comparing years with high recharge rates with years with low recharge rates. The recharge maps are presented as figures 3–1 (1996) through 3–15 (2010) in appendix 3.

Annual mean potential recharge rates had a much wider range, with maximum rates as high as 27.2 in/yr (appendix 3), in comparison to the maximum mean annual recharge rate of 17.8 in/yr for the overall period mean described in the next section, “Mean Annual Potential Recharge Estimates.” The highest annual mean recharge across the State was in 2010 (fig. 3–15), and the lowest mean recharge was in 2003 (fig. 3–8). Although precipitation variability partially explained the annual differences in potential recharge estimates, precipitation alone did not account for these differences, and other factors such as antecedent moisture conditions likely were important. Also, because differences in precipitation gradients across the State can vary from year to year, the dominant land cover and hydrologic soil group

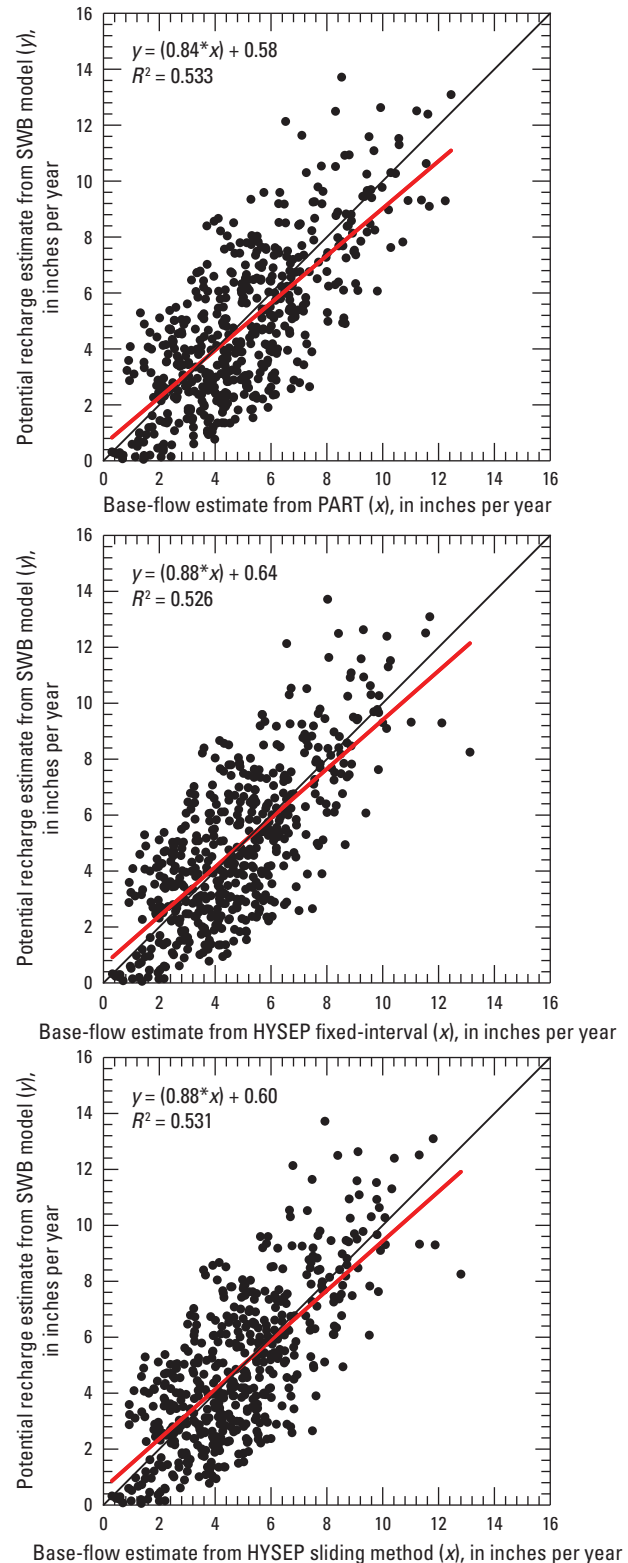


Figure 8. Relation between annual mean base-flow estimates from three different hydrograph separation techniques and the annual mean potential recharge estimates from the Soil-Water-Balance (SWB) model for 35 selected watersheds, along with linear trendline (in red), 1:1 line, linear model equation, and the coefficient of determination (R^2).

combinations for a particular region had a large effect on the resulting potential recharge value. During 1996–2010, April had the greatest mean monthly potential recharge compared to all other months, accounting for a mean of 30 percent of annual potential recharge in this single month.

Mean Annual Potential Recharge Estimates

The statewide 15-year mean annual potential recharge rate from 1996–2010 was 4.9 in/yr. The mean annual potential recharge estimates across Minnesota at a 1-km resolution for the simulation period ranged from <0.1 to 17.8 in/yr (fig. 9). Some of the lowest potential recharge rates for the simulation period (generally between 1.0 and 1.5 in/yr) were in the Red River of the North Basin of northwestern Minnesota (figs. 9 and 10). Not only is this the driest part of the State based on mean annual gross precipitation (fig. 2), but this area also has thick, clayey soils that are restrictive to infiltration as indicated by the high concentration of hydrologic soil groups C and D (fig. 4). The highest potential recharge rates were estimated in northeastern Minnesota and the Anoka Sand Plain (figs. 9 and 10). These were likely controlled by the high precipitation rates (fig. 2) and the low available soil-water capacity (fig. 5). Eighty-eight percent of the mean annual potential recharge rates (by grid cell) were between 2 and 8 in/yr from 1996–2010 (fig. 11). Only about 3 percent of all the potential recharge estimates (by grid cell) were less than 2 in/yr, and 9 percent were greater than 8 in/yr (fig. 11).

Overall, potential recharge rates increased from west to east across Minnesota, which was partially a reflection of the precipitation gradient (fig. 2). The mean annual potential recharge estimate from the SWB model was approximately 30 percent of the mean annual gross precipitation. The correlation is moderate between mean annual gross precipitation and the potential recharge estimates from the SWB model for the entire period for the 35 selected watersheds used for calibration, with an R^2 value of 0.512 (fig. 12). However, this R^2 value is weaker than those in the previous comparisons between the base-flow estimates from the hydrograph separation techniques and the potential recharge estimates from the SWB model (fig. 7), which were equal to or greater than an R^2 of 0.8. This indicates that other inputs to the SWB model, not just precipitation, were important in explaining potential recharge estimate variations across the State. For example,

potential recharge rates for most of the State were between 10 to 25 percent of the gross precipitation, with some areas with rates outside this range (fig. 13). The Anoka Sand Plain (fig. 10) and a large part of northeastern Minnesota had potential recharge rates that ranged from 25 to 40 percent of gross precipitation (fig. 13). The Anoka Sand Plain consists of porous sandy soils and most of the area was in hydrologic soil group A, which has a high infiltration capacity (Minnesota Department of Natural Resources, 1993). In northeastern Minnesota, land cover included a substantial amount of deciduous and mixed forests (fig. 3), in addition to having low available soil-water capacity (fig. 5). Conversely, northwestern Minnesota has recharge rates as low as 5 percent of gross precipitation. For the TCMA (fig. 10), potential recharge rates were more complex, ranging from <2.0 in/yr to greater than 15.0 in/yr. This wide variability reflects the various land-cover types in the TCMA, from developed, high-intensity land use to regional parks with expansive deciduous forest, open park space, and golf courses.

The total area of active cells in the Minnesota SWB model and the mean potential recharge estimates from 1996–2010 are shown in table 8 by land-cover class and hydrologic soil group. No potential recharge rate is given for the open water category, as recharge for open water cells was not considered by the SWB code. It was assumed that open water drains through surface-water features rather than recharging the underlying aquifers. The statewide area-weighted mean potential recharge ranged from 4.16 in/yr for cultivated crops to 6.93 in/yr for evergreen forests. Among urban category land-cover classes 21 through 24, land-cover class 23 (developed, medium intensity) had the highest potential recharge rate of 6.10 in/yr although less than 0.4 percent (784 km² of total 201,265 km²) of active cells were this land-cover class. The highest potential recharge estimates of all groups, where broken out by the different hydrologic soil groups, were urban land classes of 22 and 24 underlain by hydrologic soil group A; however, these groups had small land-cover areas. Pasture/hay (5.02 in/yr), woody wetlands (5.07 in/yr), and herbaceous wetlands (4.20 in/yr), along with cultivated crops, had some of the lowest potential recharge estimates compared to most of the other groups. Considering that these four land-cover classes dominated over the State (approximately 70 percent of the active model cells), the overall statewide mean annual recharge rate of 4.9 in/yr was not unexpected.

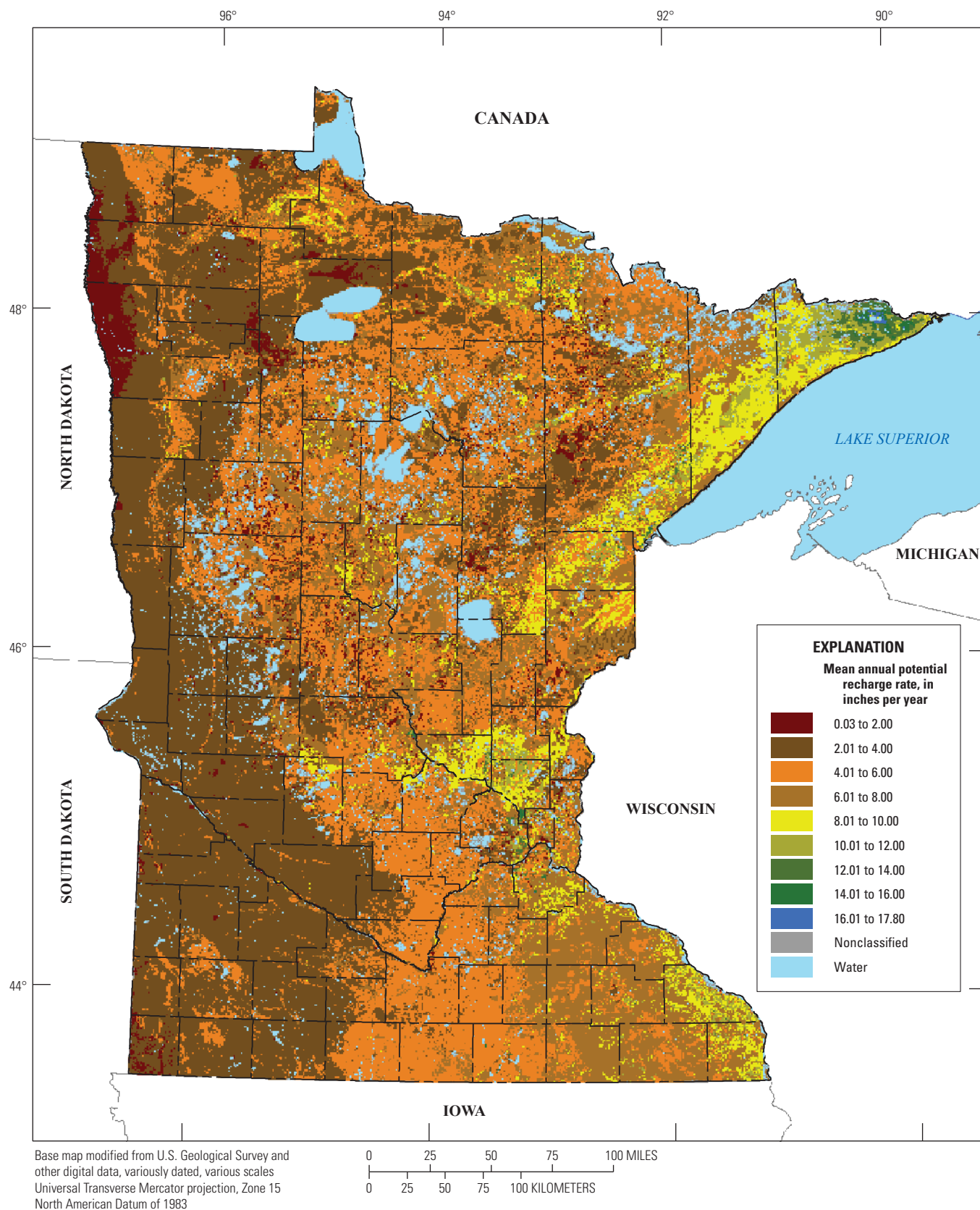


Figure 9. Mean annual potential recharge rates from 1996–2010 based on results from the Soil-Water-Balance (SWB) model for Minnesota.

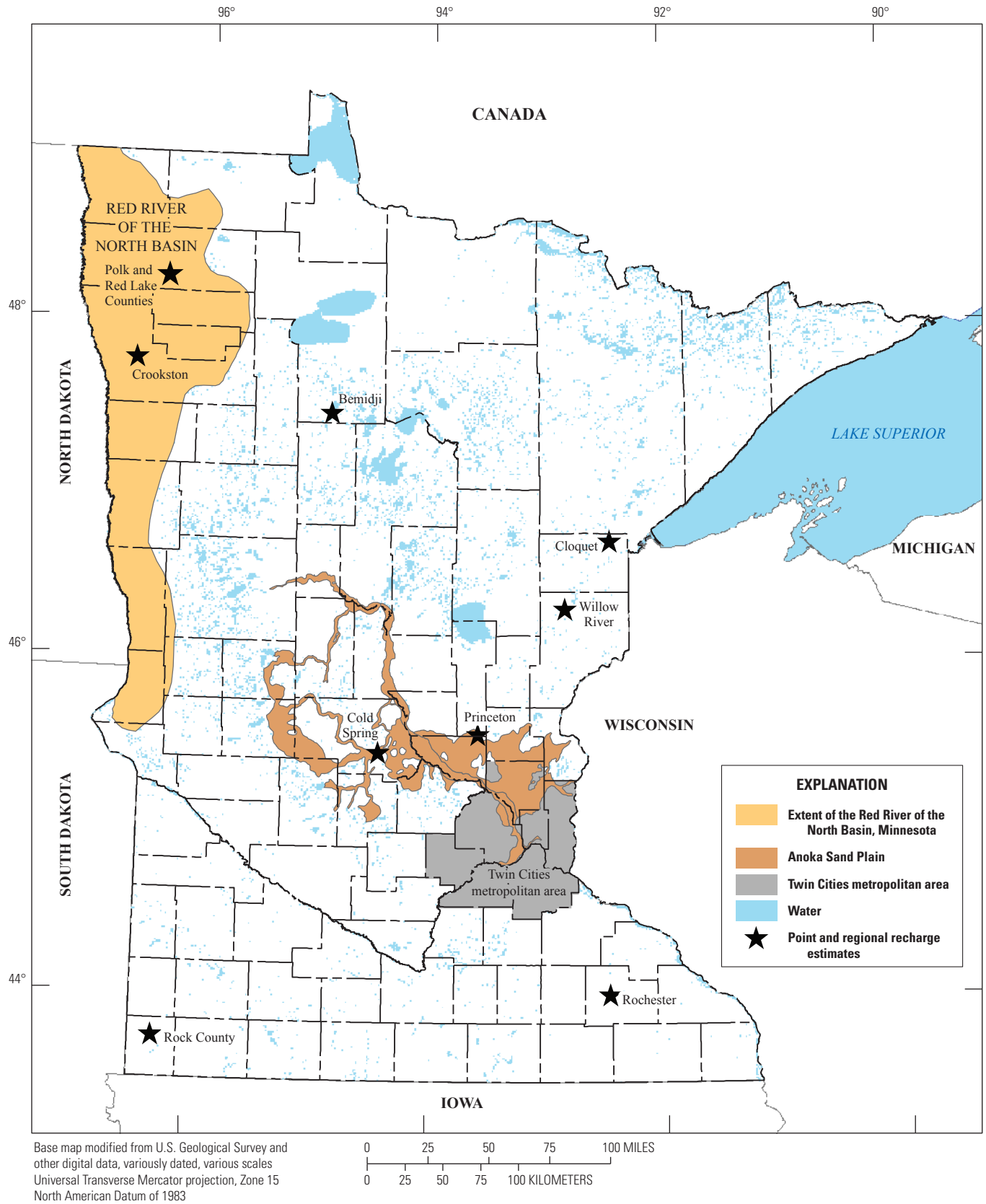


Figure 10. Locations of point and regional recharge estimates referred to in text and table 9.

Mean potential recharge rates by hydrologic soil group were a little more surprising. For example, the statewide area-weighted mean potential recharge rate for hydrologic soil group D, typically known for very slow infiltration rates (Cronshey and others, 1986), was greater than rates for hydrologic soil groups B and C. However, this result was not unreasonable given that the root-zone depths were shallower in this group and that much of the geographical extent of hydrologic soil group D was in northeastern Minnesota, where precipitation rates were the highest. Also, the predominant land-cover class in northeastern Minnesota was one of the three forest classes, all of which had high mean potential recharge rates.

The similarity in potential recharge rates between hydrologic soil groups B and C can be explained by the countering effects of the runoff curve number and the root-zone depths; the greater curve runoff numbers for soil group C soils were counterbalanced by the shallower root-zone depths (Thornthwaite and Mather, 1957) for soil group C soils. On the two ends of the spectrum, hydrologic soil group A had the highest overall potential recharge rate of 6.48 in/yr, and the organic hydrologic soil group had the lowest overall potential recharge rate of 3.57 in/yr. This low potential recharge rate for organic soils is likely due to the greater soil-water capacity of organic soils compared to non-organic soils.

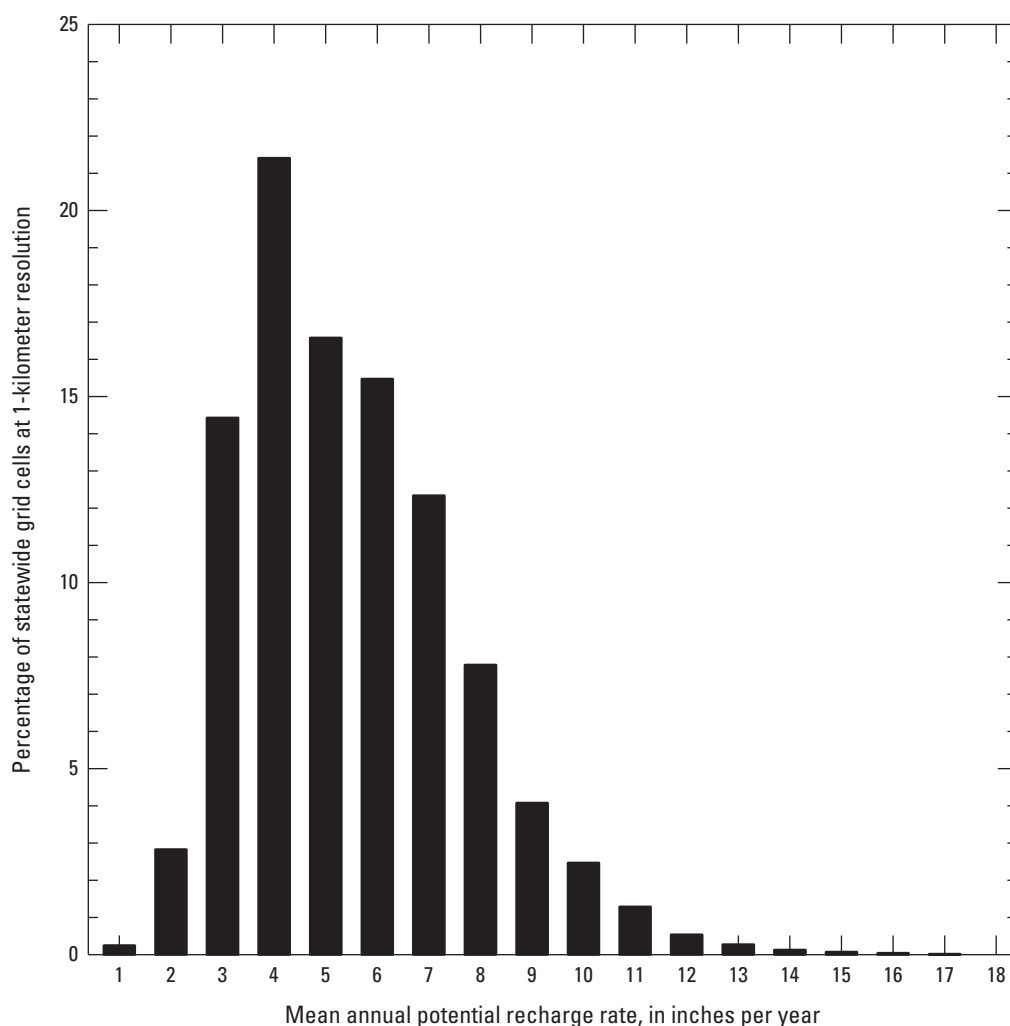


Figure 11. Histogram (by percent) of the mean annual potential recharge rates from the Soil-Water-Balance model from 1996–2010 for Minnesota.

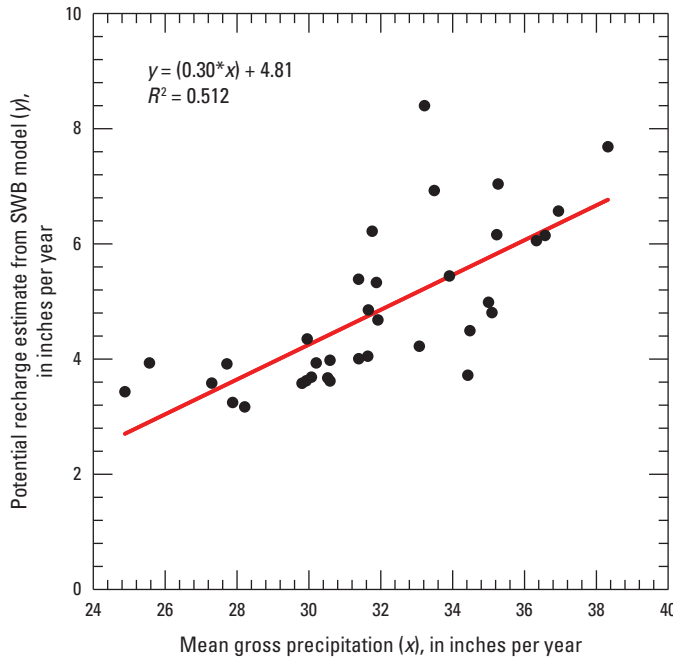


Figure 12. Relation between mean annual gross precipitation and the mean annual potential recharge estimates from the Soil-Water-Balance (SWB) model for the overall calibration period (1996–2010) for the 35 selected watersheds used for model calibration.

Comparison to the Regional Regression Recharge Model

As mentioned previously in the section “Previous Studies,” Delin and others (2007) produced mean recharge rates to surficial materials, from 1971 through 2000, for the State of Minnesota. Delin and others (2007) and Lorenz and Delin (2007) regionalized RORA watershed-scale recharge estimates (Rutledge, 1998) based on a regression model that incorporated soil and meteorological information in addition to mean annual precipitation. Soil information was incorporated in a specific yield estimate; specific yield can be related to soil texture and is a corollary to the usage of the hydrologic soil groups in the SWB model. Meteorological data were growing degree days (GDD) in lieu of an explicit calculation of ET. A statewide recharge map, similar to the map of potential recharge estimates from the SWB model shown in figure 9, was generated by applying the regression model, known as the regional regression recharge (RRR) model, to the State (appendix 4).

