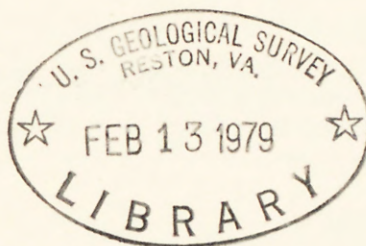






78-18



# Unsteady Solute-Transport Simulation in Streamflow Using a Finite-Difference Model

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**U.S. GEOLOGICAL SURVEY**

**Water-Resources Investigations 78-18**

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By Larry F. Land

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UNITED STATES DEPARTMENT OF THE INTERIOR

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GEOLOGICAL SURVEY

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## FACTORS FOR CONVERTING U.S. CUSTOMARY UNITS TO INTERNATIONAL SYSTEM (SI) UNITS

<u>Multiply U.S. Customary units</u>	<u>By</u>	<u>To obtain metric units</u>
foot (ft)	0.3048	meter (m)
cubic foot per second (ft <sup>3</sup> /s)	$2.832 \times 10^{-2}$	cubic meter per second (m <sup>3</sup> /s)
pound	453.6	gram (g)







# UNSTEADY SOLUTE-TRANSPORT SIMULATION IN STREAMFLOW USING A FINITE-DIFFERENCE MODEL

By Larry F. Land

## ABSTRACT

A computer program for simulating one-dimensional, unsteady solute transport in gradually varied streamflow has been developed and documented. Before using the solute-transport model, a flow model must be used to calculate and store the necessary flow data at each cross section and each time step. Such a flow model is available and documented. Given the flow and solute-inflow data, the digital model will calculate a time-series of concentration values for any point in the stream.

The conservative form of the mass-transport equation has been selected as the basis of the model. The solution of the equation is obtained with an implicit finite-difference method. The grid arrangement uses six nodal points and calculates the spatial and temporal derivatives at a slightly off-centered point. The off-centering is a compromise between numerical dispersion and accuracy. A tridiagonal matrix is created and solved at each time step by the Thomas algorithm.

The solute-transport model allows the solute to enter the stream at an unsteady rate from the upstream boundary and tributaries. A steady inflow of solute can enter the stream with lateral seepage. An unsteady solute flux, uniform over the reach, from a source or sink can be taken into account. The solute concentration can decay by using a constant decay coefficient.

## INTRODUCTION

A number of investigators have simulated mass transport in unsteady streamflow using numerical methods. Many of the studies were made in estuaries. However, a very limited amount of mass-transport modeling is done outside the academic and research communities. Possibly, the lack of outside use is due to the lack of model documentation in a user's format. The purpose of this report is to document a rather simple, general purpose, one-dimensional, one-parameter, mass-transport model for field use. The model assumes a well-mixed conservative solute that may be coming from an unsteady source and is moving in unsteady streamflow. The quantity of solute being transported is in the units of concentration. Results are reported as such.

The use of a solute transport model requires that the flow characteristics be defined at each cross section at each time step. In effect, this requires a streamflow model to calculate and temporarily store the needed values for use in the transport model. The Deterministic Models Project, U.S. Geological Survey (Land, 1978), has recently documented a streamflow model that is designed to supply the needed data.

An implicit finite-difference technique is used to solve the mass transport equation. It consists of creating a tridiagonal matrix and using the Thomas algorithm to solve the matrix for the unknown concentrations at the new time step. The computer program (J880) presented in this report is designed to compute the concentration of a water-quality constituent at any point and at any preselected time in a one-dimensional stream. The model is driven by the inflowing concentration of solute at the upstream boundary and is influenced by the solute entering the stream from tributaries and lateral ground-water inflow and from a source or sink.

#### ACKNOWLEDGMENT

The author wishes to acknowledge T. N. Keefer of SUTRON, Inc., formerly of the U.S. Geological Survey, as the original author of the model's concept and for his early testing and development.

#### BASIS FOR MODEL DEVELOPMENT

The basic equation describing one-dimensional mass transport of a conservative water-quality constituent has the form

$$\frac{\partial AC}{\partial t} + \frac{\partial AUC}{\partial x} = \frac{\partial}{\partial x} \left( AD \frac{\partial C}{\partial x} \right) \quad (1)$$

where

- A = cross-section area (square feet)
- U = cross-section average velocity (feet per second)
- C = concentration (pounds per cubic foot)
- D = dispersion coefficient (square feet per second)
- t = time (seconds)
- x = longitudinal distance (feet)

Substituting the continuity equation of water, assuming incompressibility,

$$\frac{\partial A}{\partial t} + \frac{\partial AU}{\partial x} = 0 \quad (2)$$

into an expanded form of equation 1

$$A \frac{\partial C}{\partial t} + C \frac{\partial A}{\partial t} + AU \frac{\partial C}{\partial x} + C \frac{\partial AU}{\partial x} = \frac{\partial}{\partial x} \left( AD \frac{\partial C}{\partial x} \right) \quad (3)$$



and simplifying, the remaining terms form the equation, after dividing by A

$$\frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} = \frac{1}{A} \left[ \frac{\partial}{\partial x} AD \frac{\partial C}{\partial x} \right] \quad (4)$$

Equation 4 is called the advection form without any assumptions. Equation 1 is generally known as the conservation form of the transport equation and was selected for the basic equation in this model. For a better description of field-boundary conditions, equation 1 was modified to include the solute fluxes from source or sink, lateral ground-water and tributary flow. The equation becomes:

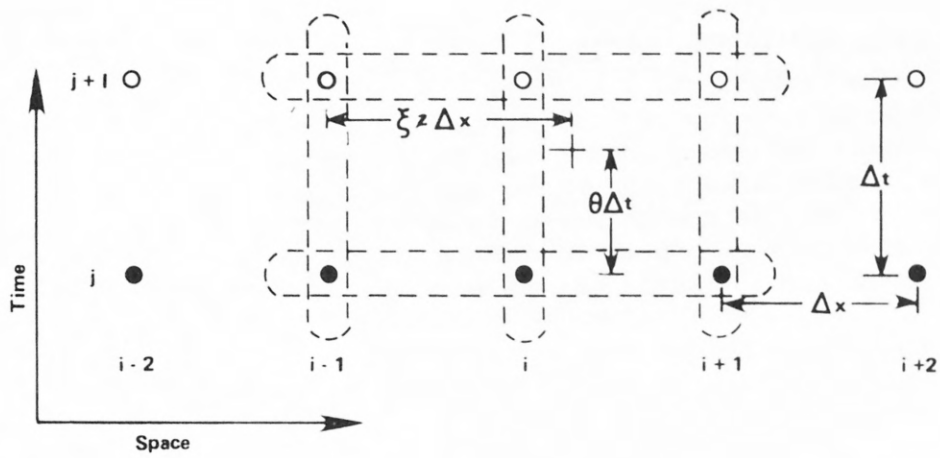
$$\frac{\partial AC}{\partial t} + \frac{\partial UAC}{\partial x} = \frac{\partial}{\partial x} (AD \frac{\partial C}{\partial x}) + \phi_{ss} + \phi_q + \phi_T - KAC \quad (5)$$

where

- K = decay coefficient (one per second)
- $\phi_{ss}$  = flux of solute to source or sink per unit length of stream (pounds per foot per second)
- $\phi_q$  = flux of solute from ground-water seepage per unit length of stream (pounds per foot per second)
- $\phi_T$  = flux of solute from tributary (pounds per foot per second)

Since the equations are linear in the transport variable, the solution with numerical methods is rather straight forward. Most of the modeling efforts in the past have dealt with ways to minimize numerical dispersion along steep concentration fronts. The selected numerical method is very similar to the implicit finite-difference scheme originally presented by Stone and Brian (1963). It uses a centered six-point grid that considers all six points in the time derivative. However, the finite-difference scheme was slightly modified by moving the point somewhat off-centered with weighting coefficients in which to evaluate the space and time derivatives. The computation stencil for the selected scheme is shown in figure 1. The point at which the derivatives was computed was moved slightly forward in time and slightly upstream in space to reduce oscillations when sudden concentration changes occur. Even with this compromise, some oscillations may result. It is particularly noticed in the form of occasional small negative concentration values. The scheme has unconditional stability; thereby allowing a time step of reasonable length for computational efficiency. However, it is desirable for purposes of accuracy to keep the value of  $U \frac{\Delta t}{\Delta x}$ , often called the Courant number, equal to or less than 2.

Solving the equations for the concentrations at the new time step is accomplished by creating a tridiagonal matrix of coefficients for the unknown concentration and a vector of known values and applying the Thomas algorithm (von Rosenberg, 1969). For n grid points, n-2 linear equations are available which have the form



● Known concentrations

○ Unknown concentrations

$\frac{\delta f}{\delta t}$  computed at each vertical band

$\frac{\delta f}{\delta x}, \frac{\delta^2 f}{\delta x^2}$  computed at each horizontal band

⊕ location of time and space derivatives

Figure 1.--Computation stencil for the finite-difference solution of the transport equation.



$$\psi_1 C_{i-1}^{j+1} + \psi_2 C_i^{j+1} + \psi_3 C_{i+1}^{j+1} = f(C_{i-1}^j, C_i^j, C_{i+1}^j) \quad (6)$$

where  $j$  is the finite-difference indexing in the time direction and  $i$  in the space direction.  $\psi_i, i=1, 2, 3$  are coefficients that are dependent on  $U, A, D, \Delta x, \Delta t$ , and the weighting coefficients  $\theta$  and  $\xi$ . Upstream and downstream boundary conditions produce two additional equations so that as many equations as unknowns are available. The upstream concentration is known while the downstream concentration is assumed to be equal to the concentration of the adjacent grid at the previous time step.

Use of the model requires consideration of the dispersion coefficient. As background, it is generally considered that neither equations 1 and 2 accurately represents dispersion of a slug injection until considerable mixing occurs. Fischer (1973) suggests some criteria for the length of time it takes for mixing to occur. However, it is also generally considered that dispersion is almost insignificant for steady injection rates (Sayer and Chang, 1968). As a result, use of dispersion coefficients requires some discretion.

The dispersion coefficient used with equation 1 is computed by an equation suggested by Fischer (1973). It is

$$\frac{D_x}{RU_*} = 250 \quad (7)$$

where

$$\begin{aligned} D_x &= \text{longitudinal dispersion coefficient (square feet per second)} \\ U_* &= \text{shear velocity (feet per second)} \\ R &= \text{hydraulic radius (feet)} \end{aligned}$$

Roache (1972) indicates that the effective numerical dispersion coefficient of a differencing scheme similar to the one used in this report is

$$D_n = 1/2 U \Delta x (1 - C_o) \quad (8)$$

where

$$\begin{aligned} D_n &= \text{numerical dispersion coefficient} \\ C_o &= U \frac{\Delta t}{\Delta x} \end{aligned}$$

In many cases the numerical dispersion is expected to equal or exceed the longitudinal dispersion. It is suggested that  $D_x$  be set to zero if  $D_n$  is greater than or approximately equal to  $D_x$ .

#### GENERAL MODEL DESIGN AND OPERATION

A schematic presentation of the model's design and operation is presented in the form of a generalized program flow chart in attachment A. A program listing is given in attachment B.

Use of the mass transport model must be preceded by the use of a flow model that computes the hydraulic variables for all cross sections and time steps. These results are stored on a direct-access storage device at the central computer. The transport model retrieves these data as needed during the computation process.

Use of the solute transport model begins by having all the control parameters and solute data input via computer cards. The program is initialized at time = 0 from the necessary data. The model then moves in the time dimension in one step intervals. For each time step flow data are retrieved from the direct access data set, and the concentrations are calculated for each interior cross section. At the upstream cross section, the solute concentration is given as boundary input and at the downstream the concentration is set equal to the concentration of the adjacent cross section for the previous time step. At preselected time steps the results are printed. At the conclusion of the run, line printer plots of computed concentration versus time may be obtained.

The reach design and the numbering system for the solute transport model is identical to the flow model. However, use of the transport model should influence the grid design at the lower end of the reach. For purposes of accuracy, the distance between the last two cross sections should be approximately equal to the water's velocity times the length of time step for the subreach between the last two cross sections. This is desirable because the constituent is assumed to move from the next-to-last cross section to the last one in one time step. Another consideration for purposes of accuracy is that the time step ( $\Delta t$ ) and the distance between cross sections ( $\Delta x$ ) should cause the Courant number,  $U \frac{\Delta t}{\Delta x}$ , to be less than or equal to 2. An example of a reach design and the numbering system is given in figure 2.

The computer program allows the solute to come into the reach at an unsteady rate from (1) the upstream inflow boundary, (2) tributaries, and (3) a source or sink. A steady inflow may enter the reach along the lateral boundary. The source or sink is a flux that adds or removes a specified amount of solute each second from each foot of stream.

The transport equation includes a decay coefficient that allows the solute to decay exponentially. The dimension of the coefficient is unit per second. The solute disappears in the units of mass per second per foot of channel length and is equal to KAC.

The computer program allows the solute entering the stream from the upstream boundary and tributaries to be a concentration of the inflowing water or a flux. Because the model transports the solute as a concentration, the flux is converted to concentration by dividing the flux by the discharge. The model units are: time in seconds, length in feet, and mass in any desired unit. Therefore, the concentration units are in mass per cubic foot and flux in mass per second.



