

Flow-Duration Curves

Manual of Hydrology: Part 2. Low-Flow Techniques

GEOLOGICAL SURVEY WATER-SUPPLY PAPER 1542-A



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By JAMES K. SEARCY

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*Methods and practices of the Geological
Survey*



UNITED STATES DEPARTMENT OF THE INTERIOR

WALTER J. HICKEL, *Secretary*

GEOLOGICAL SURVEY

William T. Pecora, *Director*

First printing 1959

Second printing 1963

Third printing 1969

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MANUAL OF HYDROLOGY: PART 2, LOW-FLOW TECHNIQUES

FLOW-DURATION CURVES

By JAMES K. SEARCY

ABSTRACT

The flow-duration curve is a cumulative frequency curve that shows the percent of time specified discharges were equaled or exceeded during a given period. It combines in one curve the flow characteristics of a stream throughout the range of discharge, without regard to the sequence of occurrence. If the period upon which the curve is based represents the long-term flow of a stream, the curve may be used to predict the distribution of future flows for water-power, water-supply, and pollution studies.

This report shows that differences in geology affect the low-flow ends of flow-duration curves of streams in adjacent basins. Thus, duration curves are useful in appraising the geologic characteristics of drainage basins.

A method for adjusting flow-duration curves of short periods to represent long-term conditions is presented. The adjustment is made by correlating the records of a short-term station with those of a long-term station.

INTRODUCTION

Flow-duration curves have been in general use since about 1915; their theory has been discussed by Foster and others. (See list of references.) This chapter describes the methods used by the Geological Survey to construct flow-duration curves from streamflow data and is a revision of instructions originally prepared by W. D. Mitchell and W. B. Langbein, for use in the Survey only, and later modified by C. H. Hardison.

The flow-duration curve (fig. 1) is a cumulative frequency curve that shows the percent of time during which specified discharges were equaled or exceeded in a given period. For example, in the period 1939-48, the daily mean flow of Bowie Creek (fig. 1) was at least 144 cubic feet per second during 90 percent of the time.

The flow-duration curve is the integral of the frequency diagram. Perhaps a simpler concept of the flow-duration curve is that it is another means of representing streamflow data combining in one curve the flow characteristics of a stream throughout the range of

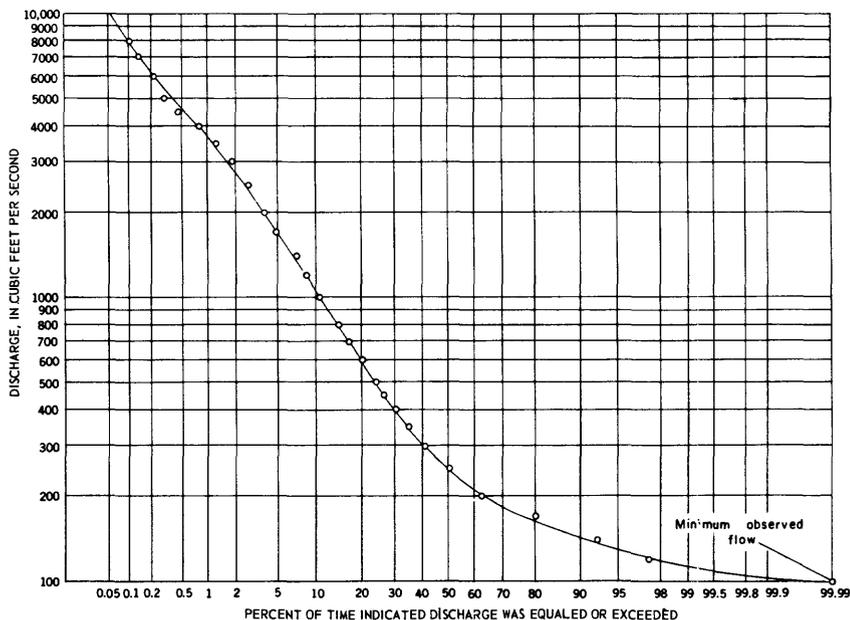


FIGURE 1.—Duration curve of daily flow, Bowie Creek near Hattiesburg, Miss., 1939-48.

discharge. Although the flow-duration curve does not show the chronological sequence of flows, it is useful for many studies.

To prepare a flow-duration curve, the daily, weekly, or monthly flows during a given period are arranged according to magnitude, and the percent of time during which the flow equaled or exceeded the specified values is computed. The curve, drawn to average the plotted points of specified discharges versus the percent of time during which they were equaled or exceeded, thus represents an average for the period considered rather than the distribution of flow within a single year.

In a strict sense, the flow-duration curve applies only to the period for which data were used to develop the curve or to the period to which the curve is adjusted. If streamflow during the period on which the flow-duration curve is based represents the long-term flow of the stream, the curve may be considered a probability curve and used to estimate the percent of time that a specified discharge will be equaled or exceeded in the future.

The flow-duration curve provides a convenient means for studying the flow characteristics of streams and for comparing one basin with another. Various uses of the flow-duration curve are discussed later.

PREPARATION OF DATA

The two principal methods used to construct flow-duration curves are (1) the calendar-year method (Barrows, 1943, p. 137-143, and Saville and Watson, 1933, p. 408-411) and (2) the total-period method.

In the calendar-year method, the discharges for one year are ranked according to magnitude (order number 1, 2, 3 * * *). This process is repeated for each year of record. The discharges for each order number are averaged. A block diagram is plotted with the abscissa in time units and the ordinate in discharge units. If a day is the time unit, the first item plotted is the average of the annual maximum days for the period of record. A percent-of-time scale can be constructed for the abscissa, if desired. The calendar-year method gives lower values for the high discharges and higher values for the low discharges than the more accurate total-period method.

In the total-period method, all discharges are placed in classes according to their magnitude. The totals are cumulated, beginning with the highest class, and the percentage of the totaled time is computed for each class. The data are then plotted with the discharge as the ordinate and the time in percent of total period as the abscissa.

The Geological Survey uses the total-period method and the discussion which follows is restricted to this method.

PERIOD USED

All complete years of record can be used to prepare a flow-duration curve; records for partial years should be excluded. The years for which records are complete need not be consecutive, but the records used should be for years in which physical conditions in the basin, such as artificial storage, diversions, or other manmade influences, were essentially the same. The double-mass curve, which is discussed in another chapter of this manual, is useful for checking the consistency of records to be used for constructing flow-duration curves.

The data for the flow-duration curve are usually prepared on a water-year basis, the same basis as that on which the Geological Survey publishes streamflow records. The use of the water year (which ends September 30) in analyses of the flow-duration curve usually divides a low-flow period. This division is of no consequence for long records, but a flow-duration curve based on the water year of lowest annual flow might not represent a combination of flows as low as that which actually occurred in a 12-month period. When the flow-duration curve is used to study the variations in streamflow from year to year, yearly curves are prepared for climatic years beginning April 1.

In some western streams, snowmelt during a few months provides practically all the flow available for use during the year. For such

streams, a "flow year" of a few months' length might be a more practical basis for flow-duration curves than a 12-month year.

Flow-duration curves for selected portions of a long record are used in adjusting the flow-duration curves for short records to the period of the long record. Flow-duration curves for the Geological Survey standard 25-year period, water years 1921-45, are useful for comparing streamflow in different parts of the United States; the period eventually will be changed to the 30 years 1931-60, to conform with the practice agreed upon by the World Meteorological Organization.

When streamflow has been regulated by storage or diversions, or when the regimen varied during the period of record, a curve for the total period has little meaning. The period used for the flow-duration curve depends on the purpose of the curve. If the curve is to be used in a hydrologic analysis of the characteristics of natural flow, only the unregulated period of record should be used. If the curve is to be used as an indication of the flow that may be expected in the future with a continuation of present conditions, only the record obtained during a period when facilities for regulation and pattern of regulation have been constant should be used. A duration curve based on the record of a short period of regulated flow and adjusted to a longer period by correlation with an unregulated stream (explained in a later section) shows the flow to be expected under the long-period hydrologic conditions, but in the pattern of regulation that existed during the short period. With the adjusted curve as a base, one can make allowances for expected additional regulation or for changes in the pattern of regulation.

TIME UNITS

The choice of a time unit, such as the day, the week, or the month, is largely a matter of weighing the accuracy of the flow-duration curve against the work involved in its preparation. The primary use of such duration curves is to show the characteristics of flow. The details of the variations in flows are obscured if the time unit is long. For most streams, the monthly discharges are unsatisfactory for showing the variation in flow, and duration curves of annual mean discharges would have but little use because their range in variation is comparatively small and because only a few values are available for defining the curve.

A study in North Carolina (Foster, 1934, p. 1236) showed differences as great as 35 percent between a duration curve based on monthly mean discharges and one based on daily mean discharges. Weekly mean discharges have been used (Saville and Watson, 1933,

p. 407) for certain relatively stable streams. Weekly means, however, are not generally available in published records, and the advantage, if any, of using the weekly mean is offset by the additional computations required.

The effect of varying the time unit (fig. 2) is not the same for all streams. Where the flow from day to day is almost uniform, as in the St. Lawrence River, the daily and weekly duration curves would be nearly identical, and the monthly duration curve would not differ greatly from the daily curve. On the other hand, if the stream is "flashy," with sudden floods lasting only a few hours or days, the daily and weekly curves will differ appreciably, and the monthly curve will differ considerably from the daily curve. Daily discharges have been used almost exclusively in recent studies.

