GEOPHYSICALLY ESTIMATED POROSITY OF SELECTED PALEOZOIC ROCKS IN THE UPPER COLORADO RIVER BASIN, COLORADO, UTAH, WYOMING, AND ARIZONA

by Gregory A. Wetherbee and William P. Van Liew

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CONVERSION FACTORS

<table>
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<tr>
<th>Multiply</th>
<th>By</th>
<th>To obtain</th>
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<tbody>
<tr>
<td>foot (ft)</td>
<td>0.3048</td>
<td>meter</td>
</tr>
<tr>
<td>gallon per minute (gal/min)</td>
<td>0.00353</td>
<td>cubic meter per second</td>
</tr>
<tr>
<td>square mile (mi²)</td>
<td>2.590</td>
<td>square kilometer</td>
</tr>
<tr>
<td>inch (in.)</td>
<td>2.54</td>
<td>centimeter</td>
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<tr>
<td>microsecond per foot (µs/ft)</td>
<td>3,281,000</td>
<td>seconds per meter</td>
</tr>
<tr>
<td>atmosphere (atm)</td>
<td>76.0</td>
<td>centimeter of mercury</td>
</tr>
<tr>
<td>gram per cubic centimeter (g/cm³)</td>
<td>62.43</td>
<td>pound per cubic foot</td>
</tr>
</tbody>
</table>

Temperature in degree Celsius (°C) may be converted to degree Fahrenheit (°F) by using the following equation:

\[ °F = \frac{9}{5} \times °C + 32.\]

The following term and abbreviation also is used in this report:
American Petroleum Institute units (API units)
ABSTRACT

As part of the Regional Aquifer Systems Analysis of the Upper Colorado River Basin, the porosity in selected Paleozoic rocks was estimated from borehole geophysical logs of oil-and-gas exploratory boreholes. Assumptions were made concerning the geophysical properties of selected sandstone, limestone, and dolomite rocks in order to calculate porosity from sonic, neutron, and bulk-density logs. Departs from conditions requisite for porosity estimations from each type of log were identified; the most common departure was the presence of shale in the formation rock. Intervals containing shale lenses, natural gas, and fractures were discarded from the analysis; however, no accounting was made for interstitial shale.

Geophysically estimated porosity values were compared with laboratory-porosity values of core samples from 19 formation intervals in 17 boreholes, and a general correspondence was established. Porosity then was calculated from the sonic, neutron, and bulk-density logs from 99 formation intervals in 63 boreholes in which all 3 geophysical logs had been run, but in which no laboratory core analysis had been done.

The grand mean geophysically estimated porosity of the sandstones that comprise the aquifers in upper Paleozoic rocks ranges from 1.0 to 16.2 percent. The grand mean geophysically estimated porosity of the carbonate rocks that comprise aquifers in the middle Paleozoic rocks ranges from 0.4 to 10.5 percent. Values of porosity estimated by this method of analysis for shaley formations are more indicative of total porosity than of effective porosity.

INTRODUCTION

During 1975, the U.S. Geological Survey began the Regional Aquifer Systems Analysis (RASA) program to provide quantitative assessments of regional aquifer systems. A regional aquifer was defined by Bennett (1979, p. 36-42):

A regional aquifer system ** may be of two general types: it may comprise an extensive set of aquifers and aquitards (confining beds) which are hydraulically connected, or it may represent a set of essentially independent aquifers which share so many common characteristics that they can be studied efficiently in a single exercise.
In anticipation of increasing ground-water use in the Upper Colorado River Basin, the U.S. Geological Survey began a regional aquifer systems analysis (UCRASA) of this area in 1981 (Taylor and others, 1983). Objectives of the UCRASA were to:

1. Identify aquifers and confining layers within the region;
2. Determine the geologic, hydrologic, and hydraulic characteristics of aquifers;
3. Determine the geochemical characteristics of ground water in these aquifers;
4. Analyze the regional flow system; and
5. Estimate the water-supply capability of the major aquifers.