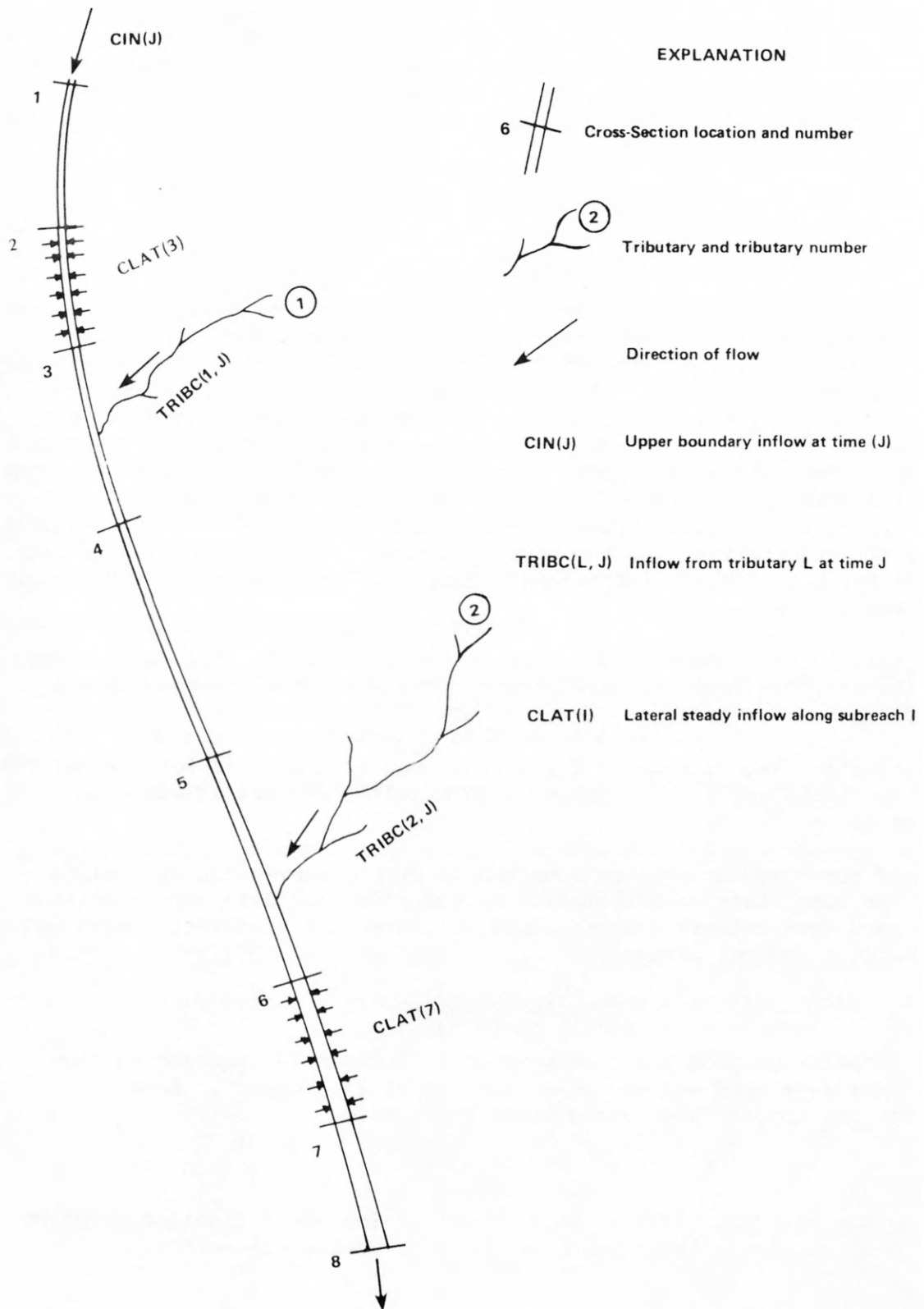


Figure 2.--Schematic diagram of grid design and numbering system used to describe a stream.

The computer program has a line printer plot routine that produces a time-series plot of concentration at five or less cross sections. The routine can also be used in a separate run to plot observed values. By laying one plot over the other, a quick and easy comparison of computed and observed values can be made during the calibration process which may be necessary to determine the concentrations of lateral inflow, and a decay coefficient.

## PROGRAM RUN PREPARATION

### Data

The first step in using the solute transport model is developing a data base of flow parameters at each cross section and time step. These parameters include (1) top width, (2) velocity, (3) cross-section area, (4) net tributary flow, (5) lateral inflow, and (6) depth. The suggested procedure is to use the linear implicit finite difference streamflow model, documented by Land (1978), to develop this data base. If this suggestion is followed the grid design used in the streamflow model must be used in the transport model. The other data preparation is essentially limited to preparing solute information. A time-series solute inflow data set must be prepared for the upstream boundary, all tributaries, and the source or sink. Single-value solute data are needed for each lateral inflow and a constant decay coefficient is specified for the solute decay.

The time interval must be the same as the flow model. All data, except flow parameters, are input by card format. The flow data are read from a direct access storage device.

A schematic diagram showing the arrangement of the cards for a model run is given in attachment C. A listing of an example data set is given in attachment D.

Use of the computer program's option to plot observed concentrations bypasses the simulation computations. However, to ease data card handling, the only card deck changes are the substitution of the time-series data and the coding of a control parameter.

### Computer Program

The computer program has been written in FORTRAN IV programming language and was developed and tested on IBM 360/91 equipment<sup>1/</sup>. Some changes may be required when using other equipment.

---

<sup>1/</sup>The use of brand names in this report is for identification purposes only and does not imply endorsement by the U.S. Geological Survey.



The program is dimensioned for 50 cross sections and 999 time steps. For simulations requiring more cross sections or time steps, these values must be increased. The program, as dimensioned, requires 240 bytes of storage on IBM 360 or 370 equipment. Compiling the program takes 5 to 8 seconds. Execution time for production runs requires 25 to 30 seconds for a reach with 50 cross sections and 999 time steps. These estimates are for the IBM H-level Fortran compiler using Opt = 2. For larger production runs, this compiler usually reduces computation time about 40 percent in comparison to the IBM G-level Fortran compiler.

#### DATA INPUT SPECIFICATIONS

Data are input into the computer program in two forms. Time-series flow data generated by the flow model must be made available in the form of direct-access data sets stored at the central computer. All other data are input via computer cards. Information on the control cards is input with the NAMELIST command. All variables are real or integer according to standard notation, that is A-H, O-Z for real and I-N for integer. All integers and real numbers without decimals must be right justified. The variables in the NAMELIST name block have the form

```
&name      VALUE1 = 1.0,  VALUE2 = 2.0,      VALUE3 = 3.0,      &END
```

The first ampersand must be in column 2.

To ease the data preparation, the cross-section data cards used in the flow model can be reused in this model after filling in two previously unused fields. The other data formats are also similar.

A description of the data input, sequence and arrangement follows.

---

#### SET NO. I    PARAMETERS

<u>Card No.</u>	<u>Variable</u>	<u>Description</u>	<u>Columns</u>
1	INFO(20)	Information card. Generally with basin name, period of record, date of run, and etc.	1-80
2	CODE	Block name for selected codes	3-6
	ICIN	Code identifying the method of entering the solute to the stream's water. 1 = concentration 2 = flux	-
	IDISP	Compute dispersion for transport equation? 0 = No 1 = Yes	-

<u>Card No.</u>	<u>Variable</u>	<u>Description</u>	<u>Columns</u>
	ISS	Inputing an unsteady source or sink 0 = No 1 = Yes	-
	IDEBUG	Print selected arrays for error tracing purposes? 0 = No 1 = Yes	-
	NZPLOT	Run to plot observed data only? 0 = No 1 = Yes	-
3	SIZE	Block name defining size of run.	3-6
	NX	Number of cross sections.	-
	NTS	Number of time steps.	-
	NTRIB	Number of tributaries with unsteady flow Maximum of 3.	-
	DT	Length of time step, seconds	-
4	INIT	Block name defining initial boundary values.	3-6
	DIFAC	Factor adjusting self-setting dispersion from unity. Use 1.0 for no adjustment.	-
	DKCOEF	Decay coefficient	-
5	CTRL	Block name for program controls.	3-6
	NPRNT	Number of cross sections with results to be printed. 0 = all N, N=1, 2, 3, . . . , NX = number of selected cross sections	-
	IPNT	Number of time steps between printouts	-
	NPLOT	Number of cross sections with results plotted on printer, Maximum of 5.	-
	IPLT	Number of time steps between adjacent points on plot.	-
6	DATE	Block name of starting date.	3-6
	IYR	Starting date - year	-
	IMON	- month	-
	IDY	- day	-
	IHR	- hour (military)	-

SET NO. II CROSS-SECTION OUTPUT

<u>Card No.</u>	<u>Variable</u>	<u>Description</u>	<u>Columns</u>
1,...	NP(I)	Cross-section number with results printed Number of values equals NPRNT. Omit when NPRNT = 0.	1-8,9-16 ....., 73-80
1	NPP(I)	Cross-section numbers with results plotted on line printer. Number of values equals NPLLOT. Maximum of 5. Omit when NPLLOT = 0.	1-8,9-16 ....., 33-40

SET NO. III CROSS-SECTION DATA<sup>1/</sup>

1,...,NX	X(I)	Channel length in downstream direction from reference to cross section (I).	1-8
	Z(I)	Elevation of low-point in cross section(I)	9-16
	CINIT(I)	Beginning concentration at cross section(I).	57-64
	CLAT(I)	Concentration of lateral inflow between cross sections(I) and (I-1).	65-72
	LTRIB(I)	Tributary number entering subreach above cross section (I). Only one tributary per subreach. Maximum of 3 for entire reach. Numbered consecutively in downstream direction.	77-80

SET NO. IV INFLOW CONCENTRATIONS<sup>2/</sup>

1,2,3,4,...	CIN(J)	Magnitude of solute inflow at upstream boundary. When ICIN=1, values are concentration; ICIN=2 values are flux. The first value corresponds to time DT which is at the end of the first time step. NTS values are required.	17-24,25-32, ....., 73-80
-------------	--------	---	---------------------------------

Footnote:

<sup>1/</sup>Cross-section cards from flow model can be reused.

<sup>2/</sup>Use for normal simulation run. Omit when NZPLOT=1.



SET NO. V      TRIBUTARY INFLOW CONCENTRATIONS<sup>2/</sup>

<u>Card No.</u>	<u>Variable</u>	<u>Description</u>	<u>Columns</u>
1,2,3,4,...	TRIBC(L,J)	Magnitude of solute inflow at tributary (L)	
1,2,3,4,...		One set for each tributary, (number of sets = NTRIB). First value corresponds to time DT which is at the end of the first time step. NTS values are required for each tributary	17-24,25-32 ..... 73-80

SET NO. VI      INFLOW FROM SOURCE<sup>2/</sup>

1,2,3,4,...	CSS(J)	Amount of solute entering stream from source or sink. Source (+), sink (-). The first value corresponds to time DT which is at the end of the first time step. NTS values are required. Omit when ISS = 0.	17-24,25-32 ..... 73-80
-------------	--------	---	-------------------------------

SET NO. VII      PLOT DATA<sup>3/</sup>

1,2,3,4,...	CSAV(I,J)	Observed concentration data. Number of sets equals NPLOT. Maximum of 5 sets.	17-24,25-32 .....
1,2,3,4,...		Number of values per set equals NTS.	73-80

Summary of card requirements:

- Set No. I.      Required.
- II.      Print card required when NOUT > 0.  
Plot card required when NPLOT > 0.
- III.      One card for each cross section.
- IV.      Required when NZPLOT = 0.
- V.      Required when NZPLOT = 0 and NTRIB > 0. Number of sets  
equals NTRIB.
- VI.      Required when NZPLOT = 0 and ISS = 1.
- VII.      Required when NZPLOT = 1. Number of sets equals NPLOT.

Footnote:

- <sup>2/</sup>Use for normal simulation run. Omit when NZPLOT=1.  
<sup>3/</sup>Use for plot of observed data. Omit when NZPLOT=0.

## PROGRAM OUTPUT

Results of calculations are printed at selected cross sections and at selected time steps. Printer plots of concentrations at selected cross sections are available for visual presentation.

To illustrate the transport model's response to a set of unsteady flow and solute loading conditions, graphs are given in figures 3 and 4 to show the flow and concentration variations in space and time. The water discharge in the stream had a base flow of 550 cubic feet per second. A temporary reservoir release added 3,500 cubic feet per second to the streamflow for a limited time. The solute inflow has a base concentration of 1 pound per cubic foot and temporary loads of 9 and 5 pounds per cubic foot. The stream also had a solute source flux other than inflow flux and a solute decay. Discharge hydrographs are given in figure 3 for the beginning, middle and ending of the 10-mile reach. Solute pollutographs are given at the same locations in figure 4.

An example of computer output in the form of tables and plots is given in attachment E.

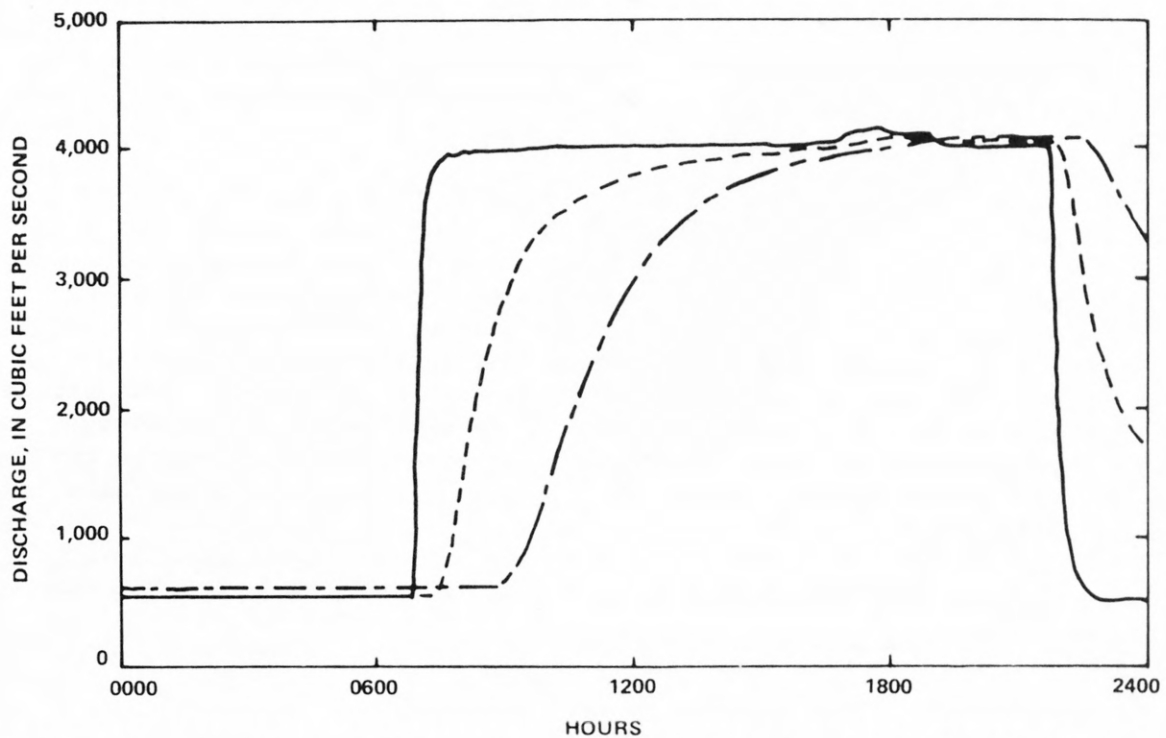


Figure 3.--Discharge hydrographs at beginning, middle, and end of a 10-mile reach used in example data set.