After a smooth curve is drawn, the fact is often overlooked that the mean discharge for the selected time unit was used as the discharge that was grouped into the class intervals. Thus, if the month were chosen as the time unit, the correct statement would be that "the monthly mean discharge was at least 150 cubic feet per second for 90 percent of the months". The daily mean flows during part of the 90 percent of the time probably were less than 150 cubic feet per

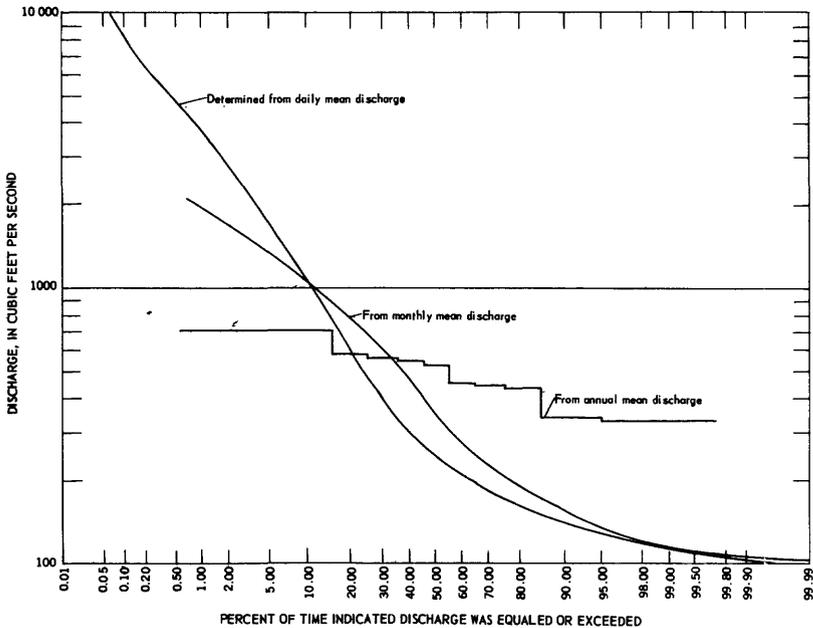


FIGURE 2.—Duration curves of daily, monthly, and annual flows, Bowle Creek near Hattiesburg, Miss., 1939-48.

second. This distinction is of minor importance when the day is chosen as the time unit, unless the stream has a large diurnal fluctuation.

CLASS INTERVALS

The class intervals should provide from 20 to 30 well-distributed points on the curve. The extreme points should be so selected as barely to include the extremes of daily discharge for the period of record. Table 1 shows recommended class intervals in cubic feet per second for ranges in discharge from 1 to 5 log cycles. Form 9-217c (fig. 4) gives an example of how table 1 is used for a stream whose range in discharge is almost within two log cycles. Class intervals recommended for 2 log cycles were chosen in preference to those recommended for 3 log cycles because the 2-cycle intervals give more points.

When flow-duration data are computed using different sets of class intervals, the data can be combined by plotting a curve of the cumulated days against the discharge for the entire period that was computed by one set of class intervals. The cumulated days for the other set of class intervals is picked from the curve. Semilogarithmic paper with a finely divided arithmetic scale is recommended for this purpose. (See fig. 3.) Discharges are plotted on the logarithmic

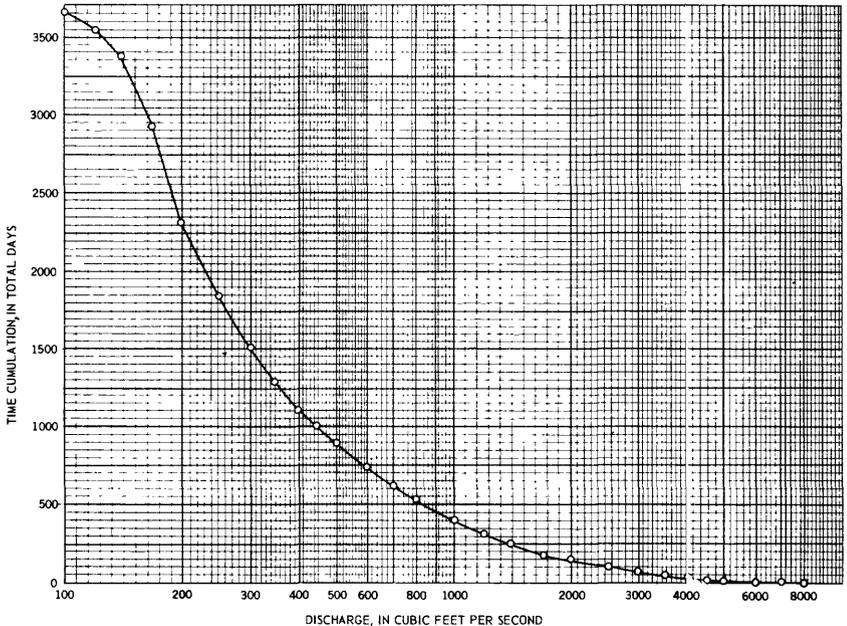


FIGURE 3.—Curve for changing class intervals on flow-duration data from Bowie Creek near Hattiesburg, Miss., 1939-48.

scale, and cumulated days are plotted on the arithmetic scale. The points are connected by straight lines. A smooth curve based on the points would be as likely to harm the results as to improve them. Data plotted in figure 3 are from figure 5.

TABLE 1.—Class limits for discharges on flow-duration table

Range in daily discharge				
1 log cycle	2 log cycles	3 log cycles	4 log cycles	5 log cycles
10	10	10	10	10
11	12	15	15	15
12	14	20	20	20
13	17	25	30	30
14	20	30	40	50
15	25	40	50	70
16	30	50	70	100
18	35	60	100	150
20	40	80	150	etc.
22	45	100	etc.	
24	50	150		
26	60	etc.		
28	70			
30	80			
33	100			
36	120			
40	etc.			
45				
50				
55				
60				
65				
70				
75				
80				
90				
100				

NOTE.—Table shows sequence of numbers for five ranges in discharge. Locate decimal point and starting discharge to suit conditions. In general, use cycle closest to observed range. Where considerable data have been tabulated at a station by using other rules for class intervals, additional data would normally be tabulated by using the class intervals previously used.

COMPILING FLOW-DURATION DATA

A digital computer or a similar machine can be used to compile the flow-duration data. The machine furnishes the same kinds of data as are shown in figure 5, including the data in columns headed "total," "total days," and "percent of time." If a machine is not available, the method shown in figures 4 and 5 is recommended for compiling the flow-duration data.

USE OF FORM 9-217C

Form 9-217c, shown in figure 4, is designed for arranging the daily flows during 1 water year, in classes according to magnitude. The lower limit of each class interval (from table 1) is tabulated in the discharge column.

For the daily discharge of each day of gaging-station record, a tally mark is made in the appropriate monthly column on the line

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representing the highest flow that the flow of the particular day equals or exceeds. The tally marks for each month are counted to ensure that one tally mark was made for each day of the month. The tally marks in each class are counted and the number is entered in

9-217c
July 1955

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File

Duration table of daily discharge, Bowie Creek near Hattiesburg, Miss.

for the year ending Sept. 30, 1943 Drainage area, 304 square miles

DISCHARGE	NUMBER OF DAYS WHEN DISCHARGE WAS EQUAL TO OR GREATER THAN THAT SHOWN IN FIRST TWO COLUMNS AND LESS THAN THAT SHOWN ON NEXT LINE												Year
	Oct.	Nov.	Dec.	Jan.	Feb.	Mar.	Apr.	MAY	June	July	Aug.	Sept.	
100													
120													5
140													4.0
170													8.5
200													4.9
250													3.0
300													1.7
350													2.1
400													1.6
450													1.6
500													1.2
600													1.0
700													.7
800													1.4
1,000													1.2
1,200													.5
1,400													.5
1,700													.5
2,000													.4
2,500													.4
3,000													
3,500													.1
4,000													.2
4,500													.2
5,000													.1
6,000													
7,000													
8,000													
10,000													.1
12,000													
14,000													.1
17,000													
	31	30	31	31	28	31	30	31	30	31	31	30	365

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FIGURE 4.—Duration of daily discharge, Bowie Creek near Hattiesburg, Miss., for year ending Sept. 30, 1943, form 9-217c.

the column for the year. The total of the yearly column should equal the number of days in the year.

An alternate method of compiling form 9-217c is to go through a month, counting the days in each class and showing the count by a numeral instead of several tally marks. A check mark is placed by each day when it is counted; this reduces the number of items to be scanned for successive class intervals.

USE OF FORM 9-217D

The yearly totals, by classes, are transferred from the yearly forms (fig. 4) to the summary form (fig. 5), by using a column for each year. Column headings, "total," "total days," and "percent of time," are added at the end of the yearly totals, and the period to which the totals apply is indicated. Class totals are cumulated from the bottom upward, and the percent of the total number of days is computed for each class summation and entered in the percent-of-time column. The columns "total days" and "percent of time" represent the time that the discharge shown in column 2 was equaled or exceeded. Column 1 is reserved for listing the equivalent of column 2 in other units, such as cubic feet per second per square mile, million gallons per day, or ratio to mean discharge.

When additional years of record become available, the total days in each class interval for those years can be added to the existing summary table to obtain a total for the entire period.

PRESENTATION OF DATA

The results of a flow-duration study may be presented in tabular or in graphical form. The tabular presentation has the advantage of being more compact than the graphical presentation, but it is somewhat less clear.

In either form of presentation, the title should show the time interval (such as "daily flow"), the name of the gaging station, and the period represented by the data.

TABULAR PRESENTATION

Tabular arrangements of flow-duration data may show either the discharge for a given percent of duration or the percent of time for a given discharge. An arrangement showing the discharge corresponding to given percents of duration is better suited to hydrologic comparisons than is an arrangement showing the percent of time for a given discharge.