The RRR and SWB models only partially overlap temporally, as the RRR model was based on mean precipitation and GDD from 1971 through 2000. The best comparison would be to run both models for the same time period, but would require

redefining the RRR model for the same time period as the SWB model (or vice versa). However, a comparison between the two models is warranted given the substantial usage of the recharge estimates from the RRR model. To make this comparison, the polygon map of recharge estimates from the RRR model available from the Minnesota Department of Natural Resources (Minnesota Department of Natural Resources, 2007) was converted to a 1-km grid. A difference map was computed by subtracting the recharge estimates for the RRR model from the potential recharge estimates for the SWB model (fig. 14). This difference map shows that the recharge estimates generally were within 3 in/yr between the RRR model and SWB model. Few parts of the State had differences between the SWB model and RRR model that were >3.0 in/yr (that is, higher recharge rates from the SWB model than from the RRR model), with the exception of northeastern Minnesota. In contrast, approximately 59 percent of the total area, particularly in north-central and parts of northeastern Minnesota, had negative differences indicating that the RRR model estimated more recharge than did the SWB model for these areas. Of the total area with negative differences, 13 percent had a difference greater than 3 in/yr estimated for the RRR model compared to the SWB model. One potential explanation for some of the negative difference areas was that the available soil-water capacity for these areas commonly is higher (fig. 5), a factor not accounted for in the RRR model. This explanation is supported because much of the area with higher SWB recharge estimates in comparison to the RRR model had low available soil-water capacity. Another potential explanation was that although the GDD do account for a primary component of ET, the GDD are not as robust as the daily calculation of water-balance components (including potential and actual ET) in the SWB model. Finally, the land-cover class for much of the area where the estimated recharge was higher for the RRR model than the SWB model was one of the two wetland groups, both of which generally had lower mean potential recharge than other land-cover classes.

Comparison to Other Recharge Estimates

Potential recharge estimates from the SWB model also were compared to other point and regional recharge estimates (table 9). Several studies scattered across Minnesota that used either water-table fluctuation methods or a groundwater-flow model to estimate recharge rates are shown in table 9. In most cases, the potential recharge estimate from the SWB model was in the same range as the other recharge estimates. For example, Delin (1991) determined estimated recharge rates of 3.0 to 6.0 in/yr to the uppermost unit of the Prairie du Chien Group based on calibrated results of a three-dimensional groundwater-flow model. Recharge estimates reported for the same areal extent in the SWB model, covering an area north/northeast of Rochester, Minnesota, ranged from 1.7 to 7.4 in/yr. Other SWB potential recharge estimates generally were within the same range as previous recharge estimates

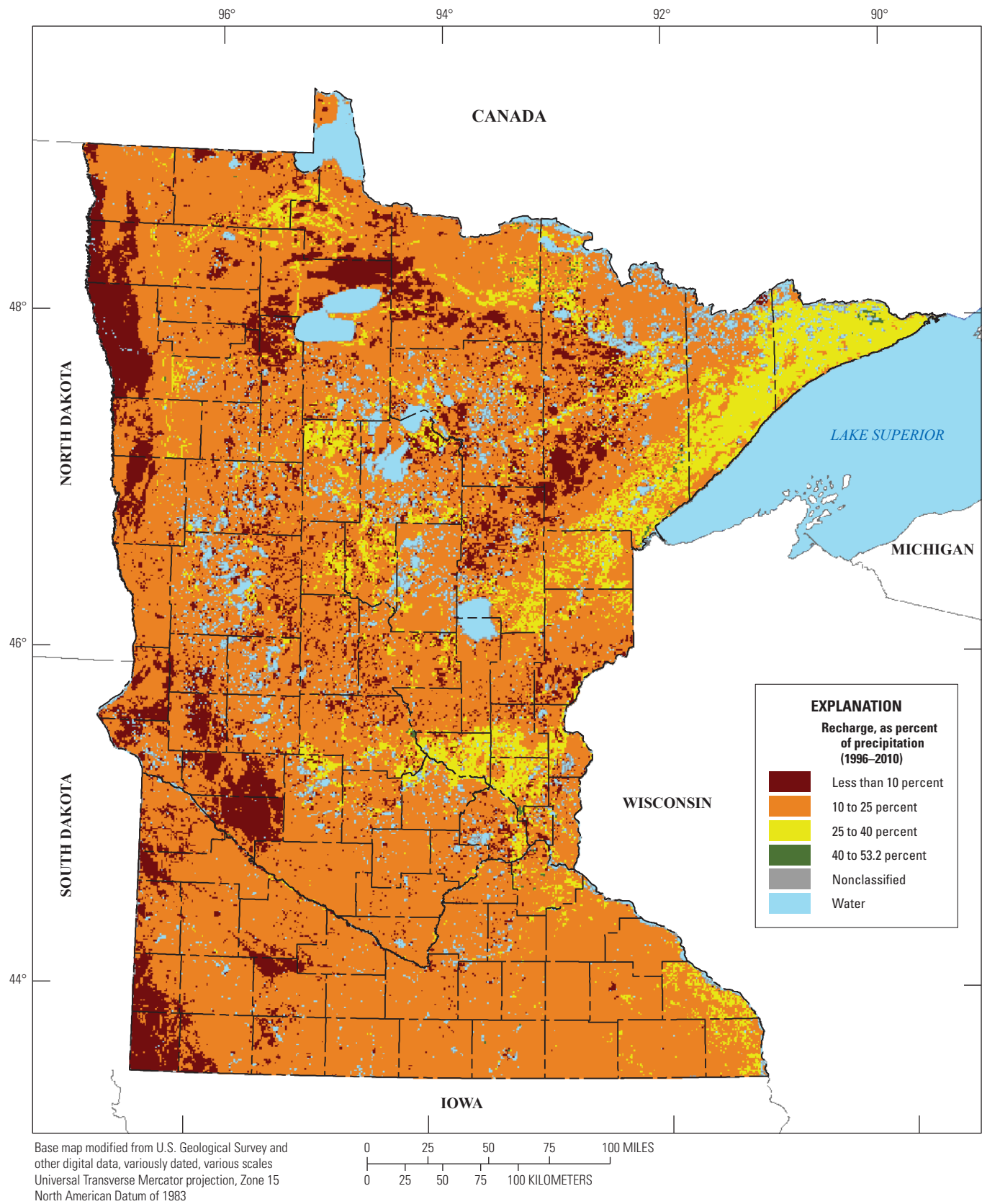


Figure 13. Mean annual potential recharge estimates from the Soil-Water-Balance (SWB) model, shown as a percentage of mean annual gross precipitation from 1996–2010.

Table 8. Total area of active cells in Soil-Water-Balance (SWB) model and mean annual potential recharge estimates, by land-cover class and hydrologic soil group, from 1996–2010.

[The statewide mean by land cover and hydrologic soil group, in *italics*, is an area-weighted mean potential recharge estimate for the entire State for active cells. NA, not applicable]

Land-cover class	Description	Total area (square kilometers)					Statewide total land cover
		Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group	
21	Developed, open space	807	2,192	1,226	135	148	4,508
22	Developed, low intensity	605	1,144	331	58	30	2,168
23	Developed, medium intensity	266	395	101	17	5	784
24	Developed, high intensity	119	164	24	15	5	327
31	Barren land (rock/sand/clay)	30	51	151	18	30	280
41	Deciduous forest	5,581	10,001	12,045	1,696	3,450	32,773
42	Evergreen forest	1,461	971	2,643	390	510	5,975
43	Mixed forest	511	641	3,183	612	351	5,298
52	Shrubland	602	630	1,388	360	235	3,215
71	Grasslands	667	2,480	920	46	162	4,275
81	Pasture/hay	2,959	8,454	5,245	280	741	17,679
82	Cultivated crops	7,477	50,256	24,801	1,372	812	84,718
90	Woody wetlands	3,129	3,200	7,336	807	12,729	27,201
95	Herbaceous wetlands	1,671	3,013	2,367	165	4,848	12,064
NA	Statewide total	25,885	83,592	61,761	5,971	24,056	201,265

Land-cover class	Description	Mean annual potential recharge (inches per year)					Statewide area-weighted mean, by land-cover class
		Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group	
21	Developed, open space	6.72	4.78	4.42	5.29	3.89	5.02
22	Developed, low intensity	7.84	5.41	4.91	5.54	3.62	5.99
23	Developed, medium intensity	7.70	5.39	4.86	5.47	4.79	6.10
24	Developed, high intensity	7.88	4.40	4.63	4.08	6.04	5.69
31	Barren land (rock/sand/clay)	6.63	4.70	5.47	3.76	2.03	4.98
41	Deciduous forest	6.48	5.85	6.27	6.94	4.43	6.02
42	Evergreen forest	6.55	6.82	7.62	7.73	4.07	6.93
43	Mixed forest	6.71	6.88	6.96	6.89	3.99	6.72
52	Shrubland	6.70	6.21	6.88	7.09	4.26	6.55
71	Grasslands	6.69	5.36	4.69	7.09	3.25	5.36
81	Pasture/hay	6.33	4.90	4.73	5.19	3.14	5.02
82	Cultivated crops	6.06	4.32	3.38	3.13	3.19	4.16
90	Woody wetlands	7.00	5.88	6.50	6.00	3.52	5.07
95	Herbaceous wetlands	6.42	4.09	4.92	5.33	3.12	4.20
NA	Statewide area-weighted mean, by hydrologic soil group	6.48	4.74	4.99	5.80	3.57	4.93

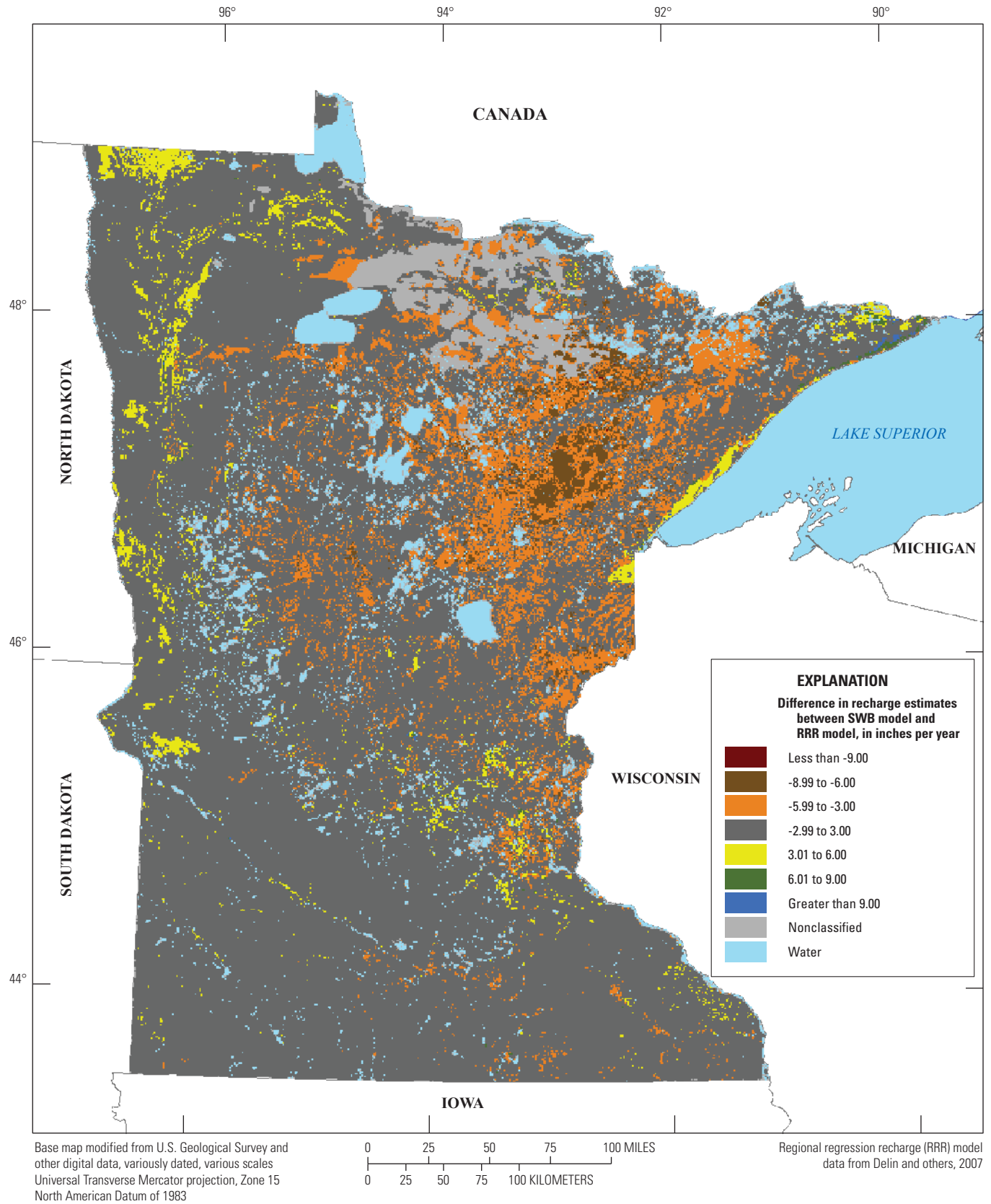


Figure 14. Difference between mean annual potential recharge estimates from the Soil-Water-Balance (SWB) model for 1996–2010 and recharge estimates from the regional regression recharge (RRR) model for 1971–2000 (Delin and others, 2007). [A negative value indicates that the RRR model recharge rate was greater than the SWB model recharge rate.]

Table 9. Comparison of selected point and regional recharge estimates to potential recharge estimates from the Soil-Water-Balance (SWB) model.

[Minn., Minnesota; WTF, water-table fluctuation; GWM, groundwater-flow model; T/H, tritium-helium; UZWB, unsaturated zone water balance; --, not available]

Reference	Areal extent of recharge estimate (nature of aquifer materials)	Recharge estimation method	Years of measurement (if available)	Point and regional recharge estimate	Potential recharge estimate from SWB model
				(inches per year)	
Cowdery and others (2007)	East of Crookston, Minn., Glacial Ridge (glacial drift aquifer)	WTF	2003–05	11.0–25.1	0.0–22.8
Delin (1991)	North/northeast of Rochester, Minn. (Prairie du Chien Group, uppermost unit)	GWM	1987–88	3.0 – 6.0	1.7–7.4
Delin and others (2000)	South of Princeton, Minn. (glacial drift aquifer, lowland site)	WTF	1992–95	4.3–10.2	8.7 – 9.3
Essaid and others (2003)	Bemidji, Minn., crude-oil spill site (glacial drift aquifer)	WTF, T/H, UZWB	--	2.8–11.8	5.9
Lindgren (1996)	Polk and Red Lake Counties (glacial drift aquifers)	WTF	1991–92	4.5–12.0	4.1–6.4
Lindgren (2001)	Cold Spring, Minn., also surrounding area (glacial till and outwash sand/gravels)	WTF	1999	5.3–8.6	4.4–9.0
Lindgren and Landon (2000)	Rock County, Minn., Rock River Valley (glacial outwash sand/gravels)	WTF	1995	2.9–8.1	1.8–2.4
Lindholm (1980)	Benton and Sherburne Counties, Anoka Sand Plain (glacial outwash sand/gravels)	WTF	1970–78	8.0 (average)	7.12 (average)
Myette (1986)	Willow River, Minn. (glacial outwash sand/gravels)	WTF	--	4.5	7.3
Myette (1986)	Cloquet, Minn. (glacial outwash sand/gravels)	WTF	--	12.7	9.0
Ruhl and others (2002)	Twin Cities Metropolitan Area (varies)	WTF	1971–99	4.5–13.6	1.9–15.4
Schoenberg (1998)	Red River Valley, Wilkins County (glacial drift aquifers)	WTF	1993	3.6–5.5	2.8–4.4
Soukup and others (1984)	Red River Valley, Wilkins County (glacial drift aquifers)	WTF	1973–80	3.4–8.5	1.0–4.8
Stark and others (1991)	Bemidji, Minn., crude-oil spill site (glacial drift aquifer)	GWM	1986–87	4.0–8.0	5.9

based on the water-table fluctuation method, such as Delin and others (2000), Lindgren (2001), Lindholm (1980), Ruhl and others (2002), Schoenberg (1998), and Stark and others (1991). Recharge estimates from Lindgren (1996) using the water-table fluctuation method had a greater range than the estimates from the SWB model. Recharge estimates from Cowdery and others (2007) for 2003–05 had a greater range, 11.0 to 25.1 in/yr, than estimates from the SWB model. In this particular case, year to year comparisons were made because the years fell into the period of record for the SWB model. For the SWB model, the recharge estimates ranged from 0.0 to 5.3 in/yr for 2003, from 1.3 to 13.1 in/yr for 2004, and from 0.0 to 22.8 in/yr for 2005. Another notable deviation from previous results was for central Rock County located in southwestern Minnesota, where the estimated potential recharge estimate from the SWB model ranged from 1.8 to 2.4 in/yr, and the recharge estimate from Lindgren and Landon (2000) ranged from 2.9 to 8.1 in/yr.

Two other regional simulations, Neff and others (2006) and Arnold and others (2002), were compared to the SWB model. Recharge estimates from the SWB compared favorably to Neff and others (2006), who provided recharge estimates for parts of northeastern Minnesota along Lake Superior. The recharge estimates by Neff and others (2006) ranged from 4.0 to 11.9 in/yr, and the potential recharge estimates from the SWB model for the same area ranged from 2.0 to 12.0 in/yr, with a few small pockets with estimates >12.0 in/yr in the SWB model near the Minnesota-Canada border. Arnold and others (2000) reported recharge estimates from two different methods, one method from the water balance component of the soil and water assessment (SWAT) model and a second method derived from a hybrid hydrograph separation technique. Both estimates from Arnold and others (2000) were <6.0 in/yr for the southeastern region of Minnesota, which are less than the upper range of estimates from the SWB model of 2.0 to >12.0 in/yr.

Sensitivity Analysis

A sensitivity analysis was completed on the final calibrated SWB model to understand the effects of controlled departures in the calibrated lookup table and control file on the model results. Only a subset of the lookup table parameters was examined in the sensitivity analysis. Any land-cover class that had less than or equal to 2 percent of the total land cover, excluding open water, across Minnesota (table 1) was ruled out as part of the sensitivity analysis, narrowing down the list to eight land-cover classes. Maximum recharge rates and interception storage were not included as part of the sensitivity analysis because a previous SWB study (Aurand, 2013) determined that SWB was not very sensitive to changes in the maximum recharge rates, and interception storage rates were shown to be insensitive in figure 22 of Westenbroek and others (2010). For the remaining two lookup table groups, runoff curve numbers and the root-zone depth, the calibrated SWB model was run for each unique combination of land-cover class and hydrologic soil group. Each lookup parameter was increased by 20 percent and decreased by 20 percent, and then compared to the calibrated SWB model.

Results are presented in table 10 as the relative percent sensitivity from the calibrated value. The calibrated value was the mean annual potential recharge estimate for the overall domain (Minnesota). Each table cell in the upper part of table 10 contains three values: the calibrated curve number (from table 3), the adjusted curve number, and relative percent sensitivity. Each cell in the lower part of table 10 contains three values: the calibrated root-zone depth (from table 3), the adjusted root-zone depth, and relative percent sensitivity. The relative percent sensitivity, as computed by equation 8 (Aurand, 2013), can be used to evaluate the percent change in the model results to overall percent change in the parameter:

$$\text{Relative percent sensitivity} = \frac{\text{Percent change in model results}}{\text{Percent change in parameter}} \times 100 \quad (8)$$

In some cases, an increase or decrease by 20 percent in the curve number would put the curve number outside the bounds of 30 to 100, which are the practical limits validated by other curve

Table 10. Summary of relative percent sensitivity analysis from the base value in the lookup table of the calibrated Soil-Water-Balance (SWB) model. Each parameter was separately adjusted by plus or minus 20 percent to calculate the relative percent sensitivity.

[**Bold** text indicates lookup table parameters with greater than 2 percent relative percent sensitivity from the calibrated lookup table parameter]

Land-cover class	Description	Input, in percent change from calibrated value	Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group
Curve number (calibrated) / curve number (adjusted) / relative percent sensitivity							
21	Developed, open space	+20	54 / 64.8 / 0.00	70 / 84 / -0.20	83 / 99.6 / -0.60	83 / 99.6 / -0.10 ^a	76 / 91.2 / -0.10
21	Developed, open space	-20	54 / 43.2 / 0.00	70 / 56 / 0.00	83 / 66.4 / 0.00	83 / 66.4 / 0.00 ^a	76 / 60.8 / 0.00
41	Deciduous forest	+20	38 / 45.6 / 0.00 ^b	55 / 66 / -0.30	70 / 84 / -5.12	77 / 92.4 / -2.71	63 / 75.6 / -0.40
41	Deciduous forest	-20	38 / 30.4 / 0.00 ^b	55 / 44 / 0.00	70 / 56 / 1.00	77 / 61.6 / 0.30	63 / 50.4 / 0.00
42	Evergreen forest	+20	38 / 45.6 / 0.00 ^b	60 / 72 / -0.10	73 / 87.6 / -1.81	79 / 94.8 / -0.60	67 / 80.4 / -0.10
42	Evergreen forest	-20	38 / 30.4 / 0.00 ^b	60 / 48 / 0.00	73 / 58.4 / 0.30	79 / 63.2 / 0.00	67 / 53.6 / 0.00
43	Mixed forest	+20	38 / 45.6 / 0.00 ^b	58 / 69.6 / -0.10	72 / 86.4 / -1.71	78 / 93.6 / -0.60	65 / 78 / -0.10
43	Mixed forest	-20	38 / 30.4 / 0.00 ^b	58 / 46.4 / 0.00	72 / 57.6 / 0.30	78 / 62.4 / 0.00	65 / 52 / 0.00
81	Pasture/hay	+20	49 / 58.8 / -0.10	69 / 82.8 / -1.91	79 / 94.8 / -6.53	83 / 99.6 / -0.10 ^a	74 / 88.8 / -0.20
81	Pasture/hay	-20	49 / 39.2 / 0.00	69 / 55.2 / 0.20	79 / 63.2 / 0.60	83 / 66.4 / 0.00 ^a	74 / 59.2 / 0.00
82	Cultivated crops	+20	67 / 80.4 / -1.81	78 / 93.6 / -98.53	83 / 99.6 / -49.34^a	83 / 99.6 / -2.51^a	82 / 98.4 / -0.70
82	Cultivated crops	-20	67 / 53.6 / 0.20	78 / 62.4 / 11.25	83 / 66.4 / 10.85^a	83 / 66.4 / 0.80 ^a	82 / 65.6 / 0.10
90	Woody wetlands	+20	60 / 72 / -0.30	60 / 72 / -0.30	60 / 72 / -0.40	60 / 72 / -0.10	60 / 72 / -0.70
90	Woody wetlands	-20	60 / 48 / 0.00	60 / 48 / 0.00	60 / 48 / 0.00	60 / 48 / 0.00	60 / 48 / 0.00
95	Herbaceous wetlands	+20	60 / 72 / -0.10	60 / 72 / -0.10	60 / 72 / -0.10	60 / 72 / 0.00	60 / 72 / -0.20
95	Herbaceous wetlands	-20	60 / 48 / 0.00	60 / 48 / 0.00	60 / 48 / 0.00	60 / 48 / 0.00	60 / 48 / 0.00

Table 10. Summary of relative percent sensitivity analysis from the base value in the lookup table of the calibrated Soil-Water-Balance (SWB) model. Each parameter was separately adjusted by plus or minus 20 percent to calculate the relative percent sensitivity.—Continued

[**Bold** text indicates lookup table parameters with greater than 2 percent relative percent sensitivity from the calibrated lookup table parameter]

Land-cover class	Description	Input, in percent change from calibrated value	Hydrologic soil group A	Hydrologic soil group B	Hydrologic soil group C	Hydrologic soil group D	Organic soil group
Root-zone, in feet (calibrated) / root-zone, in feet (adjusted) / relative percent sensitivity							
21	Developed, open space	+20	2.66 / 3.192 / -0.10	3.32 / 3.984 / -0.10	2.12 / 2.544 / -0.10	1.33 / 1.596 / -0.10	2.72 / 3.264 / -0.10
21	Developed, open space	-20	2.66 / 2.128 / 0.10	3.32 / 2.656 / 0.10	2.12 / 1.696 / 0.00	1.33 / 1.064 / 0.00	2.72 / 2.176 / 0.00
41	Deciduous forest	+20	2.77 / 3.324 / -1.91	2.31 / 2.772 / -2.61	1.85 / 2.22 / -3.42	1.62 / 1.944 / -0.50	2.08 / 2.496 / -0.80
41	Deciduous forest	-20	2.77 / 2.216 / 1.71	2.31 / 1.848 / 3.11	1.85 / 1.48 / 4.02	1.62 / 1.296 / 0.60	2.08 / 1.664 / 1.00
42	Evergreen forest	+20	3.16 / 3.792 / -0.30	2.65 / 3.18 / -0.20	2.12 / 2.544 / -0.60	1.85 / 2.22 / -0.10	2.39 / 2.868 / -0.10
42	Evergreen forest	-20	3.16 / 2.528 / 0.20	2.65 / 2.12 / 0.20	2.12 / 1.696 / 0.60	1.85 / 1.48 / 0.00	2.39 / 1.912 / 0.00
43	Mixed forest	+20	2.97 / 3.564 / -0.10	2.48 / 2.976 / -0.10	1.99 / 2.388 / -0.70	1.74 / 2.088 / -0.10	2.24 / 2.688 / -0.10
43	Mixed forest	-20	2.97 / 2.376 / 0.00	2.48 / 1.984 / 0.00	1.99 / 1.592 / 0.80	1.74 / 1.392 / 0.10	2.24 / 1.792 / 0.00
81	Pasture/hay	+20	2.56 / 3.072 / -0.60	3.2 / 3.84 / -1.51	2.56 / 3.072 / -1.21	1.70 / 2.04 / -0.10	2.87 / 3.444 / -0.10
81	Pasture/hay	-20	2.56 / 2.048 / 0.60	3.2 / 2.56 / 1.71	2.56 / 2.048 / 1.41	1.70 / 1.36 / 0.00	2.87 / 2.296 / 0.10
82	Cultivated crops	+20	2.12 / 2.544 / -2.61	1.93 / 2.316 / -16.77	1.89 / 2.268 / -6.63	1.35 / 1.62 / -0.40	1.91 / 2.292 / -0.10
82	Cultivated crops	-20	2.12 / 1.696 / 3.21	1.93 / 1.544 / 20.99	1.89 / 1.512 / 8.74	1.35 / 1.08 / 0.40	1.91 / 1.528 / 0.10
90	Woody wetlands	+20	1.30 / 1.56 / -0.90	1.44 / 1.728 / -0.70	1.30 / 1.56 / -1.81	1.14 / 1.368 / -0.20	1.37 / 1.644 / -2.81
90	Woody wetlands	-20	1.30 / 1.04 / 1.10	1.44 / 1.152 / 0.80	1.30 / 1.04 / 2.21	1.14 / 0.912 / 0.10	1.37 / 1.096 / 3.62
95	Herbaceous wetlands	+20	1.58 / 1.896 / -0.40	1.76 / 2.112 / -0.30	1.58 / 1.896 / -0.30	1.4 / 1.68 / -0.10	1.67 / 2.004 / -0.70
95	Herbaceous wetlands	-20	1.58 / 1.264 / 0.40	1.76 / 1.408 / 0.30	1.58 / 1.264 / 0.20	1.4 / 1.12 / 0.00	1.67 / 1.336 / 0.80

^aBase value adjusted from calibrated value in table 3 to avoid an unrealistic curve number greater than 100.