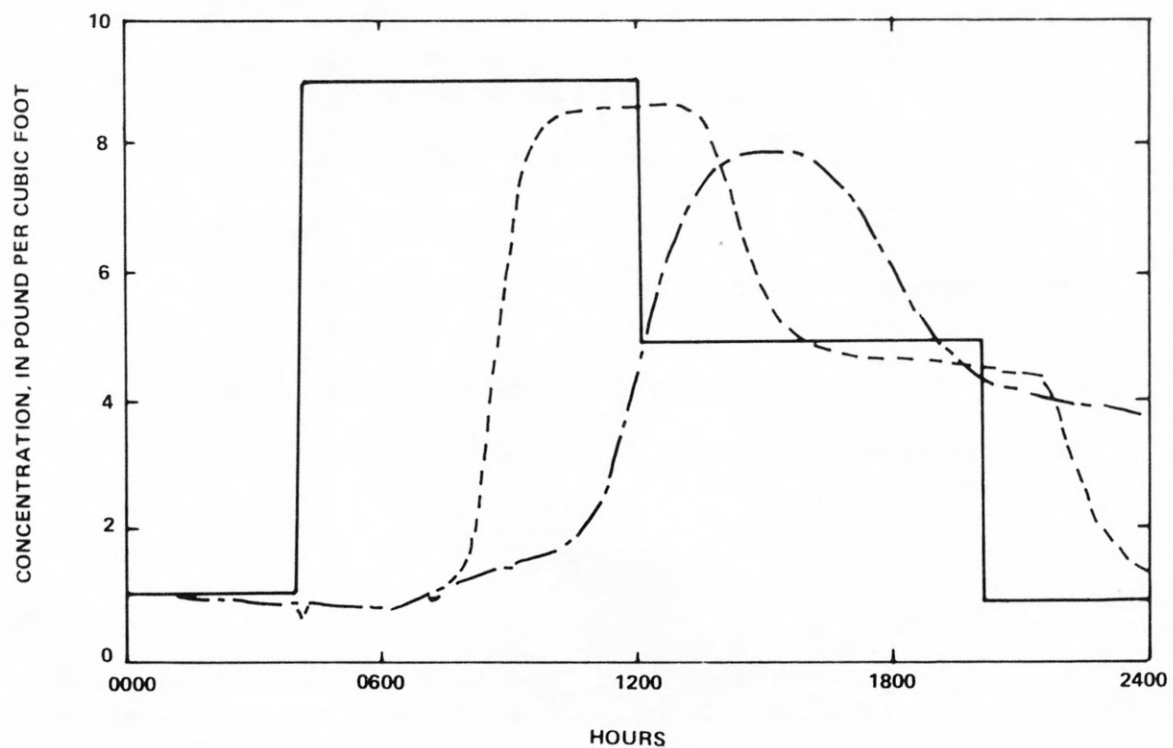


Figure 4.--Solute pollutographs computed by transport model at corresponding locations in figure 3.

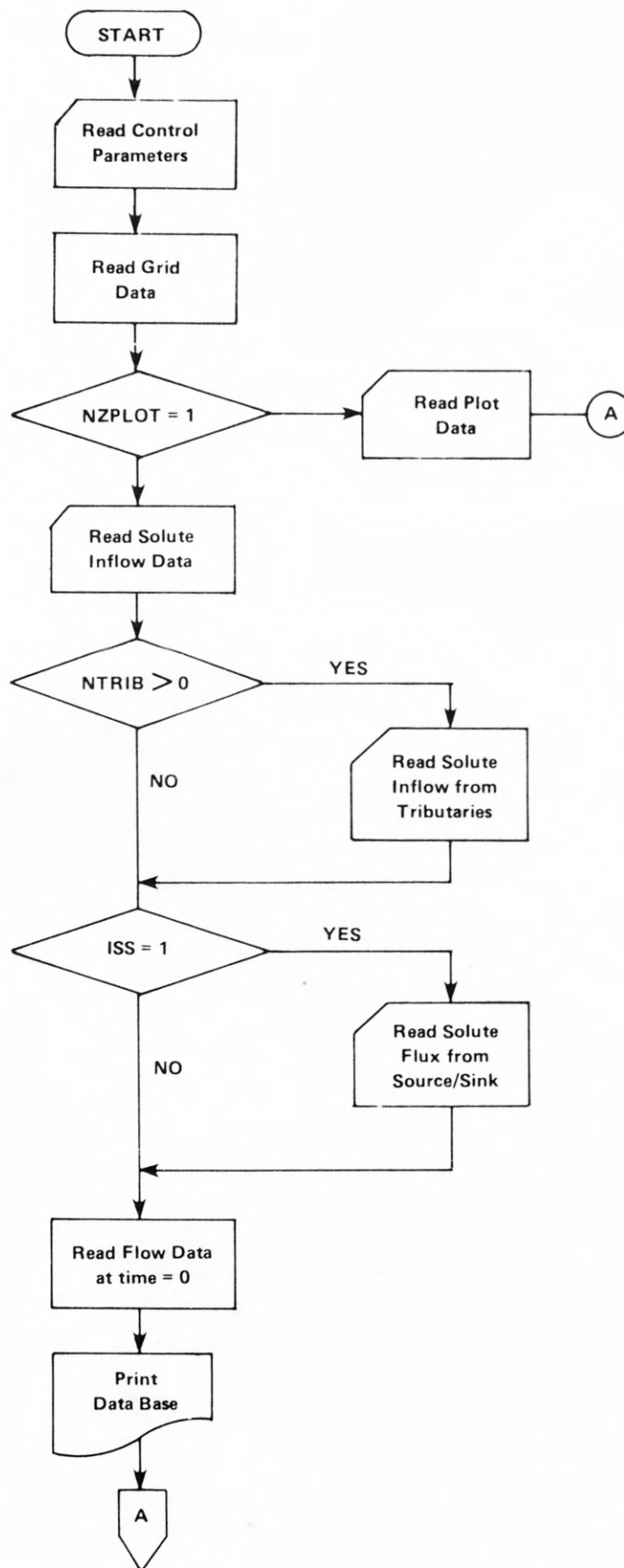


## REFERENCES

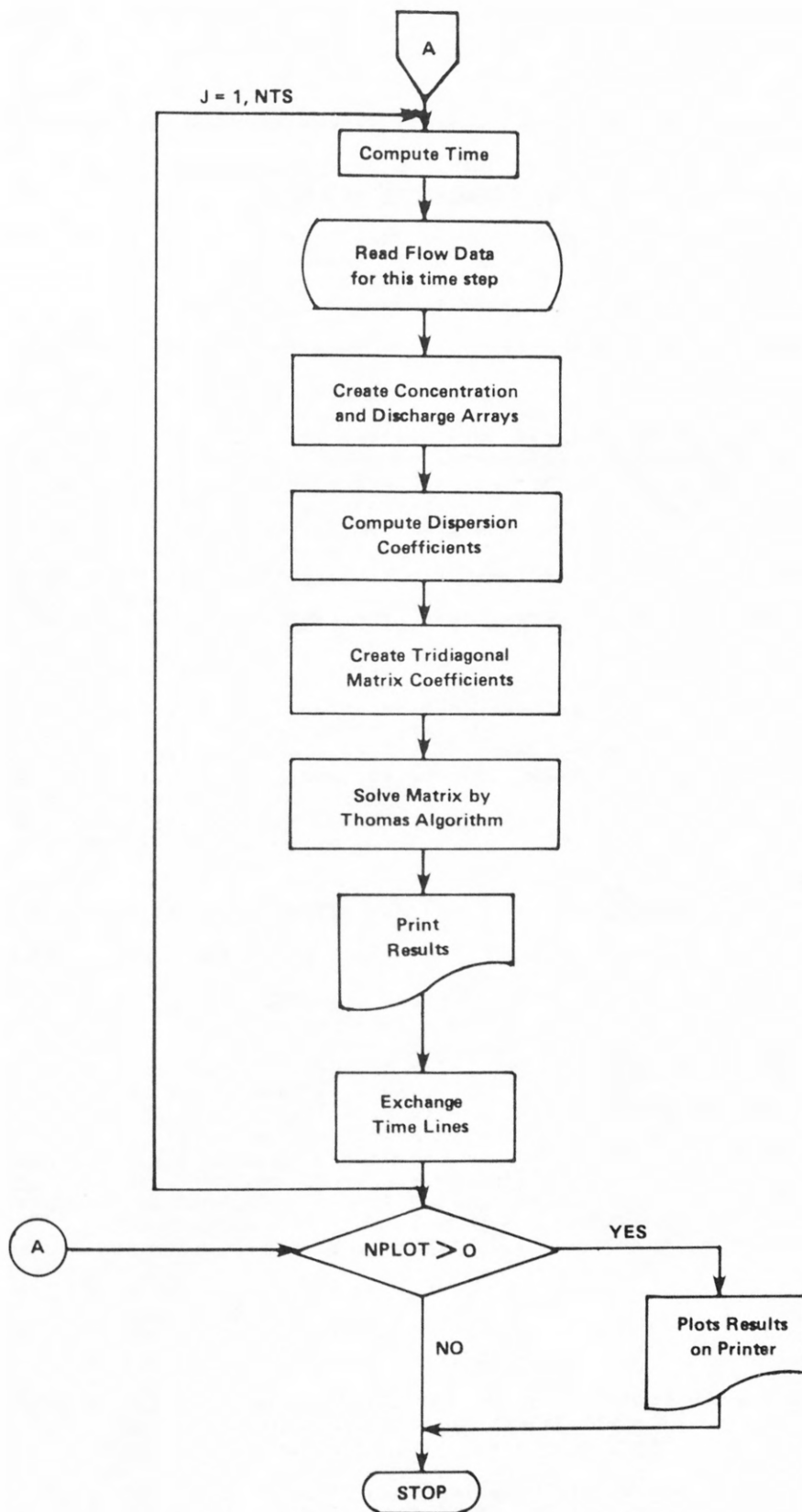
- Fisher, H. B., 1973, Longitudinal dispersion and turbulent mixing in open-channel flow: Annual Review of Fluid Mechanics, p. 59-78.
- Land, L. F., 1978, Unsteady streamflow simulation using a linear implicit finite-difference model: U.S. Geol. Survey Water-Resources Inv.
- Roache, P. J., 1972, Computational fluid dynamics: Hermosa Publishers, Albuquerque, New Mexico, p. 32-33, 65.
- Sayre, W. W. and Chang, F. M., 1968, A laboratory investigation of open-channel dispersion processes for dissolved, suspended, and floating dispersants: U.S. Geol. Survey Professional Paper 433-E, 71 p.
- Stone, H. L. and Brian, P. L. T., 1963, Numerical solution of convective transport problems: Jour. Am. Inst. Chem. Eng., v. 9, no. 5, p. 681-688.
- von Rosenberg, D. U., 1969, Methods for the numerical solution of partial differential equations: American Elsevier Publishing Company, New York, New York, p. 8, 113.