Some compilations of flow-duration data show the yearly class totals as shown in figure 5; others show skeleton tables with only enough points given to define a duration curve.

GRAPHICAL PRESENTATION

The curve in figure 1 shows the duration of daily flow of Bowie Creek near Hattiesburg for the water years 1939-48. The abscissa should be labeled as shown in this figure, rather than just "percent

9-217d
July 1966

UNITED STATES DEPARTMENT OF THE INTERIOR
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File.....

Duration table summary of daily discharge, Bowie Creek near Hattiesburg, Miss.

for the years <u>1939-48</u>		Drainage area, <u>304</u> square miles										Total	Total	Percent	
DISCHARGE		NUMBER OF DAYS WHEN DISCHARGE WAS EQUAL TO OR GREATER THAN THAT SHOWN IN FIRST TWO COLUMNS AND LESS THAN THAT SHOWN ON NEXT LINE										39-48	days	of time	
Cfs		1939	1940	1941	1942	1943	1944	1945	1946	1947	1948				
100		61	17		17							95	3653	100	
120		68	64	10	23	5	3					173	3558	97.4	
140		50	65	61	57	40	56	60	24	29	12	454	3385	92.7	
170		27	47	75	48	85	53	46	70	81	99	631	2931	80.2	
200		46	50	42	57	49	41	38	50	29	52	454	2300	63.0	
250		18	16	53	41	30	26	47	27	34	45	337	1846	50.5	
300		10	9	32	14	17	16	31	27	31	23	210	1509	41.3	
350		9	14	18	16	21	26	24	20	16	17	181	1299	35.6	
400		4	5	13	10	16	16	10	21	13	13	121	1118	30.6	
450		11	6	9	13	16	15	15	13	5	10	113	997	27.3	
500		10	11	8	11	12	18	20	20	12	20	142	884	24.2	
600		10	7	9	10	10	15	19	11	20	15	126	742	20.3	
700		4	3	7	4	7	16	14	14	14	6	89	616	16.9	
800		12	15	6	12	14	18	10	19	13	12	131	527	14.4	
1,000		7	3	5	3	12	12	10	13	11	7	83	396	10.8	
1,200		4	3	3	5	5	3	5	13	9	5	55	313	8.57	
1,400		6	12	2	7	5	13	4	11	9	9	78	258	7.06	
1,700		3	4	3	4	5	1	3	2	10	4	39	180	4.93	
2,000		2	5	1	3	4	5	5	3	7	5	40	141	3.86	
2,500		1	2	6	2	4	5	3	1	7	3	34	101	2.76	
3,000		2	4		4		3		3	4	1	21	67	1.83	
3,500			2		2	1	3	1	2	3	2	16	46	1.26	
4,000			2			2	2		1	4	2	13	30	.821	
4,500					1	2				2	1	6	17	.465	
5,000				1		1					1	3	11	.301	
6,000				1							2	3	8	.219	
7,000					1							1	5	.137	
8,000										2		2	4	.109	
10,000						1						1	2	.055	
12,000															
14,000						1						1	1	.027	
17,000															
		365	366	365	365	365	366	365	365	365	366	365			

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FIGURE 5.—Summary of duration of daily discharge, Bowie Creek near Hattiesburg, Miss., 1939-48, form 9-217d.

of time." When the curve represents basic data for the period of record, as in this figure, plotted points are shown and a smooth curve is drawn by eye to fit the data. When the duration data have been adjusted to represent a longer period, a smooth curve alone is sufficient. If the curve is merely one step in a hydrologic analysis, straight lines between successive points are preferable because they prevent introduction of differences due to personal judgment.

TYPE OF PAPER

Flow-duration curves are plotted on rectangular-coordinate paper, logarithmic paper, arithmetic-probability paper, or logarithmic-probability paper. For general use the logarithmic-probability paper is recommended.

The advantage of using a logarithmic scale for the discharge (ordinate) is apparent when it is noted that normally 3 or 4 log cycles are required for the range in discharge. An arithmetic scale that would accommodate the range in discharge of most streams would be undesirably small for all except the highest discharges.

An arithmetic scale for the percent of time is considered easier to use, but such a scale provides poor definition at the extremities, where the slope of the flow-duration curve changes rapidly. Because of the difficulty of determining the area under a curve plotted on a logarithmic-probability paper, the rectangular coordinates are often used in hydroelectric-power studies and similar studies.

A logarithmic scale for the percent of time expands one end of the curve but undesirably condenses the other end.

The probability scale expands both ends of the flow-duration curve. Data that are normally distributed plot as a straight line on probability paper. As the logarithms of discharge are more normally distributed than the discharge itself, the logarithmic-probability paper tends to straighten out the flow-duration curve.

DISCHARGE UNITS

For tabulating flow-duration data, to express discharge in cubic feet per second is most convenient because the daily discharges are published in those units. But the discharge data can be converted to any other desired unit for plotting the flow-duration curve. For example, if the duration curve is to be used for a study of flow at the gaging-station site, the ordinate can be in cubic feet per second, in million gallons per day, or in some function of discharge—such as kilowatts corresponding to the net head and plant efficiency—available at the site. If the duration curve is to be used for comparing flow characteristics among streams, to express discharge in cubic

feet per second per square mile or in ratio to average flow is suitable for the ordinate scale.

To express discharge either in cubic feet per second per square mile or in ratio to mean flow eliminates the effect of size of drainage area; but to express discharge in ratio to mean flow eliminates also the effect of differences in mean annual runoff per square mile. For many streams, comparisons based on cubic feet per second per square mile are almost identical with comparisons based on ratio to mean flow. However, among stream basins in which precipitation differs greatly, flow-duration curves based on ratio to mean flow are much closer together than those based on cubic feet per second per square mile. For example, in figure 6, flow-duration curves for three nearby stations in northeastern Georgia are shown for the water year 1952. Figure 6*A* shows the flow-duration curves in cubic feet per second per square mile, and figure 6*B* shows the same flow-duration curves in ratio to mean flow. No attempt was made to determine the average precipitation in each drainage basin, but the precipitation total for the water year 1952 is given for one precipitation station in each drainage basin.

Discharge per square mile and ratio to mean annual flow are useful conversions for hydrologic comparisons, but care should be taken not to imply that the stream with the highest yield per square mile is the best source of supply regardless of the size of its drainage area, or that the flow varies uniformly over the drainage basin.

LONG-TERM FLOW-DURATION CURVES FROM SHORT-TERM RECORDS

Very seldom do all the gaging-station records in a given area cover concurrent periods. If records are to be compared with each other, they must represent, or be adjusted to, concurrent periods, in order that differences between the records will be due to differences in climatic or drainage-basin characteristics and not to the fact that the records cover different periods of time. Furthermore, flow-duration curves based on short records are unreliable for predicting the future pattern of flow, but they can be made reliable by adjusting them to represent longer periods.

Several methods (Mitchell, 1950, p. 12-18) are available for adjusting short-term records to long-term records. In the method now used by the Geological Survey (sometimes called the index-station method), a relation is established between two stations for the short period of concurrent record by plotting a graph of the discharges for given duration points at one station against the corresponding discharges at the other station. The graph for the short period is also

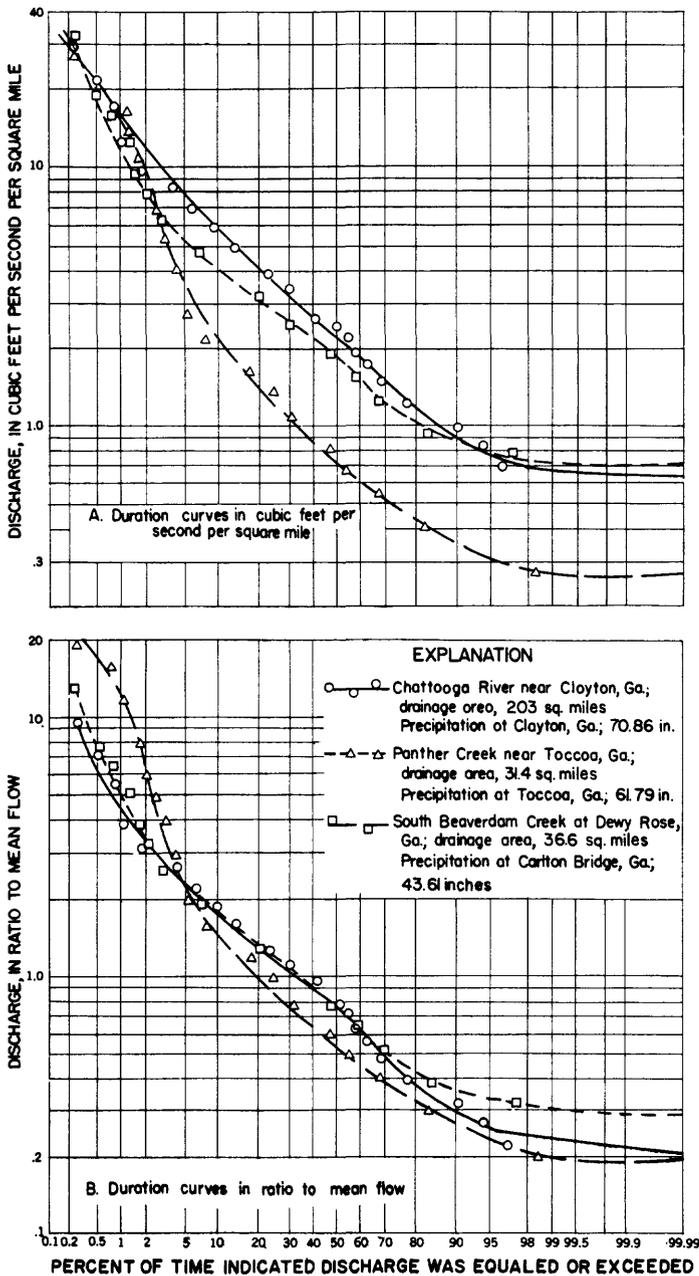


FIGURE 6.—Comparison of flow-duration curves for three nearby stations in northeastern Georgia, water year 1952.

assumed to represent the relation between the stations for a long period. If the assumption is true, the flow available 50 percent of the time at the long-term station can be used to enter the curve of relation (based on the short period of record), in order to obtain the adjusted (to long term) flow available 50 percent of the time at the short-term station. Adjusted flows for other percents of time at the short-term station can be obtained in the same manner.