In order to estimate the hydraulic characteristics of aquifers for use in flow-system analysis and subsequent development of simulation models that could be used to estimate the hydrologic effects of potential ground-water development, borehole geophysical logs were analyzed to estimate porosity in selected Paleozoic aquifers. This report is an expanded version of a paper published in American Water Resources Association monograph number 14; titled "Geophysically Determined Porosity of Paleozoic rocks in the Upper Colorado River Basin" (Wetherbee and Van Liew, 1988).

**Purpose and Scope**

This report presents the results of borehole geophysical-log analysis for the UCRASA, which includes parts of Colorado, Utah, Wyoming, and Arizona. Porosity values in this report will be used to estimate hydraulic properties of aquifers in the study area. The study area is the Upper Colorado River Basin above Lees Ferry, Ariz. The basin is in western Colorado, eastern Utah, southwestern Wyoming, northeastern Arizona, and northwestern New Mexico. The basin has an area of about 113,500 mi², but approximately 14,600 mi² of the upper part of the San Juan basin in southwestern Colorado and northwestern New Mexico has been excluded from this study and is part of a separate RASA program (fig. 1).

Regional aquifers comprised of sandstone, limestone, dolomite, and conglomerate of Paleozoic age were selected for porosity analysis. Known confining or semiconfining rocks, such as shale and evaporite deposits, were not analyzed. Data for this report were obtained from the Petrowell Libraries of the Petroleum Information Corporation¹ and included borehole geophysical logs of oil-and-gas exploratory boreholes, formation records, and laboratory analyses of borehole core samples. Data from 99 formation intervals in 63 boreholes were available for analysis in the Upper Colorado River Basin.

¹Use of company or brand names in this report is for identification purposes only and does not constitute endorsement by the U.S. Geological Survey.
Figure 1.—Location of the study area and areal extent of Paleozoic rocks in the Upper Colorado River Basin [modified from King and Beikman (1974) and Rocky Mountain Association of Geologists (1972)].
Geologic Setting

In the study area, tectonic activity has formed many uplifts and basins, as shown in figure 2. Paleozoic rocks are areally extensive in the study area and generally are continuous. They are absent in the Middle Park region, the Uinta, Uncompahgre, Gunnison, and Sawatch uplifts, the San Juan volcanic field, and the Sierra Madre and Park Ranges (figs. 1 and 2).

Representative stratigraphic columns of Paleozoic rocks in the study area, grouped by selected tectonic features, are shown on plate 1. Taylor and others (1986) divided these rocks into four hydrogeologic units that represent groups of formations that have similar hydrologic and lithologic characteristics. Because of the large study area and wide areal variations in hydrologic and lithologic characteristics, it was not possible to classify each formation as an aquifer or confining layer. In more detailed studies of Paleozoic rocks, Lindner-Lunsford and others (1989), subdivided the unit named the upper Paleozoic aquifers and confining layers into two subunits called, in descending order, the upper Paleozoic aquifers and the upper Paleozoic confining layers. In this report, these units are referred to as the aquifers in upper Paleozoic rocks and the confining units in upper Paleozoic rocks.

Units selected for porosity estimation within the upper Paleozoic aquifers subunit include rocks of the Tensleep, Coconino, and Weber Sandstones and the Maroon and Cutler Formations. Several members of the Cutler Formation, including the DeChelly Sandstone, White Rim Sandstone, and Cedar Mesa Sandstone Members, were analyzed separately. The upper Paleozoic confining layers subunit consists of Permian, Pennsylvanian, and Mississippian deposits of shale, siltstone, evaporite, carbonate, and clastic rocks.

Within the aquifers in middle Paleozoic rocks, Mississippian and Devonian formations such as the Leadville, Madison, Redwall, and Ouray Limestones were selected for analysis. These formations are homogeneous deposits of limestone and dolomite.

The aquifers and confining layers in lower Paleozoic rocks consist predominantly of limestones and dolomites with minor beds of quartzite and other formations of heterogeneous composition. Data at one site in the Bighorn Dolomite were analyzed for this unit.

The aquifers in basal Paleozoic rocks unit consist predominantly of quartzitic sandstone. Data at one site in the Sawatch Sandstone were analyzed.