## ATTACHMENTS









## B. COMPUTER PROGRAM

```

C *****
C *
C *      JB80--MASS TRANSPORT SIMULATION USING AN
C *      IMPLICIT FINITE DIFFERENCE MODEL
C *
C *      OPERATIONAL MODELS PROJECT
C *      GULF COAST HYDROSCIENCE CENTER
C *      U. S. GEOLOGICAL SURVEY - WRO
C *      DATE OF LAST PROGRAM REVISION: FEB 21, 1978
C *
C *****
C
C      DEFINE FILE 20(1000,1200,L=101)
C
C      DIMENSION CIV(1000), CSS(1000), TRIBC(3,1000), CSAV(5,1000)
C      DIMENSION CTRBNW(50), CTRBNX(50), CSSNW(50), CSSNX(50), CNW(50), C
C      INX(50), QNW(50), QNX(50), YNW(50), YNX(50)
C      DIMENSION DATANW(6,50), DATANX(6,50)
C      DIMENSION X(96), Z(96), CIVIT(50), CLAT(50), LTRIB(50), DELX(50),
C      LCLAT(50), NP(50)
C      DIMENSION A(3,50), D(50), DI(50), DIP1(50), AI(50), AIP1(50), BETA
C      I(50), GAMA(50)
C      DIMENSION MONTH(12), INFO(20), IMAGE(2450), NSCALE(5), IRNG(12), N
C      P(5)
C      LOGICAL*1 LETTER(5)
C
C      DATA THETA,Z1,FLUXUP,CRAT/0.65,0.65,0.037,1.00/
C      DATA LETTER/'A','H','C','D','E'/
C      DATA MONTH/31,28,31,30,31,30,31,31,30,31,30,31/
C      DATA IRNG/1,2,5,10,15,50,100,250,500,1000,2500,10000/
C      DATA NZPLOT,IREC/0,1/
C      DATA NSCALE/1,0,3,0,1/
C      DATA NPP/1,2,3,4,5/
C
C *****DEFINITION OF INPUT PARAMETERS*****
C
C      INFO : INFORMATION CARD
C
C      NAMELIST PARAMETERS
C      -----
C
C      CODE ----
C      ICIN : CODE IDENTIFYING THE METHOD OF ENTERING THE SOLUTE
C              TO THE STREAM'S WATER.
C              1=CONCENTRATION (MASS PER CUBIC FOOT OF INFLOW)
C              2=FLUX OF CONSTITUENT (MASS PER UNIT TIME)
C      IDISP : DISPERSION COEFFICIENT:      0=ZERO,      1=SELF-SETTING
C      ISS : ALLOW AN UNSTEADY SOURCE/SINK?  0=NO,      1=YES
C      IOEBUG: PRINT SELECTED COEFFICIENTS AND
C              PARAMETERS FOR ERROR TRACING.  0=NO,      1=YES
C      NZPLOT: RUN TO PLOT OBSERVED DATA ONLY? 0=NO,      1=YES
C
C      SIZE ----
C      NX : NUMBER OF CROSS-SECTIONS
C      NTS : NUMBER OF TIME STEPS
C      NTRIB : NUMBER OF TRIBUTARIES
C      DI : LENGTH OF TIME STEP IN SECONDS
C
C      INIT ----
C      DIFAC : MULTIPLYING FACTOR ADJUSTING SELF-SETTING DISPERSION COEF
C      UNCOEF : DECAY COEFFICIENT, K VALUE IN KAC TERM
C              0.0 = NO DECAY      * = SOME DECAY
C
C      CTRL ----
C      NPRINT : NUMBER OF X-SECTIONS PRINTED CODE: 0=ALL
C      IPNT : NUMBER OF TIME STEPS BETWEEN PRINTOUTS
C      NPLT : NUMBER OF X-SECTIONS WITH CONCENTRATION PLOTS

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C	IPLT :	NUMBER OF TIME STEPS BETWEEN POINTS ON PLOT	A	65
C	DATE ----		A	66
C	IYR :	STARTING DATE - YEAR	A	67
C	IMON :	MUNTH	A	68
C	IDY :	DAY	A	69
C	IHR :	HOUR (MILITARY)	A	70
C			A	71
C		SELECTING OUTPUT	A	72
C		-----	A	73
C	NP(K) :	X-SEC NOS. WITH RESULTS PRINTED	A	74
C	NPP(K) :	X-SEC NOS. WITH CONCENTRATION PLOTTED	A	75
C			A	76
C		CROSS-SECTION PARAMETERS	A	77
C		-----	A	78
C	X(I) :	CHANNEL LENGTH FROM BEGINNING TO X-SEC(I)	A	79
C	Z(I) :	ELEVATION OF LOW-POINT IN X-SEC(I)	A	80
C		NOTE -- X AND Z ARRAYS ARE ALSO USED FOR PLOTTING	A	81
C		PURPOSES. DIMENSION TO A MINIMUM OF 96.	A	82
C	CINIT(I) :	BEGINNING CONCENTRATION AT X-SEC(I)	A	83
C	CLAT(I) :	CONCENTRATION OF LATERAL INFLOW BETWEEN	A	84
C		X-SEC(I-1) AND X-SEC(I)	A	85
C	LTRIB(I) :	TRIB NO. AT X-SEC(I); NO. CONSEC. IN D.S. DIRECTION	A	86
C			A	87
C			A	88
C		TIME SERIES DATA	A	89
C		-----	A	90
C	CIN(J) :	QUALITY OF INFLOWING WATER	A	91
C		CONCENTRATION (MASS/CJ.FT.) WHEN ICIN=1	A	92
C		FLUX OF SOLUTE (MASS/SEC) WHEN ICIN=2	A	93
C	TRIBC(L,J) :	QUALITY OF TRIB(L) WATER	A	94
C		CONCENTRATION (MASS/CJ.FT.) WHEN ICIN=1	A	95
C		FLUX OF SOLUTE (MASS/SEC) WHEN ICIN=2	A	96
C	CSS(J) :	SOLUTE FLUX TO SOURCE/SINK (MASS/SEC/FT)	A	97
C	CSAV(-,J) :	CONCENTRATIONS TO BE PLOTTED; UP TO 5 X-SECTIONS.	A	98
C			A	99
C		MISC. PARAMETER DEFINITION	A	100
C		-----	A	101
C	DATAN*(1-6,I) :	SELECTED RESULTS AT X-SEC(I)	A	102
C		1=TOP WIDTH	A	103
C		2=VELOCITY	A	104
C		3=AREA	A	105
C		4=NET TRIBUTARY FLOW	A	106
C		5=LATERAL INFLOW	A	107
C		6=DEPTH	A	108
C	QIN*(I) :	DISCHARGE AT X-SEC(I)	A	109
C	YN*(I) :	DEPTH AT X-SEC(I)	A	110
C	CN*(I) :	CONCENTRATION AT X-SEC(I)	A	111
C	CTRBN*(I) :	CONCENTRATION OF TRIBUTARY WATER AT X-SEC(I)	A	112
C	CSSN*(I) :	FLUX OF CONSTITUENT AT X-SEC(I)	A	113
C		NOTE: --N*(I) --NW(I) NOW OR OLD TIME LEVEL	A	114
C		--NX(I) NEXT OR NEW TIME LEVEL	A	115
C			A	116
C	THETA :	VELOCITY TERM CENTERING COEFFICIENT. (MOVES POINT OF	A	117
C		TIME DERIVATIVE)	A	118
C		SUGGEST 0.50-0.65, POSSIBLE 0.51-1.0	A	119
C		LOW VALUE CAUSES ABRUPT CONCENTRATION CHANGES AND	A	120
C		MINOR OSCILLATIONS. HIGH VALUE CAUSES SMOOTHING.	A	121
C	ZI :	UPWIND/DOWNWIND COEFFICIENT. (MOVES POINT OF SPACE	A	122
C		DERIVATIVE)	A	123
C		SUGGEST 0.50-0.65, POSSIBLE 0.51-1.0.	A	124
C		SAME EFFECTS AS THETA VALUE.	A	125
C	FLUXUP :	FLUX BALANCING COEFFICIENT (STABILIZES CONC. VALUES)	A	126
C	ICYCL :	CYCLIC CODE FOR TIME TERM IN NUMERICAL TECHNIQUE	A	127
C	A( ,I) :	TRIDIAGONAL COEF MATRIX OF UNKNOWNNS	A	128



C	D(I)	:	VECTOR OF KNOWN VALUES	A 129
C	DI(I)	:	DISPERSION COEFFICIENT UPSTREAM OF X-SEC(I)	A 130
C	DIP1(I)	:	DISPERSION COEFFICIENT DOWNSTREAM OF X-SEC(I)	A 131
C	AI(I)	:	AVERAGE AREA UPSTREAM OF X-SEC(I)	A 132
C	AIPI(I)	:	AVERAGE AREA DOWNSTREAM OF X-SEC(I)	A 133
C				A 134
C			MODEL UNITS	A 135
C			-----	A 136
C	LENGTH		FEET	A 137
C	TIME		SECONDS	A 138
C	FLOW RATE		CUBIC FEET PER SECOND	A 139
C	CONCENTRATION		MASS PER CUBIC FOOT	A 140
C	FLUX		MASS PER SECOND	A 141
C				A 142
C				A 143
	NAMelist /CODE/	ICIN, IDISP, ISS, IDEBUG, NZPLOT		A 144
	NAMelist /SIZE/	NX, NTS, NTRIB, DT		A 145
	NAMelist /INIT/	DIFAC, DKCOEF		A 146
	NAMelist /CTRL/	NPRNT, IPNT, NPLOT, IPLT		A 147
	NAMelist /DATE/	IYR, IMON, IDY, IHR		A 148
C				A 149
C			READ DATA CARDS	A 150
C			-----	A 151
C			MISC.	A 152
	READ (5,830)	INFO		A 153
	READ (5,CODE)			A 154
	READ (5,SIZE)			A 155
	READ (5,INIT)			A 156
	READ (5,CTRL)			A 157
	READ (5,DATE)			A 158
	IF (NPRNT.LT.0.OR.NPRNT.GT.NX)	NPRNT=0		A 159
	IF (IPNT.LE.0)	IPNT=1		A 160
	IF (IPLT.LE.0)	IPLT=1		A 161
	IF (NPRNT.GT.0)	READ (5,820) (NP(I),I=1,NPRNT)		A 162
	IF (NPLOT.GT.0)	READ (5,820) (NPP(I),I=1,5)		A 163
	IF (MOD(IYR,4).EQ.0)	MONTH(2)=29		A 164
	NTSP1=NTS+1			A 165
C			CROSS-SECTION	A 166
	DO 10 I=1,NX			A 167
10	READ (5,720)	X(1),Z(I),CINIT(I),CLAT(I),LTRIB(I)		A 168
	IF (NZPLOT.GT.0)	GO TO 60		A 169
C			UPSTREAM TIME-SERIES DATA	A 170
	READ (5,800)	(CIN(I),I=2,NTSP1)		A 171
	CIN(1)=CIN(2)			A 172
	IF (NTRIB.EQ.0)	GO TO 30		A 173
C			TRIBUTARY TIME-SERIES DATA	A 174
	DO 20 I=1,NTRIB			A 175
	READ (5,800)	(TRIBC(I,J),J=2,NTSP1)		A 176
20	TRIBC(I,1)=TRIBC(I,2)			A 177
30	IF (ISS.LE.0)	GO TO 40		A 178
C			SOURCE/SINK TIME-SERIES DATA	A 179
	READ (5,800)	(CSS(I),I=2,NTSP1)		A 180
	CSS(1)=CSS(2)			A 181
	GO TO 80			A 182
40	DO 50 I=1,NTSP1			A 183
50	CSS(I)=0.0			A 184
	GO TO 80			A 185
C			OBSERVED DATA FOR PLOTTING	A 186
	60 DO 70 L=1,NPLOT			A 187
	70 READ (5,800)	(CSAV(L,J),J=2,NTSP1)		A 188
	GO TO 170			A 189
	80 CONTINUE			A 190
C				A 191

C	READ DATA FROM DISK	A 192
C	-----	A 193
	READ (20*IREC) DATANW	A 194
C		A 195
C	DEFINE SELECTED ARRAYS	A 196
	QLAT(1)=0.0	A 197
	DELX(1)=0.0	A 198
	QNW(1)=DATANW(2,1)*DATANW(3,1)	A 199
	YNW(1)=DATANW(6,1)	A 200
	DO 90 I=2,NX	A 201
	QNW(I)=DATANW(2,I)*DATANW(3,I)	A 202
	YNW(I)=DATANW(6,I)	A 203
	DELX(I)=X(I)-X(I-1)	A 204
	90 QLAT(I)=DATANW(5,I)*DELX(I)	A 205
C	ZERO CONCENTRATION ARRAYS	A 206
	DO 100 I=1,NX	A 207
	CNW(I)=0.0	A 208
	CIRBNW(I)=0.0	A 209
	CIRBNX(I)=0.0	A 210
	CSSNW(I)=0.0	A 211
	CSSNX(I)=0.0	A 212
	AI(I)=0.0	A 213
	AIP1(I)=0.0	A 214
	DI(I)=0.0	A 215
	100 DIP1(I)=0.0	A 216
C	SET FIRST CONCENTRATION	A 217
	IF (ICIN.EQ.2) GO TO 120	A 218