^bBase value adjusted from calibrated value in table 3 to avoid an unrealistic curve number less than 30.

number models (Van Mullem, 1989). In these cases, the calibrated model was first re-run with a slightly different lookup parameter that would allow for the 20 percent increase and decrease in the curve number to fall within the practical range of 30 to 100.

Only 21 combinations had a relative percent sensitivity that was >2 percent. Within this subset, the cultivated crops (land-cover class of 82) had the most sensitivity. In particular, changing the curve number for hydrologic soil groups B and C had the greatest effect on the overall potential recharge estimate from the SWB; increases in the curve number led to a recharge reduction, whereas a decrease in the curve number led to more infiltration and therefore more recharge. This is not unexpected given the geographical extent of the combination of land-cover class 82 with soil groups B and C, which together comprise 37.2 percent of the State. Increasing the runoff curve number from 78 to 93.6 for land-cover class 82 with soil group B caused nearly a 100 percent decrease in the overall potential recharge estimate. The only other major land cover with an appreciable number of relative percent sensitivities >2 percent was the deciduous forest group (land-cover class 41).

A sensitivity analysis also was completed by adjusting the meteorological parameters of precipitation, daily minimum air temperature, and daily maximum air temperature. This sensitivity analysis illustrates the effects of potential uncertainties in the input data on model results. Using the same methodology with relative percent sensitivity, table 11 shows the relative percent sensitivity with adjustments to meteorological parameters by 5, 10, and 20 percent.

Unlike lookup table adjustments, even 5-percent adjustments in the meteorological parameters had a substantial effect on the final potential recharge estimate. Adjustments in the minimum temperature had the smallest effects, yet even a 5-percent adjustment had a relative percent sensitivity of -25.61 percent. Increasing the minimum temperature by 20 percent had a relative percent sensitivity of 237.3 percent. Decreasing and increasing the maximum temperature had even greater effects on the relative percent sensitivity. In the cases of the minimum and maximum temperature, the high sensitivity is related to the effects on the ET, which will affect how much water moves to the root zone. To a smaller degree, changes in temperature would have an effect on whether precipitation fell as rain or snow. Precipitation also had substantial relative percent sensitivities, as precipitation shifts affect the overall amount of water available.

Overall, an evaluation of the relative percent sensitivity highlights the importance of using reliable climatological data. Small perturbations in these parameters had substantial effects on the final potential recharge estimates. For the lookup table, relative percent sensitivities generally were related to the overall geographical extent of the different land cover and hydrologic soil group combinations.

Table 11. Summary of relative percent sensitivity analysis for precipitation, daily minimum air temperature, and daily maximum air temperature from the base value used in the control file for the Soil-Water-Balance (SWB) model. Each parameter was adjusted by plus or minus 5, 10, and 20 percent, individually.

Control file parameter	Input, in percent change from calibrated value	Relative percent sensitivity
Precipitation	+20	355.3
	-20	-278.4
	+10	170.9
	-10	-151.6
	+5	83.37
	-5	-78.65
Minimum temperature	+20	237.3
	-20	-61.97
	+10	80.86
	-10	-43.19
	+5	34.65
	-5	-25.61
Maximum temperature	+20	-231.0
	-20	702.8
	+10	-142.4
	-10	247.9
	+5	-80.96
	-5	107.6

Summary

Groundwater recharge is one of the most difficult components of a water budget to ascertain, yet is an important boundary condition necessary for the quantification of water resources. In Minnesota, improved estimates of recharge are necessary because approximately 75 percent of drinking water in Minnesota and 90 percent of agricultural irrigation water are supplied from groundwater. The water that is withdrawn must be supplied by some combination of (1) increased recharge, (2) decreased discharge to streams, lakes, and other surface-water bodies, and (3) removal of water that was stored in the system. Recent pressure on groundwater resources has highlighted the need to provide more accurate recharge estimates for various tools that can assess the sustainability of long-term water use. As part of this effort, the U.S. Geological Survey, in cooperation with the Minnesota Pollution Control Agency, used the Soil-Water-Balance model to calculate mean gridded potential groundwater recharge estimates across Minnesota from 1996–2010 at a 1-kilometer (0.621-mile) resolution. The potential groundwater recharge estimates calculated for Minnesota from the Soil-Water Balance model included gridded values (1-kilometer resolution) of annual mean estimates (that is, the means for individual years from 1996 through 2010) and mean annual estimates (that is, the mean for the 15-year period 1996–2010).

The Soil-Water-Balance model uses a modified Thornthwaite-Mather soil-water-balance approach, with components of the soil-water balance calculated on a daily basis. A key advantage of this approach includes the use of commonly available geographic information system data layers that incorporate land cover, soil properties, and daily meteorological data to produce temporally and spatially variable gridded estimates of potential groundwater recharge. The Soil-Water-Balance model was calibrated by using a combination of parameter estimation techniques, making manual adjustments of model parameters, and using parameter values from previously published Soil-Water-Balance models. Each calibration simulation compared the potential recharge estimate from the model against base-flow estimates derived from three separate hydrograph separation techniques. A total of 35 Minnesota watersheds were selected for the model calibration.

Meteorological data necessary for the model included daily precipitation, minimum daily temperature, and maximum daily temperature. All of the meteorological data were provided by the Daymet dataset, which included daily continuous surfaces of key climatological data. Land-cover data were provided by the 2001 and 2006 National Land Cover Database: the 2001 classification was used from 1994 through 2003, and the 2006 classification was used from 2004 through 2010. Soil data used in the model included hydrologic soils group and the available soil-water capacity. These soil data were obtained from the Natural Resources Conservation Service Soil Survey Geographic (SSURGO) database and the State Soil Geographic (STATSGO) database.

The statewide mean annual potential recharge rate from 1996–2010 was 4.9 inches per year. Potential recharge estimates increased from west to east across Minnesota. The mean annual potential recharge estimates across Minnesota at a 1-kilometer resolution for the overall simulation period (1996–2010) ranged from less than 0.1 to 17.8 inches per year. Some of the lowest potential recharge rates for the simulation period were in the Red River of the North Basin of northwestern Minnesota, and generally were between 1.0 to 1.5 inches per year. The highest potential recharge rates were in northeastern Minnesota and the Anoka Sand Plain in central Minnesota. Eighty-eight percent of the potential recharge rates (by grid cell) were between 2 and 8 inches per year from 1996–2010. Only about 3 percent of all the potential recharge estimates (by grid cell) were less than 2 inches per year, and 9 percent of estimates were greater than 8 inches per year.

On an annual basis, however, potential recharge rates were as high as 27.2 inches per year. The highest annual mean recharge estimate across the State was for 2010, and the lowest mean recharge estimate was for 2003. Although precipitation variability partially explained the annual differences in potential recharge estimates, precipitation alone did not account for these differences, and other factors such as antecedent moisture conditions likely were important. Also, because differences in precipitation gradients across the State can vary from year to year, the dominant land-cover class and hydrologic soil group combinations had a strong effect on the resulting potential recharge value. During 1996–2010, April had the greatest monthly mean potential recharge compared to all other months, accounting for a mean of 30 percent of annual potential recharge in this single month.

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Appendixes

Appendix 1. Control File for the Minnesota Soil-Water-Balance Model

This appendix presents the control file for the Minnesota Soil-Water-Balance (SWB) model to estimate potential recharge. This control file works with the SWB executable module, compiled on October 4, 2014. Any changes to the SWB executable module with newer versions might have modifications that would require adaptations to the following control file.

```
#-----
# MODEL DOMAIN DEFINITION
#
# Definition of the model domain. Units of meters are assumed.
# All subsequent input grids must match the specified model domain exactly.
#
#           Lower LH Corner      Grid
#           |                   Cell
#   NX NY X0   Y0              Size
GRID 572 656 189775. 4816435.    1000.0
BASE_PROJECTION_DEFINITION +proj=utm +zone=15 +north +ellps=GRS80 +datum=NAD83 +units=m +no_defs
#*****
# LENGTH UNITS
#
# Must specify whether grid coordinate are given in METERS or FEET.
# This affects conversion of values from inches to acre-ft.
GRID_LENGTH_UNITS METERS
#*****
# OUTPUT CONTROL
#
SUPPRESS_SCREEN_OUTPUT
#SUPPRESS_INTEGRATED_OUTPUT
#SUPPRESS_DAILY_FILES
SUPPRESS_DISLIN_MESSAGES
#*****
# GROWING SEASON
#
# Define 1) beginning and 2) ending Julian day of growing season;
# and 3) flag indicating whether or not the problem is in the
# Northern hemisphere (possible values: TRUE / FALSE)
#
# The growing season defines only the timespan within which
# interception terms will be calculated.
#
# Other option is to use GDD alone:
# GROWING SEASON: currently dormant conditions AND annual GDD exceeds 90.
# DORMANT SEASON: currently growing season AND minimum daily air temperature is less than 28 # degrees F.
#
GROWING_SEASON GDD
#*****
# FLOW DIRECTION
#
# Flow direction for the Minnesota SWB was switched off.
# Please consult Westenbroek and others (2010) to turn on this option.
#
FLOW_DIRECTION CONSTANT 1
#*****
# To conserve disk space, real values are converted to
# integer values, and the resulting data stream is compressed using
# a simple run-length encoding (RLE) scheme. A larger value for the
```

```

# RLE multiplier preserves more of the real data value and lowers the
# amount of data compression that takes place.
#
RLE_MULTIPLIER 10000
*****
# PRECIPITATION
#
# Daymet climatological data were used for the Minnesota SWB model.
# All Daymet was stored locally to run. Simulations can be run
# "on-the-fly" by running against online Daymet climatological data;
# however, this functionality was not pursued due to speed constraints.
# All Daymet data are stored in millimeters, so SWB needs to convert to
# inches; hence, the conversion factor.
#
PRECIPITATION_NETCDF ..\daymet\%Y-%0#_prcp.nc
PRECIPITATION_GRID_PROJECTION_DEFINITION +proj=lcc +lat_1=25.0 +lat_2=60.0+lat_0=42.5 +lon_0=-100.0
+x_0=0.0 +y_0=0.0 +ellps=GRS80 +datum=NAD83 +units=m +no_def
PRECIPITATION_CONVERSION_FACTOR 0.03936996
PRECIPITATION_MISSING_VALUES_CODE -32768
PRECIPITATION_MISSING_VALUES_OPERATOR <=
PRECIPITATION_MISSING_VALUES_ACTION ZERO
*****
# TEMPERATURE
#
# All Daymet data are stored in Celsius, so SWB needs to convert to
# Fahrenheit; hence, the conversion factor and offset.
#
TEMPERATURE_NETCDF ..\daymet\%Y-%0#_tmax.nc ..\daymet\%Y-%0#_tmin.nc
TMAX_GRID_PROJECTION_DEFINITION +proj=lcc +lat_1=25.0 +lat_2=60.0 +lat_0=42.5 +lon_0=-100.0 +x_0=0.0
+y_0=0.0 +ellps=GRS80 +datum=NAD83 +units=m +no_defs
TMAX_MISSING_VALUES_CODE -128
TMAX_MISSING_VALUES_OPERATOR <=
TMAX_MISSING_VALUES_ACTION MEAN
TMAX_SCALE_FACTOR 1.8
TMAX_ADD_OFFSET 32
TMIN_GRID_PROJECTION_DEFINITION +proj=lcc +lat_1=25.0 +lat_2=60.0 +lat_0=42.5 +lon_0=-100.0 +x_0=0.0
+y_0=0.0 +ellps=GRS80 +datum=NAD83 +units=m +no_defs
TMIN_MISSING_VALUES_CODE -128
TMIN_MISSING_VALUES_OPERATOR <=
TMIN_MISSING_VALUES_ACTION MEAN
TMIN_SCALE_FACTOR 1.8
TMIN_ADD_OFFSET 32
*****
# OUTPUT GRID FILENAME SUFFIX
#
# Set the output grid filename suffix with the OUTPUT_GRID_SUFFIX
# option. This applies only to annual and monthly output grids.
# Daily grids have the filename pattern filename.###, where ###
# is the Julian day of the simulation
#
OUTPUT_GRID_SUFFIX asc
*****
# INITIAL ABSTRACTION METHOD
#
# The method for calculating the initial abstraction within the
# Runoff curve number procedure may be specified in two ways:

```

```

#
# 1) TR-55: Ia is assumed equal to 0.2 * S
# 2) Woodward and others (2003): Ia is assumed equal to 0.05 * S
#
# If the Hawkins method is used, curve numbers are adjusted
# as per Equation 9 of Woodward and others (2003). Net effect should be to
# increase runoff for smaller precip events. This method has been
# suggested to be more appropriate to long-term simulation model applications.
#
INITIAL_ABSTRACTION_METHOD TR55
*****
# INITIAL CONTINUOUS FROZEN GROUND INDEX
#
# assume that ground is initially frozen, "frozen" >= 83
#
INITIAL_FROZEN_GROUND_INDEX CONSTANT 100.0
*****
# FROZEN GROUND THRESHOLD CFGI VALUE
#
# Use this option to set a different value defining the boundary
# between "unfrozen" and "frozen" ground. Literature value is 83.
# For example, for a CFGI < 83, the ground is considered unfrozen;
# with a CFGI >= 83, the ground is considered frozen.
#
# When frozen ground conditions exist, the curve numbers are uniformly
# assumed to reflect antecedent runoff condition III (i.e. increased
# proportion of runoff for a given amount of precipitation).
#
#
UPPER_LIMIT_CFGI 83.
LOWER_LIMIT_CFGI 55.
*****
# ADDITIONAL CONTROL FACTORS FOR RAINFALL/SNOWFALL CORRECTIONS
#
# Input meteorological data can be modified by altering the
# conversion and scale factors above. These additional controls
# allow for user-intervention on how to alter rainfall, snowfall,
# or both. In the Minnesota SWB, no alteration was used and these
# values were left as 1.
#
RAINFALL_CORRECTION_FACTOR      1.00
SNOWFALL_CORRECTION_FACTOR      1.00
*****
# REFERENCE EVAPOTRANSPIRATION
#
REFERENCE_ET_SLOPE              2.3000000E-03
REFERENCE_ET_EXPONENT           5.0000000E-01
REFERENCE_ET_CONSTANT           1.7800000E+01
*****
# SOIL GROUP
#
# Curve Number Hydrologic Soil Groups: The Soil Conservation Service (SCS)
# has categorized every soil within the United States into one of four
# hydrologic soil groups based on its infiltration capacity (A - D)
# (input to the model as 1 - 4).
# "A" soils have a high minimum infiltration capacity and subsequently a low

```

```

# overland flow potential, whereas “D” soils have a very low infiltration
# capacity and subsequently a high overland flow potential.
# For further information on designation of hydrologic soil groups in Minnesota,
# consult the section on “Hydrologic soil groups”
#
SOIL_GROUP ARC_GRID input\soils_hyd_grp.asc
SOIL_GROUP_PROJECTION_DEFINITION +proj=utm +zone=15 +north +ellps=GRS80 +datum=NAD83 +units=m
+no_defs
*****
# LAND USE/COVER CLASSIFICATION
#
# The model uses land use information, together with
# the soil available water capacity information, to calculate surface
# runoff and assign a maximum soil moisture holding capacity for each
# grid cell.
# By designating as DYNAMIC, multiple classifications may be used.
# In the Minnesota SWB model,
#
LAND_USE DYNAMIC ARC_GRID input\NLCD_%Y.asc
LANDUSE_PROJECTION_DEFINITION +proj=utm +zone=15 +north +ellps=GRS80+datum=NAD83 +units=m +no_defs

*****
# SPECIFY OPEN WATER LAND USE
#
# This option forces the cells of the given land use to be treated
# as open water cells. In these cells, recharge is *NOT* calculated,
# nor is flow routing or soil-moisture accounting done. Water is
# either allowed to leave these cells as actual ET, or assumed to leave
# the grid flow out of grid via surface water features.
#
OPEN_WATER_LAND_USE 11

*****
#
# Land Use LOOKUP table:
#
# See table 3 in the main report for the Minnesota lookup table.
# Further notes on its structure are detailed in Westenbroek and others, 2010.
#
LAND_USE_LOOKUP_TABLE std_input\LU_lookup_Minnesota.txt

*****
# BASE SOIL WATER CAPACITY
#
# The model uses soil information, together with land cover information,
# to calculate surface runoff and assign a maximum soil moisture holding
# capacity to each grid cell. Soil classifications, which include the
# requisite available water capacity or textural information, are typically
# available through the state soil conservation service.
#
#
WATER_CAPACITY ARC_GRID input\soils_awc.asc
WATER_CAPACITY_PROJECTION_DEFINITION +proj=utm +zone=15 +north +ellps=GRS80+datum=NAD83 +units=m
+no_defs

*****

```



```

# SOIL MOISTURE ACCOUNTING METHOD
##
# The Thornthwaite-Mather soil moisture retention tables are included
# in the standard table "soil-moisture-retention-extended.grd"
#
SM T-M EQUATIONS
*****
# INITIAL SOIL MOISTURE
#
# If CONSTANT, initial soil moisture is specified as a PERCENTAGE saturation
# of the available water capacity.
#
# If an ASCII GRID FILE, initial soil moisture is specified in INCHES of water.
# An ASCII grid file from a 1994 simulation
# was used for initializing the model period 1995-2011. This earlier
# control file would appear the same, with the exception that this
# option would be used for soil moisture:
# INITIAL_SOIL_MOISTURE CONSTANT 100
INITIAL_SOIL_MOISTURE ARC_GRID output\future\swb_future_final_pct_sm_1994.asc
*****
# INITIAL SNOW COVER
#
# Initial snow cover is specified as an equivalent moisture value.
# This may be specified as a single constant value
# or as an ASCII grid file. An ASCII grid file from a 1994 simulation
# was used for initializing the model period 1996-2010. This earlier
# control file would appear the same, with the exception that this
# option would be used for snow cover:
# INITIAL_SNOW_COVER CONSTANT 0
#
INITIAL_SNOW_COVER ARC_GRID output\future\swb_future_final_snow_cover_1994.asc
*****
# SOLUTION METHOD
#
# Three solution methods are available for the routing of surface water
# through the model domain. The "ITERATIVE" method, the "DOWNHILL" method,
# and "NO ROUTING". The "NO ROUTING" option was used for the Minnesota
# SWB model.
#
RUNOFF C-N NO_ROUTING
*****
# EVAPOTRANSPIRATION METHOD
#
# Hargreaves (program option: "HARGREAVES" southerly lat northerly lat)
#
ET HARGREAVES 43.5 49.38

*****
# OUTPUT OPTIONS
#
# The SWB code can generate image and ARCGIS/Surfer output at the
# daily, monthly, or annual timescale. This section allows the user to
# specify exactly what output should be generated for each of 24
# internal variables at each of the three timescales.
#
# Format for specifying output options is:

```

```

# "OUTPUT_OPTIONS variable_name daily_option monthly_option annual_option",
# where the possible values for each option are:
# NONE, GRAPH (or PLOT), GRID, or BOTH
#
OUTPUT_OPTIONS RECHARGE NONE GRID GRID
OUTPUT_OPTIONS GROSS_PRECIP NONE NONE GRID
OUTPUT_OPTIONS AVG_TEMP NONE NONE GRID
OUTPUT_OPTIONS MAX_TEMP NONE NONE GRID
OUTPUT_OPTIONS MIN_TEMP NONE NONE GRID
OUTPUT_OPTIONS SM_APWL NONE NONE NONE
OUTPUT_OPTIONS SNOWCOVER NONE NONE NONE
OUTPUT_OPTIONS INTERCEPTION NONE NONE NONE
OUTPUT_OPTIONS RUNOFF_OUTSIDE NONE NONE NONE
OUTPUT_OPTIONS ACT_ET NONE NONE GRID
OUTPUT_OPTIONS REFERENCE_ET NONE NONE NONE
#*****
# OUTPUT GRID FILE FORMAT
#
# Next line specifies output grid format: ARC_GRID or SURFER
#
OUTPUT_FORMAT ARC_GRID
#*****
# BEGIN SOLUTION
#
# Minnesota SWB model runs continuously from 1996 through 2010.
#
SOLVE_NO_TS_FILE 1996 2010
#
EOJ
#

```

Appendix 2. Model Calibration Analysis

Base-flow estimates for individual years from 1996 through 2010 for the 35 reference watersheds used in model calibration analysis with annual recharge rates during the period analyzed by using PART, HYSEP fixed-interval method, and HYSEP sliding method in comparison to the estimated potential recharge rates for the same year from the Soil-Water-Balance (SWB) model are included in table 2–1. The relative error is the SWB potential recharge estimate to the mean of the three different base-flow estimates.