SELECTION OF THE INDEX STATION

In order for the index-station method to be valid, both the index station and the short-term stations must be influenced by similar climatic occurrences. Although the drainage basins of these stations need not have concurrent rains, each basin should have the same likelihood of receiving rain. Thus, a station in the rain shadow of a mountain could hardly be used to adjust the records of a stream on the opposite side of the mountain.

The index station used to adjust the record for a short-term station should be carefully selected. A gaging station whose record has previously been used in a regional low-flow analysis usually serves as a good index station. A station on the same stream as the short-term station is usually a better index station than one on a stream in an adjacent basin. The index station and the short-term station must have a sufficient period of concurrent records to establish a usable relation. Distance from other stations is a factor in selecting the index station. Records from gaging stations nearby, other factors being equal, provide better relations than records from remote stations, but usable relations have been established between stations as far apart as 50 miles, when long periods of concurrent record were available on which to establish the relation.

ESTABLISHING THE RELATION

A flow-duration curve is prepared for the short-term record (fig. 8), and a flow-duration curve for the corresponding period is prepared for the long-term record. The points are connected by straight lines rather than by a smooth curve, in order not to introduce personal interpretation of the data.

The discharges for about 15 percent-duration points, ranging from 0.5 to 99.5 percent (table 2), at the short-term station are plotted on logarithmic paper against the discharges for the same percent-duration points at the long-term station. A percent-duration point is the point on the flow-duration curve that corresponds to a specified percent of time.

A straight line or lines (connected by a transition curve at sharp breaks) are drawn through the plotted points, with the following suggestions serving as guides:

1. Straight lines or a smooth curve should be drawn in preference to a wavering line connecting all points.
2. On logarithmic paper, the upper end of the curve of relation is often a 45-degree line and is usually on the drainage-area ratio (equal-yield) line or parallel to it. If the two streams differ in their high-flow characteristics, the upper end of the curve of relation will depart from a 45-degree line.
3. If the geologic characteristics of the basins differ, the lower points will define a relation other than a 45-degree line.

TABLE 2.—Discharge of equal percent duration on two rivers in Illinois

Discharge, in cubic feet per second				
Percent duration	Kankakee River at Mokence 1946-50	Iroquois River near Chebanse 1946-50	Kankakee River at Mokence 1924-50	Iroquois River near Chebanse, adjusted to 1924-50
99.5	542	46	432	23
99	558	49	453	26.5
98	566	53	508	37.5
95	618	67	578	54
90	700	102	658	80
80	882	188	822	150
70	1,080	334	970	240
60	1,280	525	1,130	380
50	1,580	750	1,370	580
40	1,930	1,150	1,680	880
30	2,500	1,990	2,100	1,320
20	3,440	3,220	2,770	2,130
10	4,640	5,300	3,940	4,000
5	5,200	7,160	4,800	5,780
2	6,380	9,700	5,780	7,800
1	7,180	12,300	6,600	10,300
0.5	8,000	14,600	7,210	12,100

4. Little weight should be given to the points at the extreme upper or lower end when the line is drawn. Comparison of curves of relation based on successive 5-year periods shows that an apparent sharp break in the relation near the extremes is likely to be balanced by a break in the opposite direction during the next 5-year period.

To demonstrate the method, records from two stream-gaging stations in northeastern Illinois are used. The Iroquois River near Chebanse (record for water years 1924-50) is used as the short-term station with the assumption that its record covers only the water years 1946-50. The record for the index station Kankakee River at Mokence (record for water years 1916-50) is assumed to cover only the period 1924-50, so that the extension of the short-term station record may be compared with the actual record.

The flow-duration curve for 1946-50 at Kankakee River at Momence is not shown, but table 2 gives the discharge for equal percent duration picked from the curve.

The curve of relation in figure 7 is plotted from the data in the second and third columns of table 2.

ADJUSTING THE SHORT-TERM RECORD

The discharges for various percent-duration points at the long-term station (col. 4, table 2) are used as the argument in the curve of rela-

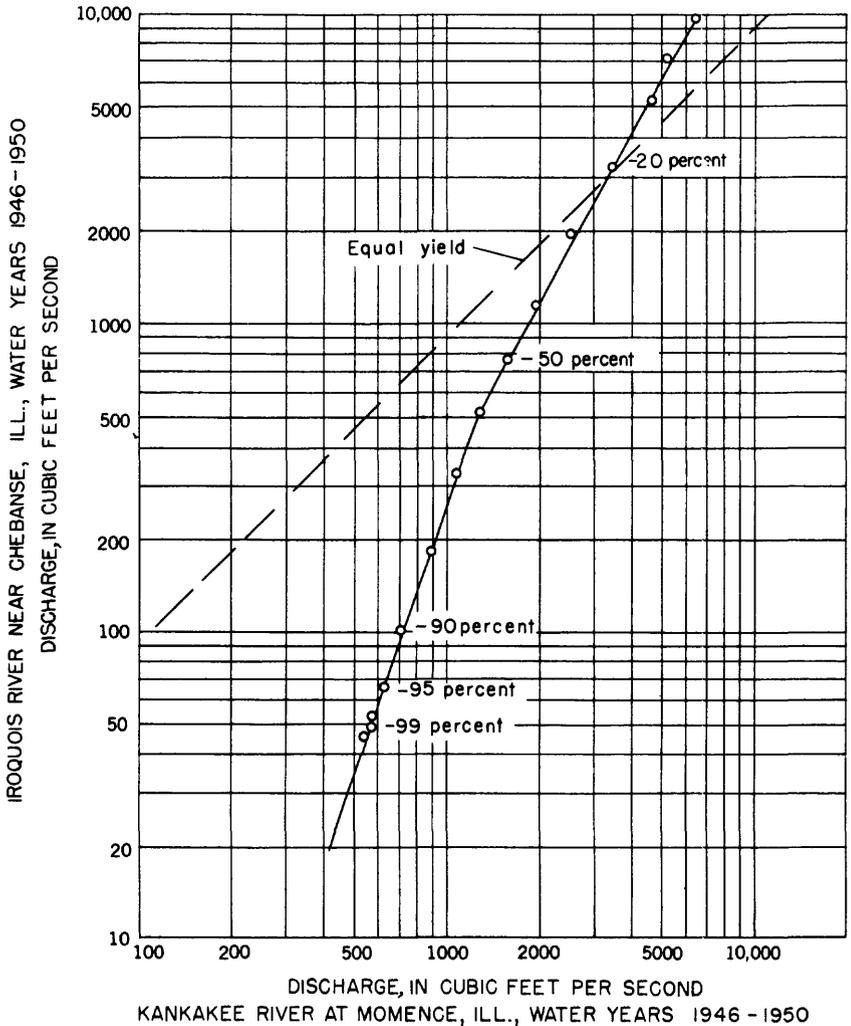


FIGURE 7.—Correlation between Kankakee River and Iroquois River, based on discharge of equal percent duration.

tion (fig. 7) to obtain the adjusted discharge at the short-term station for the particular percent-duration point. For example, the discharge of the Kankakee River (long period, 1924-50) at the 50-percent-duration point is 1,370 cfs. Entering 1,370 cfs, on figure 7, we find that the discharge (adjusted to the long period, 1924-50) of Iroquois River at the 50-percent duration point is 580 cfs. The discharge for other percent-duration points is obtained in the same way, and the adjusted values are plotted to define the adjusted curve (fig. 8).

Figure 8 shows the actual flow-duration curve for the short period (1946-50) and the flow-duration curve adjusted to the long period (1924-50). For comparison, the curve for the long period (1924-50) based on actual record is shown also. The flow-duration curve adjusted to the long period compares favorably with the actual long-period record.

ESTIMATION OF THE FLOW-DURATION CURVE

Frequently there is need for flow-duration data on streams for which there are no gaging-station records. When the low-flow end of the duration curve is of prime interest, estimates based on runoff per square mile of nearby gaged areas are seldom reliable unless it is known that the ground-water geology of the two areas is the same.

The effect of basin geology on streamflow can be evaluated by several discharge measurements made during periods of base flow. The discharge measurements at the base-flow observation point should preferably be made over a period of several years, but, regardless of when they are made, estimates of low flow based on base-flow measurements are much more reliable than those based on the runoff per square mile of nearby gaged areas.

The use of base-flow measurements for estimating a flow-duration curve is explained by an example for which the Kankakee River and Iroquois River stations are used. In this example we assume that the Iroquois River near Chebanse is ungaged, but that 10 base-flow measurements have been made. The Kankakee River at Momence is used as the index station.

Concurrent daily discharges for two days each year during the period 1946-50 are used as discharge measurements. (See table 3.) The selected days are days of base-flow periods when little change in discharge occurred at either station. The same base-flow criteria would be followed when discharge measurements are made on ungaged areas, except that the rate of change in discharge could be observed only at the gaging station. Local inquiry will usually reveal the time of the last rain on the ungaged area.