	DO 110 I=1,NX	A 219
	CNW(I)=CINIT(I)	A 220
	IF (LTRIB(I).NE.0) CTRBNW(I)=TRIBC(LTRIB(I),1)	A 221
	110 CSSNW(I)=CSS(1)	A 222
	GO TO 150	A 223
	120 CONTINUE	A 224
	DO 140 I=1,NX	A 225
	CNW(I)=CINIT(I)	A 226
	IF (LTRIB(I).EQ.0) GO TO 140	A 227
	IF (DATANW(4,I).GT.0.0) GO TO 130	A 228
	WRITE (6,1020) IMON,IDY,IYR,IHR	A 229
	CIRBNW(I)=0.0	A 230
	GO TO 140	A 231
	130 CTRBNW(I)=TRIBC(LTRIB(I),1)/DATANW(4,I)	A 232
	140 CSSNW(I)=CSS(1)	A 233
C		A 234
	150 HR=FLOAT(IHR)	A 235
	SZERO=(Z(1)-Z(NX))/(X(NX)-X(1))	A 236
	ICYCL=0	A 237
	NXN1=NX-1	A 238
	IF (NPRNT.GT.0) GO TO 170	A 239
	DO 160 I=1,NX	A 240
	160 NP(I)=I	A 241
	NPRNT=NX	A 242
	170 DTMIN=DT/60.	A 243
C	PRINT DATA	A 244
C	-----	A 245
	WRITE (6,840)	A 246
	WRITE (6,810) INFO	A 247
	WRITE (6,850) ICIN,ISS,IJISP	A 248
	WRITE (6,860) IMON,IDY,IYR	A 249
	WRITE (6,870) NX,NTS,DTMIN,NTRIB	A 250
	IF (NZPLOT.LE.0) GO TO 190	A 251
	WRITE (6,950)	A 252
	DO 180 N=1,NPLOT	A 253
	WRITE (6,970) NPP(N)	A 254

180	WRITE (6,980) (CSAV(N,J),J=2,NTSP1)	A 255
	GO TO 450	A 256
190	WRITE (6,880) DIFAC	A 257
	WRITE (6,890) DKCOEF	A 258
	WRITE (6,930)	A 259
	DO 200 I=1,NX	A 260
200	WRITE (6,940) I,X(I),DELX(I),Z(I),JNW(I),CINIT(I),QLAT(I),CLAT(I),	A 261
	1LTRIB(I)	A 262
	DO 210 I=2,NX	A 263
	DX=X(I)-X(I-1)	A 264
	IF (DX.GT.0.0) GO TO 210	A 265
	WRITE (6,960) I	A 266
	STOP	A 267
210	CONTINUE	A 268
	WRITE (6,900) (CIN(I),I=2,NTSP1)	A 269
	IF (NTRIB.EQ.0) GO TO 230	A 270
	DO 220 K=1,NTRIB	A 271
220	WRITE (6,920) K,(TRIBC(K,I),I=2,NTSP1)	A 272
230	IF (ISS.GE.1) WRITE (6,910) (CSS(I),I=2,NTSP1)	A 273
	WRITE (6,1040)	A 274
C		A 275
	WRITE (6,730) IMON,IDY,IYR,IHR	A 276
	M1=1	A 277
	M2=13	A 278
240	IF (M2.GT.NPRNT) M2=NPRNT	A 279
	WRITE (6,740) (NP(I),I=M1,M2)	A 280
	WRITE (6,750) (DATANW(2,VP(I)),I=M1,M2)	A 281
	WRITE (6,760) (YVW(NP(I)),I=M1,M2)	A 282
	WRITE (6,770) (QVW(NP(I)),I=M1,M2)	A 283
	WRITE (6,780) (CVW(I),I=M1,M2)	A 284
	WRITE (6,790)	A 285
	IF (M2.EQ.NPRNT) GO TO 250	A 286
	M1=M2+1	A 287
	M2=M2+13	A 288
	GO TO 240	A 289
250	CONTINUE	A 290
C		A 291
C		A 292
C	*****BEGIN LOOPING THROUGH MODEL IN TIME*****	A 293
	DO 430 J=1,NTS	A 294
	JP=J+1	A 295
	HR=HR+DT/60.	A 296
	IHR=INT(HR)	A 297
	IF (MOD(IHR,100).LT.60) GO TO 260	A 298
	IHR=IHR/100*100+100	A 299
	HR=FLOAT(IHR)	A 300
	IF (IHR.LE.2400) GO TO 250	A 301
	HR=HR-2400.	A 302
	IHR=MOD(IHR,2400)	A 303
	IDY=IDY+1	A 304
	IF (IDY.LE.MONTH(IMON)) GO TO 260	A 305
	IDY=1	A 306
	IMON=IMON+1	A 307
	IF (IMON.LE.12) GO TO 260	A 308
	IMON=1	A 309
	IYR=IYR+1	A 310
260	CONTINUE	A 311
	TIME=TIME+DT	A 312
	IHEC=IREC+1	A 313
	ICYCL=ICYCL+1	A 314
	IF (ICYCL.GE.4) ICYCL=1	A 315

C	READ DATA FROM DISK	A 316
C	-----	A 317
	READ (20, IREC) DATANX	A 318
C		A 319
C	COMPUTE DISCHARGE AND CONCENTRATION ARRAYS	A 320
	CNX(1)=CIN(JP)	A 321
	DO 270 I=1,NX	A 322
	QNX(I)=DATANX(2,I)*DATANX(3,I)	A 323
	YNX(I)=DATANX(6,I)	A 324
	IF (LTRIB(I).NE.0) CTRBNX(I)=TRIBC(LTRIB(I),JP)	A 325
270	CSSNX(I)=CSS(JP)	A 326
	IF (ICIN.EQ.1) GO TO 310	A 327
C	COMPUTE CONCENTRATIONS FROM MASS VALUES	A 328
	IF (CNX(1).EQ.0.0) GO TO 280	A 329
	IF (QNX(1).LE.0.0) GO TO 440	A 330
	CNX(1)=CNX(1)/QNX(1)	A 331
280	CONTINUE	A 332
	IF (NTRIB.EQ.0) GO TO 310	A 333
	DO 300 I=1,NX	A 334
	IF (CTRBX(I).EQ.0.0) GO TO 300	A 335
	IF (LTRIB(I).EQ.0) GO TO 300	A 336
	IF (DATANX(4,I).GT.0.0) GO TO 290	A 337
	WRITE (6,1020) I,MN,IDY,IYR,IHR	A 338
	CTRBX(I)=0.0	A 339
	GO TO 300	A 340
290	CTRBX(I)=CTRBX(I)/DATANX(4,I)	A 341
300	CONTINUE	A 342
310	CONTINUE	A 343
C	COMPUTE DISPERSION COEFFICIENTS	A 344
	IF (IDISP.EQ.0) GO TO 330	A 345
	AI(1)=0.	A 346
	AIPI(1)=0.	A 347
	DI(1)=0.	A 348
	DIPI(1)=0.	A 349
	AN1=DATANX(3,1)	A 350
	AN2=DATANW(3,1)	A 351
	AC1=DATANX(3,2)	A 352
	AC2=DATANW(3,2)	A 353
	DN1=DIFAC*250.*YVX(1)*(32.2*YNX(1)*SZERO)**0.5	A 354
	DN2=DIFAC*250.*YVW(1)*(32.2*YNW(1)*SZERO)**0.5	A 355
	DC1=DIFAC*250.*YVX(2)*(32.2*YNX(2)*SZERO)**0.5	A 356
	DC2=DIFAC*250.*YVW(2)*(32.2*YNW(2)*SZERO)**0.5	A 357
C	COMPUTE VALUES FOR INTERIOR X-SECTIONS	A 358
	DO 320 K=2,NXM1	A 359
	AP1=DATANX(3,K+1)	A 360
	AP2=DATANW(3,K+1)	A 361
	DP1=DIFAC*250.*YVX(K+1)*(32.2*YNX(K+1)*SZERO)**0.5	A 362
	DP2=DIFAC*250.*YVW(K+1)*(32.2*YNW(K+1)*SZERO)**0.5	A 363
	AI(K)=(AN1+AC1+AC2+AN2)/4.	A 364
	AIPI(K)=(AC2+AC1+AP2+AP1)/4.	A 365
	DI(K)=(DN1+DN2+DC1+DC2)/4.	A 366
	DIPI(K)=(DC1+DC2+DP1+DP2)/4.	A 367
	AN1=AC1	A 368
	AN2=AC2	A 369
	AC1=AP1	A 370
	AC2=AP2	A 371
	DN1=DC1	A 372
	DN2=DC2	A 373
	DC1=DP1	A 374
	DC2=DP2	A 375
320	CONTINUE	A 376



C	CREATE TRI-DIAGONAL MATRIX	A 377
C	-----	A 378
330	A(1,1)=0.0	A 379
	A(2,1)=1.0	A 380
	A(3,1)=0.0	A 381
	A(1,NX)=0.0	A 382
	A(2,NX)=1.0	A 383
	A(3,NX)=0.0	A 384
	D(1)=CNX(1)	A 385
C	BEGIN X-SEC LOOP	A 386
	DO 340 K=2,NXM1	A 387
	DIST=DELX(K)+DELX(K+1)	A 388
	EPS=DELX(K)/DIST	A 389
	DELM=1./(DIST*DELX(K))	A 390
	DELP=1./(DIST*DELX(K+1))	A 391
	DMIN=DELM*AI(K)*DI(K)	A 392
	DPLS=DELP*AIPI(K)*DIPI(K)	A 393
	DCEN=DMIN+DPLS	A 394
C	SELECT CYCLIC COEF	A 395
	IF (ICYCL.EQ.1) RHO=0.1250/DT	A 396
	IF (ICYCL.EQ.2) RHO=0.4145/DT	A 397
	IF (ICYCL.EQ.3) RHO=0.4605/DT	A 398
	UMR=(1./DT)-RHO	A 399
C	COMPUTE SUM OF LAT, TRIBS + SOURCE/SINK	A 400
	FIF=DATANX(4,K)*CTRBX(K)+QLAT(K)*CLAT(K)+CSSNX(K)*DELX(K)	A 401
	FIP1F=DATANX(4,K+1)*CTRBX(K+1)+QLAT(K+1)*CLAT(K+1)+CSSNX(K+1)*DEL	A 402
	1X(K+1)	A 403
	FIB=DATANW(4,K)*CTRBW(K)+QLAT(K)*CLAT(K)+CSSNW(K)*DELX(K)	A 404
	FIP1B=DATANW(4,K+1)*CTRBW(K+1)+QLAT(K+1)*CLAT(K+1)+CSSNW(K+1)*DEL	A 405
	1X(K+1)	A 406
C		A 407
C	CREATE INTERVAL MATRIX COEFFICIENTS	A 408
C	A MATRIX	A 409
	A(1,K)=RHO*(1.-EPS)*DATANX(3,K-1)-(ZI*THETA/DELX(K))*QNX(K-1)-DMIN	A 410
	1+DKCOEF/2.*ZI*THETA*DATANX(3,K-1)	A 411
	A(2,K)=OMR*DATANX(3,K)+THETA*((ZI/DELX(K))-((1.-ZI)/DELX(K+1)))*QNX	A 412
	1X(K)+DCEN+DKCOEF/2.*(ZI*THETA+(1.-ZI)*THETA)*DATANX(3,K)	A 413
	A(3,K)=RHO*EPS*DATANX(3,K+1)+((1.-ZI)*THETA/DELX(K+1))*QNX(K+1)-DP	A 414
	1LS+DKCOEF/2.*(1.-ZI)*THETA*DATANX(3,K+1)	A 415
C	D VECTOR	A 416
	D1K=(RHO*(1.-EPS)*DATANW(3,K-1)+(ZI*(1.-THETA)/DELX(K))*QNW(K-1)+D	A 417
	1MIN)*CNW(K-1)-DKCOEF/2.*ZI*(1.-THETA)*DATANW(3,K-1)*CNW(K-1)	A 418
	D2K=(UMR*DATANW(3,K)+(1.-THETA)*((1.-ZI)/DELX(K+1)-(ZI/DELX(K)))*Q	A 419
	1NW(K)-DCEN)*CNW(K)-DKCOEF/2.*(ZI*(1.-THETA)+(1.-ZI)*(1.-THETA))*DA	A 420
	2TANW(3,K)*CNW(K)	A 421
	D3K=(RHO*EPS*DATANW(3,K+1)-((1.-ZI)*(1.-THETA)/DELX(K+1))*QNW(K+1)	A 422
	1+DPLS)*CNW(K+1)-DKCOEF/2.*(1.-ZI)*(1.-THETA)*DATANW(3,K+1)*CNW(K+1	A 423
	2)	A 424
	D(K)=D1K+D2K+D3K	A 425
C	ADD FLUXES OF LAT AND TRIB Q'S	A 426
	DC1=-(ZI*THETA/DELX(K))*FIF	A 427
	DC2=-(ZI*(1.-THETA)/DELX(K))*FIB	A 428
	DC3=-((1.-ZI)*THETA/DELX(K+1))*FIP1F	A 429
	DC4=-((1.-ZI)*(1.-THETA)/DELX(K+1))*FIP1B	A 430
	D(K)=D(K)-DC1-DC2-DC3-DC4	A 431
C	FLUX BALANCING CORRECTION FACTOR	A 432
	D(K)=D(K)-FLXJUP*ABS(QNX(K)-QNW(K))*CNW(K)/DELX(K)	A 433
340	CONTINUE	A 434
	D(NX)=CNW(NXM1)*CRAT-DKCOEF*DATANW(3,NXM1)*CNW(NXM1)	A 435
C	END OF TRI-DIAGONAL MATRIX CREATION	A 436
C		A 437

C		THOMAS ALGORITHM	A 438
C		-----	A 439
	BETA(1)=A(2,1)		A 440
	GAMA(1)=D(1)/A(2,1)		A 441
	DO 350 I=2,NX		A 442
	BETA(I)=A(2,I)-(A(1,I)*A(3,I-1)/BETA(I-1))		A 443
	GAMA(I)=(D(I)-A(1,I)*GAMA(I-1))/BETA(I)		A 444
	IF (GAMA(I).GT.1.0E-75) GO TO 350		A 445
	GAMA(I)=0.0		A 446
350	CONTINUE		A 447
	CNX(NX)=GAMA(NX)		A 448
	KK=NX		A 449
	DO 360 I=1,NXM1		A 450
	KK=KK-1		A 451
	CNX(KK)=GAMA(KK)-(A(3,KK)*CNX(KK+1)/BETA(KK))		A 452
360	CONTINUE		A 453
C			A 454
	IF (MOD(J,IPNT).NE.0) GO TO 390		A 455
C			A 456
C		PRINT MODEL RESULTS AT SELECTED TIME STEPS	A 457
C		-----	A 458
	WRITE (6,730) IMON,IDY,IYR,IHR		A 459
	M1=1		A 460
	M2=13		A 461
370	IF (M2.GT.NPRNT) M2=NPRNT		A 462
	WRITE (6,740) (NP(I),I=M1,M2)		A 463
	WRITE (6,750) (DATANX(2,NP(I)),I=M1,M2)		A 464
	WRITE (6,760) (YXX(NP(I)),I=M1,M2)		A 465
	WRITE (6,770) (QXX(NP(I)),I=M1,M2)		A 466