The formation intervals analyzed in this study were identified by using driller-designated formation tops. Due to the lack of conformity in the stratigraphic nomenclature for Paleozoic rocks in the study area, some of the driller-designated formation tops might be erroneous, and therefore, intervals analyzed may have a lithologic composition different from that assumed for this analysis. It is possible that some of the intervals analyzed are from formations that were incorrectly identified.
Figure 2.--Principal tectonic features of the Upper Colorado River Basin [modified from Taylor and others (1986)].
METHODS OF ESTIMATING POROSITY FROM ANALYSIS OF GEOPHYSICAL LOGS

Quantitative estimates of porosity can be obtained from the analysis of each of three types of geophysical logs. Porosity can be estimated from the sonic log by using theoretical equations, from the neutron log by using an empirical approach, and from the bulk-density log by a method that uses elements of the empirical approach and the theoretical equations. Bredehoeft (1964) developed an empirical relation of porosity to permeability for the Tensleep Sandstone within the Bighorn Basin, Wyo., using porosity values estimated from sonic and neutron geophysical logs. Each type of logging tool measures a physical property that can be related to formation porosity; porosity is not measured directly by any of the three types of logging tools. Thus, different assumptions are inherent in each method used to estimate porosity from each of the three types of logs.

The sonic log records the transit time of an acoustic pulse traveling from a sonic generator in the logging tool, through the formation, and back to a receiver in the tool. In clean, consolidated formations that have uniformly distributed intergranular pores, transit time is a linear function of porosity, according to the time-average equation (Keys and MacCary, 1971; Schlumberger Limited, 1972):

\[ \phi_{\text{sonic}} = \frac{\Delta t_{\log} - \Delta t_{\text{matrix}}}{\Delta t_{\text{fluid}} - \Delta t_{\text{matrix}}} \times 100 \]  

(1)

where

\( \phi_{\text{sonic}} \) = porosity, in percent, as estimated from the sonic log;

\( \Delta t_{\log} \) = transit time of the formation that is recorded on the sonic log;

\( \Delta t_{\text{matrix}} \) = transit time of the pure rock matrix; and

\( \Delta t_{\text{fluid}} \) = transit time of the interstitial fluid.

Although the time-average equation is valid for any consistent system of units, transit times usually are expressed in units of microseconds per foot.

The time-average equation basically states that \( \Delta t_{\log} \) is the sum of the time the sonic wave takes to travel through the solid part of the formation (\( \Delta t_{\text{matrix}} \)) and the time the sonic wave takes to travel through the interstitial fluid (\( \Delta t_{\text{fluid}} \)). To estimate porosity from the sonic log, one must assume a value for \( \Delta t_{\text{matrix}} \) and \( \Delta t_{\text{fluid}} \), then read the value for \( \Delta t_{\log} \) from the sonic log. For this report, \( \Delta t_{\text{fluid}} \) is assumed to be 189 \( \mu s/ft \), a commonly assumed value for ground water, and \( \Delta t_{\text{matrix}} \) was estimated for each formation based on lithologic information.

In neutron logging, high-energy neutrons are continuously emitted from a radioactive source in the logging tool. These neutrons collide with the nuclei of the formation rock and the interstitial fluid. With each collision, a neutron loses some of its energy. The amount of energy lost is inversely
proportional to the mass of the nucleus with which the neutron collides. The nuclei of formation rock have a much greater mass than neutrons, and thus neutrons lose little energy in collisions with these nuclei. Conversely, the mass of hydrogen atoms, which are present in interstitial water, are almost equal to the mass of neutrons, and thus neutrons lose much more energy in collisions with these nuclei. Within a few microseconds, the neutrons that have collided with hydrogen atoms have been slowed enough by successive collisions that they diffuse randomly until they are captured by the nuclei of atoms such as chlorine, hydrogen, and silicon. The capturing nucleus then emits a high-energy gamma ray of capture (Schlumberger Limited, 1972).