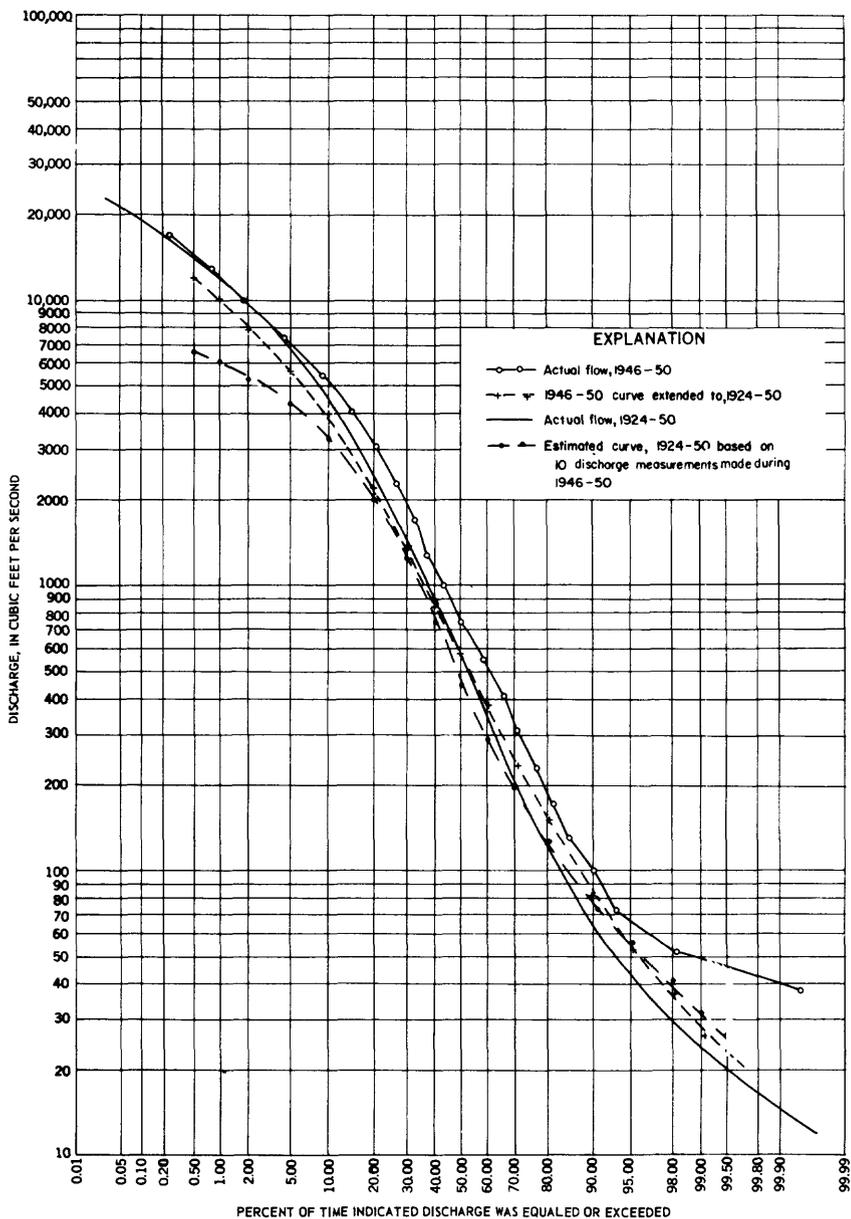


FIGURE 8.—Duration curves of daily flow, Iroquois River near Chebanse, Ill.

TABLE 3.—Days of concurrent discharge, Kankakee River and Iroquois River Stations, Ill., 1946-50

Date	Discharge, in cubic feet per second	
	Kankakee River at Momence, Ill.	Iroquois River at Chebanse, Ill.
Aug. 31, 1946	600	56
Sept. 20, 1946	525	48
July 16, 1947	1,280	306
Aug. 24, 1947	780	93
Aug. 26, 1948	682	107
Sept. 28, 1948	562	61
Sept. 1, 1949	712	107
Sept. 25, 1949	630	63
Jan. 1, 1950	4,460	4,880
Sept. 1, 1950	1,040	168

The base-flow measurements (days of concurrent discharge) are plotted on figure 9 to establish a relation between the ungaged site (Iroquois River near Chebanse) and the index station (Kankakee River at Momence). It is obvious that the measurements group near the lower end of the curve of relation and that lines of various slopes could be drawn to average the group of measurements. Thus, the measurements serve to fix the location of a line of relation but not its slope.

The characteristics of relations between gaging-station records furnish a basis for drawing the curve of relation when only the position of the curve at its lower end is known. An equal-yield line (drainage-area ratio), drawn as a 45-degree line on logarithmic paper through the plot of the drainage areas, serves as a convenient guide for this purpose. Although the curve of relation diverges from the equal-yield line at low flow, for many streams it tends to become parallel to the equal-yield line at higher flows, because, at high flow, storm runoff predominates and the base flow, affected by geology, is a negligible part of the total flow. However, when one basin contains enough storage, either on the surface or in the ground, to distribute the effect of storm precipitation over several time units, and the other basin contains comparatively little storage, the upper end of the line of relation deviates from the equal-yield line toward the station with less storage. (See fig. 7.)

For many streams in the eastern part of the country, a line through the base-flow measurements intersects the equal-yield line at a discharge about $1\frac{1}{2}$ times that of the mean discharge. The actual point of intersection is fairly stable for a given area and should preferably be located by correlating several gaging-station records. The point of intersection of the equal-yield line and low-flow line is used as a pivot point to draw a line through the average of the low-flow meas-

urements. In figure 9, a discharge $1\frac{1}{2}$ times the average discharge for the 1924-50 period at Momence was used as the pivot point. The relation based on low-flow measurements can be used to estimate a flow-duration curve in the same way that figure 7 was used to extend a flow-duration curve.

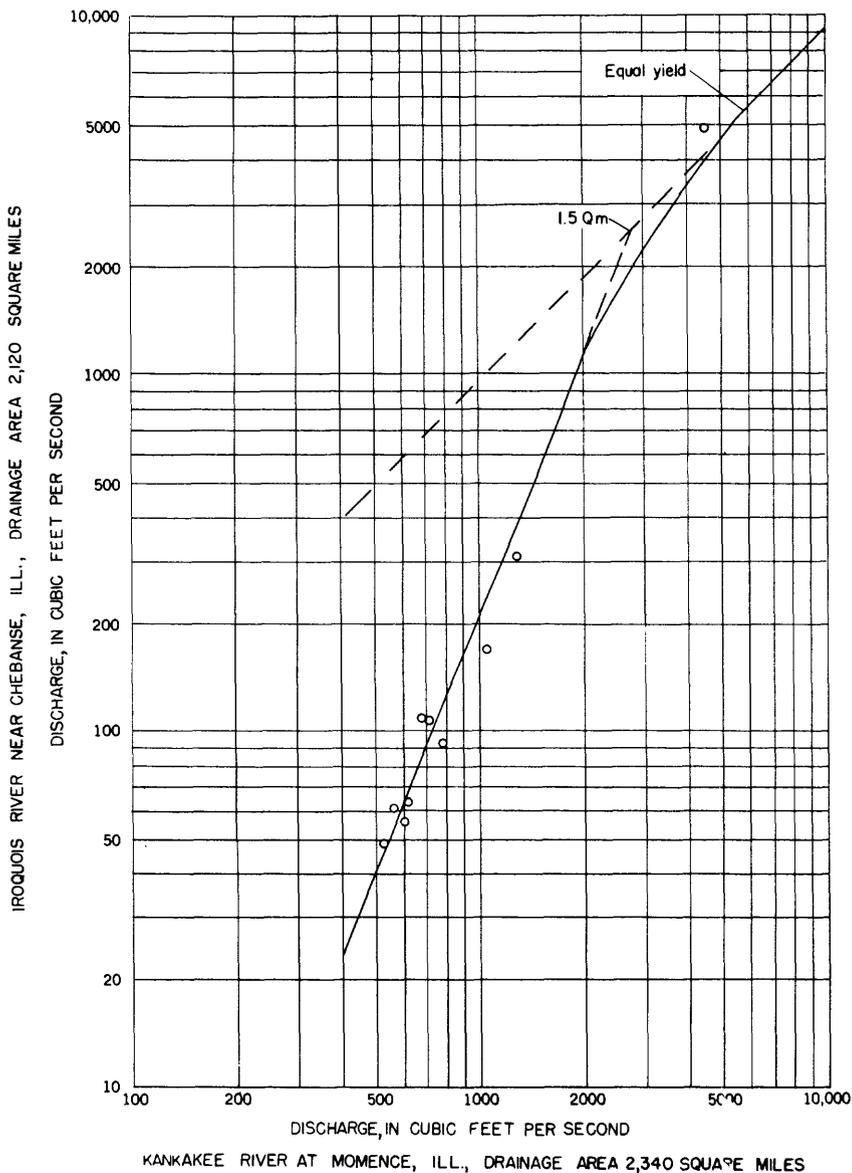


FIGURE 9.—Correlation between Kankakee River and Iroquois River, based on 10 discharge measurements, 1946-50.