	WRITE (6,780) (CNX(NP(I)),I=M1,M2)		A 467
	IF (IDEBUG.LE.0) GO TO 380		A 468
C		SET OF WRITE STATEMENTS FOR TROUBLE-SHOOTING PURPOSES	A 469
	WRITE (6,620) (A(1,NP(I)),I=M1,M2)		A 470
	WRITE (6,630) (A(2,NP(I)),I=M1,M2)		A 471
	WRITE (6,640) (A(3,NP(I)),I=M1,M2)		A 472
	WRITE (6,650) (U(NP(I)),I=M1,M2)		A 473
	WRITE (6,660) (BETA(NP(I)),I=M1,M2)		A 474
	WRITE (6,670) (GAMA(NP(I)),I=M1,M2)		A 475
	WRITE (6,680) (DI(NP(I)),I=M1,M2)		A 476
	WRITE (6,690) (DIP1(NP(I)),I=M1,M2)		A 477
	WRITE (6,700) (AI(NP(I)),I=M1,M2)		A 478
	WRITE (6,710) (AIP1(NP(I)),I=M1,M2)		A 479
380	WRITE (6,790)		A 480
	IF (M2.EQ.NPRNT) GO TO 390		A 481
	M1=M2+1		A 482
	M2=M2+13		A 483
	GO TO 370		A 484
390	CONTINUE		A 485
C		EXCHANGE TIME LEVELS	A 486
	DO 410 I=1,NX		A 487
	DO 400 L=1,6		A 488
	DATANW(L,I)=DATANX(L,I)		A 489
400	CONTINUE		A 490
	YNW(I)=YNX(I)		A 491
	QNW(I)=QNX(I)		A 492
	CNW(I)=CNX(I)		A 493
	CTRBW(I)=CTRBX(I)		A 494
	CSSW(I)=CSSX(I)		A 495
410	CONTINUE		A 496
	IF (NPLT.EQ.0) GO TO 430		A 497
	DO 420 L=1,NPLT		A 498
	K=NPP(L)		A 499
420	CSAV(L,JP)=CNX(K)		A 500

C		A 501
	430 CONTINUE	A 502
	GO TO 450	A 503
C		A 504
C	END TIME LOOP	A 505
C	* * * * *	A 506
	440 WRITE (6,1010) IMON,IDY,IYR,IHR	A 507
	STOP	A 508
C		A 509
C	PLOT DATA ON PRINTER	A 510
	-----	A 511
	450 CONTINUE	A 512
	IF (NPLOT.LE.0) GO TO 610	A 513
	DPI=DT/86400.*IPLT	A 514
	IPLT1=IPLT+1	A 515
	XM=CSAV(1,2)	A 516
	DO 470 I=1,NPLOT	A 517
	K1=0	A 518
	DO 460 K=IPLT1,NTSP1,IPLT	A 519
	K1=K1+1	A 520
	CSAV(I,K1)=CSAV(I,K)	A 521
	IF (CSAV(I,K1).GT.XM) XM=CSAV(I,K1)	A 522
	460 CONTINUE	A 523
	470 CONTINUE	A 524
C		A 525
	IXMAX=INT(XM)	A 526
	DO 480 I=1,12	A 527
	IUP=IRNG(I)	A 528
	IF (IUP.GE.IXMAX) GO TO 490	A 529
	480 CONTINUE	A 530
	490 CONTINUE	A 531
	XMAX=IRNG(I)	A 532
	XMIN=0.0	A 533
C		A 534
	BEGIN PLOTTING	A 535
	CALL PLOT1 (NSCALE,8,12,10,10)	A 536
	WRITE (6,1030)	A 537
	M1=1	A 538
	M2=96	A 539
500	IF (M2.GT.K1) M2=K1	A 540
	NOPTS=M2-M1+1	A 541
	DO 510 I=1,NOPTS	A 542
510	Z(I)=(I+M1-1)*DPI	A 543
	IF (M1.GT.1) GO TO 520	A 544
	YMIN=Z(M1)-DPI	A 545
	YMAX=Z(M2)	A 546
520	CONTINUE	A 547
	CALL PLOT2 (IMAGE,XMAX,XMIN,YMIN,YMAX,6)	A 548
	DO 530 I=1,NPLOT	A 549
	DO 530 K=1,NOPTS	A 550
530	X(K)=CSAV(I,K+M1-1)	A 551
	GO TO (540,550,560,570,580), I	A 552
	GO TO (540,550,560,570,580), I	A 553
540	CALL PLOT3 ('A',X,Z,NOPTS)	A 554
	GO TO 590	A 555
550	CALL PLOT3 ('B',X,Z,NOPTS)	A 556
	GO TO 590	A 557
560	CALL PLOT3 ('C',X,Z,NOPTS)	A 558
	GO TO 590	A 559
570	CALL PLOT3 ('D',X,Z,NOPTS)	A 560
	GO TO 590	
580	CALL PLOT3 ('E',X,Z,NOPTS)	
590	CONTINUE	

IF (M2.GE.K1) GO TO 600	A 561
CALL OMIT (5)	A 562
CALL PLOT4 (17,' TIME IN DAYS')	A 563
M1=M2+1	A 564
M2=M2+96	A 565
YDEL=YMAX-YMIN	A 566
YMIN=YMAX	A 567
YMAX=YMAX+YDEL	A 568
GO TO 500	A 569
600 CALL OMIT (-3)	A 570
CALL PLOT4 (17,' TIME IN DAYS')	A 571
WRITE (6,990)	A 572
WRITE (6,1000) (LETTER(I),NPP(I),I=1,NPLOT)	A 573
610 STOP	A 574
C	A 575
C	A 576
C	A 577
C	A 578
C	A 579
C	A 580
620 FORMAT (' ',10X,'A(1, )',13F8.4)	A 581
630 FORMAT (' ',10X,'A(2, )',13F8.4)	A 582
640 FORMAT (' ',10X,'A(3, )',13F8.4)	A 583
650 FORMAT (' ',15X,'D',13F8.4)	A 584
660 FORMAT (' ',12X,'BETA',13F8.4)	A 585
670 FORMAT (' ',12X,'GAMA',13F8.4)	A 586
680 FORMAT (' ',14X,'DI',13F8.1)	A 587
690 FORMAT (' ',12X,'DIP1',13F8.1)	A 588
700 FORMAT (' ',14X,'AI',13F8.1)	A 589
710 FORMAT (' ',12X,'AIP1',13F8.1)	A 590
720 FORMAT (2F8.0,40X,2F8.0,4X,I4)	A 591
730 FORMAT (' ',12,'/',12,'/',14,3X,I4,2X,13(5(1H-),3X))	A 592
740 FORMAT (' ',12X,'XSEC',13(3X,I2,3X))	A 593
750 FORMAT (1H ,8X,'VELOCITY',13F8.2)	A 594
760 FORMAT (1H ,11X,'DEPTH',13F8.2)	A 595
770 FORMAT (1H ,7X,'DISCHARGE',13F8.0)	A 596
780 FORMAT (1H ,3X,'CONCENTRATION',1X,13F8.3)	A 597
790 FORMAT (1H )	A 598
800 FORMAT (16X,8F8.2)	A 599
810 FORMAT ('0',//10X,20A4,//1X)	A 600
820 FORMAT (10I8)	A 601
830 FORMAT (20A4)	A 602
840 FORMAT ('0',130(1H*),//,25X,'JB80--MASS TRANSPORT SIMULATION USING 1 AN IMPLICIT FINITE DIFFERENCE MODEL.',//,1X,130(1H*))	A 603
850 FORMAT ('0',10X,'CONSTITJENT INFLOW CODE; (1) CONCENTRATION (2) F 1LUX',6(1H-),I7/11X,'SOURCE/SINK CODE; (0) NO (1) YES',25(1H-),I7/ 211X,'DISPERSION CODE; (0) ZERO (1) SELF-SETTING',14(1H-),I7)	A 604
860 FORMAT (' ',10X,'STARTING DATE',45(1H-),I4,'/',I2,'/',I4)	A 605
870 FORMAT (' ',10X,'NUMBER OF CROSS-SECTIONS',34(1H-),I7/11X,'NUMBER 1OF TIME STEPS',38(1H-),I7/11X,'LENGTH OF TIME STEP (MINUTES)',29(1 2H-),F9.1/11X,'NUMBER OF TRIBUTARIES',37(1H-),I7)	A 606
880 FORMAT (' ',10X,'MULTIPLIER FOR SELF-SETTING DISPERSION COEFFICIEN 11',8(1H-),F10.2)	A 607
890 FORMAT (' ',10X,'DECAY COEFFICIENT',41(1H-),F14.6)	A 608
900 FORMAT ('1',40X,'VALUES OF INFLOWING CONSTITUENT'/1X,120(1H-)/1X,1 12F10.2/(1X,12F10.2))	A 609
910 FORMAT ('1',40X,'VALUES OF SOURCE (+) OR SINK (-) FLJX'/1X,120(1H- 1)/1X,12F10.2/(1X,12F10.2))	A 610
920 FORMAT ('1',40X,'VALUES OF INFLOWING CONSTITUENT FROM TRIBUTARY NO 1.',I2/1X,120(1H-)/1X,12F10.2/(1X,12F10.2))	A 611
	A 612
	A 613
	A 614
	A 615
	A 616
	A 617
	A 618
	A 619
	A 620



930	FORMAT ('1',10X,31(1H-),'CROSS-SECTION AND INITIAL FLOW DATA',31(1	A 621
	1H-))//,1X,10X,'A-SEC                    A                    DELX                    Z                    STREAMFLOW	A 622
2	STREAM                    LATERAL INFLOW                    LATERAL Q                    TRIB'/1X,10X,' NO	A 623
3	(FT)                    (FT)                    (FT)                    (CFS)                    CONCENTRATION                    (CFS)	A 624
4	CONCENTRATION                    NO'/1X)	A 625
940	FORMAT (' ',114,F12.0,F11.0,F10.2,F11.1,F13.3,F12.1,F17.3,I7)	A 626
950	FORMAT ('0',////,21X,'OBJECTIVE OF THIS COMPUTER RUN IS TO PLOT K	A 627
	1DOWN HYDROGRAPH DATA')	A 628
960	FORMAT ('0','JOB ABORTED. INCORRECT CHANNEL LENGTH AT CROSS-SECTI	A 629
	ION',I4)	A 630
970	FORMAT ('1',40X,'CROSS-SECTION NUMBER',I3)	A 631
980	FORMAT ('0','OBSERVED CONSTITUENT VALUES'/1X,12F10.2/(1X,12F10.2))	A 632
990	FORMAT ('0',50X,'CONCENTRATION IN MASS PER UNIT VOLUME')	A 633
1000	FORMAT (' ',10X,'EXPLANATION: SYMBOL                    X-SECT'/28X,41,8X,I3/(28X	A 634
	1,41,8X,I3))	A 635
1010	FORMAT ('0','JOB ABORTED AT TIME = ',I2,'/',I2,'/',I4,'::',I4,' INF	A 636
	LOW INTO REACH WAS 0.0 OR LESS.'/1X,'CONCENTRATION WAS BEING COMPU	A 637
	2TED FOR A CONSTITUENT FLJX.')	A 638
1020	FORMAT ('0','AT TIME = ',I2,'/',I2,'/',I4,'::',I4,'. A TRIBUTARY FL	A 639
	LOW WAS 0.0 OR LESS. THE CONCENTRATION FROM THIS TRIBUTARY WAS SET	A 640
	2 TO 0.0')	A 641
1030	FORMAT ('1',27(14*),'GRAPH OF CONCENTRATION VS TIME AT SELECTED CR	A 642
	OSS-SECTIONS',27(14*)//1X)	A 643
1040	FORMAT ('1',30(14*),'FLOW DATA AND CONCENTRATION RESULTS AT SELECT	A 644
	ED CROSS-SECTIONS',30(14*)//4X,'DATE                    HOURS'/1X)	A 645
	END	A 646-

C	SUBROUTINE PRPLOT	B	1
C		B	2
C	PRPLOT= SUBPROGRAM OF ENTRIES TO CONSTRUCT A CONTINUOUS	B	3
C	PRINTER PLOT OF TIME SERIES DATA.	B	4
C		B	5
	IMPLICIT LOGICAL*1(W), LOGICAL*1(K)	B	6
	DIMENSION NSCALE(5), ABNDS(26), X(1), Y(1)	B	7
	LOGICAL*1 NOS(10)/'0','1','2','3','4','5','6','7','8','9'/	B	8
	LOGICAL*1 IMAGE(1),CH,LABEL(1),ERR1,ERR3,ERR5	B	9
	LOGICAL*1 VC,HC,FOR1(19),FOR2(15),FOR3(19),NC,BL,HF,HF1	B	10
	REAL*8 FOX1(3),FOX2(2),FOX3(3)	B	11
	INTEGER*2 VCR	B	12
	EQUIVALENCE (FOR1(1),FOX1(1)), (FOR2(1),FOX2(1)), (FOR3(1),FOX3(1))	B	13
	1), (VC,VCR)	B	14
	INTEGER FILE	B	15
	DATA HC/'-'/,NC/'+'/,BL/' '/,HF/'F'/,HF1/'.'/	B	16
	DATA FOX1/'(1XA1,F9','.2, 121',.A1) '/	B	17
	DATA FOX2/'(1XA1, 9',.X121A1) '/	B	18
	DATA FOX3/'(1HOF .',', F ',. ) '/	B	19
	DATA VCR/44F00/	B	20
	DATA KPLLOT1/.FALSE./,KPLLOT2/.FALSE./	B	21
	DATA KABSC,KORD,KBOTGL/3*,FALSE./	B	22
C		B	23
	ENTRY PLOT1(NSCALE,NHL,NSBH,NVL,NSBV)	B	24
	ERR1=.FALSE.	B	25
	ERR3=.FALSE.	B	26
	ERR5=.FALSE.	B	27