A detector in the neutron-logging tool records the count rate of either the gamma rays of capture or the neutrons themselves that are scattered back to the tool, depending on the type of neutron-logging tool. Thus, (1) The count rate of the gamma rays of capture measured by the one type of tool is assumed to be directly proportional to the hydrogen content of the formation interval being examined, or the count rate of neutrons measured by the other type of tool is assumed to be inversely proportional to the hydrogen content of the formation interval being examined; and (2) the formation porosity is assumed to be directly proportional to the hydrogen content of the formation interval. Neutron-logging tools are calibrated in limestone pits of known porosity, and "limestone porosity" is recorded directly on the neutron log. If a neutron log that was calibrated for limestone was used for a sandstone formation, an empirical correction was applied (Herst and Nelson, 1985, fig. 10-4C, p. 397) where:

\[
\text{Neutron-log sandstone porosity} = \text{neutron-log limestone porosity} + 3 \text{ percent}
\]

The bulk-density log records the intensity of gamma radiation that originates from a radioactive source in the logging tool and is attenuated and scattered back to a detector in the logging tool by the formation. The gamma rays emitted from the logging tool collide with electrons in the formation. At each collision, a gamma ray loses some of its energy to the electron. The number of collisions is related directly to the number of electrons in the formation. Therefore, the intensity of gamma radiation measured by the logging tool is a measure of the electron density of the formation, which is assumed to be proportional to the bulk density of the formation. Bulk-density-logging tools are calibrated in much the same way as neutron-logging tools. Once the electron density of the formation is calibrated to the bulk density of the formation, the following equation can be used to estimate porosity from the bulk-density log:

\[
\phi_{\text{density}} = \frac{\rho_{\text{matrix}} - \rho_{\text{bulk}}}{\rho_{\text{matrix}} - \rho_{\text{fluid}}} \times 100
\]

where \( \phi_{\text{density}} \) = porosity, in percent, as estimated from the bulk-density log;
\( \rho_{\text{matrix}} \) = the density of the pure rock matrix;
\( \rho_{\text{bulk}} \) = the density of the formation that is recorded on the bulk-density log; and
\( \rho_{\text{fluid}} \) = the density of the interstitial fluid.
Equation (3) is valid for any consistent system of units; however, densities usually are expressed in grams per cubic centimeter.

To estimate porosity from the bulk-density log, one must assume a value for $\rho_{\text{matrix}}$ and $\rho_{\text{fluid}}$, then read the value for $\rho_{\text{bulk}}$ from the bulk-density log. For this report, $\rho_{\text{fluid}}$ is assumed to be 1.00 g/cm$^3$, the density of water at 25 °C and 1 atm pressure. Although these exact conditions rarely exist in formation water, this parameter value gives reasonably accurate results. The parameter $\rho_{\text{matrix}}$ was estimated for each formation based on lithologic information.

For this study, the porosity analysis was not done unless all three types of logs were available, because: (1) Minimal lithologic information was available for individual boreholes that were examined, and (2) different assumptions are inherent in the method of analysis for each type of log. Relations of porosity estimations to depth were compared for each of the three methods. Departures from conditions requisite for porosity estimation by each method were identified by the characteristic response of each log to the departure from ideal conditions.

The most common departure from ideal conditions was the presence of shale in the formation rock, which is a common occurrence in the clastic sedimentary deposits of the Upper Colorado River Basin. The neutron log, which indirectly measures the hydrogen content in the formation, is affected the most, because shales commonly contain much adhered water. The sonic and bulk-density logs, which require an assumption of transit time and density of the rock matrix in order to estimate porosity, also are affected by the presence of shale. In such instances, the natural-gamma log is useful in providing supplemental information. The natural-gamma log records naturally occurring gamma radiation emitted by the formation near the borehole. In sedimentary formations, the natural-gamma log commonly indicates the shale content of the formation, because sandstone, limestone, and dolomite usually have small concentrations of radioactive isotopes, whereas shale usually contains much larger concentrations of radioactive isotopes, mostly the radioactive potassium-40 isotope (Keys and MacCary, 1971).