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.

[USGS, U.S. Geological Survey; in/yr, inches per year; Minn., Minnesota; NA, not applicable]

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Knife River near Two Harbors, Minn.	04015330	1996	10.46	9.87	10.08	10.27	0.01
Knife River near Two Harbors, Minn.	04015330	1997	8.87	8.45	8.72	8.81	0.02
Knife River near Two Harbors, Minn.	04015330	1998	6.52	6.56	6.78	12.13	0.83
Knife River near Two Harbors, Minn.	04015330	1999	10.58	10.28	9.78	11.52	0.13
Knife River near Two Harbors, Minn.	04015330	2000	5.33	5.38	5.14	4.55	-0.14
Knife River near Two Harbors, Minn.	04015330	2001	8.64	8.84	9.79	10.92	0.20
Knife River near Two Harbors, Minn.	04015330	2002	4.95	5.84	5.54	6.33	0.16
Knife River near Two Harbors, Minn.	04015330	2003	3.68	4.37	4.30	3.16	-0.23
Knife River near Two Harbors, Minn.	04015330	2004	5.65	5.40	5.78	7.64	0.36
Knife River near Two Harbors, Minn.	04015330	2005	9.29	9.11	8.69	9.46	0.05
Knife River near Two Harbors, Minn.	04015330	2006	6.20	7.30	6.71	3.89	-0.42
Knife River near Two Harbors, Minn.	04015330	2007	7.10	8.07	7.47	11.63	0.54
Knife River near Two Harbors, Minn.	04015330	2008	7.68	7.75	7.75	9.79	0.27
Knife River near Two Harbors, Minn.	04015330	2009	6.99	7.69	7.75	8.42	0.13
Knife River near Two Harbors, Minn.	04015330	2010	8.03	8.80	8.26	7.44	-0.11
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	1996	3.60	3.54	3.51	2.00	-0.44
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	1997	5.44	5.39	5.40	7.35	0.36
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	1998	4.61	4.70	4.67	6.70	0.44
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	1999	6.05	6.00	5.98	4.18	-0.30
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2000	4.43	4.36	4.36	2.83	-0.35
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2001	5.66	5.57	5.52	3.45	-0.38
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2002	3.68	3.63	3.62	2.62	-0.28
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2003	2.54	2.46	2.47	1.08	-0.57
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2004	3.38	3.28	3.26	5.85	0.77
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2005	5.61	5.46	5.48	3.16	-0.43
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2006	5.03	4.94	4.88	2.99	-0.40
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2007	4.65	4.49	4.46	4.75	0.05
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2008	4.39	4.29	4.28	5.07	0.17

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2009	7.04	6.81	6.84	6.76	-0.02
Otter Tail River below Orwell Dam near Fergus Falls, Minn.	05046000	2010	8.88	8.72	8.72	8.58	-0.02
Buffalo River near Dilworth, Minn.	05062000	1996	2.29	2.02	2.06	1.69	-0.21
Buffalo River near Dilworth, Minn.	05062000	1997	4.67	4.04	4.24	6.38	0.48
Buffalo River near Dilworth, Minn.	05062000	1998	5.13	4.49	4.55	7.79	0.65
Buffalo River near Dilworth, Minn.	05062000	1999	3.30	3.19	3.13	3.35	0.05
Buffalo River near Dilworth, Minn.	05062000	2000	3.55	3.71	3.48	2.65	-0.26
Buffalo River near Dilworth, Minn.	05062000	2001	3.97	3.78	3.89	2.63	-0.32
Buffalo River near Dilworth, Minn.	05062000	2002	1.74	1.71	1.81	1.21	-0.31
Buffalo River near Dilworth, Minn.	05062000	2003	1.25	1.35	1.37	0.72	-0.45
Buffalo River near Dilworth, Minn.	05062000	2004	2.80	2.65	2.63	5.05	0.87
Buffalo River near Dilworth, Minn.	05062000	2005	2.94	3.34	3.23	3.01	-0.05
Buffalo River near Dilworth, Minn.	05062000	2006	3.02	2.31	2.57	2.72	0.03
Buffalo River near Dilworth, Minn.	05062000	2007	2.54	2.52	2.60	4.01	0.57
Buffalo River near Dilworth, Minn.	05062000	2008	3.52	3.68	3.69	5.16	0.42
Buffalo River near Dilworth, Minn.	05062000	2009	6.04	5.39	5.76	6.60	0.15
Buffalo River near Dilworth, Minn.	05062000	2010	5.29	4.89	5.00	7.73	0.53
Wild River River at Twin Valley, Minn.	05062500	1996	3.81	3.79	3.86	1.52	-0.60
Wild River River at Twin Valley, Minn.	05062500	1997	5.37	4.87	5.07	7.87	0.54
Wild River River at Twin Valley, Minn.	05062500	1998	4.38	4.04	4.10	5.83	0.40
Wild River River at Twin Valley, Minn.	05062500	1999	6.74	6.52	6.49	5.51	-0.16
Wild River River at Twin Valley, Minn.	05062500	2000	4.96	4.79	4.64	3.90	-0.19
Wild River River at Twin Valley, Minn.	05062500	2001	4.91	4.84	4.98	2.90	-0.41
Wild River River at Twin Valley, Minn.	05062500	2003	2.14	2.02	2.03	0.45	-0.78
Wild River River at Twin Valley, Minn.	05062500	2004	3.58	3.13	3.26	6.21	0.87
Wild River River at Twin Valley, Minn.	05062500	2005	4.30	3.96	3.98	1.88	-0.54
Wild River River at Twin Valley, Minn.	05062500	2006	3.05	2.87	2.71	3.02	0.05
Wild River River at Twin Valley, Minn.	05062500	2007	2.47	2.57	2.41	4.16	0.67
Wild River River at Twin Valley, Minn.	05062500	2008	4.06	3.95	3.88	5.25	0.32

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Wild River River at Twin Valley, Minn.	05062500	2009	5.49	5.49	5.53	5.81	0.06
Wild River River at Twin Valley, Minn.	05062500	2010	5.54	4.86	5.02	7.83	0.52
Sand Hill River at Climax, Minn.	05069000	1996	1.29	2.51	2.52	1.00	-0.53
Sand Hill River at Climax, Minn.	05069000	1997	4.18	4.51	4.51	5.78	0.31
Sand Hill River at Climax, Minn.	05069000	1998	3.65	3.80	3.51	5.78	0.58
Sand Hill River at Climax, Minn.	05069000	1999	6.04	5.58	5.43	3.05	-0.46
Sand Hill River at Climax, Minn.	05069000	2000	2.70	2.39	2.40	3.61	0.45
Sand Hill River at Climax, Minn.	05069000	2001	2.53	2.74	2.51	2.28	-0.12
Sand Hill River at Climax, Minn.	05069000	2002	3.49	3.02	3.23	3.28	0.01
Sand Hill River at Climax, Minn.	05069000	2003	1.45	1.28	1.34	0.19	-0.86
Sand Hill River at Climax, Minn.	05069000	2004	2.46	2.41	2.21	4.34	0.84
Sand Hill River at Climax, Minn.	05069000	2005	2.93	2.62	2.69	2.67	-0.03
Sand Hill River at Climax, Minn.	05069000	2006	2.06	2.71	2.55	2.14	-0.12
Sand Hill River at Climax, Minn.	05069000	2007	2.11	1.95	1.83	2.69	0.37
Sand Hill River at Climax, Minn.	05069000	2008	2.40	2.17	2.18	4.68	1.08
Sand Hill River at Climax, Minn.	05069000	2009	4.36	4.33	4.20	6.11	0.42
Sand Hill River at Climax, Minn.	05069000	2010	4.93	4.22	4.39	6.10	0.35
Red Lake River near Red Lake, Minn.	05074500	2000	4.78	5.24	5.15	3.43	-0.32
Red Lake River near Red Lake, Minn.	05074500	2001	5.01	5.22	5.28	5.84	0.13
Red Lake River near Red Lake, Minn.	05074500	2002	4.72	5.01	4.94	3.84	-0.21
Red Lake River near Red Lake, Minn.	05074500	2003	0.58	0.59	0.59	0.29	-0.51
Red Lake River near Red Lake, Minn.	05074500	2004	1.32	1.47	1.49	5.29	2.71
Red Lake River near Red Lake, Minn.	05074500	2005	5.04	5.09	5.10	2.89	-0.43
Red Lake River near Red Lake, Minn.	05074500	2006	2.84	2.96	2.98	2.90	-0.01
Red Lake River near Red Lake, Minn.	05074500	2007	0.90	0.92	0.92	3.59	2.93
Red Lake River near Red Lake, Minn.	05074500	2008	1.09	1.13	1.13	3.10	1.78
Red Lake River near Red Lake, Minn.	05074500	2009	2.54	2.54	2.55	5.02	0.97
Red Lake River near Red Lake, Minn.	05074500	2010	3.29	3.29	3.23	4.71	0.44

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Thief River near Thief River Falls, Minn.	05076000	1996	5.36	4.96	5.18	2.29	-0.56
Thief River near Thief River Falls, Minn.	05076000	1997	6.01	5.47	5.60	4.82	-0.15
Thief River near Thief River Falls, Minn.	05076000	1998	2.90	2.82	2.74	4.00	0.42
Thief River near Thief River Falls, Minn.	05076000	1999	8.57	8.66	8.58	4.94	-0.43
Thief River near Thief River Falls, Minn.	05076000	2001	4.87	4.53	4.67	3.91	-0.17
Thief River near Thief River Falls, Minn.	05076000	2002	5.48	5.24	5.08	4.78	-0.09
Thief River near Thief River Falls, Minn.	05076000	2003	0.30	0.32	0.30	0.32	0.04
Thief River near Thief River Falls, Minn.	05076000	2004	5.67	5.42	5.48	5.11	-0.08
Thief River near Thief River Falls, Minn.	05076000	2005	5.35	5.12	5.02	1.54	-0.70
Thief River near Thief River Falls, Minn.	05076000	2008	0.84	0.98	0.93	3.23	2.52
Thief River near Thief River Falls, Minn.	05076000	2009	4.09	4.64	4.53	4.49	0.02
Thief River near Thief River Falls, Minn.	05076000	2010	5.82	5.47	5.48	7.56	0.35
Clearwater River at Plummer, Minn.	05078000	1996	4.71	4.66	4.83	1.49	-0.69
Clearwater River at Plummer, Minn.	05078000	1997	6.67	5.93	6.04	5.75	-0.07
Clearwater River at Plummer, Minn.	05078000	1998	2.94	2.73	2.77	3.75	0.33
Clearwater River at Plummer, Minn.	05078000	1999	5.97	5.50	5.47	5.22	-0.08
Clearwater River at Plummer, Minn.	05078000	2000	4.26	4.06	3.96	3.64	-0.11
Clearwater River at Plummer, Minn.	05078000	2001	5.70	5.34	5.46	3.40	-0.38
Clearwater River at Plummer, Minn.	05078000	2002	3.50	3.29	3.39	4.09	0.21
Clearwater River at Plummer, Minn.	05078000	2003	1.66	1.60	1.58	0.20	-0.88
Clearwater River at Plummer, Minn.	05078000	2004	2.81	2.49	2.54	4.53	0.73
Clearwater River at Plummer, Minn.	05078000	2005	3.47	3.71	3.53	1.77	-0.51
Clearwater River at Plummer, Minn.	05078000	2006	2.67	2.13	2.35	2.50	0.05
Clearwater River at Plummer, Minn.	05078000	2007	2.74	2.21	2.39	3.38	0.38
Clearwater River at Plummer, Minn.	05078000	2008	2.64	2.55	2.61	3.44	0.32
Clearwater River at Plummer, Minn.	05078000	2009	5.68	5.20	5.12	4.67	-0.12
Clearwater River at Plummer, Minn.	05078000	2010	5.08	4.49	4.48	6.53	0.39
Lost River at Oklee, Minn.	05078230	1996	3.89	4.43	3.89	1.04	-0.74
Lost River at Oklee, Minn.	05078230	1997	4.26	3.94	4.01	4.94	0.21

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Lost River at Oklee, Minn.	05078230	1998	2.25	2.23	2.17	3.54	0.59
Lost River at Oklee, Minn.	05078230	1999	4.76	4.45	4.55	4.25	-0.07
Lost River at Oklee, Minn.	05078230	2000	2.66	2.46	2.43	3.43	0.36
Lost River at Oklee, Minn.	05078230	2001	4.21	3.49	3.64	3.11	-0.18
Lost River at Oklee, Minn.	05078230	2002	2.32	2.02	2.17	3.82	0.76
Lost River at Oklee, Minn.	05078230	2003	1.14	1.04	0.99	0.14	-0.86
Lost River at Oklee, Minn.	05078230	2004	2.50	2.10	2.18	4.27	0.89
Lost River at Oklee, Minn.	05078230	2005	2.99	2.74	2.69	1.50	-0.46
Lost River at Oklee, Minn.	05078230	2006	1.79	1.39	1.53	2.26	0.44
Lost River at Oklee, Minn.	05078230	2007	1.95	1.70	1.83	2.88	0.58
Lost River at Oklee, Minn.	05078230	2008	2.40	2.14	2.16	2.55	0.14
Lost River at Oklee, Minn.	05078230	2009	4.48	3.88	4.05	4.51	0.09
Lost River at Oklee, Minn.	05078230	2010	3.58	3.26	3.33	6.43	0.90
Middle River at Argyle, Minn.	05087500	1996	2.52	2.07	2.40	2.69	0.15
Middle River at Argyle, Minn.	05087500	1997	4.41	2.81	3.20	4.80	0.38
Middle River at Argyle, Minn.	05087500	1998	2.85	2.16	2.44	3.43	0.38
Middle River at Argyle, Minn.	05087500	1999	5.70	5.91	5.63	2.21	-0.62
Middle River at Argyle, Minn.	05087500	2000	3.03	2.88	3.10	3.44	0.14
Middle River at Argyle, Minn.	05087500	2001	3.16	2.65	2.77	2.82	-0.01
Middle River at Argyle, Minn.	05087500	2002	2.23	1.97	1.80	4.15	1.08
Middle River at Argyle, Minn.	05087500	2003	0.70	0.58	0.58	0.20	-0.68
Middle River at Argyle, Minn.	05087500	2004	3.34	3.15	2.74	3.99	0.30
Middle River at Argyle, Minn.	05087500	2005	3.76	4.27	4.03	0.94	-0.77
Middle River at Argyle, Minn.	05087500	2006	3.25	1.87	2.25	2.49	0.01
Middle River at Argyle, Minn.	05087500	2007	1.70	1.36	1.48	3.15	1.08
Middle River at Argyle, Minn.	05087500	2008	1.66	1.30	1.36	4.59	2.19
Middle River at Argyle, Minn.	05087500	2009	3.89	3.75	3.94	4.35	0.13
Middle River at Argyle, Minn.	05087500	2010	4.19	3.54	3.65	8.22	1.17

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
South Branch Two Rivers at Lake Bronson, Minn.	05094000	1996	5.54	5.72	5.60	2.93	-0.48
South Branch Two Rivers at Lake Bronson, Minn.	05094000	1997	4.34	3.40	3.38	5.08	0.37
South Branch Two Rivers at Lake Bronson, Minn.	05094000	1998	1.45	1.83	1.78	3.52	1.09
South Branch Two Rivers at Lake Bronson, Minn.	05094000	1999	5.89	4.69	5.19	1.90	-0.64
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2000	2.59	2.79	3.03	5.49	0.96
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2001	4.39	4.15	4.25	3.00	-0.30
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2002	3.46	3.16	3.45	4.31	0.28
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2003	0.38	0.52	0.48	0.29	-0.37
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2004	5.28	4.92	5.01	4.81	-0.05
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2005	5.09	5.43	5.02	2.80	-0.46
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2006	2.84	3.42	2.91	3.08	0.01
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2007	0.96	1.05	1.09	4.08	2.95
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2008	0.93	0.91	0.92	2.87	2.12
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2009	6.74	6.19	6.12	6.25	-0.02
South Branch Two Rivers at Lake Bronson, Minn.	05094000	2010	3.96	4.32	3.91	8.56	1.11
Kawishiwi River near Winton, Minn.	05127000	1996	9.72	13.13	12.80	8.25	-0.31
Kawishiwi River near Winton, Minn.	05127000	1997	7.05	7.33	7.40	8.47	0.17
Kawishiwi River near Winton, Minn.	05127000	1998	5.28	5.78	5.84	9.35	0.66
Kawishiwi River near Winton, Minn.	05127000	1999	11.39	11.02	11.32	9.32	-0.17
Kawishiwi River near Winton, Minn.	05127000	2000	7.28	6.45	6.64	4.18	-0.38
Kawishiwi River near Winton, Minn.	05127000	2001	11.22	11.54	11.31	12.51	0.10
Kawishiwi River near Winton, Minn.	05127000	2002	4.61	4.22	4.48	3.25	-0.27
Kawishiwi River near Winton, Minn.	05127000	2003	4.50	4.27	4.29	3.20	-0.26
Kawishiwi River near Winton, Minn.	05127000	2004	6.57	6.71	6.64	6.24	-0.06
Kawishiwi River near Winton, Minn.	05127000	2005	6.28	6.21	6.08	8.52	0.38
Kawishiwi River near Winton, Minn.	05127000	2007	8.31	8.42	8.39	12.49	0.49
Kawishiwi River near Winton, Minn.	05127000	2008	9.45	9.86	9.80	9.66	-0.00
Kawishiwi River near Winton, Minn.	05127000	2009	6.28	6.49	6.47	7.43	0.16
Kawishiwi River near Winton, Minn.	05127000	2010	2.35	2.24	2.27	4.72	1.06

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Little Fork River at Littlefork, Minn.	05131500	1996	8.66	7.70	7.53	4.91	-0.38
Little Fork River at Littlefork, Minn.	05131500	1997	6.97	6.49	6.48	6.07	-0.09
Little Fork River at Littlefork, Minn.	05131500	1998	4.05	3.69	3.65	4.12	0.09
Little Fork River at Littlefork, Minn.	05131500	1999	8.69	7.46	7.65	8.82	0.11
Little Fork River at Littlefork, Minn.	05131500	2000	5.14	4.77	4.57	2.79	-0.42
Little Fork River at Littlefork, Minn.	05131500	2001	10.72	8.89	9.54	7.82	-0.20
Little Fork River at Littlefork, Minn.	05131500	2002	4.43	4.16	4.13	3.65	-0.14
Little Fork River at Littlefork, Minn.	05131500	2003	3.19	2.89	2.99	1.52	-0.50
Little Fork River at Littlefork, Minn.	05131500	2004	7.17	6.46	6.22	7.35	0.11
Little Fork River at Littlefork, Minn.	05131500	2005	6.34	6.29	5.79	5.80	-0.06
Little Fork River at Littlefork, Minn.	05131500	2006	4.07	3.63	3.72	3.42	-0.10
Little Fork River at Littlefork, Minn.	05131500	2007	3.71	3.24	3.23	7.02	1.07
Little Fork River at Littlefork, Minn.	05131500	2008	6.65	6.31	5.98	5.37	-0.15
Little Fork River at Littlefork, Minn.	05131500	2009	6.56	5.84	6.22	7.30	0.18
Little Fork River at Littlefork, Minn.	05131500	2010	4.75	4.28	4.30	3.97	-0.11
Big Fork River at Big Falls, Minn.	05132000	1998	4.32	3.93	4.07	3.91	-0.05
Big Fork River at Big Falls, Minn.	05132000	1999	8.92	8.14	8.10	8.14	-0.03
Big Fork River at Big Falls, Minn.	05132000	2000	5.07	4.51	4.59	3.05	-0.35
Big Fork River at Big Falls, Minn.	05132000	2001	9.04	8.72	8.44	7.36	-0.16
Big Fork River at Big Falls, Minn.	05132000	2002	4.78	4.28	4.28	3.20	-0.28
Big Fork River at Big Falls, Minn.	05132000	2003	2.44	2.22	2.21	0.57	-0.75
Big Fork River at Big Falls, Minn.	05132000	2004	6.07	5.43	5.44	6.90	0.22
Big Fork River at Big Falls, Minn.	05132000	2005	6.71	6.14	6.26	5.34	-0.16
Big Fork River at Big Falls, Minn.	05132000	2006	4.41	4.14	4.11	3.14	-0.26
Big Fork River at Big Falls, Minn.	05132000	2007	2.53	2.47	2.39	5.02	1.04
Big Fork River at Big Falls, Minn.	05132000	2008	4.91	4.69	4.71	4.26	-0.11
Big Fork River at Big Falls, Minn.	05132000	2009	5.63	5.25	5.15	6.45	0.21
Big Fork River at Big Falls, Minn.	05132000	2010	5.86	5.42	5.32	3.49	-0.37

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Crow Wing River at Nimrod, Minn.	05244000	1996	6.82	6.56	6.57	2.88	-0.57
Crow Wing River at Nimrod, Minn.	05244000	1997	7.86	7.69	7.68	9.63	0.24
Crow Wing River at Nimrod, Minn.	05244000	1998	7.24	6.90	6.89	5.84	-0.17
Crow Wing River at Nimrod, Minn.	05244000	1999	8.69	8.26	8.25	7.25	-0.14
Crow Wing River at Nimrod, Minn.	05244000	2000	6.67	6.55	6.57	4.55	-0.31
Crow Wing River at Nimrod, Minn.	05244000	2001	6.86	6.48	6.52	5.15	-0.22
Crow Wing River at Nimrod, Minn.	05244000	2002	5.27	5.07	5.05	4.18	-0.18
Crow Wing River at Nimrod, Minn.	05244000	2003	3.98	3.78	3.79	0.77	-0.80
Crow Wing River at Nimrod, Minn.	05244000	2004	4.56	4.47	4.42	6.75	0.51
Crow Wing River at Nimrod, Minn.	05244000	2005	5.96	5.83	5.80	3.94	-0.33
Crow Wing River at Nimrod, Minn.	05244000	2006	4.94	4.73	4.73	3.57	-0.26
Crow Wing River at Nimrod, Minn.	05244000	2007	5.15	4.84	4.82	6.20	0.26
Crow Wing River at Nimrod, Minn.	05244000	2008	5.49	5.33	5.35	6.53	0.21
Crow Wing River at Nimrod, Minn.	05244000	2009	6.87	6.73	6.70	6.74	-0.00
Crow Wing River at Nimrod, Minn.	05244000	2010	6.67	6.44	6.39	6.79	0.04
Long Prairie River at Long Prairie, Minn.	05245100	1996	5.92	5.56	5.54	2.51	-0.56
Long Prairie River at Long Prairie, Minn.	05245100	1997	5.80	5.75	5.65	5.42	-0.05
Long Prairie River at Long Prairie, Minn.	05245100	1998	4.43	4.30	4.30	3.82	-0.12
Long Prairie River at Long Prairie, Minn.	05245100	1999	6.16	6.04	6.00	2.37	-0.61
Long Prairie River at Long Prairie, Minn.	05245100	2000	3.17	3.07	3.04	1.45	-0.53
Long Prairie River at Long Prairie, Minn.	05245100	2001	8.02	7.25	7.42	5.30	-0.30
Long Prairie River at Long Prairie, Minn.	05245100	2002	4.84	4.65	4.56	4.06	-0.13
Long Prairie River at Long Prairie, Minn.	05245100	2003	5.49	5.09	5.15	2.23	-0.57
Long Prairie River at Long Prairie, Minn.	05245100	2004	3.07	2.95	2.95	2.47	-0.18
Long Prairie River at Long Prairie, Minn.	05245100	2005	6.40	6.13	6.13	6.61	0.06
Long Prairie River at Long Prairie, Minn.	05245100	2006	4.65	4.48	4.43	2.26	-0.50
Long Prairie River at Long Prairie, Minn.	05245100	2007	4.11	3.90	3.90	5.46	0.37
Long Prairie River at Long Prairie, Minn.	05245100	2008	4.41	4.28	4.29	3.21	-0.26
Long Prairie River at Long Prairie, Minn.	05245100	2009	5.57	5.18	5.23	6.98	0.31
Long Prairie River at Long Prairie, Minn.	05245100	2010	6.47	6.19	6.24	9.18	0.46