	KPLLOT1=.TRUE.	B	28
	KPLLOT2=.FALSE.	B	29
	NH=IABS(NHL)	B	30
	NSH=IABS(NSBH)	B	31
	NV=IABS(NVL)	B	32
	NSV=IABS(NSBV)	B	33
	NSCL=NSCALE(1)	B	34
	IF (NH*NSH*NV*NSV.NE.0) GO TO 10	B	35
	KPLLOT=.FALSE.	B	36
	ERR1=.TRUE.	B	37
	RETURN	B	38
10	KPLLOT=.TRUE.	B	39
	IF (NV.LE.25) GO TO 20	B	40
	KPLLOT=.FALSE.	B	41
	ERR3=.TRUE.	B	42
	RETURN	B	43
20	CONTINUE	B	44
	NV=N-1	B	45
	NV=N+1	B	46
	NDH=NH*NSH	B	47
	NDHP=NDH+1	B	48
	NDV=NV*NSV	B	49
	NDVP=NDV+1	B	50
	NIMG=(NDHP*NDVP)	B	51
	IF (NDV.LE.120) GO TO 30	B	52
	KPLLOT=.FALSE.	B	53
	ERR5=.TRUE.	B	54
	RETURN	B	55
30	CONTINUE	B	56
	IF (NSCL.EQ.0) GO TO 40	B	57
	F5Y=10.**NSCALE(2)	B	58
	F5X=10.**NSCALE(4)	B	59
	IY=MIN0(IABS(NSCALE(3)),7)+1	B	60
	IX=MIN0(IABS(NSCALE(5)),9)+1	B	61
	GO TO 50	B	62

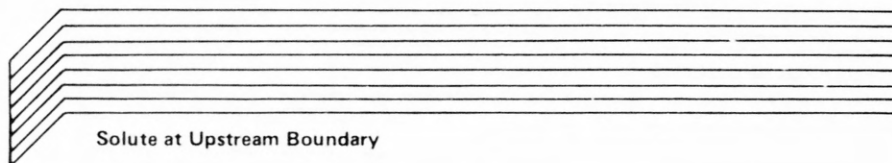
40	FSY=1.	B	63
	FSX=1.	B	64
	IY=4	B	65
	IX=4	B	66
50	FUR1(10)=NOS(IY)	B	67
	NA=MIN0(IX,NSV)-1	B	68
	NS=NA-MIN0(NA,120-NDV)	B	69
	NB=11-NS+NA	B	70
	I1=NB/10	B	71
	I2=NB-I1*10	B	72
	FUR3(6)=NOS(I1+1)	B	73
	FUR3(7)=NOS(I2+1)	B	74
	FUR3(9)=NOS(NA+1)	B	75
	IF (NV.GT.0) GO TO 70	B	76
	DO 60 J=1,18	B	77
60	FUR3(J)=BL	B	78
	GO TO 80	B	79
70	I1=NV/10	B	80
	I2=NV-I1*10	B	81
	FUR3(11)=NOS(I1+1)	B	82
	FUR3(12)=NOS(I2+1)	B	83
	FUR3(13)=HF	B	84
	I1=NSV/100	B	85
	I3=NSV-I1*100	B	86
	I2=I3/10	B	87
	I3=I3-I2*10	B	88
	FUR3(14)=NOS(I1+1)	B	89
	FUR3(15)=NOS(I2+1)	B	90
	FUR3(16)=NOS(I3+1)	B	91
	FUR3(17)=HF1	B	92
	FUR3(18)=FUR3(9)	B	93
80	IF (KPL0T1) RETURN	B	94
	KPL0T1=.TRUE.	B	95
C		B	96
	ENTRY PLOT2(IMAGE,XMAX,XMIN,YMAX,YMIN,FILE)	B	97
	IFL=FILE	B	98
	KPL0T2=.TRUE.	B	99
	IF (KPL0T1) GO TO 90	B	100
	NSCL=0	B	101
	NH=5	B	102
	NSH=10	B	103
	NV=10	B	104
	NSV=10	B	105
	GO TO 10	B	106
90	CONTINUE	B	107
	IF (KPL0T) GO TO 100	B	108
	IF (ERR1) WRITE (IFL,300)	B	109
	IF (ERR3) WRITE (IFL,310)	B	110
	IF (ERR5) WRITE (IFL,320)	B	111
	RETURN	B	112
100	YMX=YMAX	B	113
	DM=(YMAX-YMIN)/FLOAT(NDH)	B	114
	DV=(XMAX-XMIN)/FLOAT(NDV)	B	115
	DO 110 I=1,NVP	B	116
110	ABNOS(I)=(XMIN+FLOAT((I-1)*NSV)*DV)*FSX	B	117
	DO 120 I=1,NIMG	B	118
120	IMAGE(I)=BL	B	119
	DO 160 I=1,NJHP	B	120
	I2=I*NDVP	B	121
	I1=I2-NDV	B	122
	KNHOR=MOD(I-1,NSH).NE.0	B	123
	IF (KNHOR) GO TO 140	B	124

DO 130 J=I1,I2	B 125
130 IMAGE(J)=HC	B 126
140 CONTINUE	B 127
DO 160 J=I1,I2,NSV	B 128
IF (KNHOR) GO TO 150	B 129
IMAGE(J)=NC	B 130
GO TO 160	B 131
150 IMAGE(J)=VC	B 132
160 CONTINUE	B 133
XMIN1=XMIN-DV/2.	B 134
YMIN1=YMIN-DH/2.	B 135
RETURN	B 136
C	B 137
ENTRY PLOT3(CH,X,Y,N3)	B 138
IF (KPLLOT2) GO TO 180	B 139
170 WRITE (IFL,330)	B 140
180 CONTINUE	B 141
IF (.NOT.KPLOT) RETURN	B 142
IF (N3.GT.0) GO TO 190	B 143
KPLOT=.FALSE.	B 144
WRITE (IFL,340)	B 145
RETURN	B 146
190 DO 260 I=1,N3	B 147
IF (DV) 210,200,210	B 148
200 DUM1=0	B 149
GO TO 220	B 150
210 CONTINUE	B 151
DUM1=(X(I)-XMIN1)/DV	B 152
220 IF (DH) 240,230,240	B 153
230 DUM2=0	B 154
GO TO 250	B 155
240 CONTINUE	B 156
DUM2=(Y(I)-YMIN1)/DH	B 157
250 CONTINUE	B 158
IF (DUM1.LT.0..OR.DUM2.LT.0.) GO TO 260	B 159
IF (DUM1.GE.NDVP.OR.DUM2.GE.NDHP) GO TO 260	B 160
NX=1+INT(DUM1)	B 161
NY=1+INT(DUM2)	B 162
J=(NDHP-NY)*NDVP+NX	B 163
IMAGE(J)=CH	B 164
260 CONTINUE	B 165
RETURN	B 166
C	B 167
ENTRY PLOT4(NL,LABEL)	B 168
ENTRY FPLLOT4(NL,LABEL)	B 169
IF (.NOT.KPLOT) RETURN	B 170
IF (.NOT.KPLOT2) GO TO 170	B 171
DO 280 I=1,NDHP	B 172
IF (I.EQ.NDHP.AND.KBOTGL) GO TO 280	B 173
WL=BL	B 174
IF (I.LE.NL) WL=LABEL(I)	B 175
IC=I*NDVP	B 176
II=I2-NDV	B 177
IF (MOD(I-1,NSH).EQ.0.AND..NOT.KORD) GO TO 270	B 178
WRITE (IFL,F0R2) WL,(IMAGE(J),J=I1,I2)	B 179
GO TO 280	B 180
270 CONTINUE	B 181
ORDNO=(YMX-FLOAT(I-1)*DH)*FSY	B 182
IF (I.EQ.NDHP) ORDNO=YMIN	B 183
WRITE (IFL,F0R1) WL,ORDNO,(IMAGE(J),J=I1,I2)	B 184
280 CONTINUE	B 185
IF (KABSC) GO TO 290	B 186
WRITE (IFL,F0R3) (ABNUS(J),J=1,NVP)	B 187

290	RETURN	B 188
C		B 189
	ENTRY OMIT(LSW)	B 190
	KABSC=MOD(LSW,2).EQ.1	B 191
	KORD=MOD(LSW,4).GE.2	B 192
	KROTGL=LSW.GE.4	B 193
	RETURN	B 194
C		B 195
C		B 196
300	FORMAT (T5,'SOME PLOT1 ARG. ILLEGALLY 0')	B 197
310	FORMAT (T5,'NO. OF VERTICAL LINES >25')	B 198
320	FORMAT (T5,'WIDTH OF GRAPH >121')	B 199
330	FORMAT (T5,'PLOT2 MUST BE CALLED')	B 200
340	FORMAT (T5,'PLOT3, ARG2 ) 0')	B 201
	END	B 202-

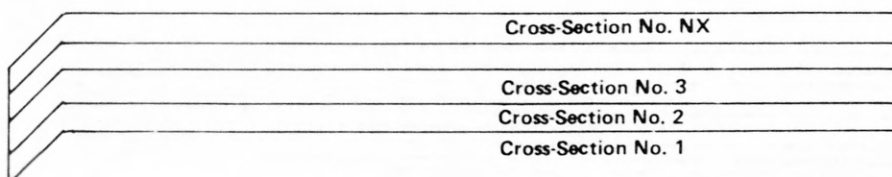


C. SCHEMATIC DIAGRAM OF CARD DECK FOR SOLUTE-TRANSPORT SIMULATION



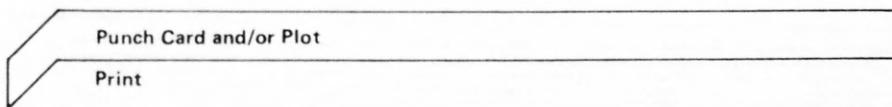
SET NO. IV. INFLOW CONCENTRATIONS

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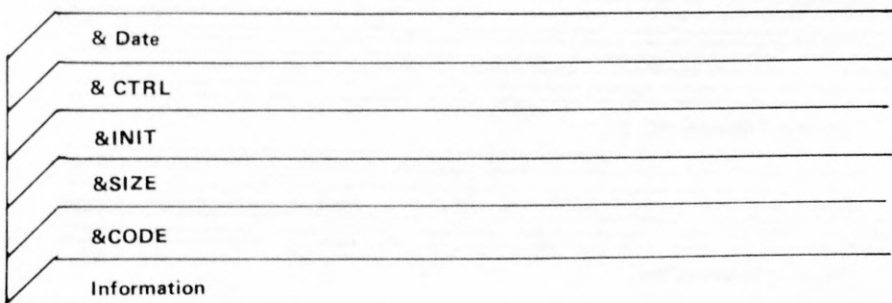
SET NO. III CROSS-SECTION DATA

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SET NO. II CROSS-SECTION OUTPUT

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SET NO. I. PARAMETERS

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The diagram illustrates a multi-layered structure, likely a membrane or a series of thin films, represented by a series of parallel horizontal lines. The structure is divided into three distinct regions, each labeled with text:

- Solute Concentrations NPLOT**: This label is positioned in the upper-middle section of the diagram.
- Solute Concentrations 2**: This label is positioned in the middle section of the diagram.
- Solute Concentrations 1**: This label is positioned in the lower section of the diagram.

The labels are placed within the gaps between the horizontal lines, suggesting they represent different layers or regions of the structure. The overall layout is clean and technical, typical of a scientific or engineering diagram.

The diagram illustrates a multi-layered structure, likely a membrane or a series of thin films, represented by a series of parallel horizontal lines. The structure is divided into three distinct regions, each labeled with text:

- Solute Concentrations NPLOT**: This label is positioned in the upper-middle section of the diagram.
- Solute Concentrations 2**: This label is positioned in the middle section of the diagram.
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The labels are placed within the gaps between the horizontal lines, suggesting they represent different layers or regions of the structure. The overall layout is clean and technical, typical of a scientific or engineering diagram.

Solute from Source or Sink

Solute from Source or Sink

The diagram shows a series of horizontal lines representing layers, with a vertical line on the left side. Three specific layers are labeled from top to bottom:

- Solute at Tributary No. NTRIB
- Solute at Tributary NO. 2
- Solute at Tributary No. 1

The diagram shows a series of horizontal lines representing layers, with a vertical line on the left side. Three specific layers are labeled with text boxes:

- Solute at Tributary No. NTRIB**: Located in the upper-middle section of the diagram.
- Solute at Tributary NO. 2**: Located in the lower-middle section of the diagram.
- Solute at Tributary No. 1**: Located at the bottom of the diagram.

The diagram shows a series of horizontal lines representing layers, with a vertical line on the left side. Three specific layers are labeled with text boxes:

- Solute at Tributary No. NTRIB**: Located in the upper-middle section of the diagram.
- Solute at Tributary NO. 2**: Located in the lower-middle section of the diagram.
- Solute at Tributary No. 1**: Located at the bottom of the diagram.

The diagram shows a series of horizontal lines representing layers, with a vertical line on the left side. Three specific layers are labeled with text boxes:

- Solute at Tributary No. NTRIB**: Located in the upper-middle section of the diagram.
- Solute at Tributary NO. 2**: Located in the lower-middle section of the diagram.
- Solute at Tributary No. 1**: Located at the bottom of the diagram.

D. LISTING OF CARD DECK FOR SOLUTE-TRANSPORT SIMULATION