Logs from borehole 44, which penetrates the Weber Sandstone of Pennsylvanian age, illustrate the usefulness of the natural-gamma log as an aid in determining lithology (fig. 3). At depths of about 3,330, 3,355, and 3,380 ft, the neutron log and the natural-gamma log each have a deflection or "spike" toward the right, indicating that shale was penetrated. When the neutron log and the natural-gamma log had positive deflections at the same depth, the porosity value obtained from the neutron log was considered invalid and was not used in this porosity analysis; however, no accounting was made for interstitial shale. For this reason, porosity values obtained from the neutron log in shaley formations are more indicative of the total porosity, including the percent pore volume that contains adhered water, rather than the effective porosity, which is the porosity value that most often is used to estimate hydraulic properties of aquifers.
Formation intervals in which natural gas was present were identified by the characteristic response of the neutron and bulk-density logs. The density of gases is small compared to that of liquids and solids, and the bulk-density-log analysis, which assumes only liquid water and solid rock matrix, erroneously interprets the small density of gas as due to water-filled porosity. Therefore, the porosity value estimated from the bulk-density log in the presence of natural gas will be larger than the actual porosity. Conversely, the porosity value estimated from the neutron log in the presence of natural gas will be smaller than the actual porosity, because the hydrogen density of gas is less than that of water. The opposite response of these two logs is known as the "football effect" (Brock, 1986, p. 93) and is used to indicate the presence of natural gas (fig. 4). Porosity values for formation intervals that displayed the football effect were considered invalid and were not recorded.
Fractures were identified by the characteristic response of the three porosity logs and the caliper log. The porosity from the bulk-density log deflects in a positive direction in response to a fracture because of the relatively large volume of water in the fracture compared to porosity from interstitial water content elsewhere on the log. The neutron log also deflects in a positive direction due to the large volume of water. The sonic log, however, responds differently to the fracture. The sonic-logging tool records the first acoustic pulse to travel through the formation to a receiver in the tool. Since the acoustic pulse travels faster through the solid formation than through the water-filled fracture, the first pulse to arrive at the receiver will have traveled through the solid formation around the fracture rather than through the fracture. Therefore, the recorded transit time does not indicate the presence of the fracture (Brock, 1986). The caliper
log, which records the borehole diameter, also is useful for identifying irregularities in the borehole wall and confirming the locations of fractures identified by the three geophysical logs. An example of the characteristic response of these logs to a fracture is shown in figure 5. Porosity values for formation intervals for which fractures were identified were considered to be anomalous and thus were not recorded.

![Diagram showing Caliper log and porosity from sonic, neutron, and bulk-density logs showing response to a fracture.](image)

Figure 5.--Caliper log and porosity from sonic, neutron, and bulk-density logs showing response to a fracture [modified from Wetherbee and Van Liew, 1988, p. 168].

Other departures from the inherent assumptions in porosity estimation were not accounted for. No allowances for variations in temperature, pressure, or interstitial-fluid salinity were made. For further information about the theory that supports the methods of analysis described in the preceding paragraphs, the reader is referred to Keys and MacCary (1971), Schlumberger Limited (1972), and Brock (1986).
In the absence of detailed lithologic information, matrix parameters for the geophysical-porosity analysis were selected based on: (1) General lithologic type, (2) the value that made all three geophysical-log-porosity values converge, and (3) the value that resulted in agreement between the geophysically estimated porosity and the porosity from core analysis. The matrix parameters used for sonic-log and bulk-density-log analysis are listed in table 1. In order to determine matrix parameters that resulted in agreement between geophysically estimated porosity and porosity from core analysis, data from borehole geophysical logs of oil-and-gas exploratory boreholes and from laboratory analysis of borehole core samples taken at 1-ft intervals were obtained from the Petrowell Libraries of the Petroleum Information Corporation for 19 formation intervals in 17 boreholes that penetrate aquifers of Paleozoic age. For each formation interval, average values of $\Delta t_{\text{matrix}}$ and $\rho_{\text{bulk}}$ were obtained from the sonic and bulk-density logs at 1-ft intervals, matrix parameters were assumed, and porosity values were calculated for each log at 1-ft intervals and plotted with depth below land surface. Empirical corrections for lithology were applied to porosity values estimated from the neutron log where needed (eq. 2), and neutron-log porosity also was plotted with depth below land surface. The laboratory core-porosity values then were compared with these geophysical-porosity values. Depth corrections were made in some instances, by comparing qualitative changes in the relations of porosity to depth.