In the example, index-station discharges for the 17 percent-duration points in column 4 of table 2 are used as the argument in figure 9 to obtain discharges for the corresponding percent-duration points at the ungaged site. The data thus obtained are plotted on figure 8 so that the estimated flow-duration curve might be compared with the duration curve based on actual record. Although in the example the duration curve is estimated throughout its range, reports published by the Geological Survey usually show only the lower half of the curve, because the relation at higher flows may not follow the equal-yield line. It will be seen in figure 7 that the upper line of relation between the stations used in the example actually crosses the equal-yield line. The result of assuming an equal-yield relation is seen on figure 8 by the departure of the estimated curve below 10 percent of the time.

The line of relation should not be extended to flows much lower than those measured at the ungaged site unless one has a thorough knowledge of the geology of the two drainage basins. Some lines of relation have a second break at an extremely low flow, particularly when one stream goes dry and the other is perennial.

HYDROLOGIC SIGNIFICANCE OF THE FLOW-DURATION CURVE

The water measured at a gaging station is the surface outflow of the drainage basin above a specified point on the stream. Thus, the streamflow record integrates the effects of climate, topography, and geology, and gives a distribution of runoff both in time and in magnitude. When the flows are arranged according to frequency of occurrence and a flow-duration curve is plotted, the resulting curve shows the integrated effect of the various factors that affect runoff.

It is important to keep in mind that the flow-duration curve is an average curve for the period upon which it is based. To say that a flow-duration curve based on a 15-year record represents the distribution of the yearly flow is incorrect. The flow lower than that which was equaled or exceeded 96.7 percent of the time might have occurred during one 6-month period of a 15-year drought. Such a flow would not be expected, on the average, 3.3 percent of the time each year, but would be expected, on the average, 50 percent of the time during one year of each 15-year period. The flow-duration curve for the period is often supplemented by flow-duration curves for the year of lowest runoff and the year of maximum runoff.

SHAPE OF CURVE

As the shape of the flow-duration curve is determined by the hydrologic and geologic characteristics of the drainage area, the curve may be used to study the characteristics of a drainage basin or to compare the characteristics of one basin with those of another. A curve with a steep slope throughout denotes a highly variable stream whose flow is largely from direct runoff, whereas a curve with a flat slope reveals the presence of surface- or ground-water storage, which tends to equalize the flow. The slope of the lower end of the duration curve shows the characteristics of the perennial storage in the drainage basin; a flat slope at the lower end indicates a large amount of storage; and a steep slope indicates a negligible amount. Streams whose high flows come largely from snowmelt tend to have a flat slope at the upper end. The same is true for streams with large flood-plain storage or those that drain swamp areas.

The statistics of the duration curve are discussed in papers by Foster (1924, 1934), Slade (1936), Beard (1943), and others. The work of Elderton (1953) also contains valuable information on the statistical and mathematical basis of the duration curve. Such a discussion is beyond the scope of this chapter.

MEAN

The area under the flow-duration curve is a measure of the discharge available 100 percent of the time. Dividing the area by 100 (base of the curve—100 percent of the time) gives the average ordinate which, multiplied by the scale factor (see section on water-power studies), is the mean discharge. Similarly, the area under a portion of the curve, divided by the percent of time of that portion, represents the mean flow during the particular percent of time. This property of the curve has important applications in some studies, but finding the scale factor of a flow-duration curve plotted on logarithmic-probability paper is somewhat complicated.

MEDIAN

The median flow is the curve value at 50 percent of the time.

MODE

The point of inflection of a flow-duration curve plotted on rectangular-coordinate paper occurs at the modal flow. This inflection point can be detected on figure 10, where the frequency curve of a hypothetical stream has been plotted with its flow-duration curve. However, the inflection point of a flow-duration curve is usually not

definite enough for determining accurately the modal flow from the flow-duration curve and, when logarithmic and probability scales are used for plotting, the mode does not fall at the apparent inflection point.

The modal value has been suggested (Meyer, 1928, p. 119) as an appropriate "normal" flow, as it is the flow that occurs most often.

USES OF THE FLOW-DURATION CURVE

As early as 1908, Mead (1908, p. 184-189) presented flow-duration curves in cubic feet per second per square mile for six Michigan rivers to show their similarity, and, at the same time, to point out the error that might result from estimating the flow of an ungaged stream. Mead states, "This form of diagram represents the best basis for the comparative study of streamflow for power purposes where storage is not considered, and where the continuous power of the passing stream is to be investigated."

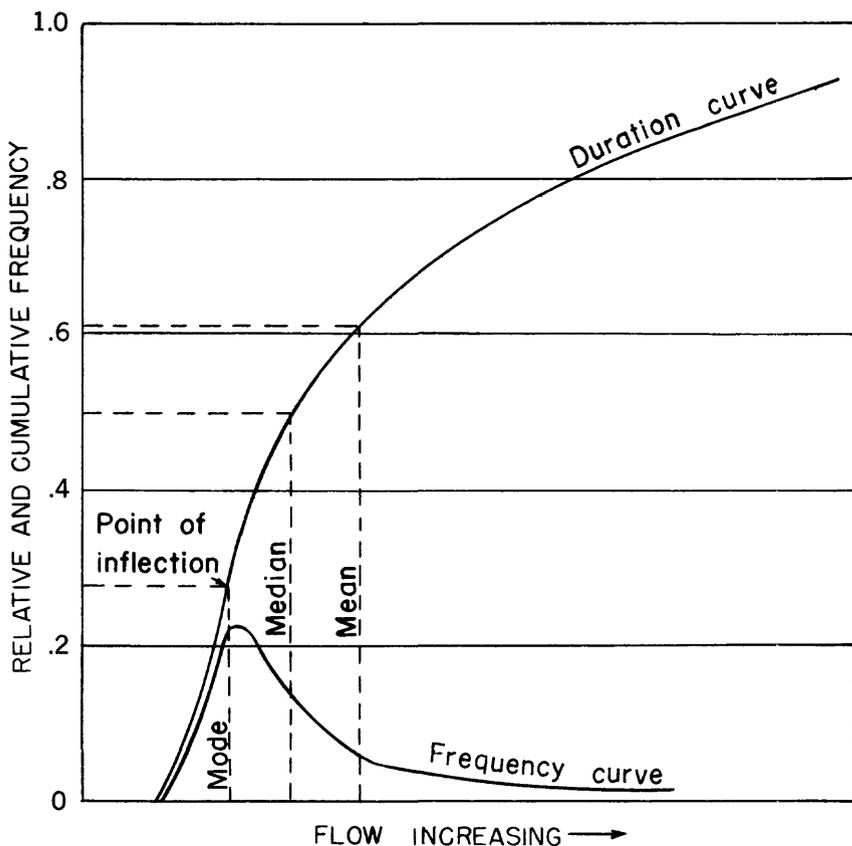


FIGURE 10.—Relation of duration and frequency curve.

It was not until about 1915, however, that flow-duration curves came into general use in the United States, and about 1920 the Geological Survey adopted the flow-duration curve as a basis for defining rates of flow to be used in computing waterpower statistics.

In 1930 the International Advisory Committee on Rating of Rivers adopted certain percent-duration points for quoting power statistics. W. G. Hoyt (1934, p. 1240-1243) stated that "It is doubtful whether agreement could have been reached on the basis of any defined rates of flow other than those obtained through the use of the duration curve."

One of the earliest uses of the flow-duration curve was for waterpower studies. The subject is discussed by many writers, among whom are Barrows (1943, p. 137-192), Hickox and Wessenauer (1933), and Foster (1934).

Bead (1943) and Pettis (1934, p. 1237-1240) have applied the upper end of the flow-duration curve to flood studies.

More recently the flow-duration curve has been used for preliminary investigations of water supply, location of industrial plants, pollution studies, and many other purposes. Simple examples of a few uses of the flow-duration curve are given in the following sections.

STUDYING THE EFFECT OF GEOLOGY ON LOW FLOWS

The flow-duration curve is a valuable medium for studying and comparing drainage basin characteristics, particularly the effect of basin geology on low flows. Except in basins with a highly permeable surface, the distribution of high flows is governed largely by the climate, the physiography, and the plant cover of the basin. The distribution of low flows is controlled chiefly by the geology of the basin. Thus, the lower end of the flow-duration curve is a valuable means for studying the effect of geology on the ground-water runoff to the stream. Where the stream drains a single formation, the position of the low-flow end of the curve is an index of the contribution to streamflow by the formation. The effect of geology on low flow in Ohio has been discussed by Cross (1949), Cross and Bernhagen (1949, p. 5), and Schneider (1957).

Six streamflow records for southern Mississippi are used to illustrate the effect of geology on low flow. The area selected has a fairly uniform climate and little difference in elevation. The map showing outcrops of the principal formations (fig. 11) is adapted from plate 2, Water-Supply Paper 576 (Stephenson and others, 1928). Details, such as variations within the principal formation outcrop and outcrops within the immediate vicinity of the streams, have been omitted.

Descriptions of the formations (from pl. 2, WSP 576) are as follows:

Citronelle formation...Sand, gravel, and clay.

Catahoula sandstone...Irregularly bedded sand, sandstone, and clay.

Vicksburg group.....Limestone, marl, clay, and sand.

Jackson group.....Basal portion. Moodys Branch formation shells embedded in quartz sand and glauconite; upper portion Yazoo clay—clay, more or less calcareous, with some sand and marl.