```
&CODE      ICIN=1,      IDISP=1,      ISS=1,      IDEBUG=0,      NZPLOT=0
&SIZE      Nx=30,      NTS=288,      NT<18=1,      DT=300.
&INIT      DIFAC=1.0,      DKCOEF=0.00001
&CTRL      NPRINT=13,      IPNT=24,      VPLOT=3,      IPLT=3
&DATE      IYR=1976,      IMON=4,      IDY=1,      IHR=0
```

&END  
&END  
&END  
&END  
&END  
25

[illegible][illegible]



SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.10	.10	.10	.10	.10	.10	.10	.10
SOURCE / SINK	.10	.10	.10	.10	.10	.10	.10	.10
SOURCE / SINK	.10	.10	.10	.10	.10	.10	.10	.10
SOURCE / SINK	.10	.10	.10	.10	.10	.10	.10	.10
SOURCE / SINK	.10	.10	.10	.10	.10	.10	.10	.10
SOURCE / SINK	.10	.10	.10	.10	.10	.10	.10	.10
SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.05	.05	.05	.05	.05	.05	.05	.05
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00
SOURCE / SINK	.00	.00	.00	.00	.00	.00	.00	.00

## E. OUTPUT EXAMPLE

\*\*\*\*\*  
 J880--MASS TRANSPORT SIMULATION USING AN IMPLICIT FINITE DIFFERENCE MODEL  
 \*\*\*\*\*

EXAMPLE: J880 MASS TRANSPORT MODEL SIMULATION

CONSTITUENT INFLOW CODE# (1) CONCENTRATION (2) FLUX-----	1
SOURCE/SINK CODE# (0) NO (1) YES-----	1
DISPERSION CODE# (0) ZERO (1) SELF-SETTING-----	1
STARTING DATE-----	4/ 1/1976
NUMBER OF CROSS-SECTIONS-----	30
NUMBER OF TIME STEPS-----	288
LENGTH OF TIME STEP (MINUTES)-----	5.0
NUMBER OF TRIBUTARIES-----	1
MULTIPLIER FOR SELF-SETTING DISPERSION COEFFICIENT-----	1.00
DECAY COEFFICIENT-----	0.000010

-----CROSS-SECTION AND INITIAL FLOW DATA-----								
X-SEC NO	X (FT)	DELTA (FT)	Z (FT)	STREAMFLOW (CFS)	STREAM CONCENTRATION	LATERAL INFLOW (CFS)	LATERAL W CONCENTRATION	TRIB NO
1	1584.	0.	910.54	550.0	1.000	0.0	0.0	0
2	2217.	633.	909.53	550.0	1.000	0.0	0.0	0
3	3000.	783.	908.10	550.0	1.000	0.0	0.0	0
4	4000.	1000.	906.13	550.0	1.000	0.0	0.0	0
5	5121.	1121.	903.76	550.0	1.000	0.0	0.0	0
6	6969.	1848.	901.15	550.0	1.000	0.0	0.0	0
7	9873.	2904.	898.04	550.0	1.000	0.0	0.0	0
8	12302.	2429.	896.96	550.0	1.000	0.0	0.0	0
9	13575.	1373.	895.97	550.0	1.000	0.0	0.0	0
10	14361.	686.	895.87	550.0	1.000	0.0	0.0	0
11	15153.	792.	894.16	590.0	1.000	0.0	0.0	1
12	17793.	2640.	897.55	590.0	1.000	0.0	0.0	0
13	18585.	792.	897.55	590.0	1.000	0.0	0.0	0
14	19536.	951.	897.45	590.0	1.000	0.0	0.0	0
15	22334.	2798.	897.03	590.0	1.000	0.0	0.0	0
16	25291.	2957.	900.52	590.0	1.000	0.0	0.0	0
17	27350.	2059.	899.61	590.0	1.000	0.0	0.0	0
18	30488.	3536.	898.90	590.0	1.000	0.0	0.0	0
19	32419.	1531.	897.49	590.0	1.000	0.0	0.0	0
20	33586.	1267.	895.59	610.0	1.000	20.0	1.000	0
21	35481.	1795.	894.48	610.0	1.000	0.0	0.0	0
22	37066.	1585.	893.27	635.0	1.000	25.0	1.000	0
23	39758.	2692.	891.46	635.0	1.000	0.0	0.0	0
24	43349.	3591.	890.85	635.0	1.000	0.0	0.0	0
25	45038.	1689.	887.84	635.0	1.000	0.0	0.0	0
26	46517.	1479.	888.26	635.0	1.000	0.0	0.0	0
27	48101.	1584.	890.39	635.0	1.000	0.0	0.0	0
28	49685.	1584.	890.21	635.0	1.000	0.0	0.0	0
29	51533.	1848.	889.44	635.0	1.000	0.0	0.0	0
30	52747.	1214.	889.36	635.0	1.000	0.0	0.0	0

[illegible]

[illegible]



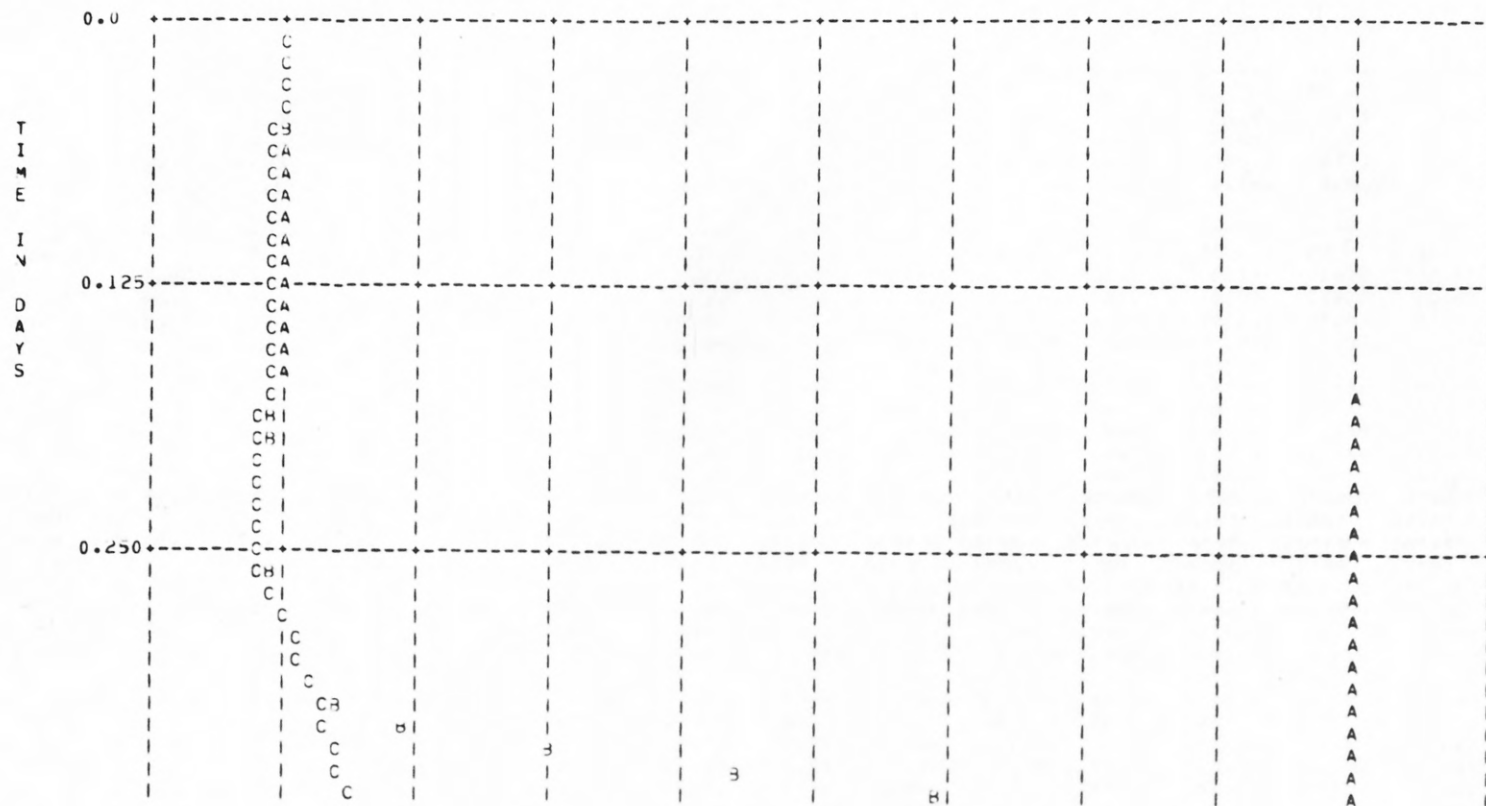
[illegible]

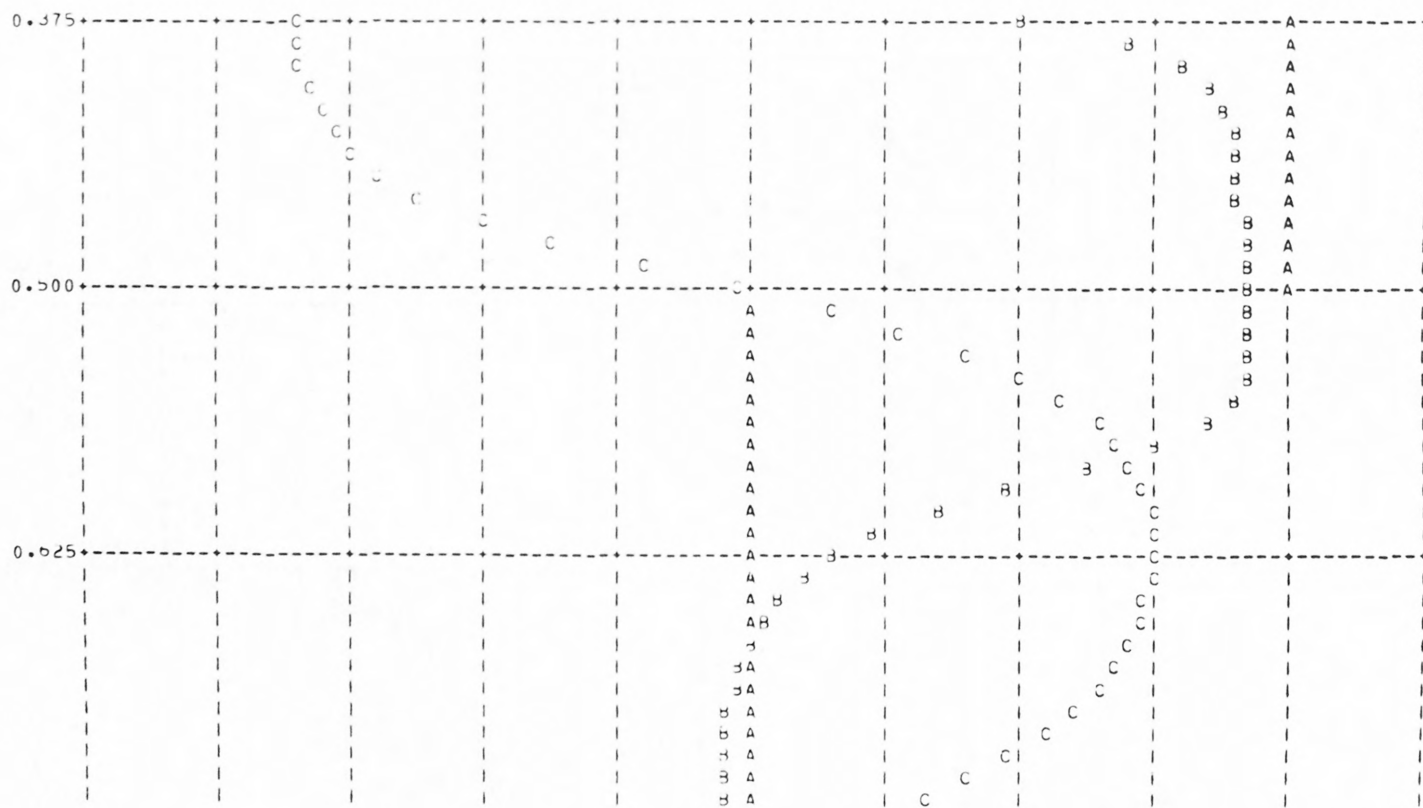
\*\*\*\*\*FLOW DATA AND CONCENTRATION RESULTS AT SELECTED CROSS-SECTIONS\*\*\*\*\*

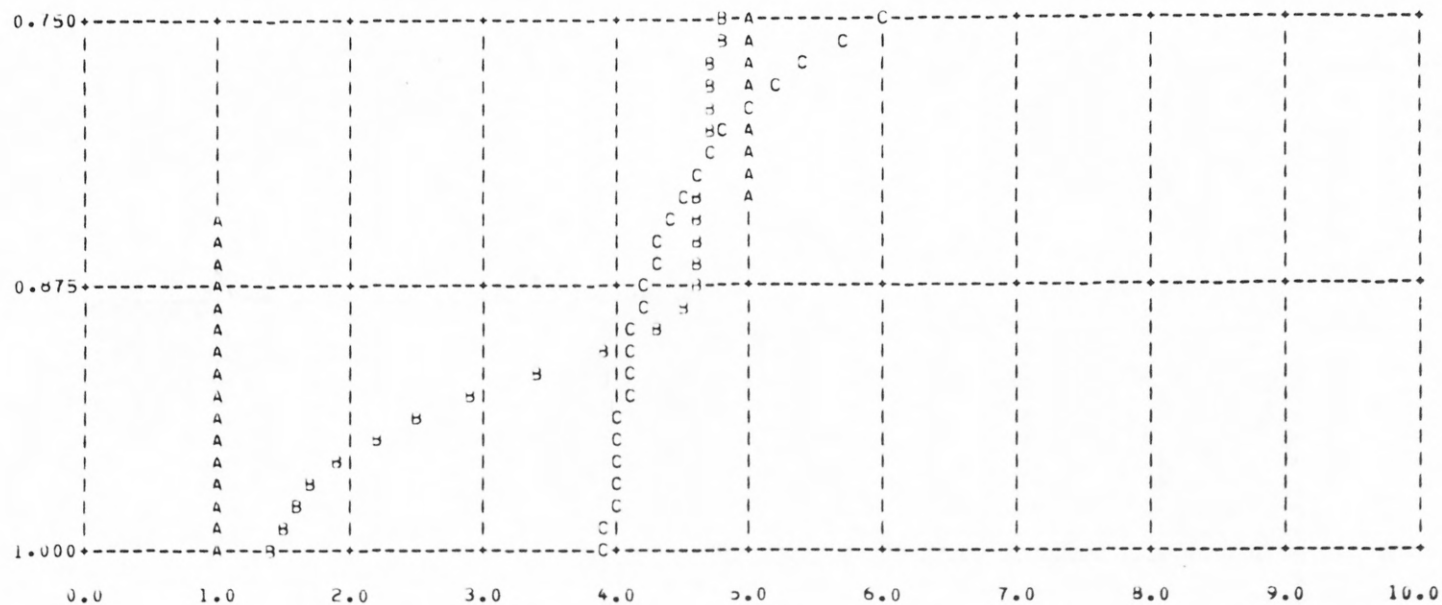
DATE	HOURS													
4/ 1/1976	0	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30	
VELOCITY	1.09	1.33	1.80	0.73	0.46	0.86	1.28	1.50	0.87	0.92	1.89	1.44	1.65	
DEPTH	2.02	2.02	1.70	5.20	7.33	5.60	2.20	2.97	4.33	5.16	2.21	2.59	2.40	
DISCHARGE	550.	550.	550.	550.	550.	590.	590.	590.	635.	635.	635.	635.	635.	
CONCENTRATION	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
4/ 1/1976	200	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30	
VELOCITY	0.77	1.33	1.79	0.73	0.46	0.86	1.28	1.50	0.87	0.85	1.38	0.99	1.04	
DEPTH	2.84	2.02	1.71	5.21	7.32	5.59	2.20	2.86	4.31	5.49	2.85	3.48	3.49	
DISCHARGE	550.	550.	550.	549.	549.	588.	586.	585.	631.	624.	602.	590.	582.	
CONCENTRATION	1.000	0.994	0.984	0.947	0.936	0.930	0.927	0.927	0.933	0.926	0.922	0.925	0.922	
4/ 1/1976	400	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30	
VELOCITY	0.77	1.33	1.79	0.73	0.46	0.86	1.28	1.50	0.87	0.84	1.37	1.01	1.06	
DEPTH	2.84	2.02	1.71	5.21	7.33	5.60	2.21	2.86	4.30	5.50	2.98	3.61	3.62	
DISCHARGE	550.	550.	550.	550.	549.	589.	589.	588.	632.	629.	624.	621.	620.	
CONCENTRATION	1.000	0.994	0.984	0.935	0.891	0.875	0.864	0.862	0.871	0.867	0.862	0.862	0.860	
4/ 1/1976	600	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30	
VELOCITY	0.77	1.33	1.79	0.73	0.46	0.86	1.28	1.50	0.87	0.84	1.37	1.01	1.07	
DEPTH	2.84	2.02	1.71	5.21	7.33	5.60	2.21	2.87	4.31	5.63	3.01	3.65	3.66	
DISCHARGE	550.	550.	550.	550.	550.	590.	590.	589.	634.	632.	631.	630.	629.	
CONCENTRATION	9.000	8.950	8.860	5.605	1.179	0.848	0.815	0.806	0.815	0.810	0.806	0.807	0.804	
4/ 1/1976	800	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30	
VELOCITY	2.55	2.99	3.61	3.14	1.91	2.63	2.12	1.68	0.98	0.84	1.37	1.01	1.07	
DEPTH	5.98	6.39	6.07	7.77	9.33	7.21	3.26	3.09	4.34	5.64	3.02	3.66	3.67	
DISCHARGE	3964.	3963.	3942.	3568.	2931.	2349.	1443.	712.	649.	634.	633.	633.	633.	
CONCENTRATION	9.000	8.985	8.962	9.324	6.849	3.795	1.444	1.547	1.415	1.318	1.322	1.344	1.315	

4/ 1/1976 1000	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.67	2.99	3.49	2.57	1.87	2.88	2.54	2.93	1.58	2.01	2.12	1.44	1.35
DEPTH	6.03	6.49	6.40	10.26	12.11	10.10	6.45	7.65	9.59	7.54	4.71	5.32	5.32
DISCHARGE	4023.	4023.	4018.	3916.	3774.	3687.	3481.	3144.	2800.	2064.	1553.	1316.	1165.
CONCENTRATION	9.000	8.985	8.963	8.885	8.761	8.625	8.220	6.819	4.308	2.073	1.832	1.804	1.765
4/ 1/1976 1200	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.67	2.99	3.41	2.45	1.82	2.82	2.46	2.90	1.78	2.09	2.17	1.83	1.89
DEPTH	6.04	6.53	6.56	10.97	12.85	10.88	7.35	9.08	11.56	11.28	8.66	9.33	9.33
DISCHARGE	4035.	4035.	4032.	3992.	3938.	3931.	3852.	3731.	3655.	3377.	3102.	2982.	2910.
CONCENTRATION	9.000	8.996	8.993	8.975	8.940	8.726	8.641	8.559	8.272	7.236	5.938	5.208	4.897
4/ 1/1976 1400	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.58	2.98	3.38	2.40	1.80	2.79	2.42	2.87	1.78	2.05	2.18	1.95	2.04
DEPTH	6.05	6.55	6.65	11.26	13.17	11.21	7.71	9.59	12.37	12.54	10.05	10.73	10.73
DISCHARGE	4047.	4047.	4044.	4021.	3995.	4014.	3978.	3924.	3922.	3813.	3715.	3674.	3650.
CONCENTRATION	5.000	5.004	5.022	5.073	5.728	6.572	7.983	8.539	8.458	8.313	8.144	8.033	7.850
4/ 1/1976 1600	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.57	2.98	3.36	2.37	1.79	2.77	2.40	2.86	1.78	2.05	2.19	1.99	2.10
DEPTH	6.04	6.55	6.68	11.39	13.31	11.36	7.88	9.82	12.68	13.13	10.55	11.22	11.23
DISCHARGE	4035.	4035.	4041.	4034.	4023.	4052.	4036.	4011.	4035.	3991.	3952.	3936.	3927.
CONCENTRATION	5.000	4.998	4.993	4.965	4.904	4.895	5.090	5.650	6.464	7.510	7.921	7.971	7.842
4/ 1/1976 1800	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.71	3.01	3.39	2.41	1.82	2.81	2.41	2.88	1.79	2.06	2.19	2.00	2.12
DEPTH	6.14	6.57	6.83	11.54	13.45	11.49	8.01	9.96	12.85	13.34	10.76	11.44	11.44
DISCHARGE	4154.	4158.	4154.	4154.	4137.	4150.	4134.	4100.	4121.	4086.	4062.	4053.	4047.
CONCENTRATION	5.000	4.997	4.993	4.965	4.875	4.819	4.783	4.780	4.812	5.268	5.773	6.030	6.003
4/ 1/1976 2000	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.58	2.98	3.34	2.35	1.79	2.76	2.38	2.86	1.79	2.06	2.20	2.02	2.13
DEPTH	6.05	6.56	6.73	11.54	13.47	11.52	8.05	10.04	12.95	13.50	10.92	11.59	11.59
DISCHARGE	4047.	4044.	4044.	4049.	4054.	4099.	4106.	4112.	4159.	4153.	4143.	4139.	4136.
CONCENTRATION	5.000	4.987	4.962	4.860	4.730	4.645	4.582	4.526	4.454	4.438	4.482	4.524	4.459
4/ 1/1976 2200	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	2.27	2.51	3.11	2.29	1.76	2.74	2.37	2.86	1.79	2.05	2.19	2.02	2.13
DEPTH	5.06	5.89	5.40	11.47	13.42	11.48	8.03	10.02	12.94	13.51	10.93	11.60	11.61
DISCHARGE	2871.	3173.	3587.	3924.	3977.	4060.	4079.	4089.	4137.	4141.	4142.	4143.	4143.
CONCENTRATION	1.000	1.014	1.006	0.985	1.702	2.562	3.873	4.323	4.284	4.206	4.171	4.158	4.082

4/ 1/1976 2400	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----
XSEC	1	2	4	7	10	13	16	19	22	25	28	29	30
VELOCITY	0.77	1.32	1.67	0.67	0.62	1.25	1.51	2.03	1.37	1.66	2.00	1.86	2.01
DEPTH	2.54	2.03	1.85	3.10	10.24	8.49	5.27	7.45	10.38	12.27	9.72	10.40	10.41
DISCHARGE	550.	550.	555.	800.	1050.	1330.	1674.	2120.	2494.	2974.	3274.	3398.	3472.
CONCENTRATION	1.000	0.995	0.983	0.959	1.089	1.195	1.645	2.373	3.097	3.787	3.925	3.942	3.886







EXPLANATION: SYMBOL X-SECT

A	1
B	15
C	30