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Sauk River near St. Cloud, Minn.	05270500	1996	5.44	5.48	5.54	2.35	-0.57
Sauk River near St. Cloud, Minn.	05270500	1997	6.16	5.89	5.57	5.74	-0.02
Sauk River near St. Cloud, Minn.	05270500	1998	4.33	4.11	4.16	3.46	-0.18
Sauk River near St. Cloud, Minn.	05270500	1999	4.00	3.89	3.90	2.43	-0.38
Sauk River near St. Cloud, Minn.	05270500	2000	1.74	1.67	1.66	1.61	-0.05
Sauk River near St. Cloud, Minn.	05270500	2001	6.59	6.08	6.13	7.50	0.20
Sauk River near St. Cloud, Minn.	05270500	2002	5.50	5.26	5.26	8.03	0.50
Sauk River near St. Cloud, Minn.	05270500	2003	4.36	4.11	4.08	2.27	-0.46
Sauk River near St. Cloud, Minn.	05270500	2004	3.05	2.82	2.85	3.51	0.21
Sauk River near St. Cloud, Minn.	05270500	2005	5.49	5.01	5.07	7.49	0.44
Sauk River near St. Cloud, Minn.	05270500	2006	3.74	3.41	3.48	2.52	-0.29
Sauk River near St. Cloud, Minn.	05270500	2007	3.34	3.27	3.27	6.72	1.04
Sauk River near St. Cloud, Minn.	05270500	2008	3.66	3.63	3.67	3.09	-0.15
Sauk River near St. Cloud, Minn.	05270500	2009	5.80	5.57	5.34	7.62	0.37
Sauk River near St. Cloud, Minn.	05270500	2010	7.00	6.33	6.42	8.44	0.28
Elk River near Big Lake, Minn.	05275000	1996	6.02	5.99	5.87	2.95	-0.51
Elk River near Big Lake, Minn.	05275000	1997	6.69	6.09	6.16	7.05	0.12
Elk River near Big Lake, Minn.	05275000	1998	4.36	4.18	4.15	3.37	-0.20
Elk River near Big Lake, Minn.	05275000	1999	3.80	3.85	3.78	3.11	-0.18
Elk River near Big Lake, Minn.	05275000	2000	2.32	2.27	2.29	1.44	-0.37
Elk River near Big Lake, Minn.	05275000	2001	6.31	5.69	5.89	9.59	0.61
Elk River near Big Lake, Minn.	05275000	2002	9.93	9.31	9.12	12.62	0.34
Elk River near Big Lake, Minn.	05275000	2003	6.13	5.80	5.78	3.14	-0.47
Elk River near Big Lake, Minn.	05275000	2004	5.37	5.40	5.36	6.48	0.20
Elk River near Big Lake, Minn.	05275000	2005	7.50	7.10	7.11	9.25	0.28
Elk River near Big Lake, Minn.	05275000	2006	5.00	4.78	4.77	2.99	-0.38
Elk River near Big Lake, Minn.	05275000	2007	4.11	4.16	4.14	8.66	1.09
Elk River near Big Lake, Minn.	05275000	2008	4.96	4.87	4.91	5.65	0.15
Elk River near Big Lake, Minn.	05275000	2009	4.89	4.57	4.60	7.79	0.66
Elk River near Big Lake, Minn.	05275000	2010	7.82	7.52	7.50	9.18	0.21

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Rum River near St. Francis, Minn.	05286000	1996	6.18	6.12	6.19	2.88	-0.53
Rum River near St. Francis, Minn.	05286000	1997	5.66	5.42	5.21	6.91	0.27
Rum River near St. Francis, Minn.	05286000	1998	3.40	3.30	3.25	3.80	0.15
Rum River near St. Francis, Minn.	05286000	1999	4.32	3.86	3.92	3.95	-0.02
Rum River near St. Francis, Minn.	05286000	2000	2.61	2.43	2.42	2.21	-0.11
Rum River near St. Francis, Minn.	05286000	2001	7.26	6.65	6.69	10.30	0.50
Rum River near St. Francis, Minn.	05286000	2002	9.43	8.75	8.84	10.25	0.14
Rum River near St. Francis, Minn.	05286000	2003	7.17	6.90	6.82	3.43	-0.51
Rum River near St. Francis, Minn.	05286000	2004	5.22	5.31	5.25	6.10	0.16
Rum River near St. Francis, Minn.	05286000	2005	7.53	7.60	7.43	7.89	0.05
Rum River near St. Francis, Minn.	05286000	2006	5.12	4.78	4.77	2.68	-0.45
Rum River near St. Francis, Minn.	05286000	2007	3.70	3.60	3.58	8.40	1.32
Rum River near St. Francis, Minn.	05286000	2008	5.03	5.36	5.09	6.36	0.23
Rum River near St. Francis, Minn.	05286000	2009	4.43	4.00	4.07	8.04	0.93
Rum River near St. Francis, Minn.	05286000	2010	6.27	5.61	5.70	9.19	0.57
Elk Creek near Champlin, Minn.	05287890	1996	5.27	4.88	5.00	1.82	-0.64
Elk Creek near Champlin, Minn.	05287890	1997	5.17	4.90	4.77	6.47	0.31
Elk Creek near Champlin, Minn.	05287890	1998	3.05	3.05	2.99	2.46	-0.19
Elk Creek near Champlin, Minn.	05287890	1999	5.33	5.10	5.02	1.85	-0.64
Elk Creek near Champlin, Minn.	05287890	2000	1.43	1.38	1.35	0.05	-0.96
Elk Creek near Champlin, Minn.	05287890	2001	7.37	7.58	7.24	6.76	-0.09
Elk Creek near Champlin, Minn.	05287890	2002	12.45	11.69	11.81	13.09	0.09
Elk Creek near Champlin, Minn.	05287890	2003	5.04	5.32	5.11	2.37	-0.54
Elk Creek near Champlin, Minn.	05287890	2004	5.12	4.80	4.77	5.64	0.15
Elk Creek near Champlin, Minn.	05287890	2005	4.54	4.18	4.27	7.66	0.77
Elk Creek near Champlin, Minn.	05287890	2006	3.85	3.70	3.74	3.96	0.05
Elk Creek near Champlin, Minn.	05287890	2007	4.33	4.30	4.29	7.56	0.76
Elk Creek near Champlin, Minn.	05287890	2008	3.61	3.62	3.66	1.95	-0.46
Elk Creek near Champlin, Minn.	05287890	2009	1.91	1.92	1.93	4.42	1.30
Elk Creek near Champlin, Minn.	05287890	2010	4.94	4.79	4.89	6.00	0.23

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Pomme de Terre River at Appleton, Minn.	05294000	1996	3.40	3.26	3.24	2.37	-0.28
Pomme de Terre River at Appleton, Minn.	05294000	1997	4.99	4.89	4.73	5.77	0.19
Pomme de Terre River at Appleton, Minn.	05294000	1998	2.48	2.49	2.47	2.79	0.13
Pomme de Terre River at Appleton, Minn.	05294000	2004	1.99	2.02	2.00	2.73	0.36
Pomme de Terre River at Appleton, Minn.	05294000	2005	3.36	3.33	3.29	2.95	-0.11
Pomme de Terre River at Appleton, Minn.	05294000	2006	3.03	2.91	2.95	1.87	-0.37
Pomme de Terre River at Appleton, Minn.	05294000	2007	2.97	2.86	2.89	5.03	0.73
Pomme de Terre River at Appleton, Minn.	05294000	2008	2.31	2.58	2.52	2.56	0.04
Pomme de Terre River at Appleton, Minn.	05294000	2009	3.95	3.96	4.01	6.60	0.66
Pomme de Terre River at Appleton, Minn.	05294000	2010	5.12	5.02	5.00	6.66	0.32
Chippewa River near Milan, Minn.	05304500	1996	4.66	4.51	4.51	2.29	-0.50
Chippewa River near Milan, Minn.	05304500	1997	5.97	5.87	5.53	5.50	-0.05
Chippewa River near Milan, Minn.	05304500	1998	3.72	3.48	3.45	2.69	-0.24
Chippewa River near Milan, Minn.	05304500	1999	3.93	3.74	3.80	1.20	-0.69
Chippewa River near Milan, Minn.	05304500	2000	1.53	1.49	1.49	0.93	-0.38
Chippewa River near Milan, Minn.	05304500	2001	5.68	5.22	5.06	5.42	0.02
Chippewa River near Milan, Minn.	05304500	2002	2.64	2.54	2.54	2.28	-0.12
Chippewa River near Milan, Minn.	05304500	2003	2.02	1.99	1.97	1.44	-0.28
Chippewa River near Milan, Minn.	05304500	2004	1.90	1.77	1.80	2.69	0.48
Chippewa River near Milan, Minn.	05304500	2005	4.37	4.19	4.11	5.06	0.20
Chippewa River near Milan, Minn.	05304500	2006	3.53	3.39	3.37	2.14	-0.38
Chippewa River near Milan, Minn.	05304500	2007	2.37	2.17	2.20	5.37	1.39
Chippewa River near Milan, Minn.	05304500	2008	1.97	1.88	1.86	2.44	0.28
Chippewa River near Milan, Minn.	05304500	2009	3.46	3.11	3.11	6.78	1.10
Chippewa River near Milan, Minn.	05304500	2010	5.31	4.83	4.98	8.05	0.60
Yellow Medicine River near Granite Falls, Minn.	05313500	1996	3.22	3.01	3.00	1.20	-0.61
Yellow Medicine River near Granite Falls, Minn.	05313500	1997	6.29	5.90	5.45	5.27	-0.10
Yellow Medicine River near Granite Falls, Minn.	05313500	1998	2.26	2.63	2.52	3.55	0.44
Yellow Medicine River near Granite Falls, Minn.	05313500	1999	2.14	1.95	1.95	0.36	-0.82

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Yellow Medicine River near Granite Falls, Minn.	05313500	2000	0.49	0.43	0.45	0.23	-0.49
Yellow Medicine River near Granite Falls, Minn.	05313500	2001	3.31	3.78	3.93	6.05	0.65
Yellow Medicine River near Granite Falls, Minn.	05313500	2002	2.27	2.14	2.11	1.35	-0.38
Yellow Medicine River near Granite Falls, Minn.	05313500	2003	1.02	0.96	0.90	0.59	-0.39
Yellow Medicine River near Granite Falls, Minn.	05313500	2004	1.46	1.40	1.37	3.33	1.36
Yellow Medicine River near Granite Falls, Minn.	05313500	2005	2.21	1.89	1.95	2.59	0.28
Yellow Medicine River near Granite Falls, Minn.	05313500	2006	3.51	3.32	3.26	2.37	-0.30
Yellow Medicine River near Granite Falls, Minn.	05313500	2007	2.79	2.45	2.48	4.62	0.79
Yellow Medicine River near Granite Falls, Minn.	05313500	2008	2.17	2.15	2.09	1.38	-0.35
Yellow Medicine River near Granite Falls, Minn.	05313500	2009	1.46	1.51	1.44	4.89	2.32
Yellow Medicine River near Granite Falls, Minn.	05313500	2010	9.98	9.81	9.30	9.78	0.01
Redwood River near Marshall, Minn.	05315000	1996	3.72	3.45	3.42	1.00	-0.72
Redwood River near Marshall, Minn.	05315000	1997	6.67	5.65	5.76	5.44	-0.10
Redwood River near Marshall, Minn.	05315000	1998	3.59	3.31	3.25	5.08	0.50
Redwood River near Marshall, Minn.	05315000	1999	4.08	3.63	3.72	1.35	-0.65
Redwood River near Marshall, Minn.	05315000	2000	1.44	1.26	1.24	0.67	-0.49
Redwood River near Marshall, Minn.	05315000	2001	5.96	5.46	5.41	6.45	0.15
Redwood River near Marshall, Minn.	05315000	2002	3.11	2.81	2.82	1.80	-0.38
Redwood River near Marshall, Minn.	05315000	2003	1.62	1.39	1.51	1.18	-0.21
Redwood River near Marshall, Minn.	05315000	2004	2.13	1.89	1.82	4.12	1.12
Redwood River near Marshall, Minn.	05315000	2005	2.15	1.96	1.96	2.95	0.46
Redwood River near Marshall, Minn.	05315000	2006	4.03	3.67	3.69	2.99	-0.21
Redwood River near Marshall, Minn.	05315000	2007	4.29	3.97	3.92	5.49	0.35
Redwood River near Marshall, Minn.	05315000	2008	3.12	2.79	2.81	1.86	-0.36
Redwood River near Marshall, Minn.	05315000	2009	1.60	1.48	1.46	4.06	1.68
Redwood River near Marshall, Minn.	05315000	2010	11.56	9.56	9.88	10.62	0.03
Cottonwood River near New Ulm, Minn.	05317000	1996	4.26	3.50	3.61	1.73	-0.54
Cottonwood River near New Ulm, Minn.	05317000	1997	6.75	6.09	6.47	5.08	-0.21
Cottonwood River near New Ulm, Minn.	05317000	1998	3.71	3.39	3.43	2.87	-0.18

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Cottonwood River near New Ulm, Minn.	05317000	1999	3.22	2.89	2.90	0.89	-0.71
Cottonwood River near New Ulm, Minn.	05317000	2000	1.21	0.99	1.01	0.52	-0.52
Cottonwood River near New Ulm, Minn.	05317000	2001	6.14	5.40	5.22	7.62	0.36
Cottonwood River near New Ulm, Minn.	05317000	2002	3.61	3.01	3.10	1.62	-0.50
Cottonwood River near New Ulm, Minn.	05317000	2003	1.94	1.64	1.65	0.45	-0.74
Cottonwood River near New Ulm, Minn.	05317000	2004	2.88	2.51	2.61	4.88	0.83
Cottonwood River near New Ulm, Minn.	05317000	2005	3.59	3.33	3.40	5.25	0.53
Cottonwood River near New Ulm, Minn.	05317000	2006	5.21	4.56	4.56	3.08	-0.35
Cottonwood River near New Ulm, Minn.	05317000	2007	3.73	2.96	3.24	6.06	0.83
Cottonwood River near New Ulm, Minn.	05317000	2008	3.03	2.89	2.97	1.78	-0.40
Cottonwood River near New Ulm, Minn.	05317000	2009	1.72	1.66	1.62	3.99	1.40
Cottonwood River near New Ulm, Minn.	05317000	2010	9.35	7.93	8.15	9.45	0.11
Little Cottonwood River near Courtland, Minn.	05317200	1996	6.72	7.00	6.75	2.58	-0.62
Little Cottonwood River near Courtland, Minn.	05317200	1997	6.66	6.82	6.93	4.65	-0.32
Little Cottonwood River near Courtland, Minn.	05317200	1998	4.02	4.21	4.13	2.39	-0.42
Little Cottonwood River near Courtland, Minn.	05317200	1999	3.72	3.57	3.66	1.08	-0.70
Little Cottonwood River near Courtland, Minn.	05317200	2000	1.81	1.65	1.71	0.95	-0.45
Little Cottonwood River near Courtland, Minn.	05317200	2001	8.97	8.51	8.91	7.48	-0.15
Little Cottonwood River near Courtland, Minn.	05317200	2002	4.20	4.02	4.00	2.06	-0.49
Little Cottonwood River near Courtland, Minn.	05317200	2003	2.06	1.98	2.00	0.14	-0.93
Little Cottonwood River near Courtland, Minn.	05317200	2004	2.40	2.52	2.44	4.71	0.92
Little Cottonwood River near Courtland, Minn.	05317200	2005	4.12	3.83	3.96	6.06	0.53
Little Cottonwood River near Courtland, Minn.	05317200	2006	4.92	5.01	4.94	4.18	-0.16
Little Cottonwood River near Courtland, Minn.	05317200	2007	5.08	4.85	4.91	7.00	0.42
Little Cottonwood River near Courtland, Minn.	05317200	2008	4.22	4.13	4.21	2.26	-0.46
Little Cottonwood River near Courtland, Minn.	05317200	2009	2.67	2.77	2.74	4.55	0.67
Watonwan River near Garden City, Minn.	05319500	1996	5.99	5.59	5.49	2.63	-0.54
Watonwan River near Garden City, Minn.	05319500	1997	7.46	7.82	7.61	3.89	-0.49
Watonwan River near Garden City, Minn.	05319500	1998	4.24	3.85	3.95	2.34	-0.42

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Watonwan River near Garden City, Minn.	05319500	1999	4.25	4.37	4.31	1.36	-0.68
Watonwan River near Garden City, Minn.	05319500	2000	1.29	1.18	1.15	0.97	-0.20
Watonwan River near Garden City, Minn.	05319500	2001	7.65	7.76	7.39	6.51	-0.14
Watonwan River near Garden City, Minn.	05319500	2002	2.18	1.99	2.03	2.31	0.12
Watonwan River near Garden City, Minn.	05319500	2003	2.42	2.17	2.20	0.14	-0.94
Watonwan River near Garden City, Minn.	05319500	2004	3.61	3.43	3.36	4.44	0.28
Watonwan River near Garden City, Minn.	05319500	2005	6.72	6.55	6.39	6.56	0.00
Watonwan River near Garden City, Minn.	05319500	2006	5.94	6.19	6.07	4.68	-0.23
Watonwan River near Garden City, Minn.	05319500	2007	4.70	4.57	4.31	7.42	0.64
Watonwan River near Garden City, Minn.	05319500	2008	4.42	3.93	4.20	2.40	-0.43
Watonwan River near Garden City, Minn.	05319500	2009	2.01	1.99	1.96	5.11	1.57
Watonwan River near Garden City, Minn.	05319500	2010	10.91	10.00	10.10	9.30	-0.10
Le Sueur River near Rapidan, Minn.	05320500	1996	5.14	4.08	4.27	2.63	-0.41
Le Sueur River near Rapidan, Minn.	05320500	1997	6.19	5.17	5.58	4.55	-0.19
Le Sueur River near Rapidan, Minn.	05320500	1998	5.90	5.37	5.21	4.12	-0.25
Le Sueur River near Rapidan, Minn.	05320500	1999	8.06	6.54	7.40	6.24	-0.15
Le Sueur River near Rapidan, Minn.	05320500	2000	4.34	4.45	4.00	3.47	-0.19
Le Sueur River near Rapidan, Minn.	05320500	2001	8.58	8.17	7.84	7.68	-0.06
Le Sueur River near Rapidan, Minn.	05320500	2002	3.90	3.19	3.40	2.84	-0.19
Le Sueur River near Rapidan, Minn.	05320500	2003	3.23	2.71	2.75	0.61	-0.79
Le Sueur River near Rapidan, Minn.	05320500	2004	5.72	3.90	4.68	7.08	0.48
Le Sueur River near Rapidan, Minn.	05320500	2005	6.96	5.98	5.71	5.39	-0.13
Le Sueur River near Rapidan, Minn.	05320500	2006	6.08	6.17	5.98	5.19	-0.15
Le Sueur River near Rapidan, Minn.	05320500	2007	7.56	6.68	6.75	9.26	0.32
Le Sueur River near Rapidan, Minn.	05320500	2008	4.66	4.17	4.17	2.89	-0.33
Le Sueur River near Rapidan, Minn.	05320500	2009	2.64	2.17	2.20	3.75	0.60
Le Sueur River near Rapidan, Minn.	05320500	2010	11.67	10.14	9.92	9.10	-0.14
High Island Creek near Henderson, Minn.	05327000	1996	3.61	3.61	3.63	2.58	-0.29
High Island Creek near Henderson, Minn.	05327000	1997	7.97	7.56	7.46	7.27	-0.05

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
High Island Creek near Henderson, Minn.	05327000	1998	4.82	5.12	4.84	1.81	-0.63
High Island Creek near Henderson, Minn.	05327000	1999	3.74	3.85	3.87	1.38	-0.64
High Island Creek near Henderson, Minn.	05327000	2000	0.68	0.70	0.69	0.07	-0.90
High Island Creek near Henderson, Minn.	05327000	2001	6.24	6.72	6.58	7.55	0.16
High Island Creek near Henderson, Minn.	05327000	2002	3.75	3.66	3.59	4.67	0.27
High Island Creek near Henderson, Minn.	05327000	2003	2.16	2.17	2.19	0.59	-0.73
High Island Creek near Henderson, Minn.	05327000	2004	4.29	4.78	4.74	4.85	0.05
High Island Creek near Henderson, Minn.	05327000	2005	4.86	4.92	5.06	3.93	-0.21
High Island Creek near Henderson, Minn.	05327000	2006	4.47	4.28	4.28	2.83	-0.35
High Island Creek near Henderson, Minn.	05327000	2007	3.15	3.02	3.01	6.46	1.11
High Island Creek near Henderson, Minn.	05327000	2008	2.70	2.61	2.70	1.34	-0.50
High Island Creek near Henderson, Minn.	05327000	2009	3.35	3.82	3.84	6.73	0.83
High Island Creek near Henderson, Minn.	05327000	2010	10.29	9.85	9.85	7.62	-0.24
Kettle River below Sandstone, Minn.	05336700	1996	9.81	9.40	9.52	6.07	-0.37
Kettle River below Sandstone, Minn.	05336700	1997	8.39	7.63	7.83	7.98	0.00
Kettle River below Sandstone, Minn.	05336700	1998	5.64	5.43	5.41	6.49	0.18
Kettle River below Sandstone, Minn.	05336700	1999	9.03	8.34	8.35	6.33	-0.26
Kettle River below Sandstone, Minn.	05336700	2000	6.59	5.66	5.71	3.95	-0.34
Kettle River below Sandstone, Minn.	05336700	2001	8.80	9.32	8.80	10.93	0.22
Kettle River below Sandstone, Minn.	05336700	2002	8.39	7.21	7.50	8.89	0.15
Kettle River below Sandstone, Minn.	05336700	2003	6.94	6.03	6.39	3.54	-0.45
Kettle River below Sandstone, Minn.	05336700	2004	7.15	6.20	6.31	5.55	-0.15
Kettle River below Sandstone, Minn.	05336700	2005	8.30	7.23	7.57	6.30	-0.18
Kettle River below Sandstone, Minn.	05336700	2006	5.19	4.62	4.66	2.61	-0.46
Kettle River below Sandstone, Minn.	05336700	2007	4.66	4.48	4.38	8.51	0.89
Kettle River below Sandstone, Minn.	05336700	2008	8.43	7.76	7.90	7.68	-0.04
Kettle River below Sandstone, Minn.	05336700	2009	6.52	5.73	6.00	8.50	0.40
Kettle River below Sandstone, Minn.	05336700	2010	8.31	7.28	7.30	10.52	0.38