### Table 1. Summary of matrix parameters used for porosity estimation

<table>
<thead>
<tr>
<th>Rock matrix</th>
<th>Sonic-log matrix transit time, $\Delta t_{\text{matrix}}$ (microseconds per foot)</th>
<th>Bulk-density log matrix density, $\rho_{\text{matrix}}$ (grams per cubic centimeter)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sandstone</td>
<td>53.3 or 51.3</td>
<td>2.68</td>
</tr>
<tr>
<td>Limestone and Dolomite</td>
<td>43.5 or 47.5</td>
<td>2.71 or 2.87</td>
</tr>
</tbody>
</table>

An example of the comparison of geophysically estimated porosity and laboratory core porosity using different values for $\Delta t_{\text{matrix}}$ is shown in figure 6. For this example, $\Delta t_{\text{matrix}}$ was chosen to be 51.3 $\mu$s/ft, because porosity estimated with this parameter better approximates the laboratory core porosity than the $\Delta t_{\text{matrix}}$ value of 55.6 $\mu$s/ft. Ultimately, this analysis led to assignment of specific $\Delta t_{\text{matrix}}$ and $\rho_{\text{matrix}}$ values for individual formations. These matrix parameter assignments are listed in table 2.
Once the matrix parameters for each formation were selected and it was determined that there was a general correspondence between the variability of geophysically estimated porosity and the variability of laboratory core porosity, porosity was estimated for boreholes in which all three geophysical logs, but for which no laboratory analyses of cores were available. Data from 99 formation intervals in 63 boreholes were available for analysis. For this phase of the analysis, representative values of $\Delta t_{\text{log}}$ and $\rho_{\text{bulk}}$ were selected by eye from the sonic and bulk-density logs at 10-ft intervals, matrix parameters established in the comparison of geophysically estimated porosity with laboratory core analysis were used, and an estimated porosity value for each log was calculated for each 10-ft interval and plotted with depth below land surface.
Table 2.--Matrix parameters used for porosity estimation for individual formations

<table>
<thead>
<tr>
<th>Driller-designated formation name</th>
<th>Sonic-log matrix transit time, $\Delta t_{\text{matrix}}$ (microseconds per foot)</th>
<th>Bulk-density log matrix density, $\rho_{\text{matrix}}$ (grams per cubic centimeter)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Aquifers in upper Paleozoic rocks</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Coconino Sandstone</td>
<td>53.3</td>
<td>2.68</td>
</tr>
<tr>
<td>Cutler Formation</td>
<td>53.3</td>
<td>2.68</td>
</tr>
<tr>
<td>DeChelly Sandstone Member</td>
<td>53.3</td>
<td>2.68</td>
</tr>
<tr>
<td>White Rim Sandstone Member</td>
<td>53.3</td>
<td>2.68</td>
</tr>
<tr>
<td>Cedar Mesa Sandstone Member</td>
<td>53.3</td>
<td>2.68</td>
</tr>
<tr>
<td>Maroon Formation</td>
<td>51.3</td>
<td>2.68</td>
</tr>
<tr>
<td>Tensleep Sandstone</td>
<td>51.3</td>
<td>2.68</td>
</tr>
<tr>
<td>Weber Sandstone</td>
<td>51.3</td>
<td>2.68</td>
</tr>
<tr>
<td><strong>Aquifers in middle Paleozoic rocks</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Leadville Limestone</td>
<td>47.5</td>
<td>2.71</td>
</tr>
<tr>
<td>Madison Limestone</td>
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<td>Redwall Limestone</td>
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<td>2.71</td>
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<td>Ouray Limestone</td>
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<td>2.87</td>
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<tr>
<td>Undifferentiated Mississippian carbonate rocks</td>
<td>4.35, 47.5</td>
<td>2.71, 2.87</td>
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<td><strong>Aquifers in lower and basal Paleozoic rocks</strong></td>
<td></td>
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<tr>
<td>Bighorn Dolomite</td>
<td>43.5, 47.5</td>
<td>2.71, 2.87</td>
</tr>
<tr>
<td>Sawatch Quartzite</td>
<td>51.3</td>
<td>2.68</td>
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</tbody>
</table>