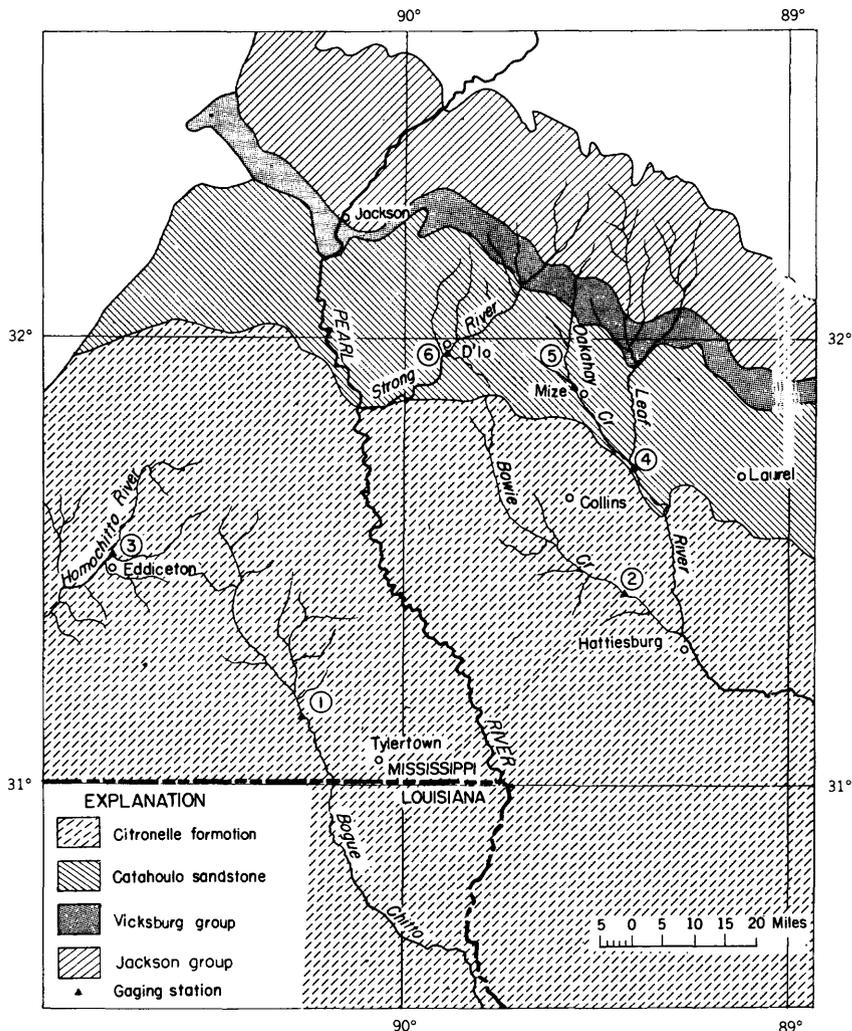


FIGURE 11.—Geologic map of area in southern Mississippi having approximately uniform climate and altitude.

Figure 12 shows flow-duration curves for six southern Mississippi streams plotted from data in "Surface Waters of Mississippi" (Anderson, 1950). Curves 1, 2, and 3 represent streams draining the Citronelle formation outcrop; curves 4, 5, and 6 represent streams that contain outcrops from the Catahoula sandstone, the Vicksburg group, and the Jackson group.

It is apparent from figures 11 and 12 that streams draining the same geologic formations have more nearly the same low-flow duration in cubic feet per second per square mile than nearby streams draining different geologic formations. For example, the flow-duration curve for Bowie Creek (curve 2 on figures 11 and 12) more nearly resembles the curve for Bogue Chitto (curve 1) than that of the nearby Leaf River near Collins (curve 4).

Where the yield per square mile to streamflow from adjacent geologic formations differs greatly, the index stations, to be used with discharge measurements at base-flow observation points, should measure single geologic formations whenever possible. In some drainage basins containing several formations, it may be possible to estimate the average yield per square mile of the whole basin by adding the proportional contribution of each geologic formation.

This discussion has been oversimplified to illustrate the principles involved. Even if the geologic formation is the same throughout a basin, other factors, such as variations in permeability of the formation, the character of the underlying formation, and the depth of incision of the stream, affect the low-flow characteristics at a particular point on a stream. For example, although the streams represented by curves 1, 2, and 3 (fig. 12) all drain from the Citronelle formation, curve 3 differs greatly from curves 1 and 2.

This discussion of the effect of geology on streamflow provides a warning against estimating low flow from ungaged areas without carefully studying the area and making base-flow measurements at several different points. In such a study, knowledge of the geology of a basin can seldom be used to make quantitative estimates of low-flow potential of streams, but it will help to explain the differences.

WATERPOWER STUDIES

The flow-duration curve is used for preliminary studies of plant capacity, economic feasibility of projects, and pondage (Barrows, 1943; p. 159-191 and Foster, 1934; p. 1230-1234). Its use in a multiple-plant development is discussed by Hickox and Wessenauer (1933).

As a simple example, assume that a "run of the river" hydroelectric plant is at a site with a net head of 100 feet and that the

flow-duration curve is the one shown in figure 13. The tentative turbine capacity is 6,000 cfs. The preliminary study requires an estimate of the average yearly output in million kilowatt-hours at the wheel shaft for primary and for secondary power, assuming 80-percent turbine efficiency, a load factor of 100 percent, and no loss or waste of power.

The area below the duration curve and the turbine capacity line represents the flow available for producing power. Flow in excess of 6,000 cfs cannot be used by the turbine. The scale factor (value of each small square) can be determined by computing the number of squares (500) that represents 1,000 cfs, 100 percent of the time. In figure 12 the scale value of each square is 1,000 (cfs) divided by 500 (squares), or 2 cfs for each square.

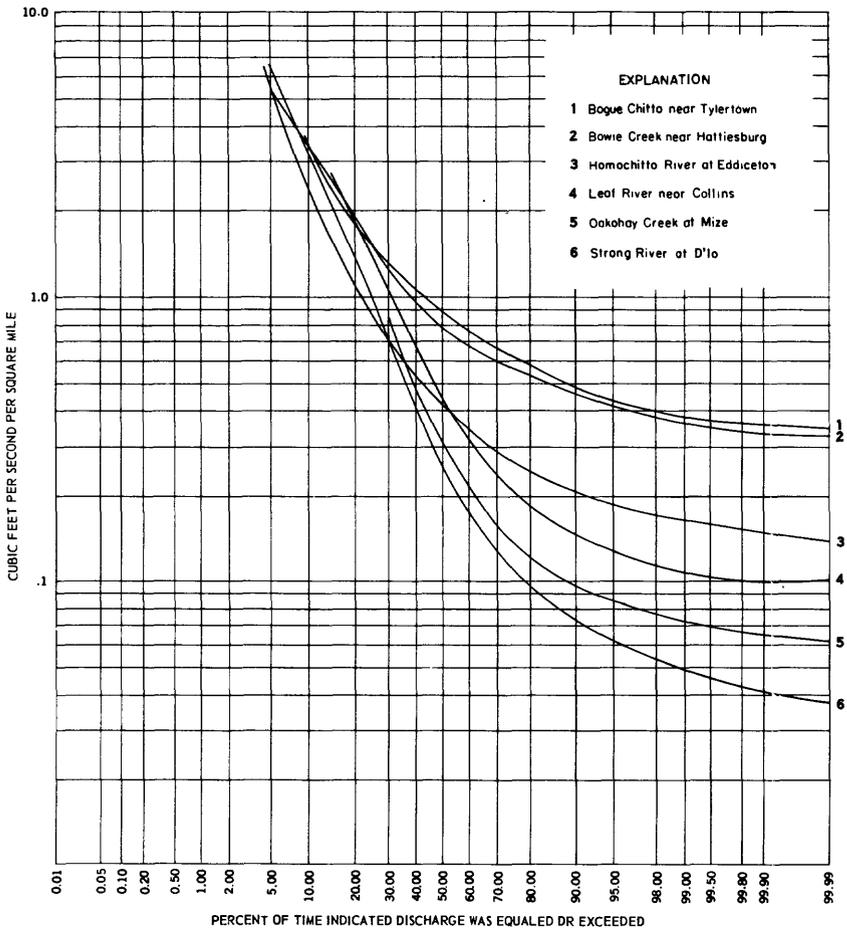


FIGURE 12.—Flow-duration curves for selected Mississippi streams, 1939-48.

The average yearly output at the wheel shaft for 1 cfs, with 80-percent efficiency and with a 100-ft head, is computed as follows:

$$\frac{62.4 \times 100 \times .80 \times 6535}{550} = 59,338 \text{ (kilowatt-hour)}$$

The upper limit of primary power (power available continuously) is the horizontal line through the minimum flow (800 cfs in this example). Thus, the primary power is 800 (cfs) \times 59,338 = 47.5 million