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Snake River near Pine City, Minn.	05338500	1996	7.38	7.48	7.48	2.65	-0.64
Snake River near Pine City, Minn.	05338500	1997	5.92	5.70	5.88	6.04	0.03
Snake River near Pine City, Minn.	05338500	1998	3.48	3.39	3.40	3.89	0.14
Snake River near Pine City, Minn.	05338500	1999	5.56	5.36	5.35	3.78	-0.30
Snake River near Pine City, Minn.	05338500	2000	4.05	4.09	3.92	2.14	-0.47
Snake River near Pine City, Minn.	05338500	2001	9.58	9.68	8.99	9.69	0.03
Snake River near Pine City, Minn.	05338500	2002	9.55	8.87	9.12	8.47	-0.08
Snake River near Pine City, Minn.	05338500	2003	7.02	6.48	6.70	2.79	-0.59
Snake River near Pine City, Minn.	05338500	2004	5.84	5.89	5.93	4.15	-0.29
Snake River near Pine City, Minn.	05338500	2005	8.42	7.97	8.27	6.39	-0.22
Snake River near Pine City, Minn.	05338500	2006	4.37	4.23	4.16	1.94	-0.54
Snake River near Pine City, Minn.	05338500	2007	4.88	5.18	4.94	7.42	0.48
Snake River near Pine City, Minn.	05338500	2008	8.00	8.56	8.53	6.77	-0.19
Snake River near Pine City, Minn.	05338500	2009	6.11	5.62	5.93	7.35	0.25
Snake River near Pine City, Minn.	05338500	2010	9.44	8.50	8.68	8.18	-0.08
Vermillion River near Empire, Minn.	05345000	1996	6.76	6.60	6.59	6.29	-0.05
Vermillion River near Empire, Minn.	05345000	1997	10.59	10.20	10.33	11.30	0.09
Vermillion River near Empire, Minn.	05345000	1998	12.24	12.12	11.88	9.30	-0.23
Vermillion River near Empire, Minn.	05345000	1999	8.60	8.27	8.23	6.10	-0.27
Vermillion River near Empire, Minn.	05345000	2000	6.20	5.90	6.01	3.84	-0.36
Vermillion River near Empire, Minn.	05345000	2001	7.46	7.20	7.28	8.22	0.12
Vermillion River near Empire, Minn.	05345000	2002	9.69	8.87	9.16	11.09	0.20
Vermillion River near Empire, Minn.	05345000	2003	6.07	5.85	5.85	2.35	-0.60
Vermillion River near Empire, Minn.	05345000	2004	5.99	5.90	5.83	6.42	0.09
Vermillion River near Empire, Minn.	05345000	2005	6.78	6.45	6.54	7.20	0.09
Vermillion River near Empire, Minn.	05345000	2006	5.75	5.67	5.64	5.39	-0.05
Vermillion River near Empire, Minn.	05345000	2007	5.74	5.68	5.62	9.59	0.69
Vermillion River near Empire, Minn.	05345000	2008	4.89	4.64	4.69	4.22	-0.11
Vermillion River near Empire, Minn.	05345000	2009	3.00	2.93	2.91	5.61	0.90
Vermillion River near Empire, Minn.	05345000	2010	7.56	7.26	7.43	8.67	0.17

Table 2-1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Cannon River at Welch, Minn.	05355200	1996	5.79	5.32	5.38	4.17	-0.24
Cannon River at Welch, Minn.	05355200	1997	8.99	8.28	8.52	7.53	-0.12
Cannon River at Welch, Minn.	05355200	1998	9.11	8.01	8.26	6.09	-0.28
Cannon River at Welch, Minn.	05355200	1999	8.53	7.76	7.81	7.84	-0.02
Cannon River at Welch, Minn.	05355200	2000	6.04	5.68	5.46	3.90	-0.32
Cannon River at Welch, Minn.	05355200	2001	8.77	8.43	8.46	8.41	-0.02
Cannon River at Welch, Minn.	05355200	2002	6.37	5.81	5.84	6.23	0.04
Cannon River at Welch, Minn.	05355200	2003	4.53	4.12	4.12	1.34	-0.68
Cannon River at Welch, Minn.	05355200	2004	7.10	6.31	6.28	7.69	0.17
Cannon River at Welch, Minn.	05355200	2005	6.77	5.99	6.11	5.45	-0.13
Cannon River at Welch, Minn.	05355200	2006	6.10	5.58	5.73	5.11	-0.12
Cannon River at Welch, Minn.	05355200	2007	7.80	6.72	6.66	10.53	0.49
Cannon River at Welch, Minn.	05355200	2008	5.88	5.47	5.51	3.60	-0.36
Cannon River at Welch, Minn.	05355200	2009	3.14	2.95	2.96	3.95	0.31
Cannon River at Welch, Minn.	05355200	2010	10.21	8.26	8.55	8.97	-0.00
South Fork Zumbro River at Rochester, Minn.	05372995	1996	5.72	5.00	5.10	4.72	-0.11
South Fork Zumbro River at Rochester, Minn.	05372995	1997	7.16	6.62	6.83	5.35	-0.22
South Fork Zumbro River at Rochester, Minn.	05372995	1998	7.24	6.91	6.81	5.63	-0.19
South Fork Zumbro River at Rochester, Minn.	05372995	1999	8.53	8.03	7.93	13.71	0.68
South Fork Zumbro River at Rochester, Minn.	05372995	2000	6.13	6.03	5.60	6.00	0.01
South Fork Zumbro River at Rochester, Minn.	05372995	2001	9.61	9.08	8.78	9.41	0.03
South Fork Zumbro River at Rochester, Minn.	05372995	2002	6.23	5.65	5.74	3.99	-0.32
South Fork Zumbro River at Rochester, Minn.	05372995	2003	4.44	4.09	4.11	2.05	-0.51
South Fork Zumbro River at Rochester, Minn.	05372995	2004	6.98	6.60	6.35	7.27	0.09
South Fork Zumbro River at Rochester, Minn.	05372995	2005	5.43	4.87	4.98	4.53	-0.11
South Fork Zumbro River at Rochester, Minn.	05372995	2006	6.64	6.34	6.23	5.92	-0.08
South Fork Zumbro River at Rochester, Minn.	05372995	2007	11.62	10.15	10.42	12.39	0.15
South Fork Zumbro River at Rochester, Minn.	05372995	2008	8.61	7.86	7.92	5.11	-0.37
South Fork Zumbro River at Rochester, Minn.	05372995	2009	4.50	4.18	4.14	4.04	-0.06
South Fork Zumbro River at Rochester, Minn.	05372995	2010	8.73	8.04	7.68	8.38	0.03

Table 2–1. Annual mean base-flow estimates rates from 1996–2010 using three hydrograph separation techniques for the 35 streamgages used in model calibration analysis in comparison to the estimated annual potential recharge rates for the same period from the Soil-Water-Balance (SWB) model.—Continued

USGS streamgage name or statistic	USGS streamgage number	Year	Base-flow estimate (in/yr)			Potential recharge rate from SWB model (in/yr)	Relative error ^c
			PART ^a (in/yr)	HYSEP fixed-interval method ^b	HYSEP sliding method ^b		
Cedar River near Austin, Minn.	05457000	1996	5.74	5.09	5.15	3.34	-0.37
Cedar River near Austin, Minn.	05457000	1997	7.22	6.89	6.82	4.49	-0.36
Cedar River near Austin, Minn.	05457000	1998	8.04	7.65	7.52	4.98	-0.36
Cedar River near Austin, Minn.	05457000	1999	9.51	9.23	9.08	11.59	0.25
Cedar River near Austin, Minn.	05457000	2000	6.85	6.27	6.24	5.23	-0.19
Cedar River near Austin, Minn.	05457000	2001	9.39	8.95	9.08	9.50	0.04
Cedar River near Austin, Minn.	05457000	2002	4.36	4.03	4.04	2.44	-0.41
Cedar River near Austin, Minn.	05457000	2003	4.34	4.19	4.35	1.35	-0.68
Cedar River near Austin, Minn.	05457000	2004	8.33	7.14	7.36	8.77	0.15
Cedar River near Austin, Minn.	05457000	2005	6.49	6.19	5.95	4.82	-0.22
Cedar River near Austin, Minn.	05457000	2006	7.70	7.53	7.64	7.10	-0.07
Cedar River near Austin, Minn.	05457000	2007	10.29	9.58	9.59	10.30	0.05
Cedar River near Austin, Minn.	05457000	2008	6.48	6.61	6.23	6.00	-0.07
Cedar River near Austin, Minn.	05457000	2009	5.23	4.54	4.65	4.40	-0.08
Cedar River near Austin, Minn.	05457000	2010	9.22	8.61	8.57	7.85	-0.11
Minimum	NA	NA	0.30	0.32	0.30	0.05	-0.96
Maximum	NA	NA	12.45	13.13	12.80	13.71	2.95

^aRutledge (1998).

^bSloto and Crouse (1996).

^cThe relative error is the SWB potential recharge estimate to the mean of the three different base-flow estimates (equation 7).

Appendix 3. Annual Mean Potential Recharge Estimates, 1996–2010

This section presents the annual mean potential recharge maps for each year from 1996 through 2010 (figs. 3–1 through 3–15). As mentioned within the section “Annual Mean Potential Recharge Estimates,” the mean annual potential recharge estimate for the period 1996–2010 (fig. 9) is the best estimate of potential recharge. Although the annual mean potential recharge maps are useful for comparing years with high recharge rates to years with low recharge rates, these maps should only be used as a guide for the range of potential recharge values because of the lag-time issue explained in the report.

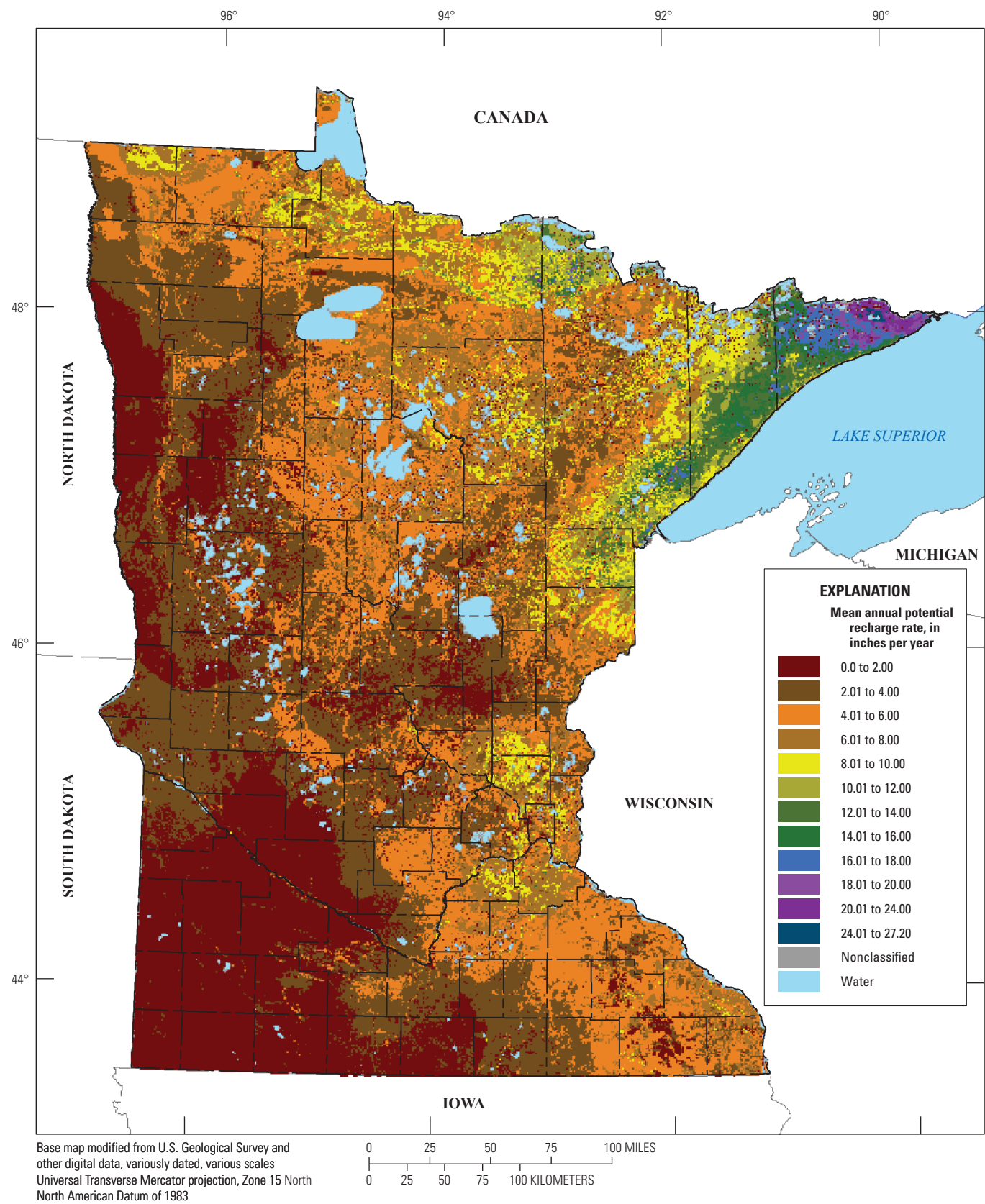


Figure 3–1. Annual mean potential recharge for 1996, based on results from the Minnesota Soil-Water-Balance (SWB) model.

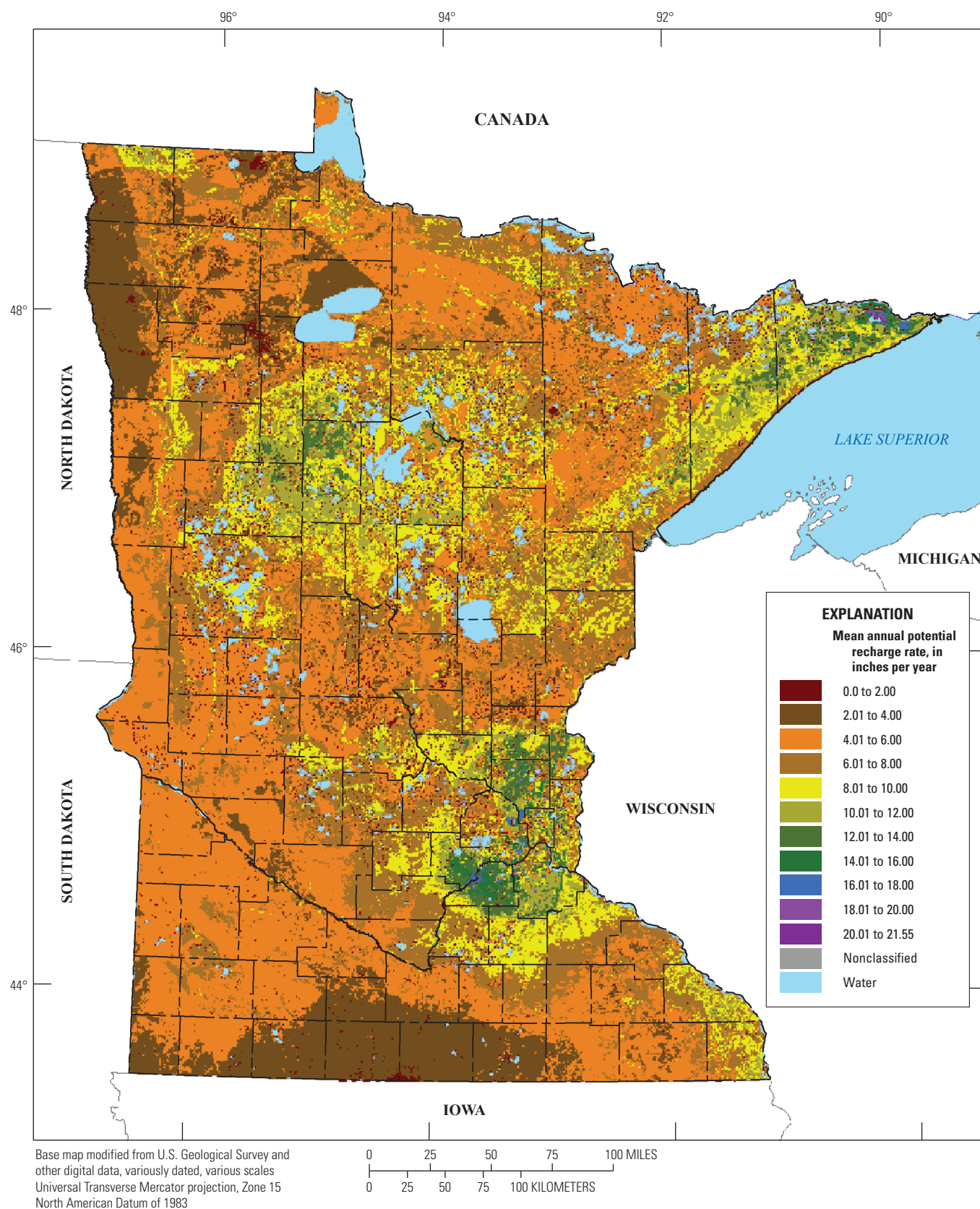


Figure 3–2. Annual mean potential recharge for 1997, based on results from the Minnesota Soil-Water-Balance (SWB) model.

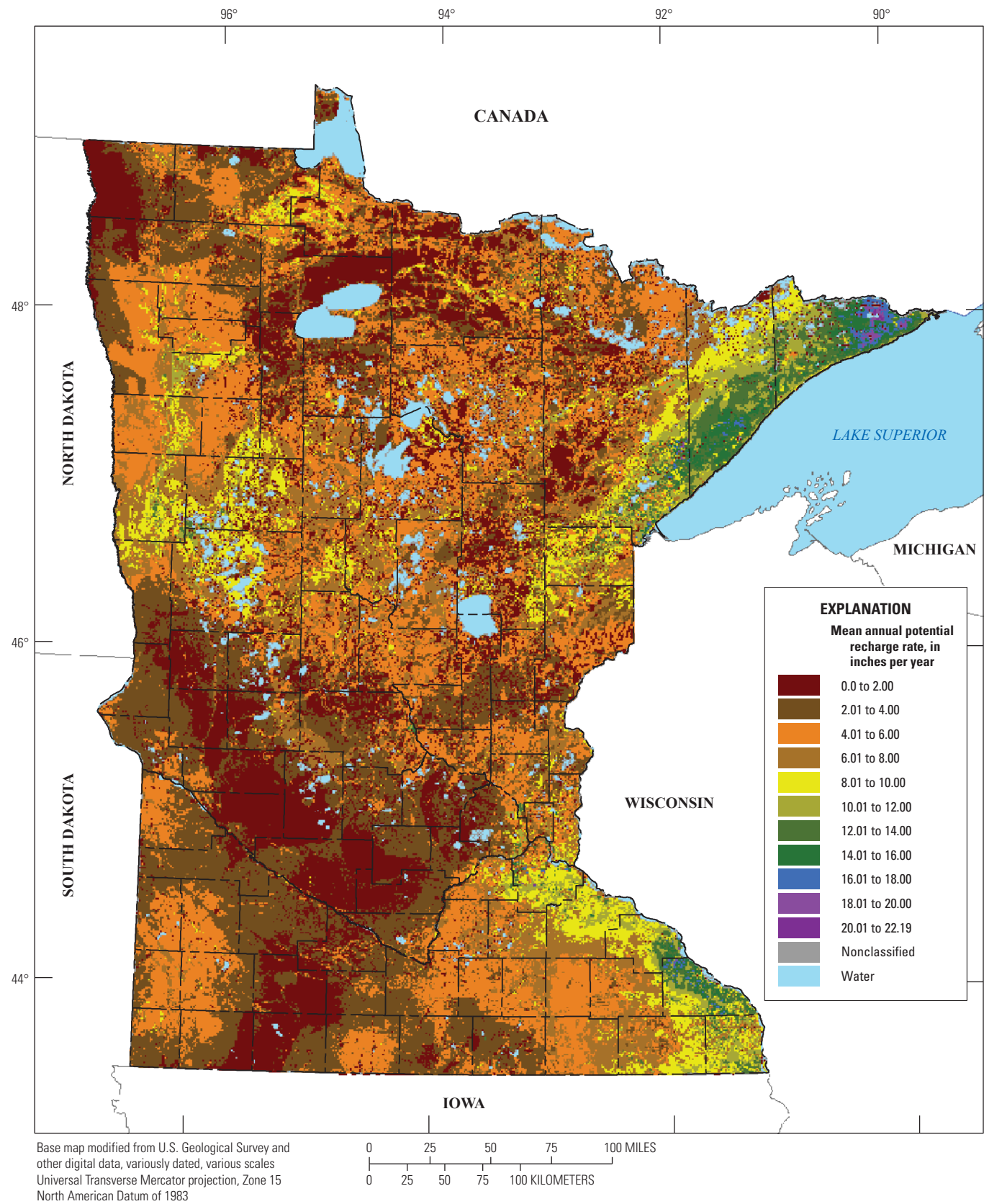


Figure 3–3. Annual mean potential recharge for 1998, based on results from the Minnesota Soil-Water-Balance (SWB) model.

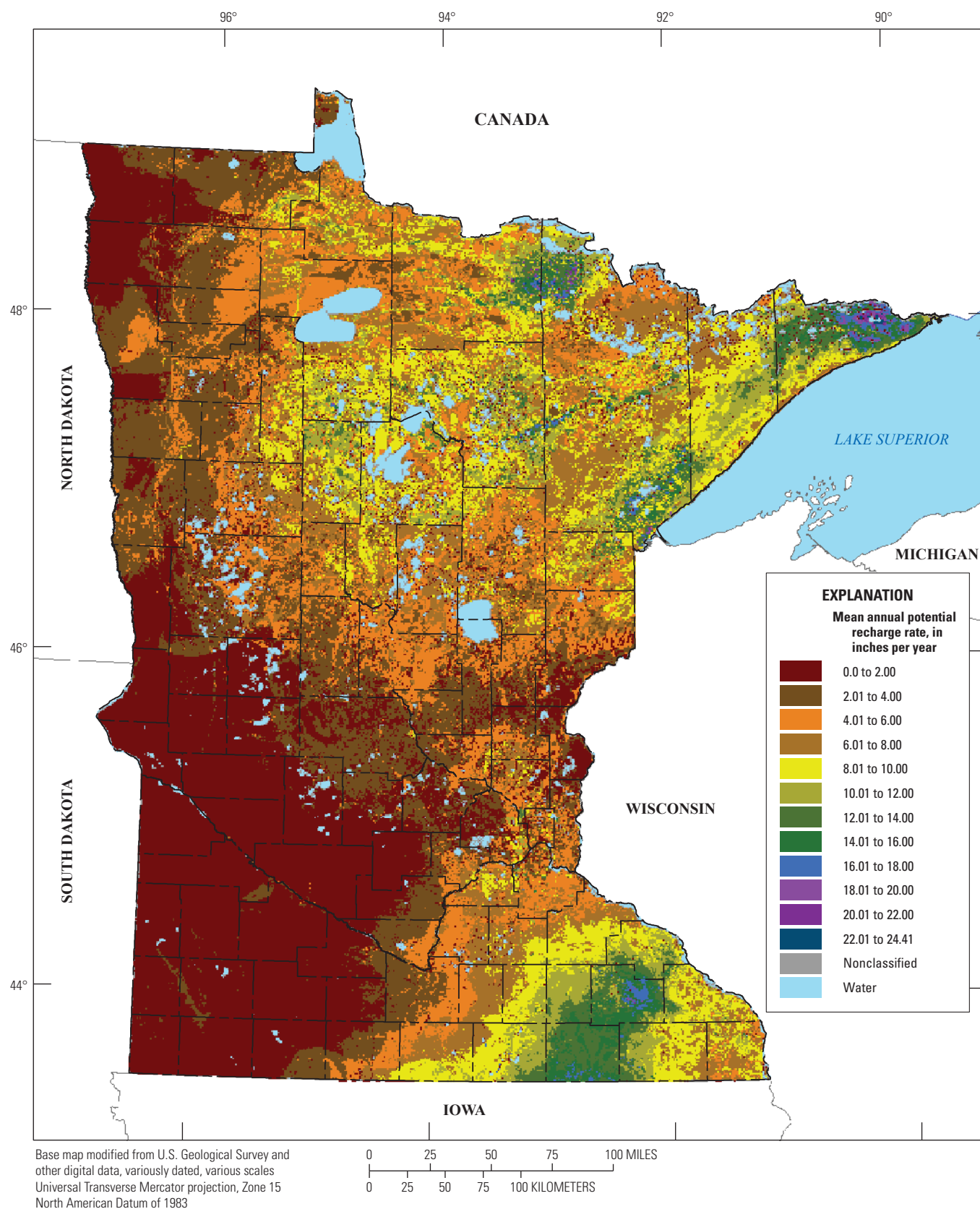


Figure 3-4. Annual mean potential recharge for 1999, based on results from the Minnesota Soil-Water-Balance (SWB) model.