After the estimated porosity logs were inspected for departures from ideal conditions, the mean of the estimated porosity values from the three geophysical logs for each 10-ft interval in each borehole was calculated. The porosity values estimated from the logs that indicated departures from ideal conditions were not included in these calculations. Then the grand mean porosity for the entire interval of interest was determined by computing the mean of the means of the estimated geophysical-porosity values for each 10-ft interval. Grand mean geophysically estimated porosity might be a biased estimate of porosity for intervals that have large variance in porosity over large intervals of borehole. An analysis of variance was used to determine which of the three geophysical logs was the best estimation of grand mean geophysically determined porosity, but the results of this test were inconsistent. Therefore, it was determined that no single geophysical log was unbiased, and the grand mean geophysically estimated porosity was calculated using all three geophysical logs without regard to variance.
Eighty boreholes were selected for estimation of porosity by geophysical methods. These boreholes were assigned serial numbers for identification purposes. The locations of the 17 boreholes for which porosity estimated by geophysical methods was compared to laboratory determinations of porosity from core samples are shown in figure 7. Mean porosity values estimated from geophysical logs did not compare exactly with porosity values determined from laboratory analyses of core samples, but a general correspondence was evident. Differences in some intervals can be attributed to limitations of logging devices and methods. Geophysical logs measure a physical property of the formation and borehole fluid within the radius of investigation of the logging device as it moves up the borehole. The radius of investigation of the sonic, neutron, and bulk-density logs varies from about 0.5 to about 3.5 ft (Keys and MacCary, 1971). Furthermore, the response of the neutron and bulk-density logs is statistical in nature. The detectors in these logging tools count neutrons or gamma rays that are scattered back to the tool from the formation. The counts are averaged over a selected interval of time, known as the time constant. Therefore, the response on the logs from which porosity is calculated is dependent on the time constant and the rate at which the tool moves up the borehole, which is known as the logging speed. Laboratory core analyses were done on samples of core that were, at most, only a few inches long and taken at 1-ft intervals. Because of the smaller sample volume, porosity determined from core samples plotted with depth often varied more than geophysically estimated porosity, which tends to average porosity over a larger sample volume. An example of this phenomenon is shown in figure 8, especially in the interval from 3,000 to 3,030 ft.

Other factors also affect the comparison between geophysically estimated and laboratory core-porosity values. Often, cores are altered by the coring process. Furthermore, in-situ pressures are relieved when the core is extracted, and the core samples expand and cool. In fact, an argument can be made that geophysical-log data yield a better over-all representation of porosity than most laboratory core analyses, because of the inherent variability of most geologic formations and the small sample provided by individual cores (F.L. Paillet, U.S. Geological Survey, written commun., 1987). A comparison of porosity estimated by geophysical methods and by laboratory core analyses for various formations is shown in figures 8 through 14.

The locations of the 63 boreholes for which all three geophysical logs, but for which no laboratory core-porosity analyses were available, are shown on plates 2 and 3. The grand mean geophysically estimated porosity values for boreholes that penetrate the aquifers in upper Paleozoic rocks are shown at the location of the boreholes in figure 15; the grand mean geophysically estimated porosity values for aquifers in the middle, lower, and basal Paleozoic rocks are shown at the location of the boreholes in figure 16. Due to the limited radius of investigation of the geophysical logs compared to the distances between boreholes that were analyzed and to variations of porosity in a vertical profile, grand mean porosity values were not contoured. Boreholes 45 and 46 (pl. 2), which are too close together to plot separately, have grand mean porosity values of 15.7 and 9.5 percent, respectively (fig. 15).
Figure 7.--Locations of boreholes used for comparison of geophysical-porosity and laboratory core-porosity values.
Figure 8.—Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the White Rim Sandstone Member of the Cutler Formation in borehole 67.
Figure 9.--Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the Weber Sandstone in borehole 44.
Figure 10.--Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the Tensleep Sandstone in borehole 17.
Figure 11.—Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the Tensleep Sandstone in borehole 21.
Figure 12.--Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the Tensleep Sandstone in borehole 20.
Figure 13.--Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the Tensleep Sandstone in borehole 5.
Figure 14.--Comparison of porosity values estimated by geophysical methods and by laboratory core analysis for the Leadville Limestone in borehole 76.
Figure 15.--Grand mean geophysically estimated porosity of aquifers in upper Paleozoic rocks.
Figure 16.—Grand mean geophysically estimated porosity of aquifers in the middle, lower, and basal Paleozoic rocks.
The ranges of grand mean geophysically estimated porosity values for each hydrogeologic unit or subunit are listed in table 3. The distribution of grand mean geophysically estimated porosity for the sandstone aquifers in the upper Paleozoic rocks is shown in figure 17. The distribution of grand mean geophysically estimated porosity for the carbonate aquifers in the middle Paleozoic rocks is shown in figure 18. Values of porosity estimated by this method of analysis for shaley intervals probably are larger than the actual porosity values.