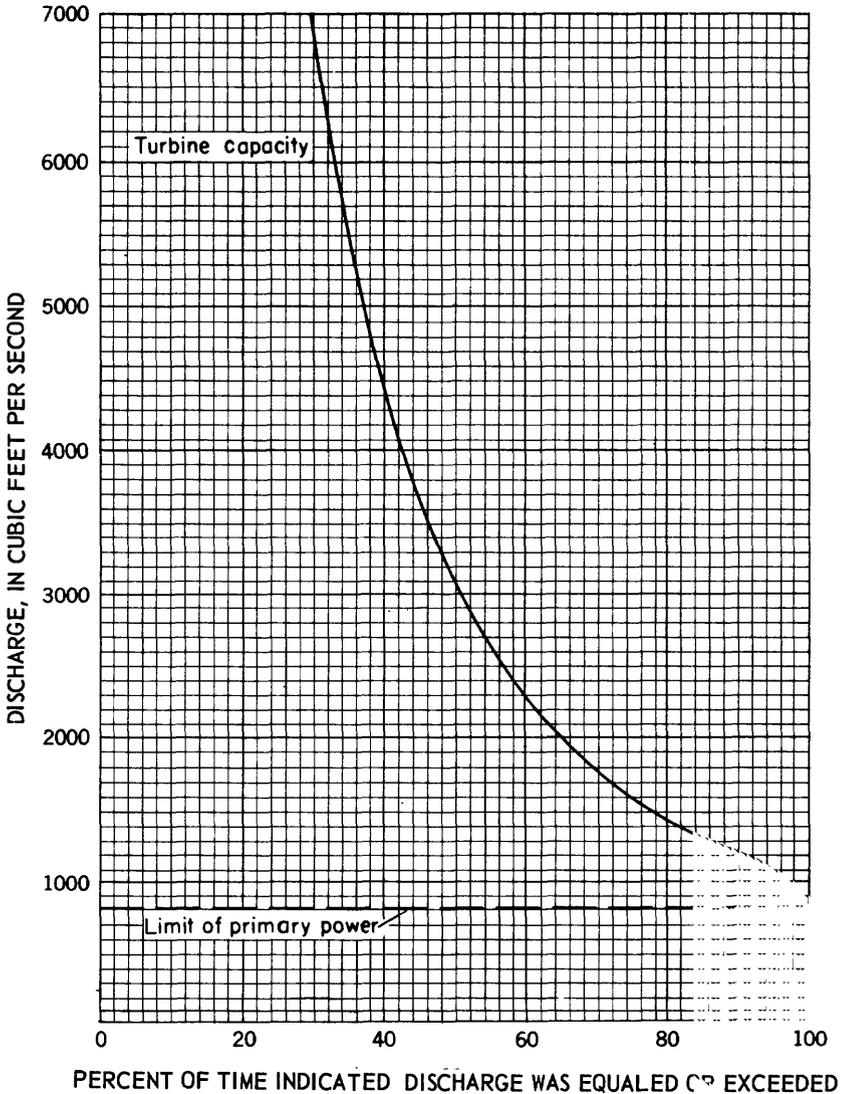


FIGURE 13.—Flow-duration curve applied to hydropower study.

kilowatt-hours yearly. The discharge available to produce secondary power is represented by the area bound by the upper limit of primary power, the turbine-capacity line, and the flow-duration curve. This area is determined by planimetry, by counting squares, or by scaling. In the example, the area is 1,380 squares and the flow is 2,760 cfs ($2 \times 1,380$). The secondary power is thus

$$59,338 \times 2,760 = 163.8 \text{ million kilowatt-hours yearly}$$

STREAM-POLLUTION STUDIES

To illustrate the use of the flow-duration curve in a preliminary analysis of the degree of treatment required, the following data are assumed:

1. No contamination above point under investigation.
2. Allowable BOD (biochemical oxygen demand) for stream below the disposal plant is 4 ppm.
3. The allowable BOD (4 ppm) may be exceeded not more than 1 percent of the time, on the average.
4. Flow equals or exceeds 10 cfs 99 percent of the time.
5. Sewage flow is 1,000,000 gallons per day (1.55 cfs).
6. BOD of untreated sewage is 200 ppm.

Compute the degree of treatment required:

The allowable BOD below disposal plant outlet = $4 \text{ ppm} \times (10 \text{ cfs} + 1.55 \text{ cfs})$.

The BOD of the sewage = $200 \text{ ppm} \times 1.55 \text{ cfs}$.

The degree (D) of BOD not removed by treatment ($D \times 200 \times 1.55$) must not exceed the allowable (4×11.55) or

$$D = \frac{4 \times 11.55}{200 \times 1.55} = 0.15 \text{ or } 15 \text{ percent. Thus, } 85 \text{ percent of the}$$

BOD must be removed by the sewage disposal plant.

QUALITY-OF-WATER STUDIES

The quality of surface streams is often shown by duration curves of sediment, turbidity, hardness, or some other quality-of-water characteristic. These duration curves are obtained in a manner similar to that described for flow-duration curves.

If the quality-of-water data are insufficient for direct computation of some descriptive statistics, such as frequency distribution, annual loads, annual average concentrations, and standard deviations, flow-duration curves can be used sometimes to make approximations. The suitability of this technique is dependent on the correlation of the quality characteristics against stream discharge. The error of the approximation includes both the error of the flow-duration curve and the error of estimate for the correlation.

For each sample, the quality-of-water characteristic to be shown is plotted against the stream discharge at the time of collection. A rating curve of quality-of-water characteristic versus discharge is drawn to average the plotted points. The duration curve of stream-flow is converted to a curve showing frequency of a specified quality characteristic by looking up the discharge at several percent-duration points and obtaining the corresponding value of the quality-of-water characteristic from the rating curve. These values are plotted against the appropriate percent of time to obtain points for drawing the quality-of-water frequency curve. The quality-frequency curve developed thus is divided into convenient segments or groups, and the desired statistical description is computed in the customary manner.

VARIABILITY INDEXES

An important characteristic of the flow of a stream is its variability. Variability of streamflow is the result of variability in precipitation as modified by basin characteristics. Storage, either on the surface or in the ground, serves to reduce the variability of flow. As an illustration of the range in variability of streams, the May 1955 flow of a station in Michigan was among the lowest 25 percent of record although the flow was 93 percent of the median, whereas at a station in California the flow was not among the lowest 25 percent of record although it was only 10 percent of the median.

The slope of the flow-duration curve is a quantitative measure of the variability. Several indexes of this slope have been used. In 1920 the Geological Survey adopted the flow available 50 percent of the time (q_{50}) and the flow available 90 percent of the time (q_{90}) as standards of flow for waterpower statistics. The q_{90} is a measure of the prime power and the q_{50} is an index of the power potential with storage. Together, the two indicate the variability of flow.

LANE'S VARIABILITY INDEX

Lane and Lei (1950) introduced an index of variability, which was defined as the standard deviation of the logarithms of the stream discharge. On log-probability paper this index represents the fall (in terms of log cycles) of the duration curve in one standard deviation. The index can be estimated by scaling the value from a plot on logarithmic paper, or it can be computed as follows:

1. From the duration curve, pick values of discharge at 10-percent intervals from 5 percent to 95 percent of the time.
2. Look up the logarithms of these discharges and compute the standard deviation of the logarithms (index of variability):
 - a. Obtain mean of the logarithms.
 - b. Compute differences of each of the 10 logarithms from the mean.
 - c. Square the differences.
 - d. Obtain the sum of the squares.
 - e. Divide the sum of the squares by 9.
 - f. Extract the square root of the results of step e.

Lane and Lei (1950) discussed the use of their variability index in studying streamflow characteristics and proposed that an estimated variability index be used with an estimated mean annual discharge to produce a synthetic flow-duration curve. They found that large drainage areas tended to have lower values of variability than small ones.

Mitchell (1957, p. 161-166) found that, for Illinois, Lane's variability index differed considerably from one region to another, yet when the values of the index were plotted on a map, a consistent pattern was observed. The map of Illinois showing regional values of the variability index was presented for use in deriving synthetic duration curves for unmeasured areas.

A synthetic duration curve based on an estimated variability index and an estimated median flow may be accurate for the portion of the flow-duration curve that plots as a straight line on log-probability paper. Likewise, a duration curve, drawn as the average of the duration curves of nearby gaged streams draining areas that are apparently similar, may be reliable considerably below the median point but may depart radically at the extreme low end. The end points of the flow-duration curve cannot be accurately determined from the slope of the straight portion of the flow-duration curve. This statement can be verified for the low-flow end by studying the flow-duration curves of figure 12 and the location of the gaging stations on figure 11. Although the end portions of the flow-duration curve occupy a sizable space on probability paper, the percentage of time during which the inaccurately determined flows occur is small, and for some studies a synthetic curve may be suitable. When the extreme low end of the flow-duration curve is important, base-flow measurements should be made at the unmeasured site and correlated with the concurrent discharge at a stream-gaging station. (See the section on estimation of the flow-duration curve.)

RELIABILITY OF AN INDIVIDUAL STATION RECORD

A gaging-station record, however long, represents only a small sample of the long-term flow characteristics of the stream. The reliability of the record for predicting the behavior of the stream depends upon the accuracy and consistency of the record and upon how well the period of record represents the long-term flow of the stream.

The need for accurate records of basic data is obvious, but consistency of the record often does not receive enough emphasis. A 30-year record collected during 10 years of natural flow conditions, 10 years of irrigational or storage developments, and 10 years under changed basin conditions cannot serve as the basis for predicting future flows. Other major changes in the basin also affect the record. Changes in gage location or measuring section, even without appreciable change in drainage area, can affect the consistency of the record. This is particularly true of areas underlain by limestone, where low flows vary widely within short reaches of the same stream. Before analysis, records should be examined for consistency and the drainage basin history should be studied for information on developments that might affect the consistency of the record.

Even though a gaging-station record is accurate and consistent, it may not be representative of the long-term flow of the stream. This is particularly true of short-term records, which may include a predominance of dry or of wet years. Duration curves for such records should be adjusted to a long-term period by correlation with records at a long-term gaging station.

If no long-term gaging station record for an area is available, a regional analysis of all the short-term records for the area will improve the reliability of each of the flow-duration curves. A regional analysis of flow-duration data consists of (a) establishing a relation (as in fig. 7) between each individual station and a "pivot" station, (b) transferring the flow-duration curve of each individual station to the pivot station by using the curve of relation, (c) drawing an average or composite curve for the pivot station, and (d) transferring the composite curve of the pivot station back through the curve of relation to the individual station.

Regional analysis modifies the individual gaging-station record so that a chance occurrence of an event, such as a local shower during an extreme drought in a particular drainage basin, will not unduly affect the analysis. Likewise, regional analysis takes into account the failure of such an event to occur within a particular drainage basin when the event did occur within other basins in the region.

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