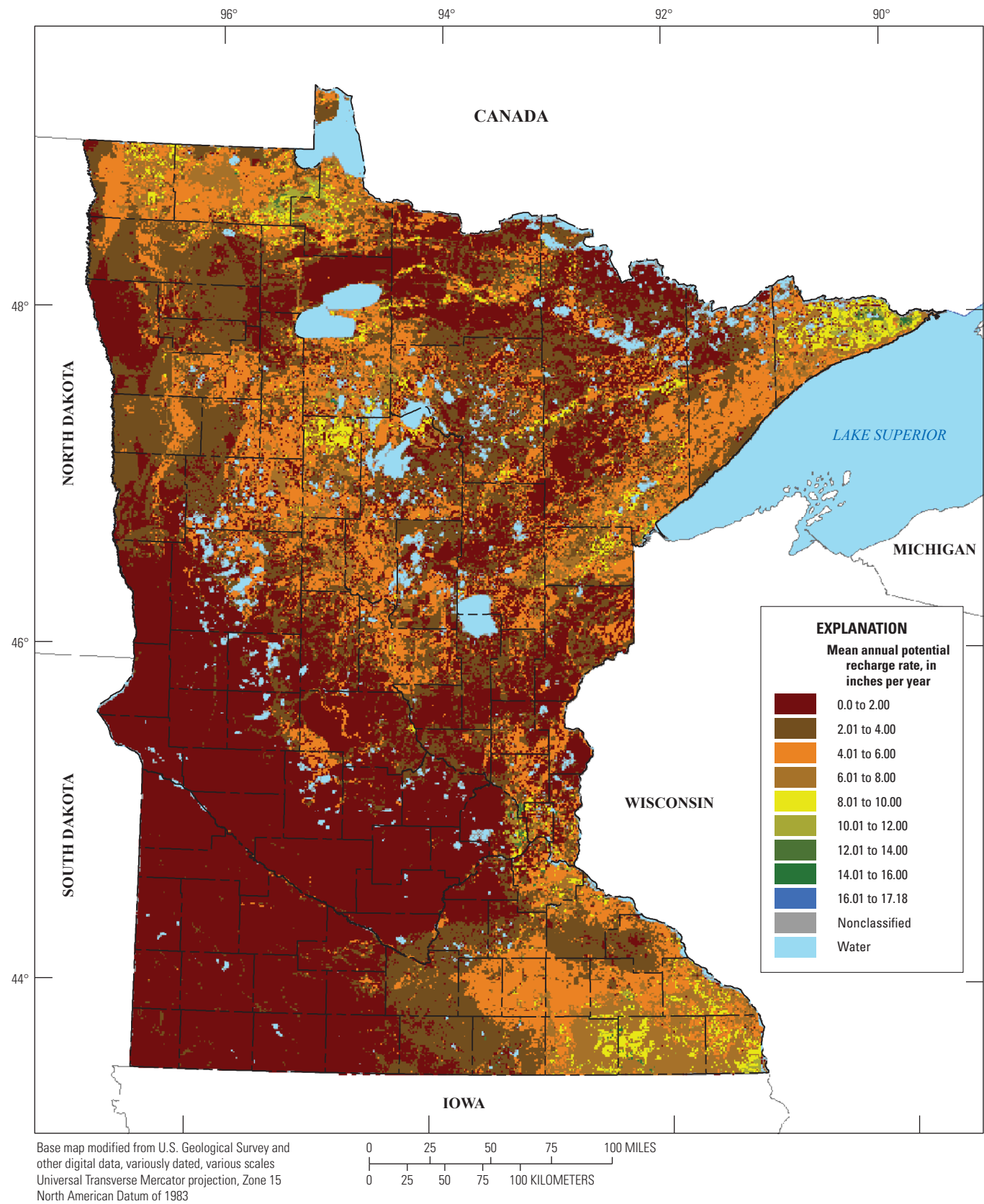


Figure 3–5. Annual mean potential recharge for 2000, based on results from the Minnesota Soil-Water-Balance (SWB) model.

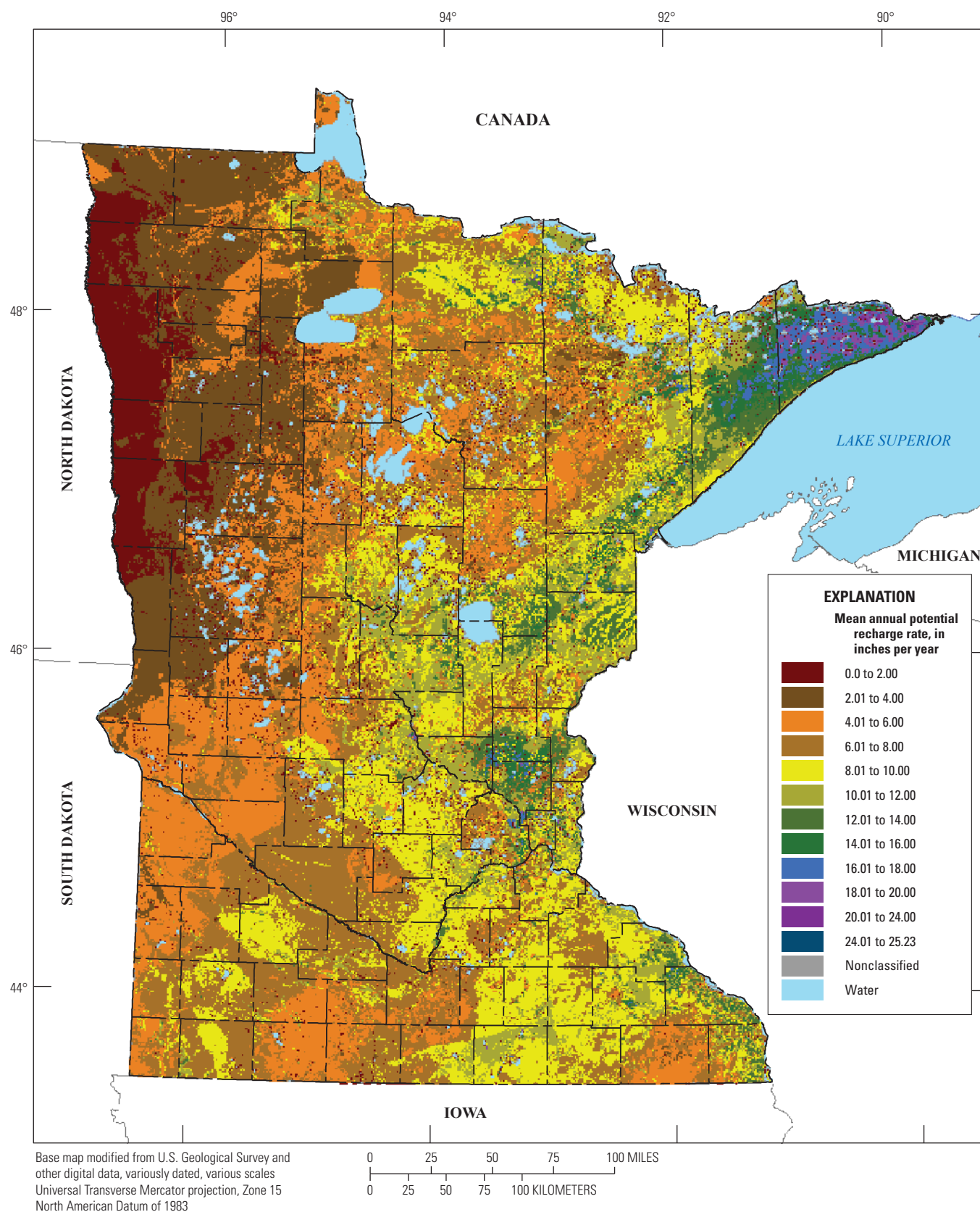


Figure 3–6. Annual mean potential recharge for 2001, based on results from the Minnesota Soil-Water-Balance (SWB) model.

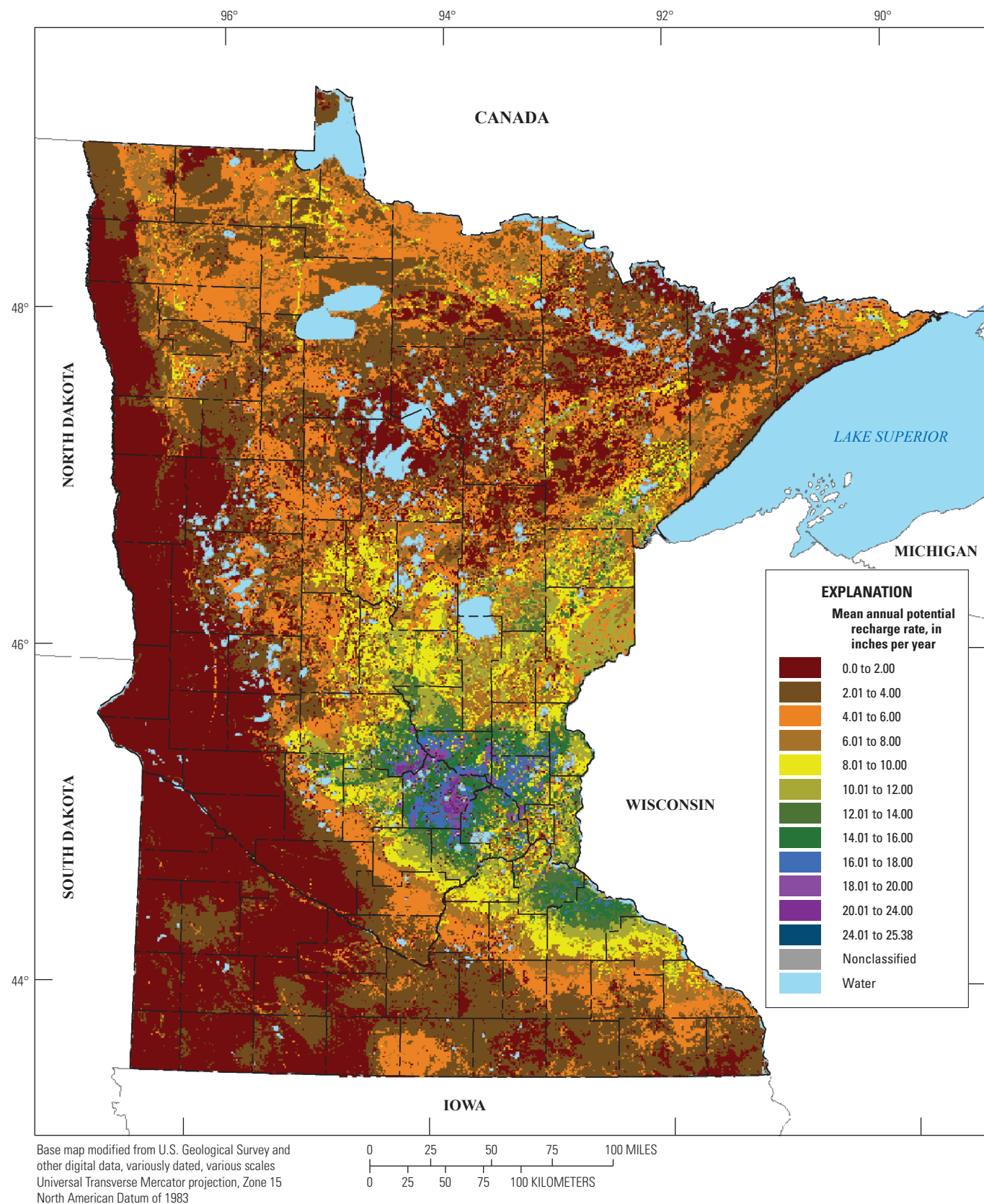


Figure 3–7. Annual mean potential recharge for 2002, based on results from the Minnesota Soil-Water-Balance (SWB) model.

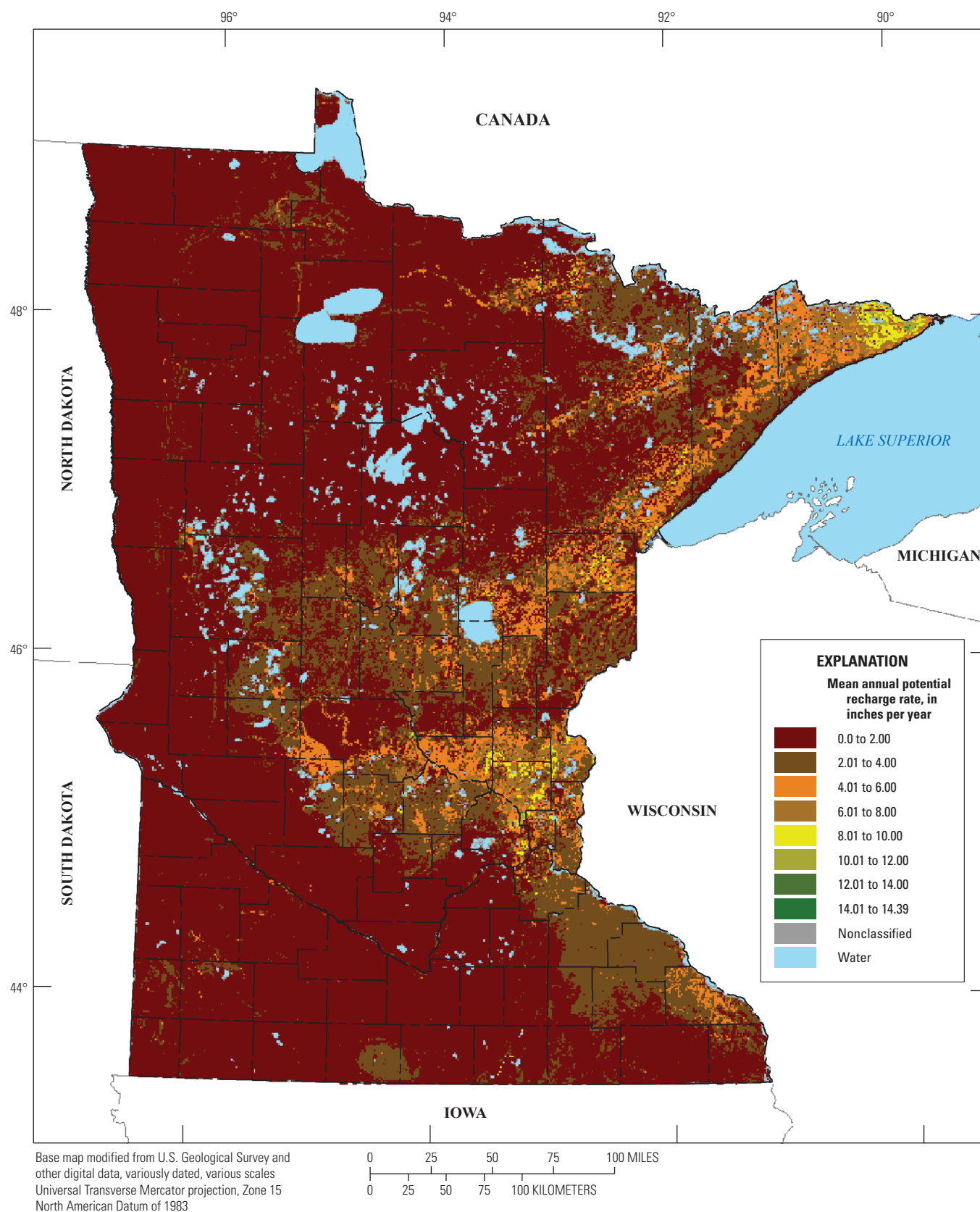


Figure 3–8. Annual mean potential recharge for 2003, based on results from the Minnesota Soil-Water-Balance (SWB) model.

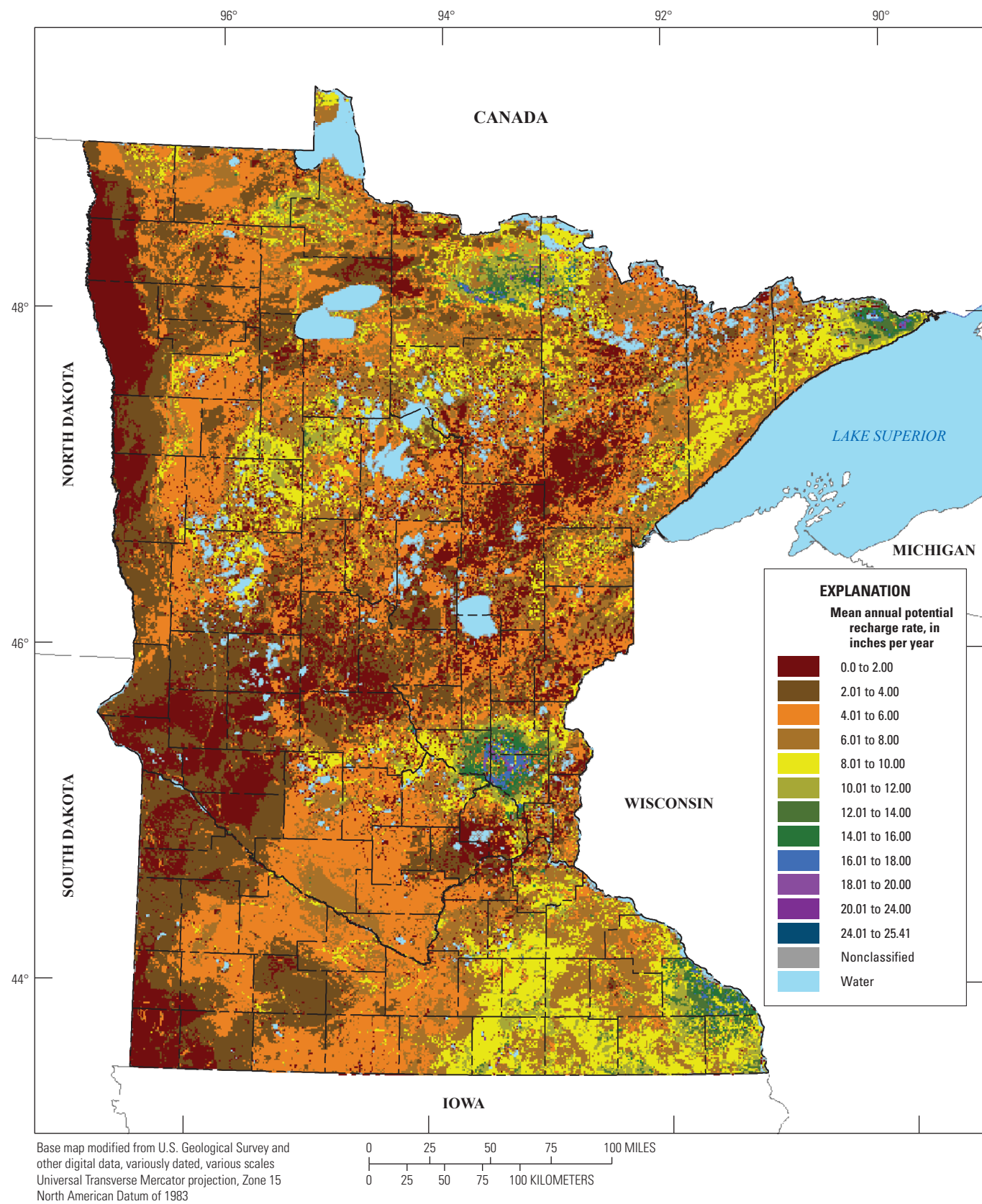


Figure 3–9. Annual mean potential recharge for 2004, based on results from the Minnesota Soil-Water-Balance (SWB) model.

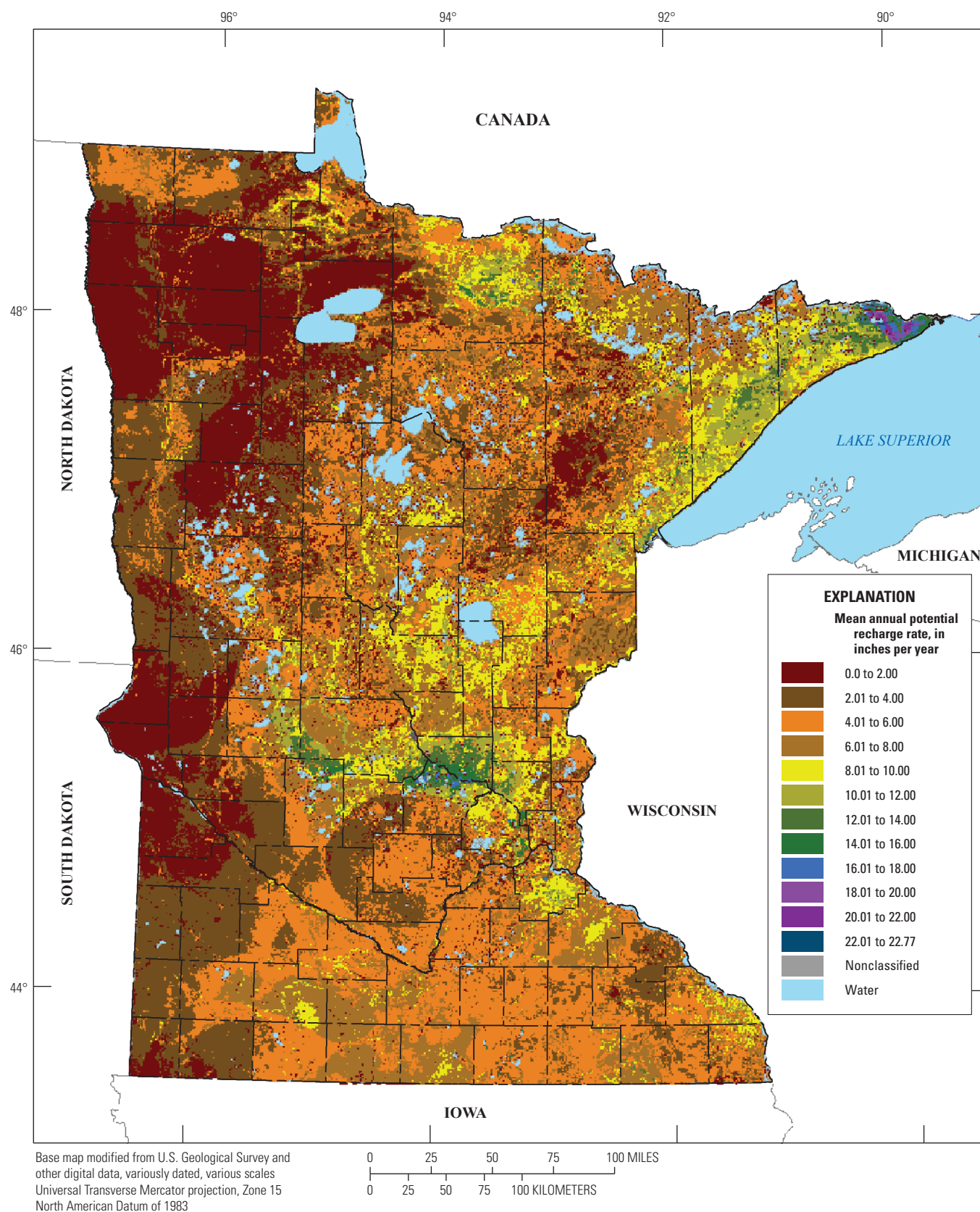


Figure 3–10. Annual mean potential recharge for 2005, based on results from the Minnesota Soil-Water-Balance (SWB) model.