Table 3.--Ranges of grand mean geophysically estimated porosity values

<table>
<thead>
<tr>
<th>Hydrogeologic unit</th>
<th>General lithologic type</th>
<th>Range of grand mean geophysically estimated porosity (percent)</th>
<th>Number of formation intervals analyzed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aquifers in upper Paleozoic rocks</td>
<td>Sandstone</td>
<td>1.0 to 16.2</td>
<td>59</td>
</tr>
<tr>
<td>Aquifers in middle Paleozoic rocks</td>
<td>Limestone and dolomite</td>
<td>0.4 to 10.5</td>
<td>38</td>
</tr>
<tr>
<td>Aquifers in lower Paleozoic rocks</td>
<td>Limestone and dolomite</td>
<td>5.0</td>
<td>1</td>
</tr>
<tr>
<td>Aquifers in basal Paleozoic rocks</td>
<td>Quartzite</td>
<td>11.7</td>
<td>1</td>
</tr>
</tbody>
</table>

Because the porosity values obtained herein are to be used to estimate hydraulic characteristics of the aquifers in Paleozoic rocks for use in flow-system analysis, grand mean porosity values for large intervals may be misleading. A large percentage of the total ground-water flow may occur within relatively small intervals of high porosity and hydraulic conductivity. Therefore, the distribution of porosity estimated from each geophysical log throughout the interval of interest for each of the 99 formation intervals that were analyzed is shown on plates 2 and 3.

SUMMARY

As part of the Regional Aquifer Systems Analysis of the Upper Colorado River Basin, the porosity in selected Paleozoic rocks was estimated from borehole geophysical logs of oil-and-gas exploratory boreholes. Assumptions were made concerning the geophysical properties of selected sandstone, limestone, and dolomite rocks in order to calculate porosity from sonic,
neutron, and bulk-density logs. Departures from conditions requisite for porosity estimation from each type of log were identified by the characteristic response of each log to the departure from ideal conditions. The most common departure from ideal conditions was the presence of shale in the formation rock. Formation intervals containing natural gas and fractured intervals also were identified. Intervals containing shale lenses, natural gas, and fractures were discarded from the analysis; however, no accounting was made for interstitial shale.

Geophysically estimated porosity values were compared with laboratory porosity values of core samples from 19 formation intervals in 17 boreholes, and a general correspondence was established. Porosity then was calculated from the sonic, neutron, and bulk-density logs from 99 formation intervals in 63 boreholes for which all 3 geophysical logs had been run, but for which no laboratory core analysis had been done. The mean value of porosity from the three geophysical logs for each 10-foot interval was calculated, and the grand mean porosity for each formation of interest in each borehole was calculated from the mean porosity values from the 10-foot intervals.
Figure 18.--Distribution of grand mean geophysically estimated porosity of aquifers in the middle Paleozoic rocks.

The grand mean geophysically estimated porosity of the sandstone aquifers in the upper Paleozoic rocks ranges from 1.0 to 16.2 percent. The grand mean geophysically estimated porosity of the carbonate aquifers in the middle Paleozoic rocks ranges from 0.4 to 10.5 percent. Values of porosity estimated by this method of analysis for shaley formations are more indicative of total porosity than of effective porosity. Effective porosity is the value that most often is used to estimate hydraulic properties of aquifers.
SELECTED REFERENCES


____ 1980, Stratigraphic sections of Middle Jurassic San Rafael Group from Wilson arch to Bluff in southeastern Utah: U.S. Geological Survey Oil and Gas Chart OC-102.


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