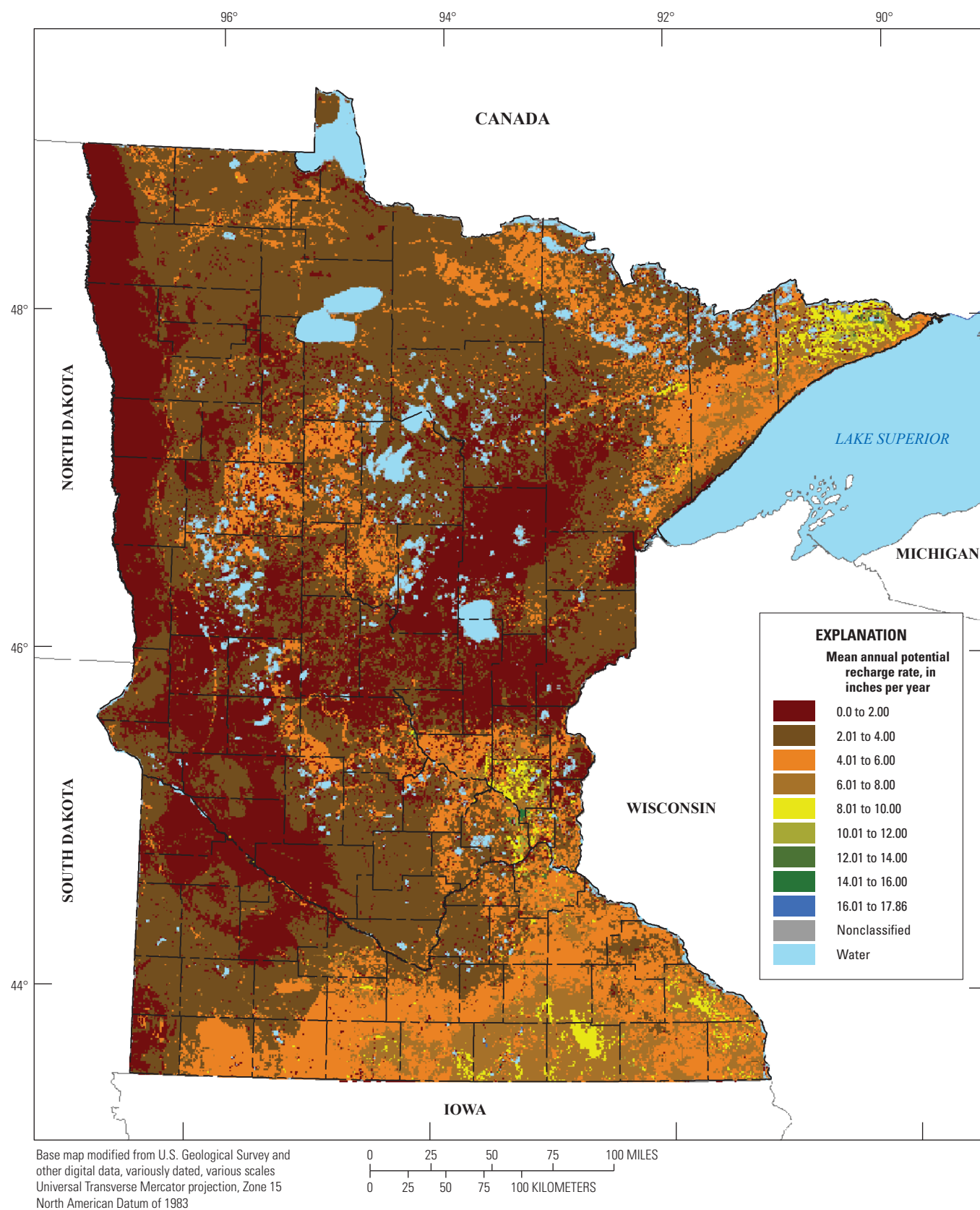


Figure 3–11. Annual mean potential recharge for 2006, based on results from the Minnesota Soil-Water-Balance (SWB) model.

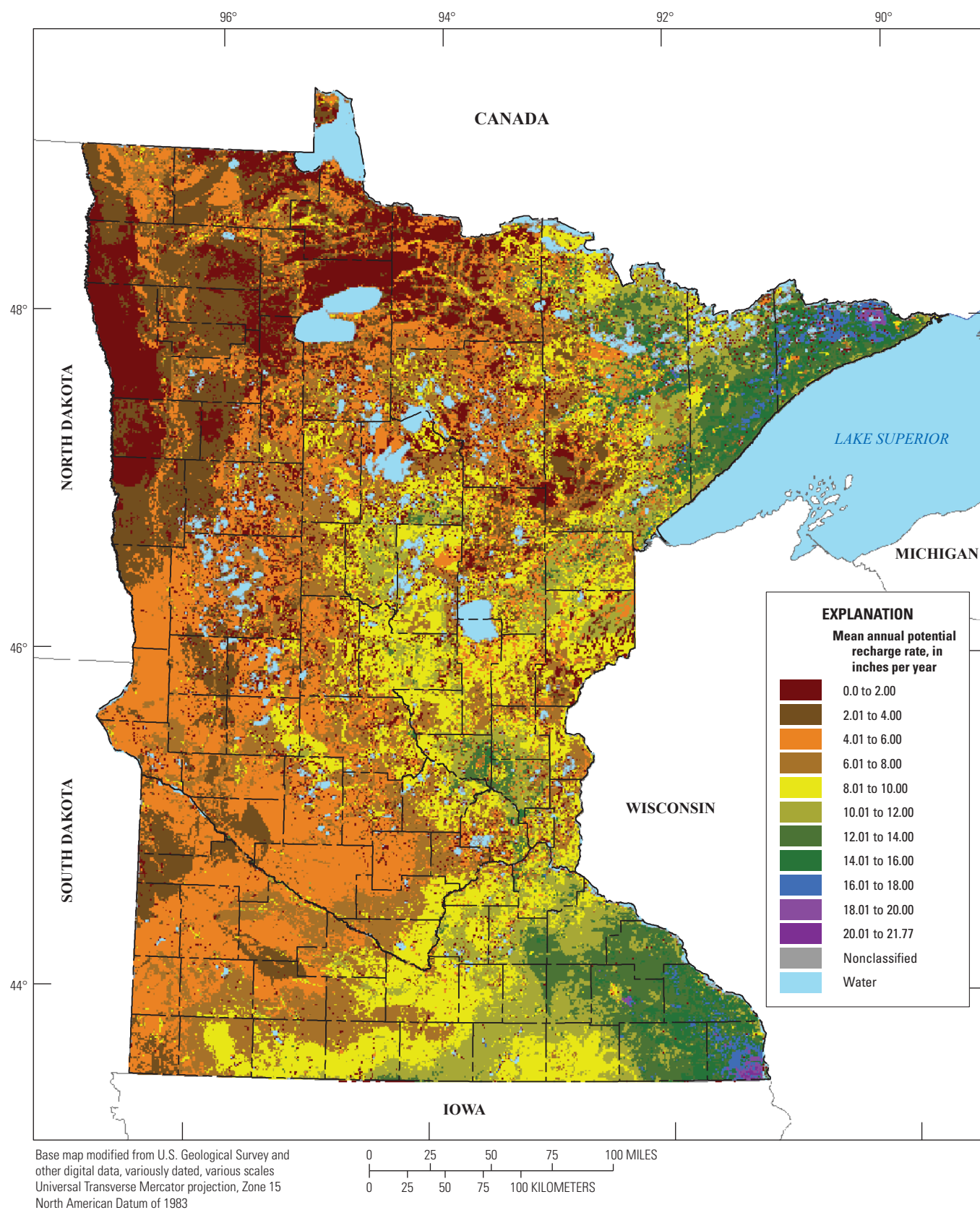


Figure 3–12. Annual mean potential recharge for 2007, based on results from the Minnesota Soil-Water-Balance (SWB) model.

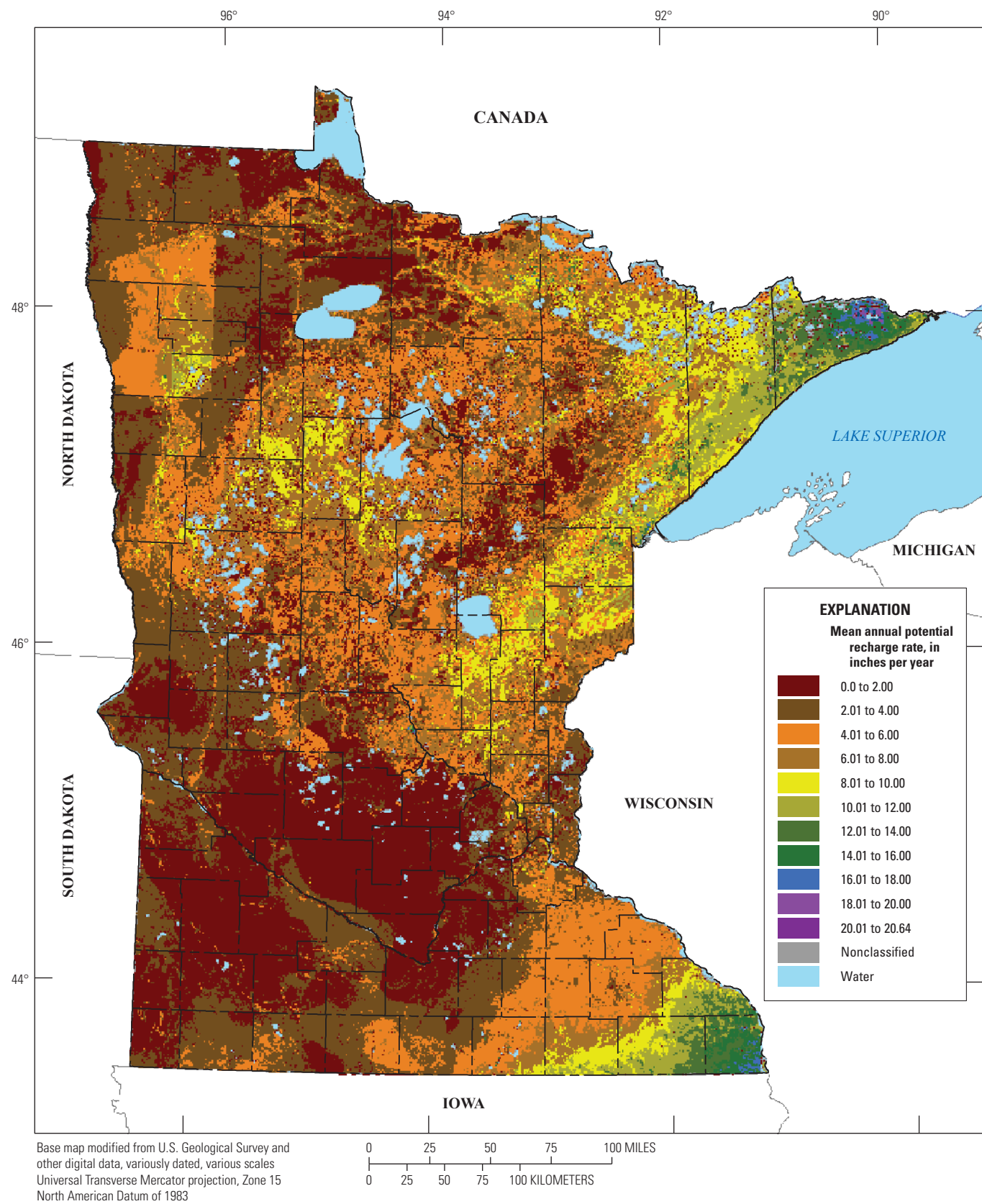


Figure 3–13. Annual mean potential recharge for 2008, based on results from the Minnesota Soil-Water-Balance (SWB) model.

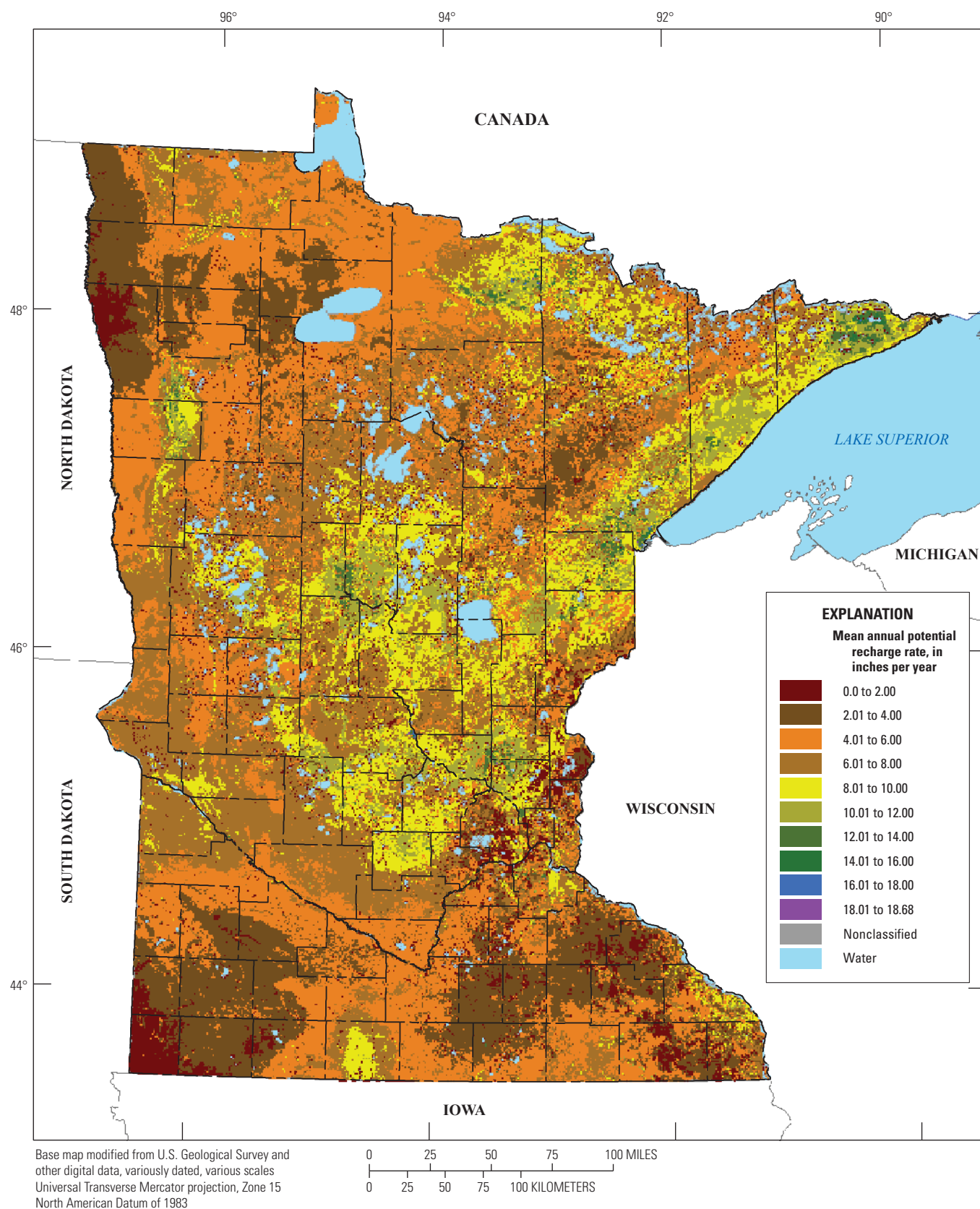


Figure 3–14. Annual mean potential recharge for 2009, based on results from the Minnesota Soil-Water-Balance (SWB) model.

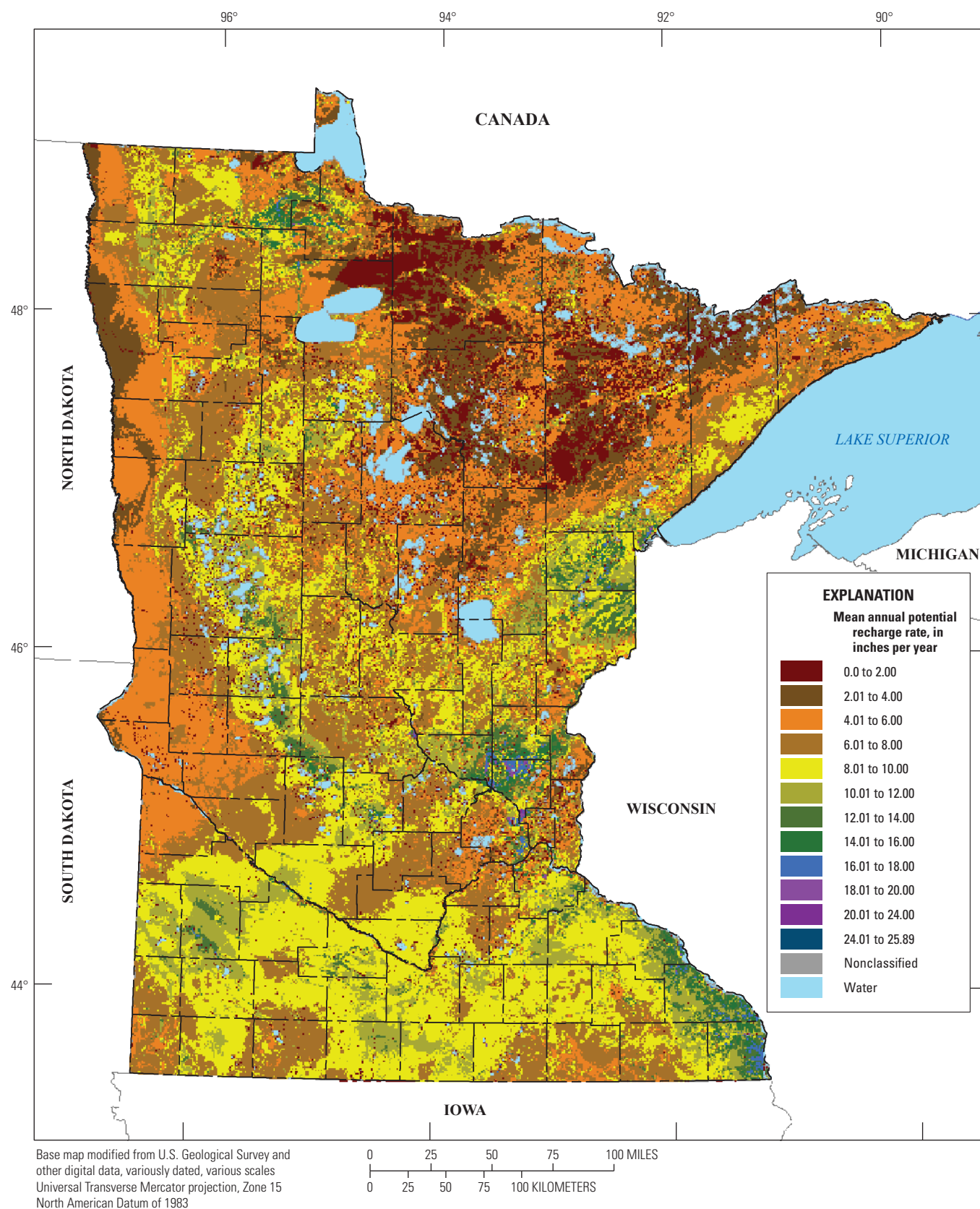


Figure 3–15. Annual mean potential recharge for 2010, based on results from the Minnesota Soil-Water-Balance (SWB) model.

Appendix 4. Regional Regression Recharge, 1971–2000

This section presents figure 4–1, which reproduces the Delin and others (2007) mean annual recharge rates to surficial materials, from 1971 through 2000, for the State of Minnesota.

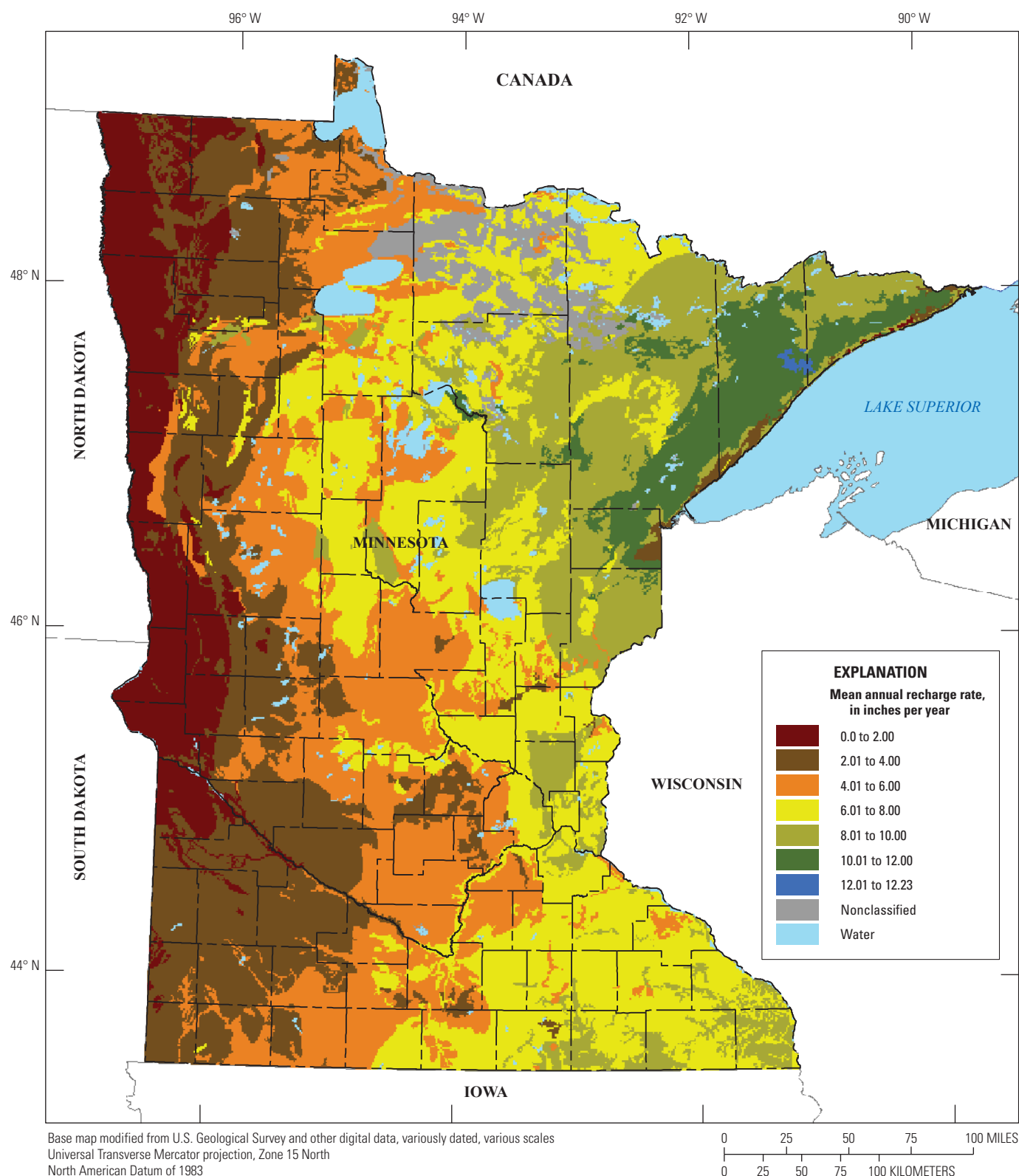


Figure 4–1. Mean annual recharge rates to surficial materials in Minnesota from 1971–2000 based on the regional regression recharge model of Delin and others (2007).

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